

Resolving Cosmological Tensions with Unparticles

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Outline

- Introduction
- Beyond the scalar field paradigm
- Banks-Zaks Cosmology
- Emergent Unparticles DE Model and the tensions
- Phenomenological fluid approach (WiP)
- Conclusions

COSMOLOGY CRASH SLIDE

- Consider the FLRW metric with no spatial curvature. Define the critical density

$$\rho_c = \frac{3H_0^2}{8\pi G}, \quad \Omega_{0i} = \frac{\rho}{\rho_c}, \quad w_i = \frac{p_i}{\rho_i}, \quad EOS$$

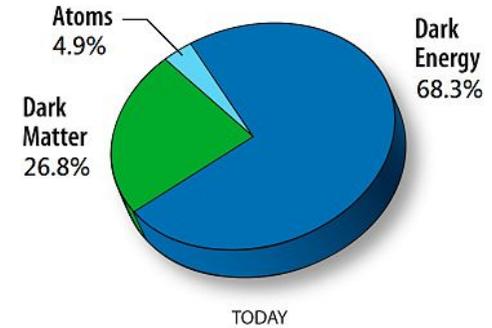
$$H(z)^2 = H_0^2 \sum_i \Omega_{0i} (1+z)^{3+3w_i}, \quad \dot{H} = -H_0^2 \sum_i \frac{3+3w_i}{2} \Omega_{0i} (1+z)^{3+3w_i}$$

- For $z < 3400$ (equality of matter and radiation), equations simplify further:

$$H(z)^2 \simeq H_0^2 [\Omega_{m0} (1+z)^3 + 1 - \Omega_{m0}], \quad \dot{H} \simeq -\frac{3}{2} H_0^2 \Omega_{m0} (1+z)^3$$

- LCDM model $\sim 1\%$ accuracy (CMB) $H_0 = 67.4 \pm 0.5$, $\Omega_{m0} = 0.315 \pm 0.007$

$$H_0, \Omega_b, \Omega_c, \tau, \sigma_8, n_s; \quad \Omega_{m0} = \Omega_b + \Omega_c; \quad \Omega_{m0} + \Omega_{\Lambda 0} = 1$$



Fundamental Problems in Cosmology

- Big Bang Singularity - Artymowski, IBD, Kumar JCAP 2019 +WIP.
- Early Universe - Inflation/Bounce? Which model? Connection with SM Artymowski, IBD, Thattarampilly JCAP 2020, IBD, Thattarampilly 2308.00256
- Nature of present acceleration - CC? Dark Energy? Modified gravity? Which model?

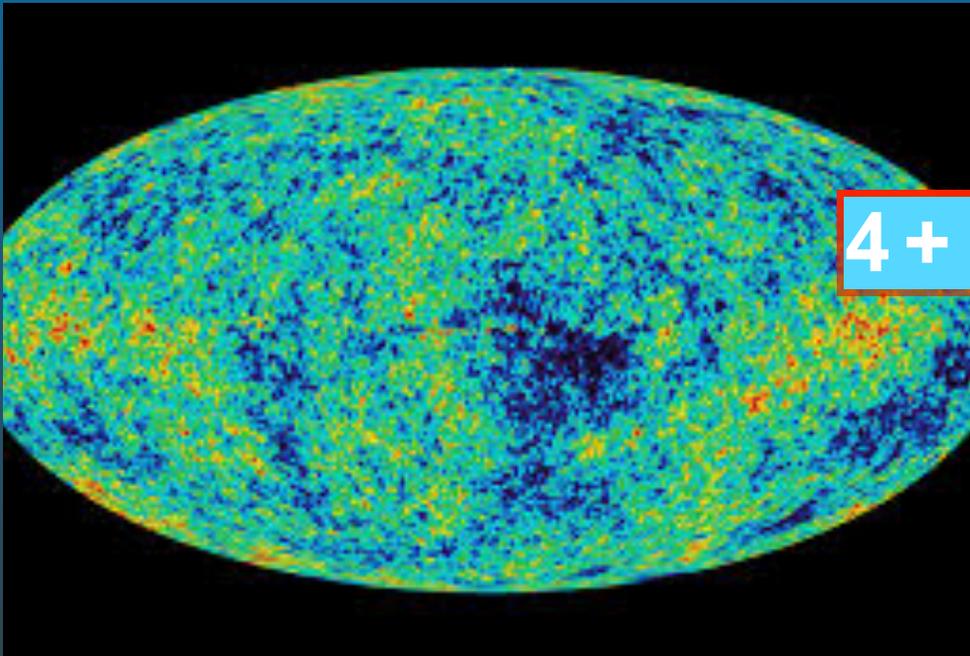
- Nature of Dark Matter

Scalar Fields!

-
- The Hubble Tension
 - The LSS (S_8) Tension

- H_0 is the most important cosmological measurement and is relevant for fundamental physics as well.

$z > 1$



$$H_0 = 67.4 \pm 0.5 \text{ km/sec/Mpc}$$
$$H_0 = 67.4 \pm 1.2 \text{ km/sec/Mpc}$$

4+ SIGMA!

$z < 1$



$$H_0 = 73 \pm 1 \text{ km/sec/Mpc}$$

$$69.8 \pm 1.9$$

$$73.6 \pm 3.9$$

$$73.3 \pm 1.8$$

$$74.8 \pm 3.1$$

$$76.5 \pm 4.0$$

THE LSS S_8 TENSION

- Measurements of matter fluctuations on large scales is

given by $S_8 = \sigma_8 \sqrt{\frac{\Omega_{m0}}{0.3}}$

2-3 SIGMA!

