

# Simultaneous alleviation of major cosmological tensions through $\Lambda_s$ CDM cosmology

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Workshop on Tensions in Cosmology  
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Corfu, Greece

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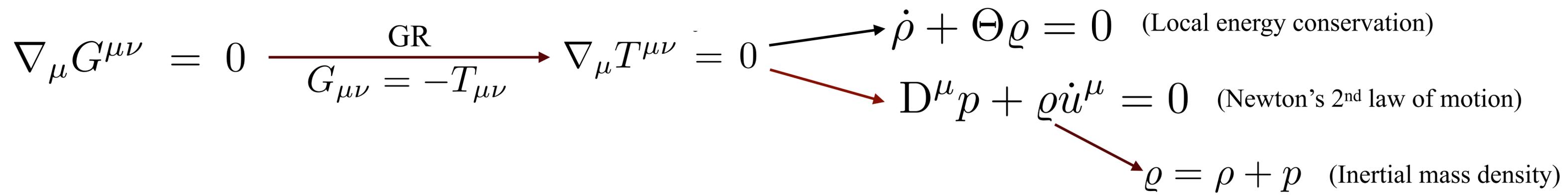


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1773-2023

**TÜBA**  
TÜRKİYE BİLİMLER AKADEMİSİ  
TURKISH ACADEMY OF SCIENCES



**cost**  
EUROPEAN COOPERATION  
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Cosmological Constant or the usual vacuum energy of QFT

$$\varrho_{\Lambda} = 0$$

See Nihan's talk

Simple-gDE:

$$\varrho = \text{constant}$$

Acquaviva, Akarsu, Katirci & Vazquez PRD (2021), arXiv:2104.02623

gDE: Graduated dark energy

$$\varrho = \gamma \rho_0 \left( \frac{\rho}{\rho_0} \right)^{\lambda}$$

The simplest dynamical deviation from zero inertial mass density of the usual vacuum energy density. Inspired by *Graduated inflationary universes*, Barrow, PLB, 1990.

$$\rho = \rho_0 [1 + 3\gamma(\lambda - 1) \ln a]^{\frac{1}{1-\lambda}} \xrightarrow[m \text{ and } n \text{ are odd integers}]{\frac{1}{1-\lambda} = \frac{m}{n}} \rho = \rho_0 \text{sgn}[1 - \Psi \ln a] |1 - \Psi \ln a|^{\frac{1}{1-\lambda}}$$

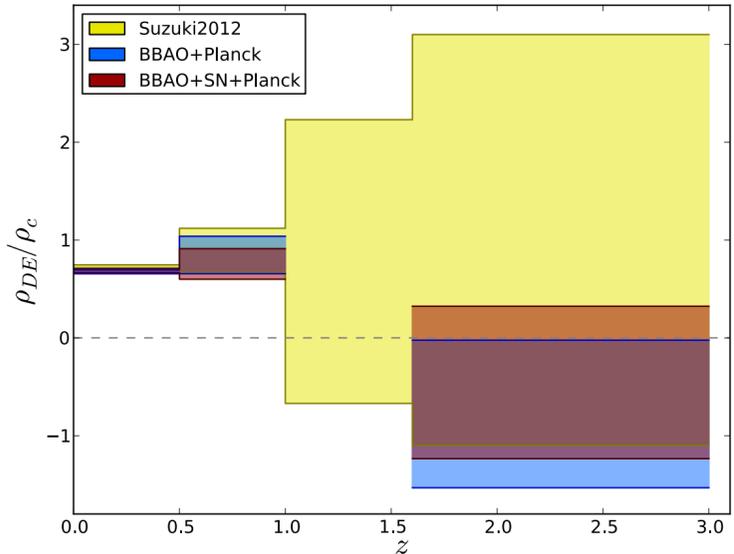
EoS parameter

$$w = -1 + \frac{\gamma}{1 + 3\gamma(\lambda - 1) \ln a}$$

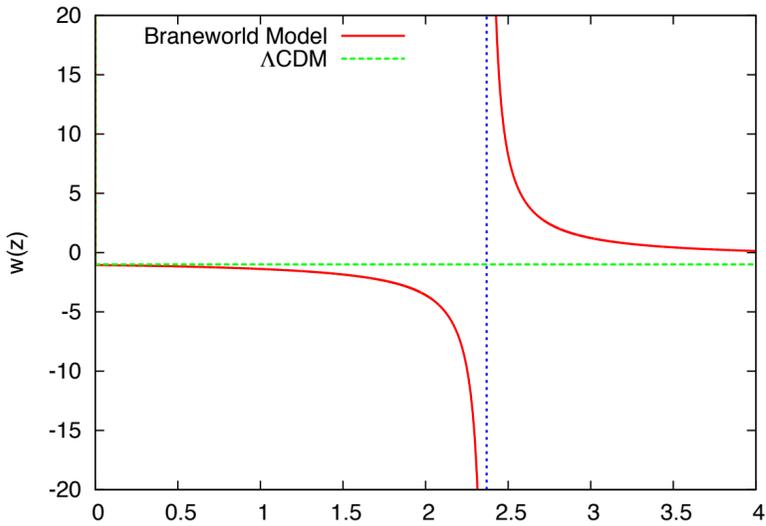
$$\Psi \equiv -3\gamma(\lambda - 1) < 0 \quad \lambda < 1 \quad \gamma < 0$$

Sign changing energy density requires an EoS exhibiting a singularity/pole. (Özülker, PRD 2022, arXiv:2203.04167) See Emre's talk

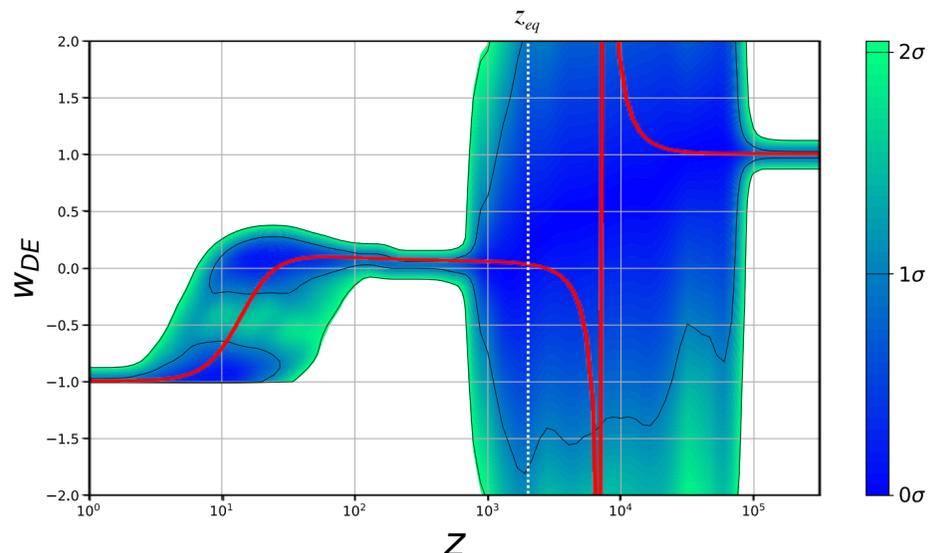
Under these conditions energy density takes negative values in the past and EoS exhibits singularity/pole during its sign change