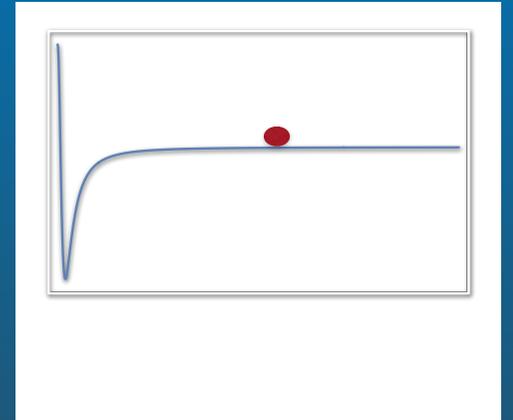
- σ_8 are the linear matter fluctuations smoothed over 8h Mpc
- Ω_{m0} is the relative matter energy density.
- CMB (Planck measurement) $S_8 = 0.834 \pm 0.016$
- (Also KiDs ...) DES $S_8 = 0.776 \pm 0.017$

**Most attempts to reduce
one tension
result in
increasing the other!**

SCALAR FIELDS IN COSMOLOGY

- Daily practice in theoretical physics $T(t,x)$
- A single DOF, with a flat potential - everyone can do that!
- Abundant in String Theory and extensions of the SM
- Fine-tuned models? organizing principle?
- Field Theory is much richer - confinement, strong interactions, topological defects, conformal symmetry...
- The Swampland Conjecture - in QG potentials are steep (see however, IBD, PRD 2018 “Draining the Swampland”)

$$\Delta\phi \lesssim 1, \quad \frac{V'}{V} \gtrsim 1 \quad \text{OR} \quad \frac{V''}{V} \gtrsim 1$$



PROBLEMS WITH PRESENT ACCELERATION (CC/DE)

- CC is the simplest parametrization of the observed acceleration
- The CC is related to zero point vacuum fluctuations of fields and respects Lorentz inv., for a cutoff M , we expect $\rho_{\Lambda} \sim M^4$
- For any fundamental energy scale M , we find a CC much smaller than expected - *The Cosmological Constant Problem*
 $\rho_{\Lambda}^{\text{obs.}} \sim 10^{-10} \text{erg/cm}^3$, $M_{\text{QCD}} \sim 10^{36} \text{erg/cm}^3$, $M_{\text{EW}} \sim 10^{47} \text{erg/cm}^3$, $M_{\text{pl}} \sim 10^{110} \text{erg/cm}^3$.

WHY NOW?

- Energy Density of matter $\sim a^{-3}$, radiation $\sim a^{-4}$, CC $\sim a^0$.
- Completely different scaling which is why we had a radiation dominated universe followed by matter domination.
- Why do we have today $\frac{\rho_m}{\rho_\Lambda} \sim 1$?
- Requires fine-tuned initial conditions in the early universe. Especially for scalar fields.

BEYOND SCALAR FIELDS IN COSMOLOGY

- Daily practice in theoretical physics $T(t,x)$ 
- ~~A single DOF, with a flat potential—everyone can do that!~~
Emergent single DOF with an equation of state - everyone can do that! 
- Abundant in String Theory and extensions of the SM 
- ~~Fine-tuned models? organizing principle?~~
- Field Theory is much richer - confinement, strong interactions, topological defects, conformal symmetry... 
- ~~The Swampland Conjecture—in QG potentials are steep~~

BANKS-ZAKS COSMOLOGY

- Consider a sector with conformal symmetry (SU(3) with N_f massless fermions) weakly coupled to the SM (suppressed by $\Lambda_{\mathcal{U}}$).
- At high temperature ($T \gg \Lambda_{\mathcal{U}}$) conformal symmetry is restored and the sector behaves like radiation.
- At low temperature the coupling to SM breaks the symmetry - “unparticles” with anomalous scaling T^δ .

BANKS-ZAKS COSMOLOGY - UNPARTICLES

- Theory with conformal symmetry, slightly displaced from its conformal fixed point. β function vanishes in the conformal limit.

- Very general, based on dimensional analysis, any broken CFT $\theta_{\mu}^{\mu} \sim \left(\frac{T}{\Lambda_{\mathcal{U}}} \right)^{4+\delta}$

- The thermal average gives: $\theta_{\mu}^{\mu} = \rho - 3p \propto T^{\delta}$

- $\rho = \sigma T^4 + BT^{4+\delta}$

- $p = \frac{1}{3}\sigma T^4 + \frac{B}{\delta+3}T^{4+\delta}$

- The equation of state is not (nearly) constant anymore $w \equiv \frac{p}{\rho} = \frac{1}{3} \frac{\sigma + \frac{3B}{\delta+3}T^{\delta}}{\sigma + BT^{\delta}}$

BANKS-ZAKS COSMOLOGY - CONSEQUENCES $w(T)$

- Naturally behaves as different fluids at different epochs
- Can temporarily violate the Null Energy Condition (NEC) - No Big Bang singularity without QG or non-canonical Lagrangians
- Can have a limiting temperature - an effective CC!

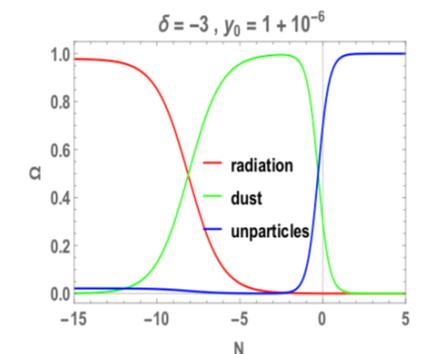
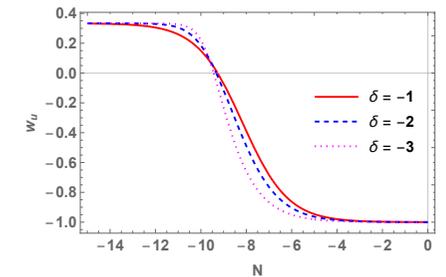
UNPARTICLES AS DARK ENERGY- UDE

- @ high T, $w=1/3$ -radiation. @ low T, limiting temperature T_c .
Dim-less temperature $y=T/T_c$

$$w \equiv \frac{p}{\rho} = \frac{1}{3} \frac{\sigma + \frac{3B}{3+\delta} T^\delta}{\sigma + BT^\delta}$$

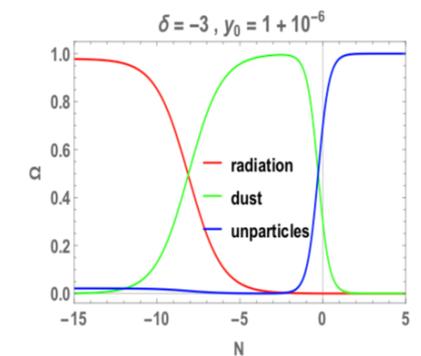
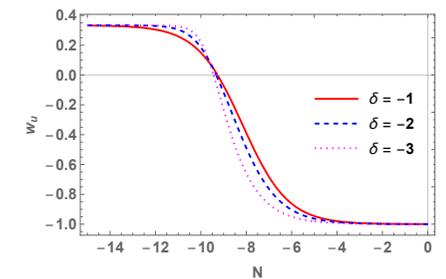
- $-3 < \delta < 0, \quad B < 0 \Rightarrow \quad T > T_c = \left[\frac{4(\delta + 3)}{3(\delta + 4)} \left(-\frac{\sigma}{B} \right) \right]^{\frac{1}{\delta}}$

- The dynamical evolution starts from high T and asymptotes to T_c .
- Unparticles start as radiation and as they asymptote to T_c they behave as a CC.
- Deviations can only come from higher loop corrections of the beta function.



UDE- PROS.

- No fine-tuning of initial conditions. Radiation and CC behavior are predictions.
- No “Swampland conjectures”, no scalar fields, no modified gravity.
- B is fixed by present day DE density. We are very close to the critical temperature $y_0 - 1 \lesssim 10^{-4}$



UDE - PREDICTIONS

- Special redshift dependence of w :

$$w_u \simeq -1 + 4(\delta + 4)(y_0 - 1)(1 + z)^3$$

- Contributes to N_{eff} , consistency condition, current limits

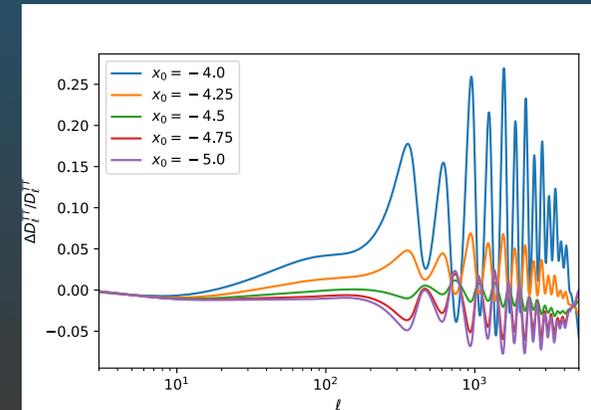
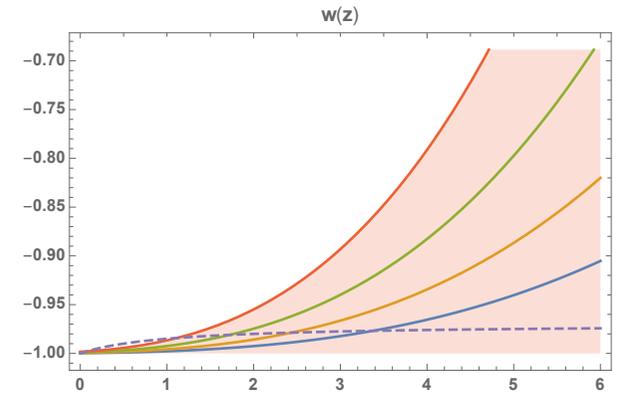
$$\Delta N_{\text{eff}} \lesssim 0.19:$$

$$w_u(z) \simeq -1 + 0.58(1 + z)^3 \left(-1 - \frac{4}{\delta} \right)^{1/4} \left[\frac{\Omega_{r0}}{\Omega_{u0}} \Delta N_{\text{eff}} \right]^{3/4}$$

- Perturbation observables $(\gamma, f\sigma_8)$ - as LCDM to 0.1%

$$\delta'_u = - (1 + w_u) (\theta_u - 3\Phi') - \frac{a'}{a} \left(\frac{\delta p_u}{\delta \rho_u} - w_u \right) \delta_u,$$

$$\theta'_u = -\frac{a'}{a} (1 - 3w_u) \theta_u - \frac{w'_u}{1 + w_u} \theta_u + \frac{\delta p_u}{\delta \rho_u} k^2 \delta_u + k^2 \Phi$$