Aubourg et al. (BOSS Collab.), PRD (2015), arXiv:1411.1074



Sahni, Shafieloo & Starobinsky, APJ Let (2014), arXiv:1406.2209



Akarsu, Katirci, Özdemir & Vazquez, EPJC (2020) arXiv:1903.06679

**gDE-CDM, replaces the  $\Lambda$  of  $\Lambda$ CDM with the gDE**

$$\frac{H^2}{H_0^2} = \Omega_{r,0} a^{-4} + \Omega_{m,0} a^{-3} + \Omega_{DE,0} \text{sgn}[1 - \Psi \ln a] |1 - \Psi \ln a|^{\frac{1}{1-\lambda}}$$

$$\frac{\rho_{DE}}{\rho_{c,0}} = \Omega_{DE,0} \text{sgn}[1 - \Psi \ln a] |1 - \Psi \ln a|^{\frac{1}{1-\lambda}}$$

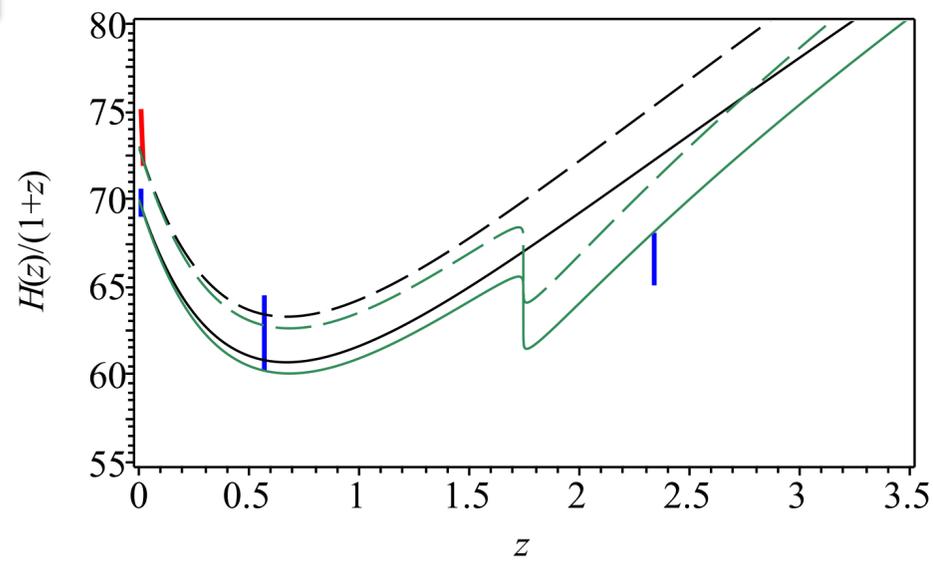
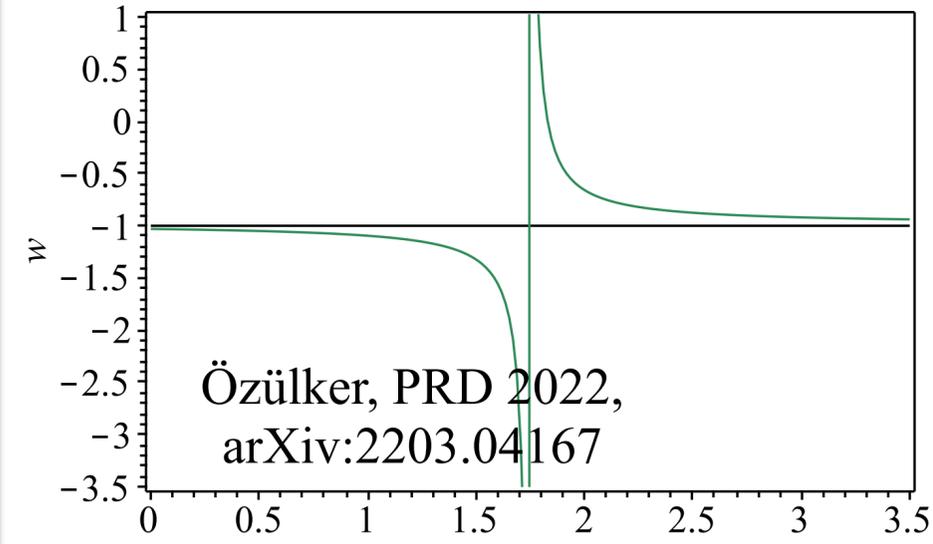
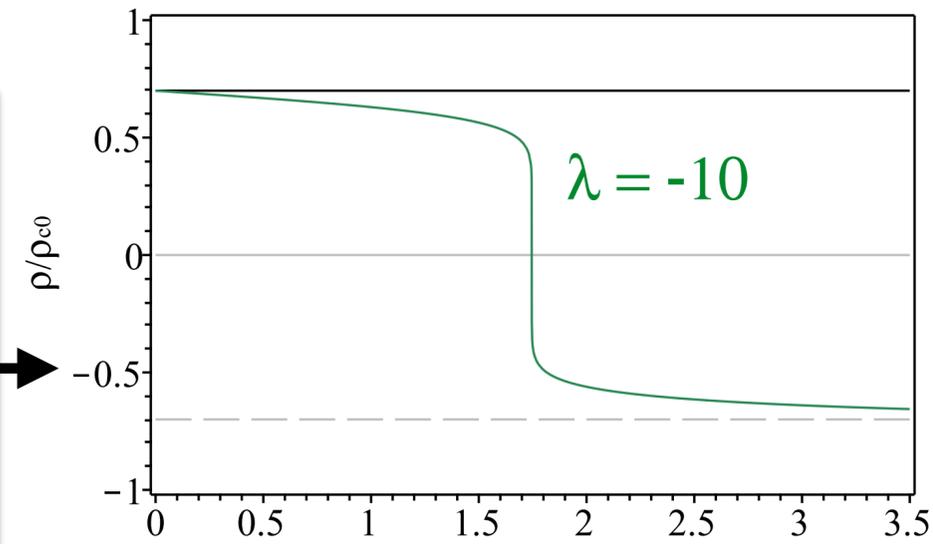
$$\rho_{gDE} = \rho_{gDE0} \text{sgn}[1 + \Psi \ln(1 + z)] |1 + \Psi \ln(1 + z)|^{\frac{1}{1-\lambda}}$$

gDE density changes sign at  $z_{\dagger} = e^{-\Psi^{-1}} - 1$

**$\Lambda_s$ CDM?**

$$\frac{\rho_{DE}}{\rho_{c,0}} \rightarrow \Omega_{DE,0} \text{sgn}[1 - \Psi \ln a] \text{ as } \lambda \rightarrow -\infty$$

$$\Lambda \rightarrow \Lambda_s \equiv \Lambda_{s0} \text{sgn}[z_{\dagger} - z]$$