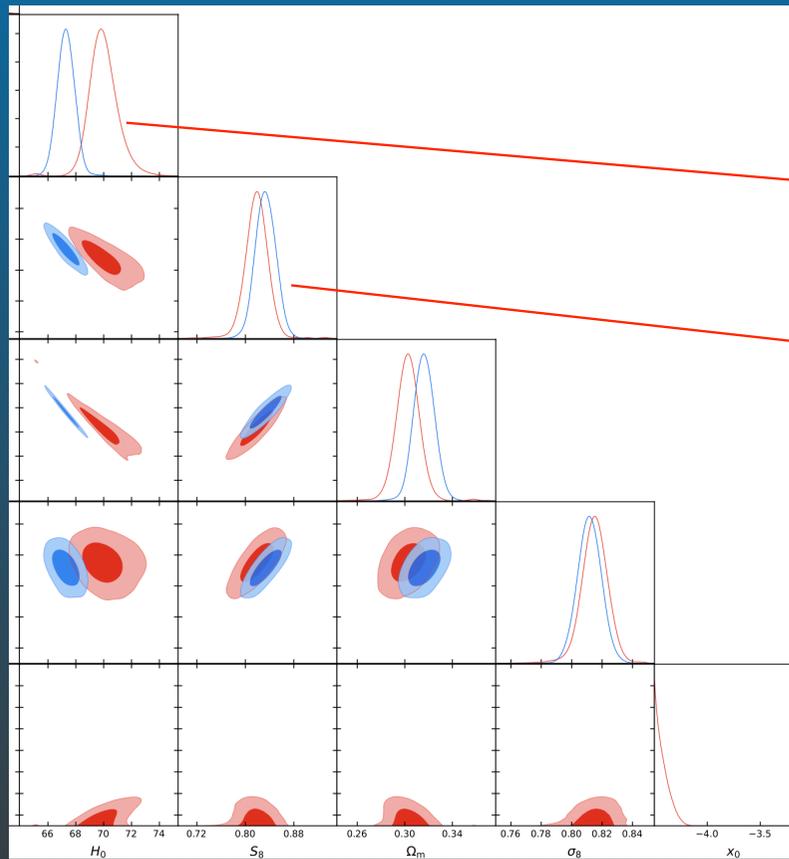


UDE AND LCDM - LIKELIHOOD ANALYSIS

- Perform likelihood analysis of UDE and compare to LCDM
- Consider various data sets, each time removing one that is causing the tension.
- For UDE fix $\delta = -3$, data is insensitive to the exact value.
- Flat priors for the different parameters
 $H_0, \Omega_b, \Omega_c, \tau, \sigma_8, n_s; \quad y_0 = 1 + 10^{x_0}, \quad x_0 \in [-6, -3]$
- Model mostly changes the Early Universe $z > 1$.

RESULTS

Planck Only

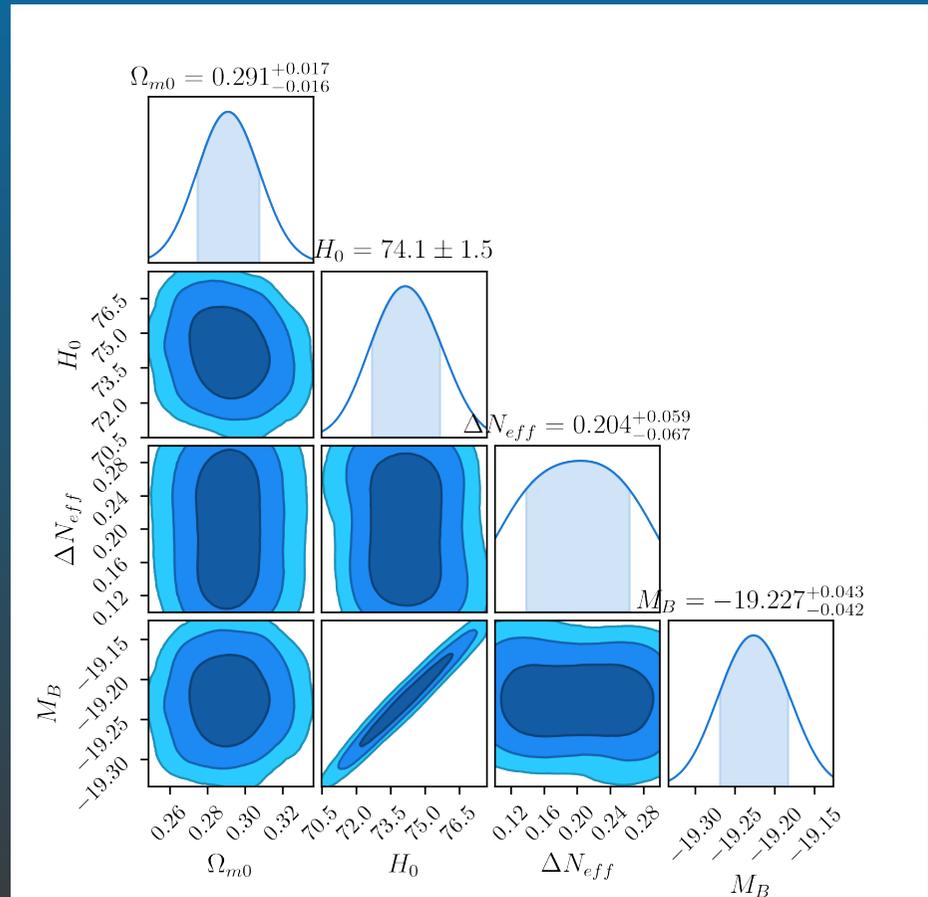


Hubble is shifted
Towards SN value!

S_8 is reduced
towards DES value!