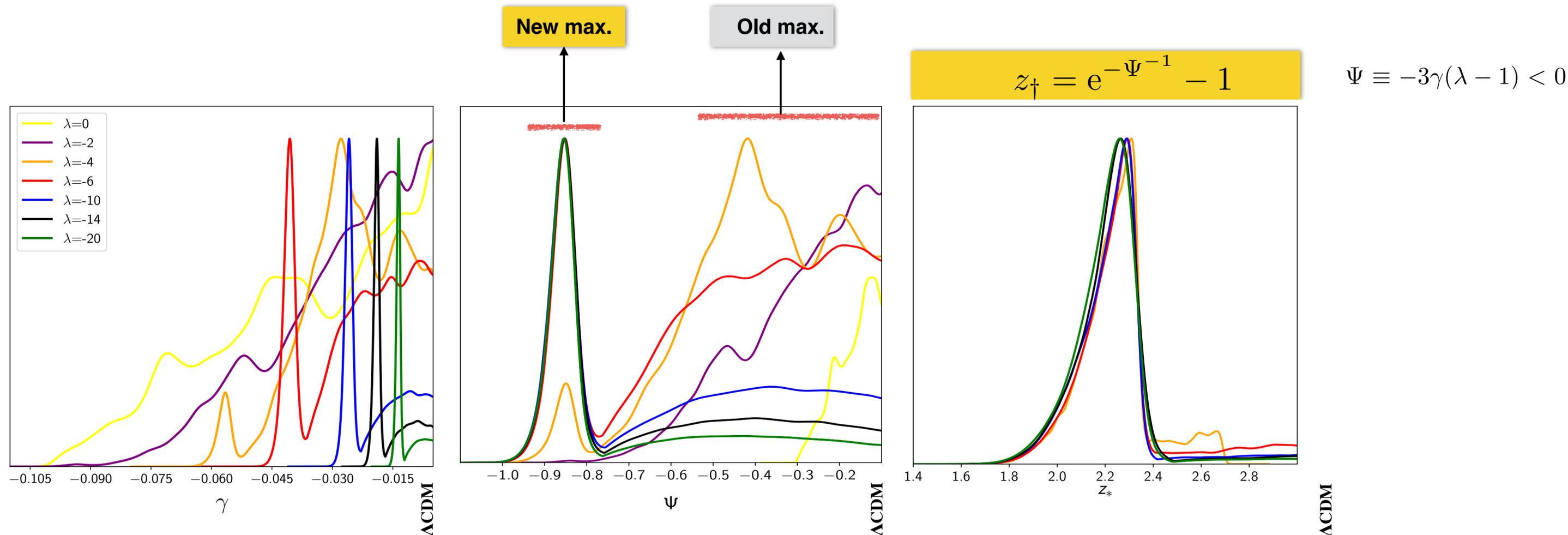


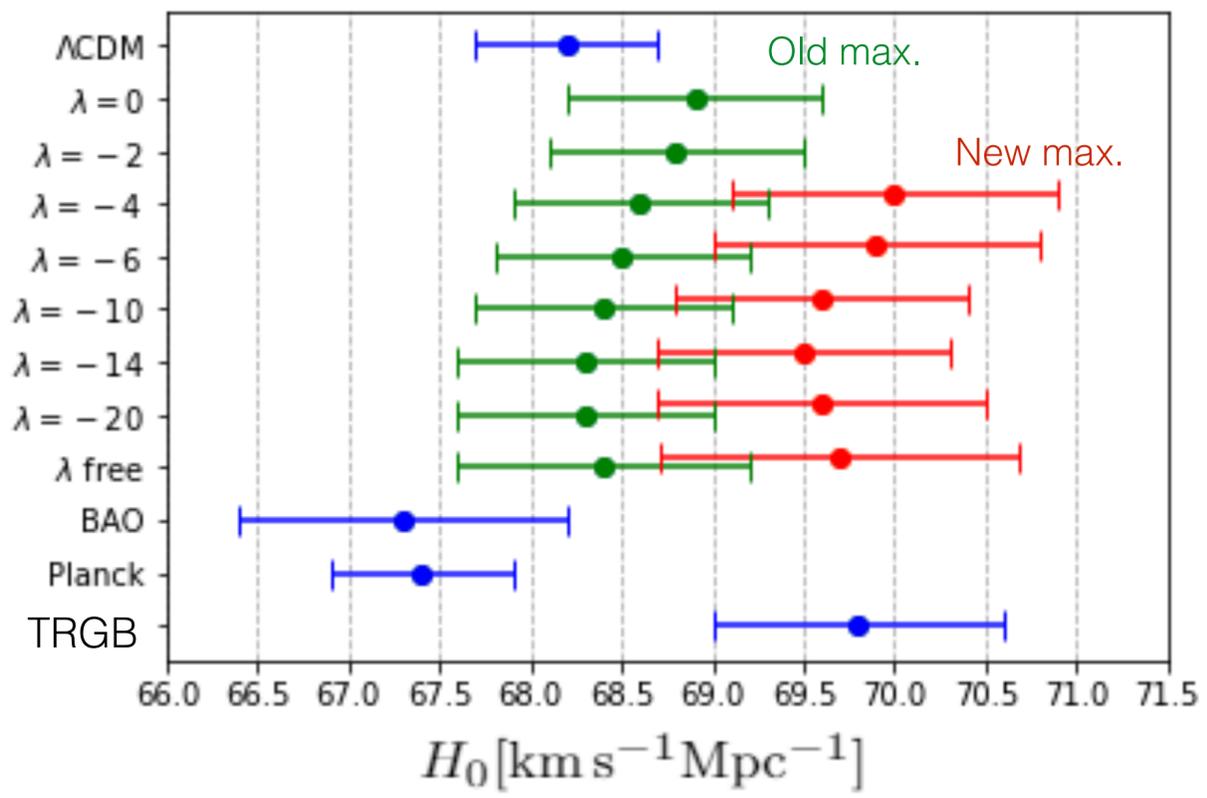
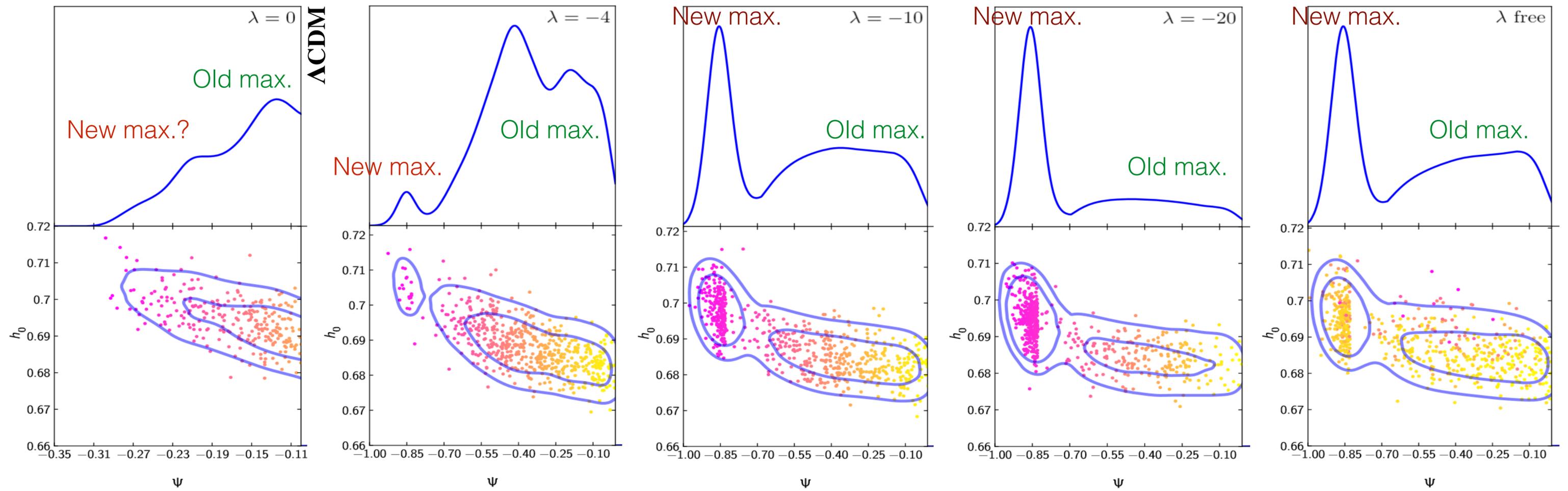
Massive Brans-Dicke gravity extension of the standard  $\Lambda$ CDM model

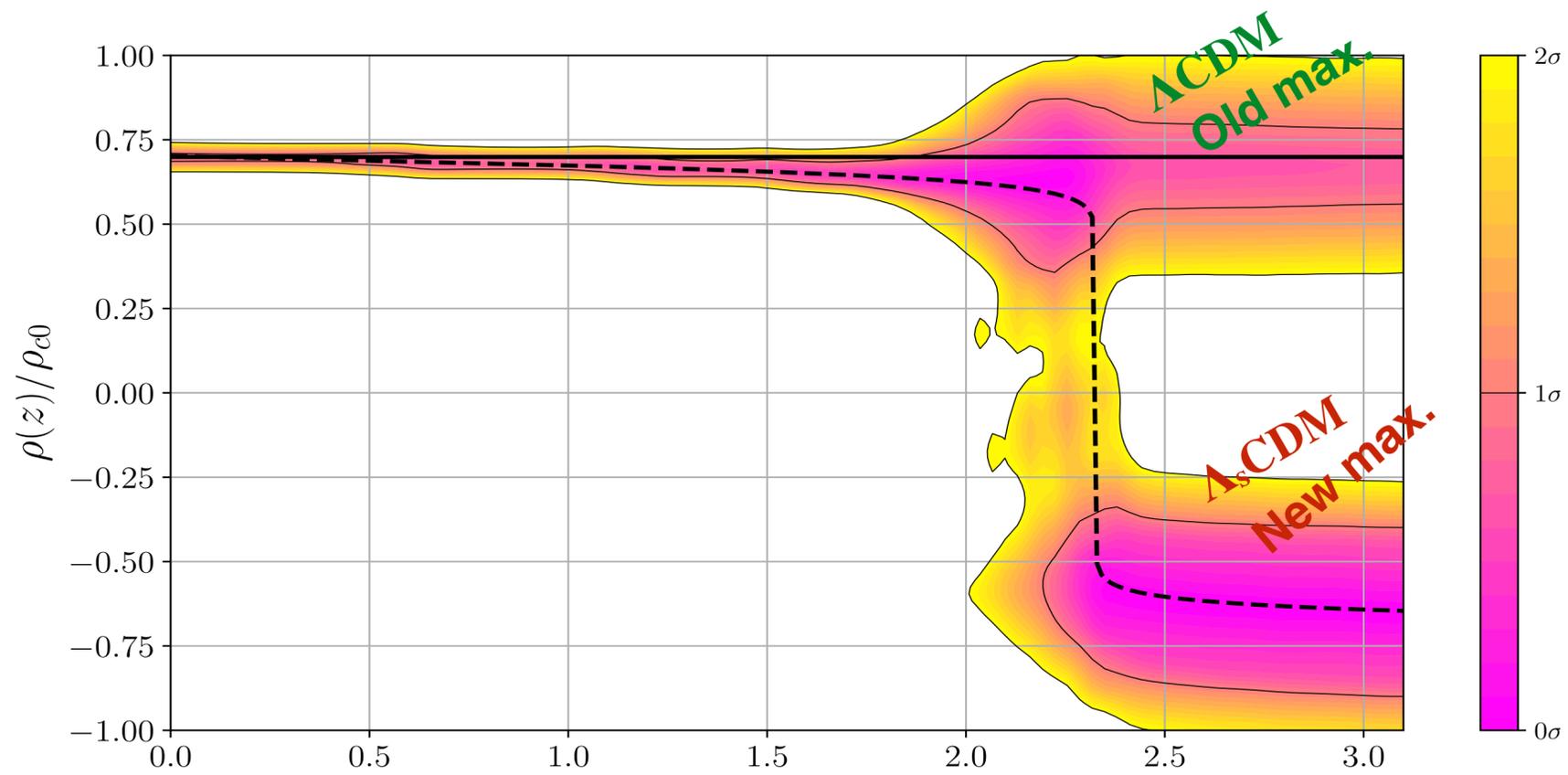
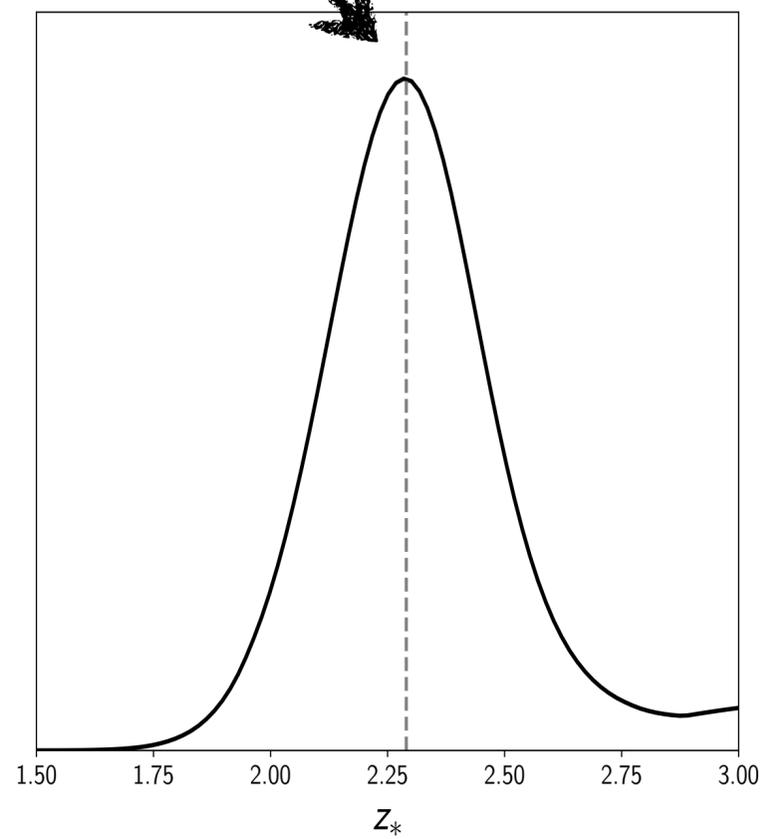
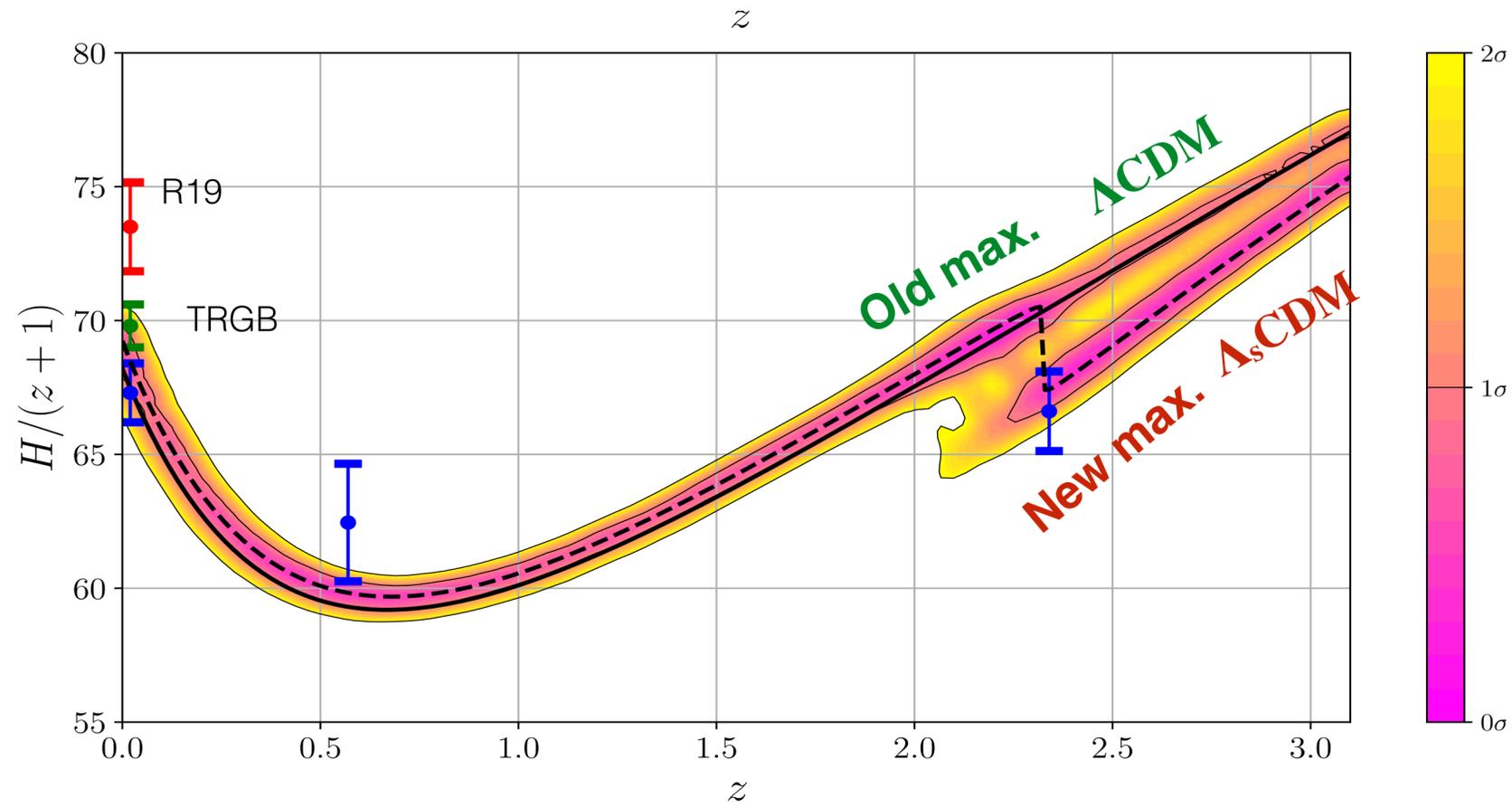
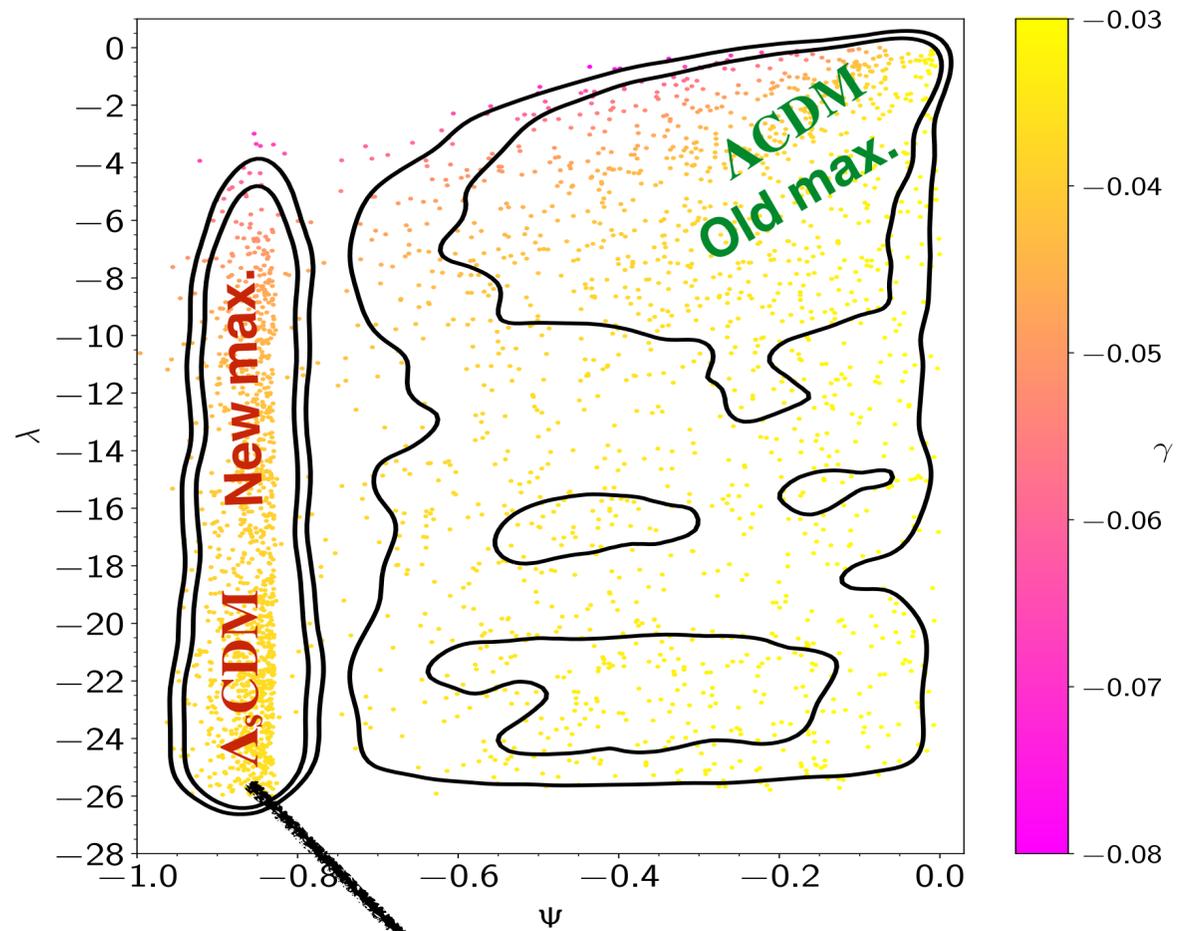
$$S_{\text{JBD}} = \int d^4x \sqrt{-g} \left[ \frac{\varphi^2}{8} R - \omega \left( \frac{1}{2} \nabla_{\mu} \varphi \nabla^{\mu} \varphi + \frac{1}{2} M^2 \varphi^2 \right) \right] + S_{\text{Matter}},$$