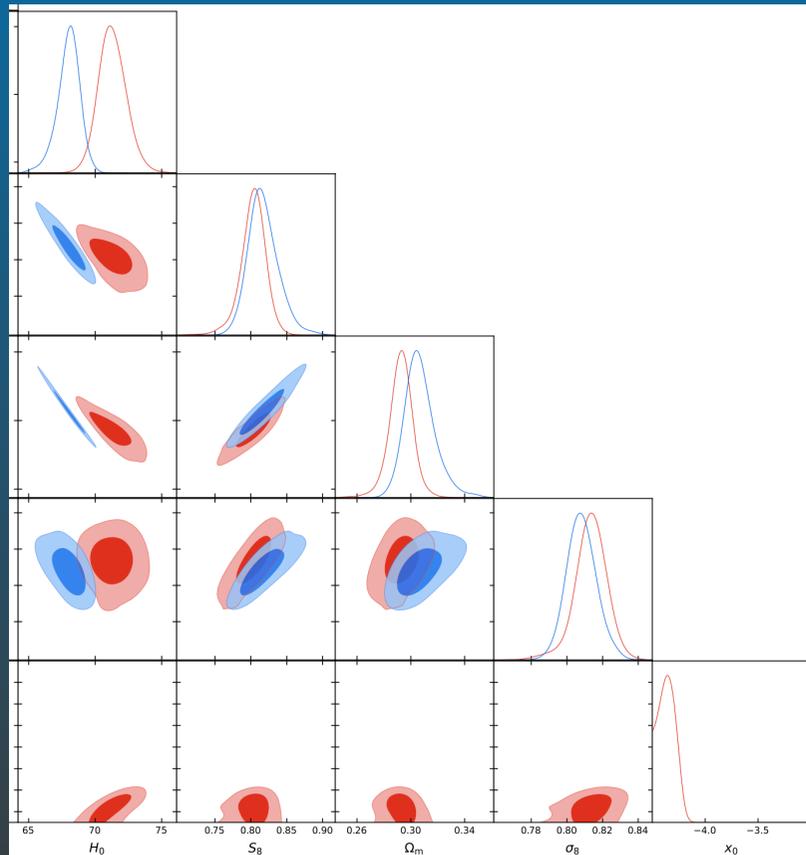
$$\Delta\chi^2 = 2.14 : - ($$

SN Only



RESULTS

Planck+Pantheon+SHoES



Hubble is shifted
Towards SN value!

S_8 is reduced
towards DES value!

$$\Delta\chi^2 \simeq -11!$$

LCDM

UDE

H_0	$68.00^{+0.92}_{-0.70}$ (68.46)	$71.29^{+0.96}_{-1.1}$ (71.18)
σ_8	$0.8082^{+0.0079}_{-0.0088}$ (0.8045)	$0.8132^{+0.0093}_{-0.0078}$ (0.813)
S_8	$0.817^{+0.017}_{-0.023}$ (0.8045)	$0.803^{+0.018}_{-0.014}$ (0.806)
Ω_m	$0.3069^{+0.0088}_{-0.013}$ (0.3005)	$0.2926^{+0.0087}_{-0.0077}$ (0.295)

RESULTS

Planck+Lensing+BAO+DES+Pantheon+SHoES

Hubble is shifted
Towards SN value!

S_8 is reduced
towards DES value!

$$\Delta\chi^2 = -7.24!$$

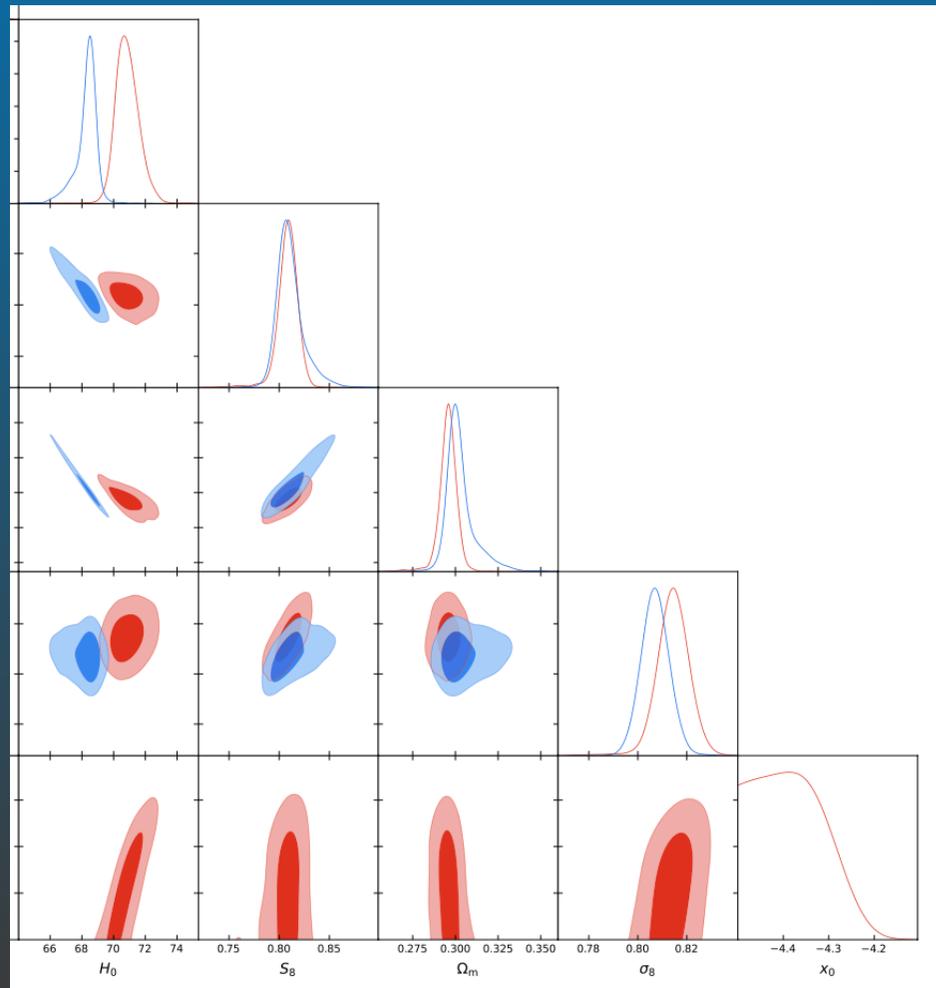
LCDM

UDE

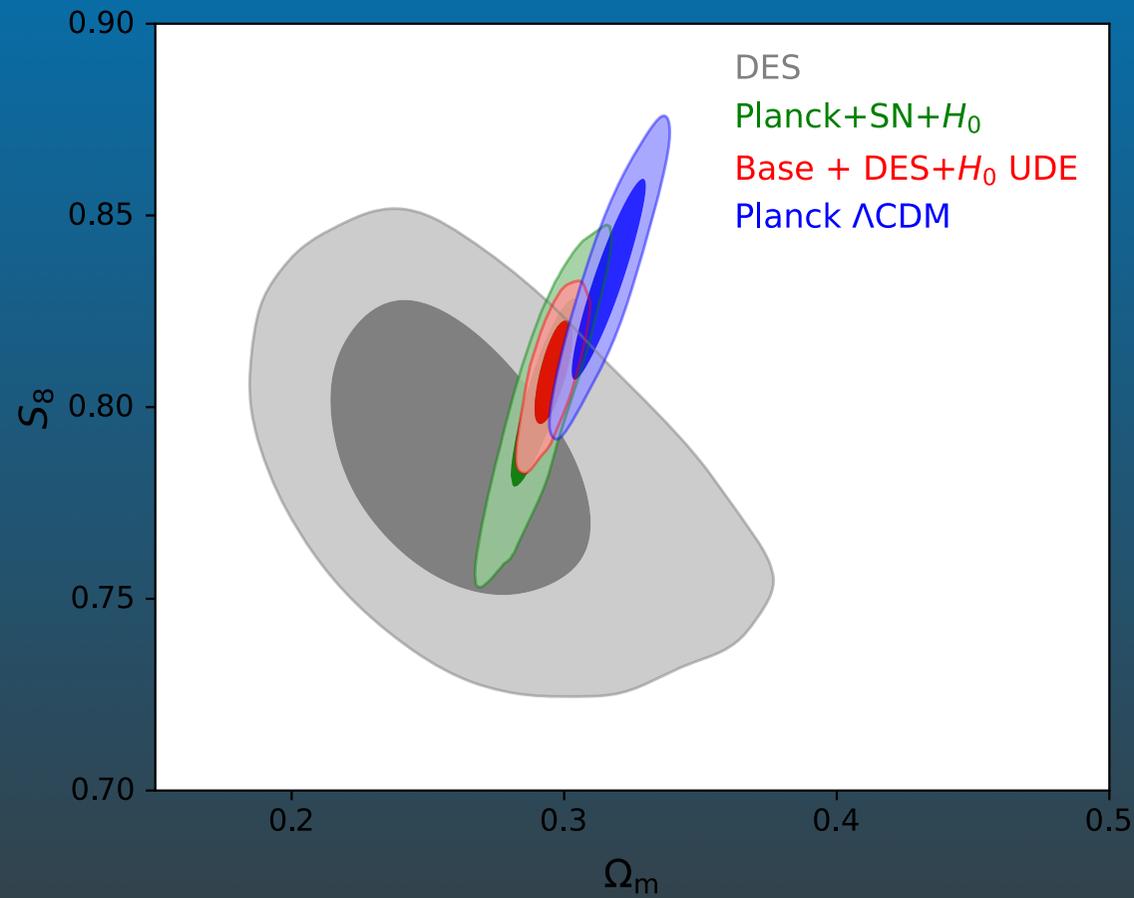
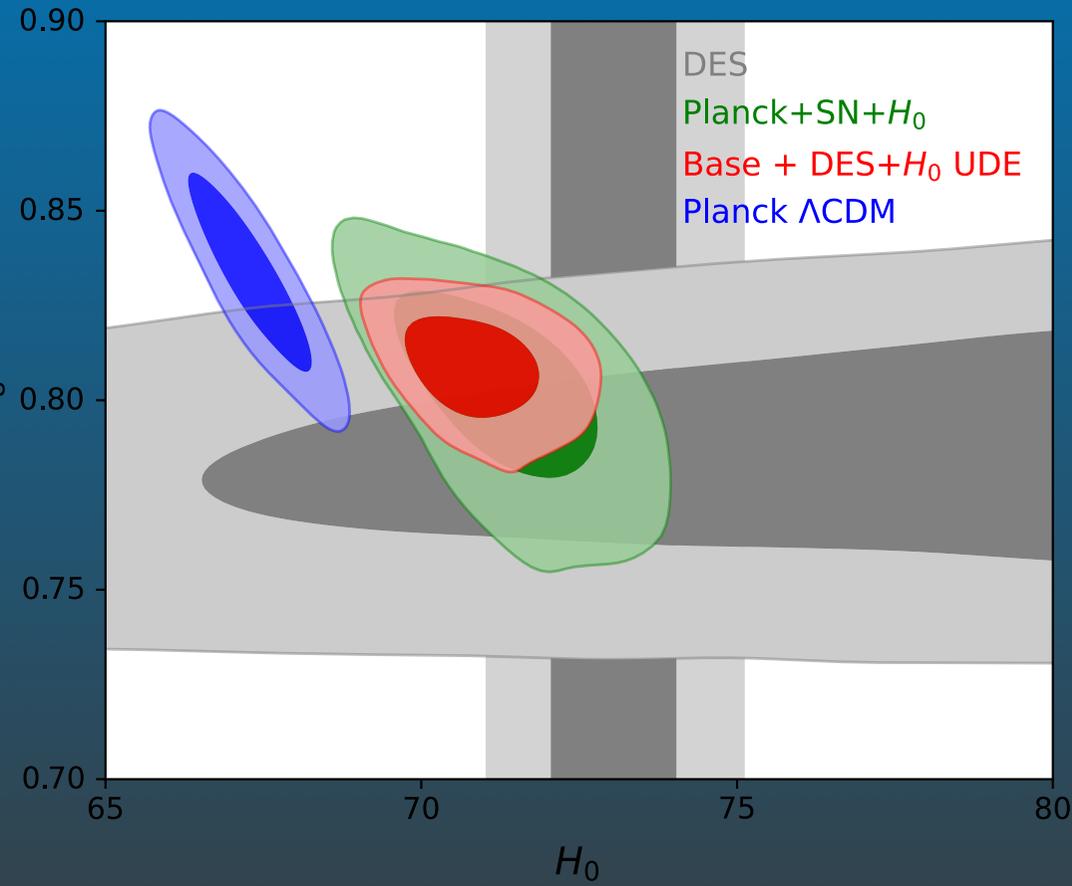
H_0	$68.28^{+0.71}_{-0.31}$ (68.47)	$70.87^{+0.61}_{-0.79}$ (70.76)
σ_8	0.8071 ± 0.0059 (0.8069)	0.8142 ± 0.0073 (0.8140)
S_8	$0.8111^{+0.0080}_{-0.015}$ (0.8075)	$0.808^{+0.010}_{-0.0078}$ (0.8093)
Ω_m	$0.3030^{+0.0038}_{-0.0091}$ (0.3004)	$0.2956^{+0.0049}_{-0.0041}$ (0.2965)