# Constraints on gDE-CDM from PLK+BAO+SN (JLA)+ $H$ (Cosmic Chronometers)

$\lambda$	$\Omega_{m,0}$	$h_0$	$\gamma = w_0 + 1$	$\Psi$	$z_*$	$t_0$ [Gyr]	$-2\Delta \ln \mathcal{L}_{\max}$	
$\Lambda$ CDM	0.302(6)	0.682(5)	0	0	—	13.806(22)	0.0	
0	0.297(7)	0.689(7)	$> -0.08$	$> -0.25$	—	13.796(24)	0.02	
-2	0.297(7)	0.688(7)	$> -0.06$	$> -0.61$	—	13.795(25)	0.02	
-4	0.289(6), 0.298(7)	0.700(9), 0.686(7)	$-0.057(2), > -0.048$	$-0.86(3), > -0.73$	2.31(12), —	13.714(25), 13.791(26)	1.0, 0.02	
-6	0.292(6), 0.299(6)	0.699(9), 0.685(7)	$-0.039(1), > -0.037$	$-0.86(3), > -0.77$	2.31(12), —	13.715(25), 13.792(27)	2.0, 0.01	
-10	0.294(6), 0.299(6)	0.696(8), 0.684(7)	$-0.025(1), > -0.021$	$-0.86(3), > -0.69$	2.32(12), —	13.722(27), 13.797(25)	4.4, 0.02	
-14	0.296(6), 0.300(6)	0.695(8), 0.683(7)	$-0.019(1), > -0.017$	$-0.86(3), > -0.76$	2.33(12), —	13.719(31), 13.794(27)	5.3, 0.01	
-20	0.297(6), 0.300(6)	0.696(9), 0.683(7)	$-0.013(1), > -0.012$	$-0.86(3), > -0.76$	2.32(12), —	13.718(31), 13.795(26)	6.0, 0.02	
$\lambda$ free	-17.9(5.8)	0.296(6), 0.299(7)	0.697(9), 0.684(8)	$-0.017(8), > -0.074$	$-0.85(4), > -0.69$	2.32(19), —	13.719(30), 13.795(24)	6.4, 0.01







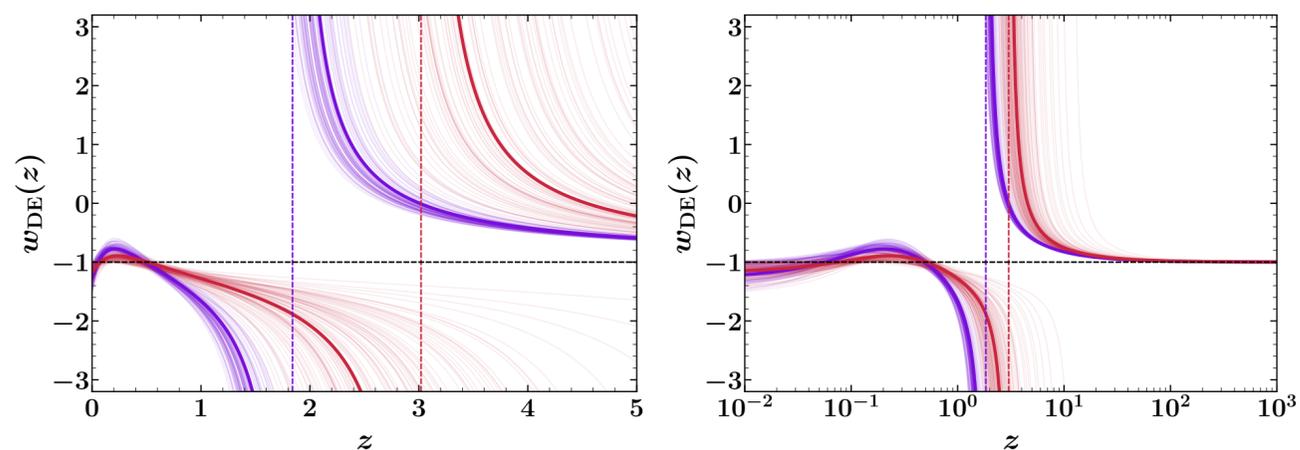
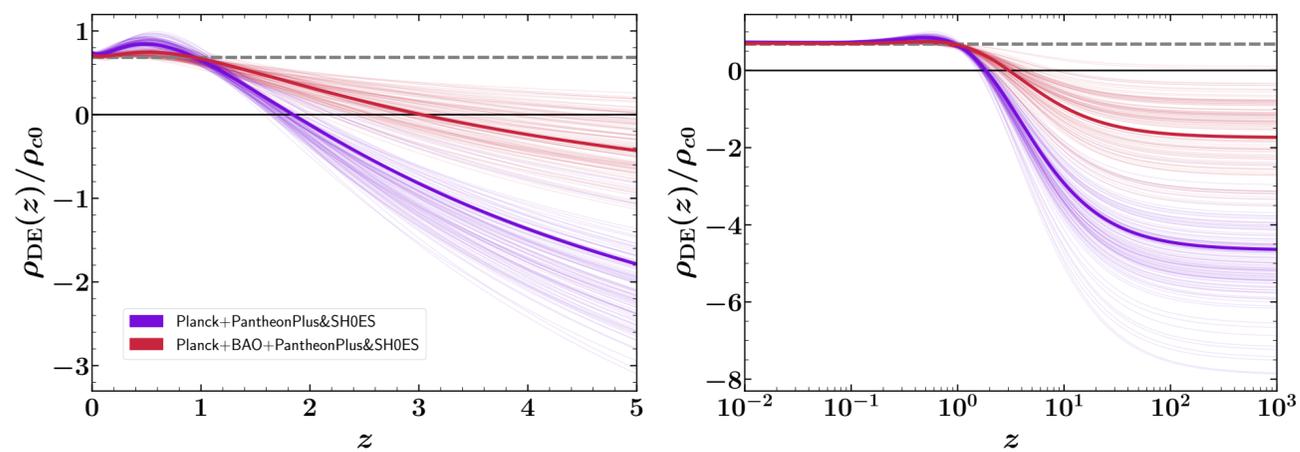
# Omnipotent dark energy: A phenomenological answer to the Hubble tension

(Adil, Akarsu, Di Valentino, Nunes, Ozulker, Sen, Specogna, arXiv:2306.08046)

Density	EoS	Scaling in $z$	Scaling in $a$	Naming
$\rho > 0$	$w > -1$	$d\rho/dz > 0$	$d\rho/da < 0$	p-quintessence
	$w = -1$	$d\rho/dz = 0$	$d\rho/da = 0$	positive-CC
	$w < -1$	$d\rho/dz < 0$	$d\rho/da > 0$	p-phantom
$\rho < 0$	$w > -1$	$d\rho/dz < 0$	$d\rho/da > 0$	n-quintessence
	$w = -1$	$d\rho/dz = 0$	$d\rho/da = 0$	negative-CC
	$w < -1$	$d\rho/dz > 0$	$d\rho/da < 0$	n-phantom

**An example:** DMS20 parametrization, Di Valentino, Mukherjee & Sen, Entropy 2021, arXiv:2005.12587

$$\rho_{\text{DE}}(a) = \rho_{\text{DE}0} \frac{1 + \alpha(a - a_m)^2 + \beta(a - a_m)^3}{1 + \alpha(1 - a_m)^2 + \beta(1 - a_m)^3}$$