Improvement in the likelihood persists for
all other combinations of data sets by at least $|\Delta\chi^2| > 2.1$

Both tensions are reduced to
less than 1 STD w.r.t SHoES and DES!



RESULTS



Clear improvement in concordance and likelihood!

PHENOMENOLOGICAL FLUID WITH “TRACKER MECHANISM”

- Could unparticle behavior be more robust?
- Any DE model needs a “tracker mechanism” - DE “tracks” the matter or radiation to avoid fine tuning.
- Possibility of measuring the spatial curvature. *Leonard et al. 2016* -need theoretical insights.
- Could some of the tensions be just parametrization issues?
- Parametrize a relatively sudden transition.

PHENO. FLUID DE

- Theoretical priors:
- 1) Fulfill the Null Energy Condition $w \geq -1$
- 2) Today $w \sim -1$
- 3) At early times $w = 1/3$ (or 0) for tracker mechanism

- Speed of sound $c_s^2 = 1$ or 0 or open $0 \leq c_s^2 \leq 1$ and adiabatic speed of sound:

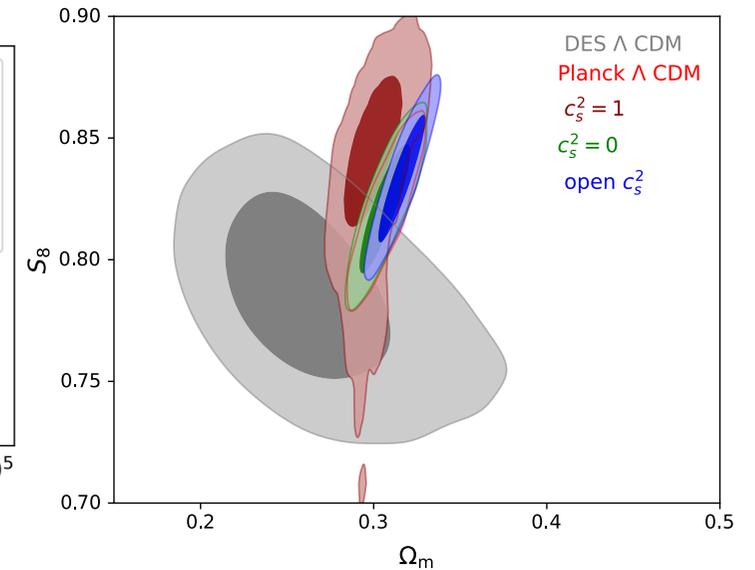
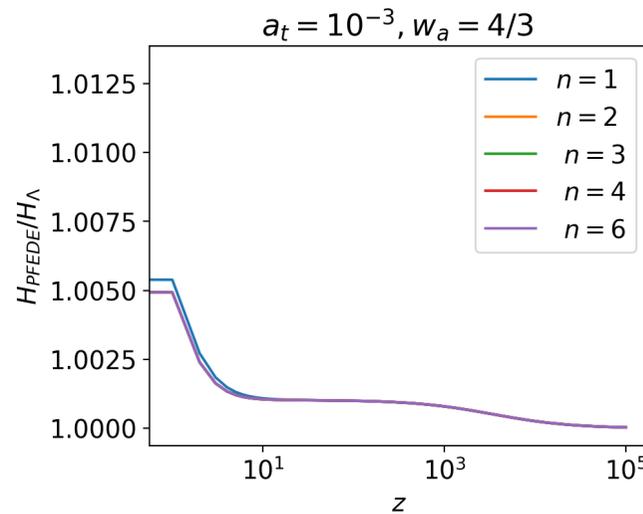
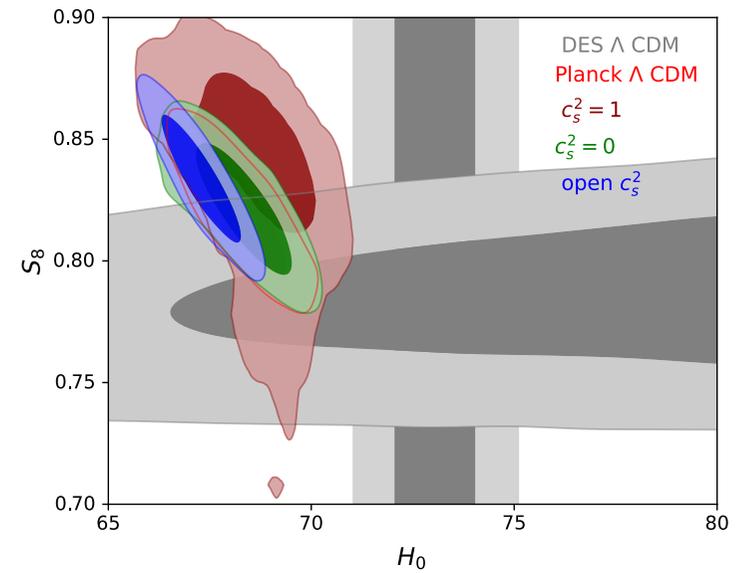
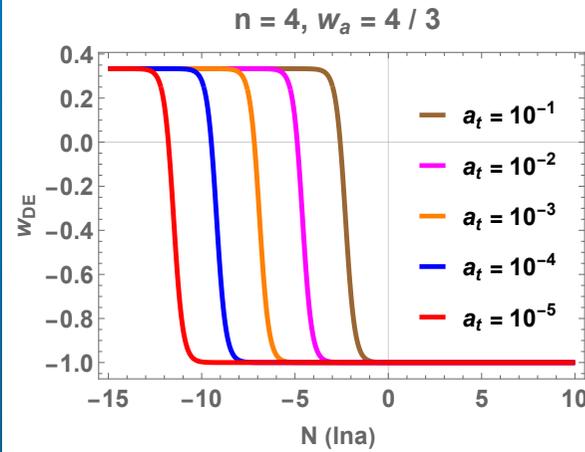
$$c_a^2 = w_{DE} \left(1 - \frac{n}{4}\right) + \frac{n}{12}$$