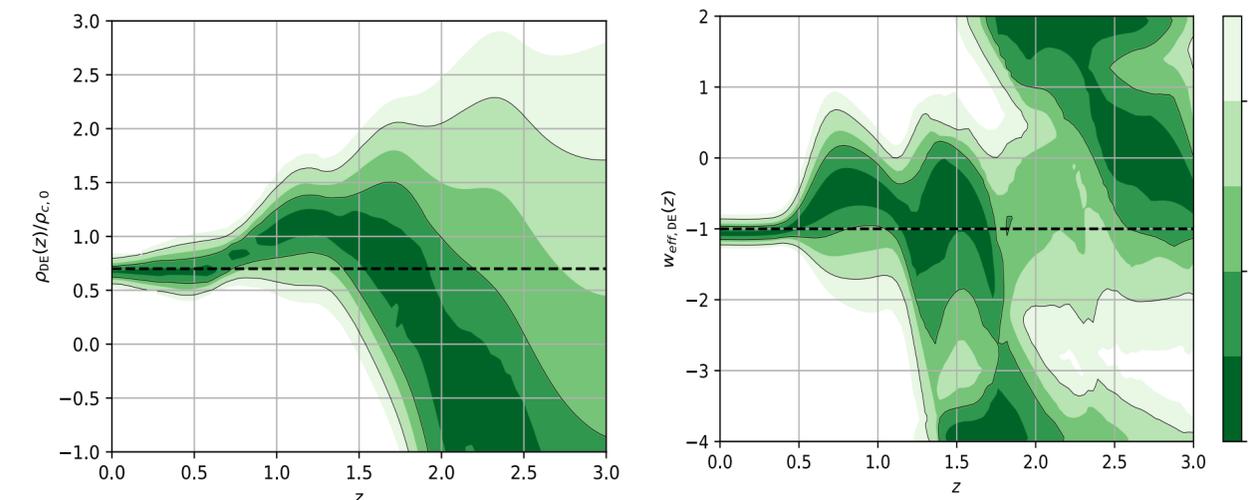
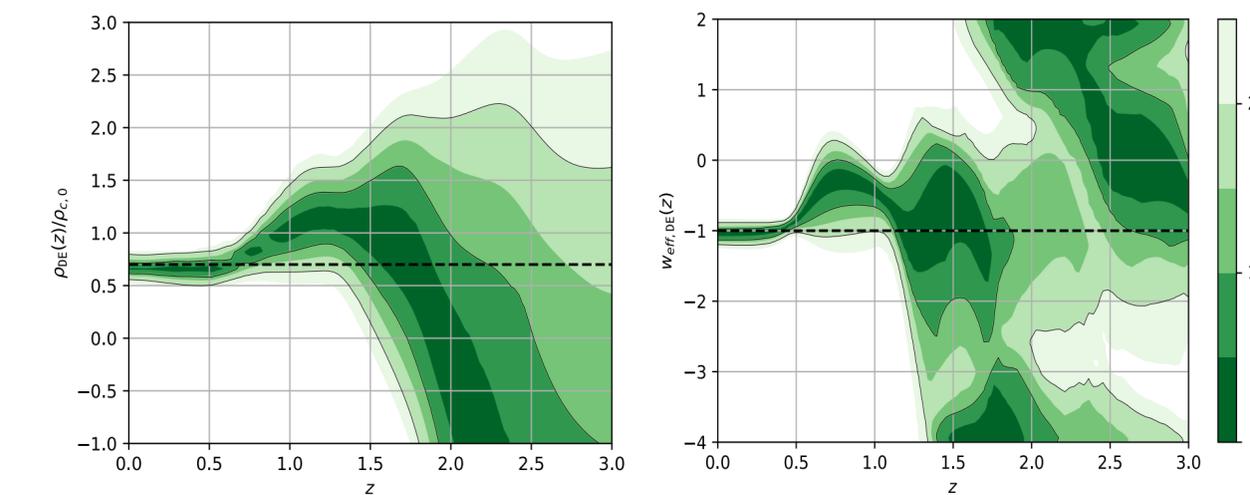
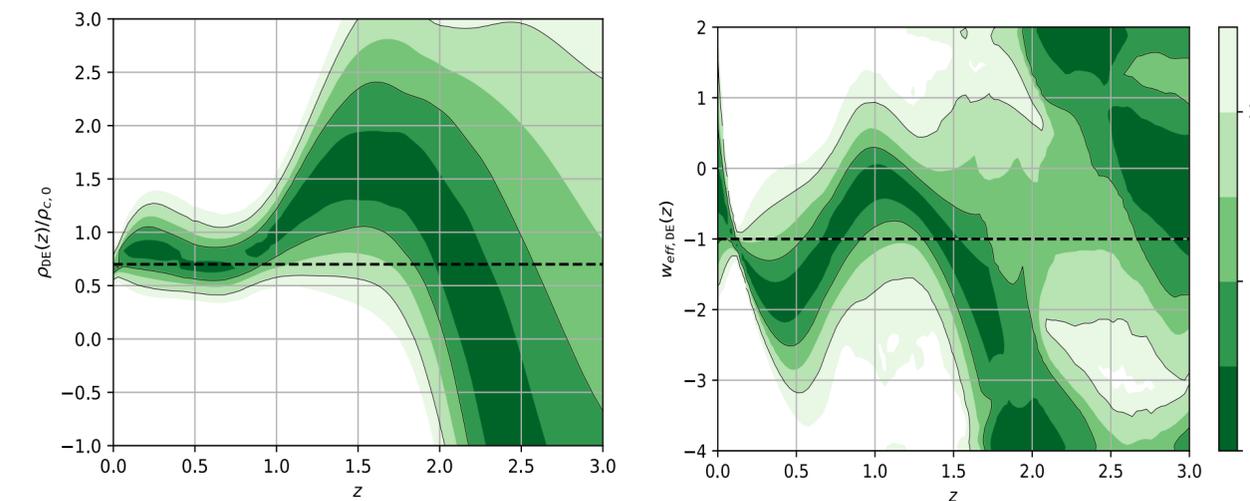


# Model-independent reconstruction of the Interacting Dark Energy

**Kernel: Binned and Gaussian process** (Escamilla, Akarsu, Di

Valentino, Vazquez, arXiv:2305.16290)

See Luis' talk



## Some theoretical realizations...?

### The meaning of imaginary space (Alexandre, Gielen & Magueijo arXiv:2306.11502)

They show that a classical metric signature change across boundaries with a degenerate metric in different formulations of general relativity allows for classical solutions where the open dS patch can arise from a portion of AdS space time.

$$\tilde{\Lambda} = \text{sgn}(\tilde{a}^2) \Lambda$$

### Constructing 4D $\Lambda_s$ CDM models from the presence higher dimensions (Akarsu, Bulduk, Katırcı, Özüiker, Perivolaropoulos, in progress)

$$ds^2 = -dt^2 + a^2(t) (dx_1^2 + dx_2^2 + dx_3^2) + s^2(t) \frac{dy_1^2 + \dots + dy_n^2}{\left[1 + \frac{k_{\text{int}}}{4} (y_1^2 + \dots + y_n^2)\right]^2}$$

$$\tilde{T}_\mu^\nu = \text{diag}[-\tilde{\rho}, \tilde{p}_{\text{ext}}, \tilde{p}_{\text{ext}}, \tilde{p}_{\text{ext}}, \tilde{p}_{\text{int}}, \dots, \tilde{p}_{\text{int}}]$$

$$\tilde{\chi} = \tilde{\Lambda} - \frac{n(n-1)}{2} \frac{k_{\text{int}}}{s^2}$$

$$k_{\text{int}} < 0$$

(Stability condition)

$$\tilde{w}_{\text{ext}} = 0 \quad \tilde{w}_{\text{int}} = -\frac{1}{2} + \left( \frac{(n-1)(n+2)}{2\tilde{\kappa}} \frac{k_{\text{int}}}{s_*^2} - \frac{\tilde{\Lambda}}{\tilde{\kappa}} \right) \frac{a^3}{\rho_{\text{m}0}}$$

$$G_{4\text{D}} \propto \frac{1}{V_{\text{int}}} \propto \frac{\tilde{G}}{s^n} \longrightarrow \frac{G_{4\text{D}0}}{G_{4\text{D}p}} = \left( \frac{s_p}{s_0} \right)^n = \left( \frac{\tilde{\chi}_0 - \tilde{\Lambda}}{\tilde{\chi}_p - \tilde{\Lambda}} \right)^{n/2}$$

$$a \rightarrow 0 \quad \tilde{w}_{\text{ext}} = 0 \quad \tilde{w}_{\text{int}} \rightarrow -\frac{1}{2}$$

**(black strings/branes)** Akarsu, Chopovsky, Zhuk, PLB 2018, arXiv:1711.08372: Satisfy the gravitational tests for the parameterized post-Newtonian parameter  $\gamma$  at the same level of accuracy as GR. Preferable from the thermodynamical point of view. Averaging over the Universe, they do not destroy the stabilization of the internal space.