- a_t transition redshift.

$$w_{DE}(a) = -1 + \frac{4/3}{1 + (a/a_t)^n}$$

RESULTS

- Slight reduction in H_0 and S_8 tension. $H_0 \sim 69$, $S_8 \sim 0.81$.
- Less statistically significant.
- $\Delta\chi^2 \simeq -2.7$
- $n > 3$ preferred
- In all cases, $z_t \sim 30$.



BEYOND SCALAR FIELD SUMMARY

- Within UDE cosmological concordance is largely restored for **both Hubble and S_8 tension**
- Pheno. Fluid approach not as successful. Still $z_t \sim 30$
- Going beyond weakly coupled scalar fields opens a new model space with different problems and opportunities.
- Generic arguments about conformal symmetry and dim. analysis.
- Useful for fundamental problems - **Big Bang singularity, Swampland, CC...** and for practical ones - **Hubble tension, S_8 tension, N_{eff} , ...**
- Highly predictive, consistency condition - detected within a decade or bound consistency approaching LCDM.
- Future directions - interactions with CMB, N_{eff} , growth of fluctuations

BACKUP: HUBBLE TENSION REVISITED

- SN Ia: do not assume a model except isotropic redshift.

- Consider only low redshift SN Ia, $z \ll 1$.

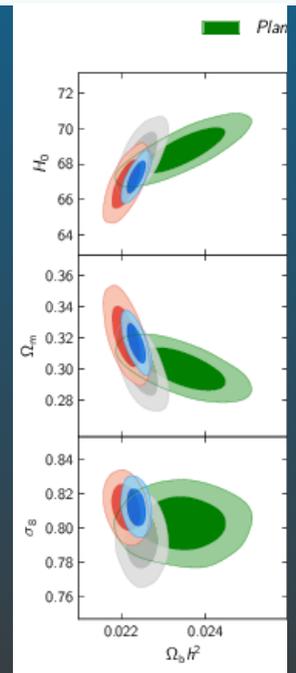
$$d_L(z) = \frac{1+z}{H_0} \int_0^z \frac{dz'}{\sqrt{\Omega_m(1+z')^3 + 1 - \Omega_m}} \underset{z \ll 1}{\approx} \frac{z}{H_0} \left[1 + \left(1 - \frac{3}{4}\Omega_m \right) z \right]$$

- Measure Hubble $H_0^{SN,obs.} = 73 \pm 1 \text{ km/sec/Mpc}$

- Use Hubble and high redshift $z \sim 1$ for matter density Ω_{m0} , CC etc.

- CMB: Take all possible data. Assume a model (like LCDM)

- Infer the model parameters from a likelihood analysis



BACKUP 2: EARLY UNIVERSE

- Consider unparticles+fluid.

$$H(z)^2 = H_0^2 \sum_i \Omega_{0i} (1+z)^{3+3w_i}, \quad \dot{H} = -H_0^2 \sum_i \frac{3+3w_i}{2} \Omega_{0i} (1+z)^{3+3w_i}$$

- Violates NEC near the Bounce.
- New stable solutions- de Sitter Bounce, standard Bounce, cyclic universe.
- Analysis of the different phases

$$\rho = \sigma T^4 + BT^{4+\delta}$$

$$p = \frac{1}{3}\sigma T^4 + \frac{B}{\delta+3} T^{4+\delta}$$

- Calculation of the primordial spectra and stability of the cyclic/bounce scenarios.

Artymowski, IBD, Kumar JCAP 2019 +WiP