?: Rapid transition of Geff at  $z \approx 0.01$  as a possible solution of the Hubble and growth tensions, Marra & Perivolaropoulos, PRD 2021, arXiv:2102.06012

$\Lambda_s$  CDM MODEL: SIGN-SWITCHING  $\Lambda$ 

$$\frac{\rho_{\text{DE}}}{\rho_{\text{c},0}} \rightarrow \Omega_{\text{DE},0} \text{sgn}[1 - \Psi \ln a] \quad \text{as} \quad \lambda \rightarrow -\infty$$

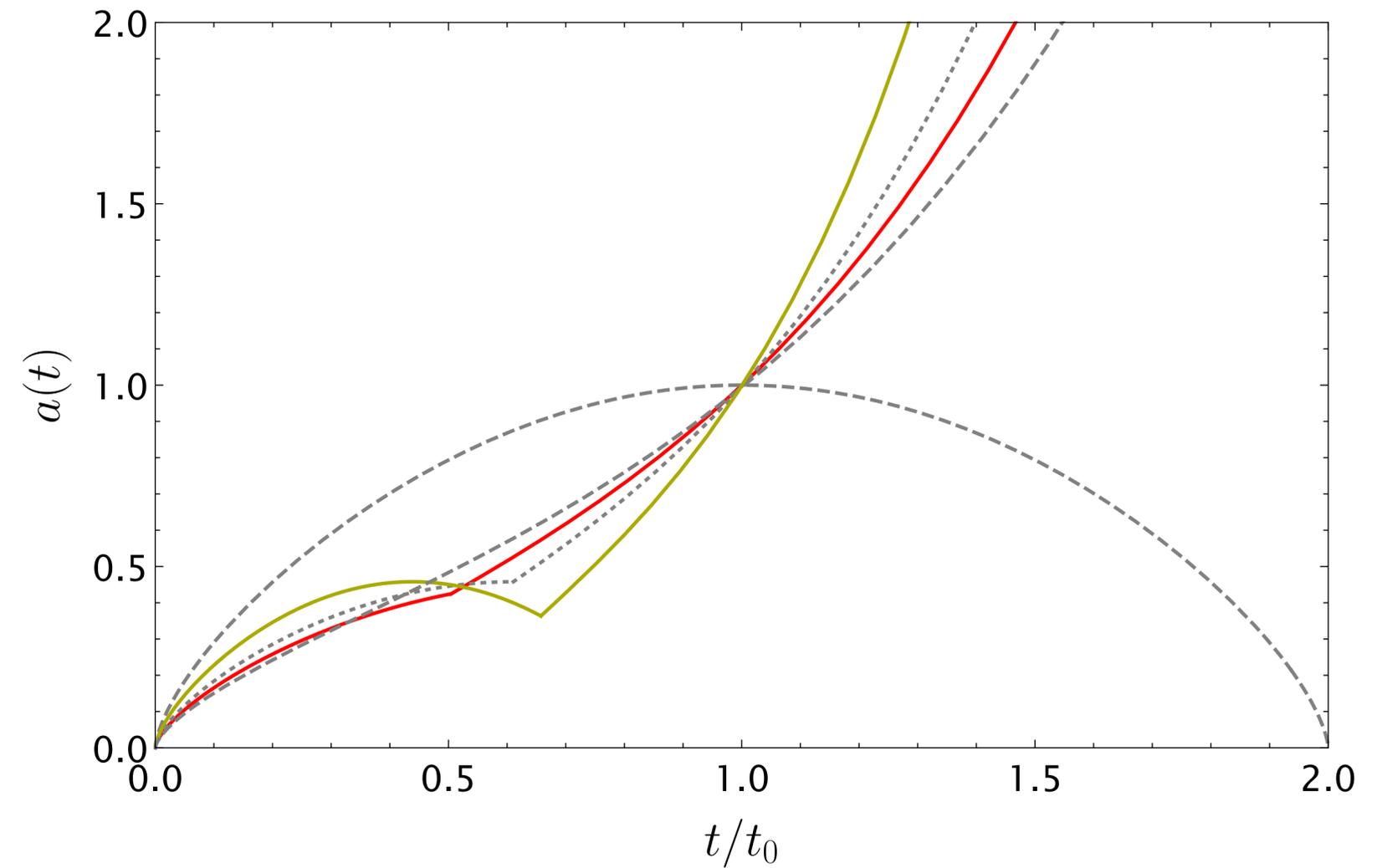
$$\Lambda \rightarrow \Lambda_s \equiv \Lambda_{s0} \text{sgn}[z_{\dagger} - z]$$

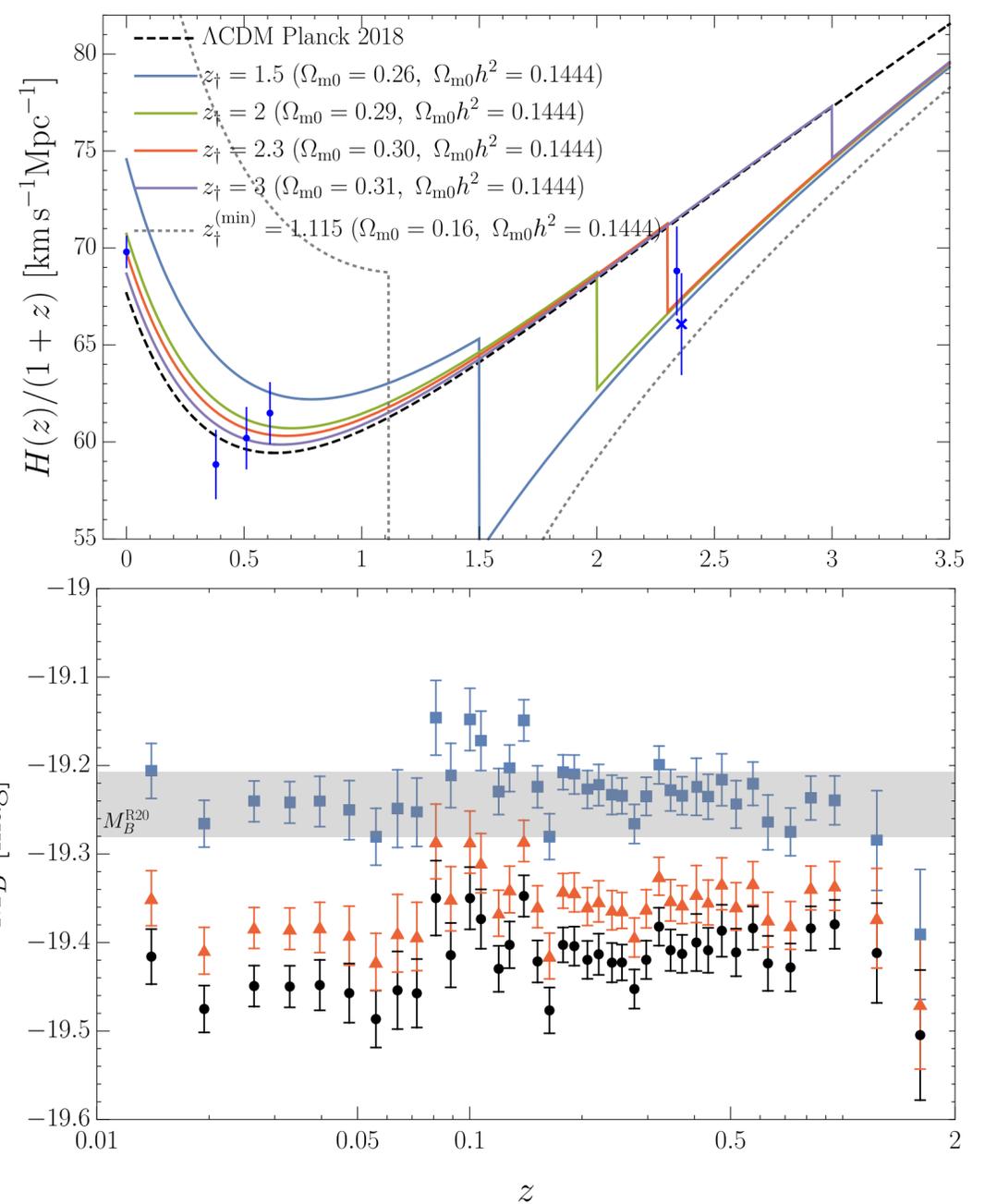
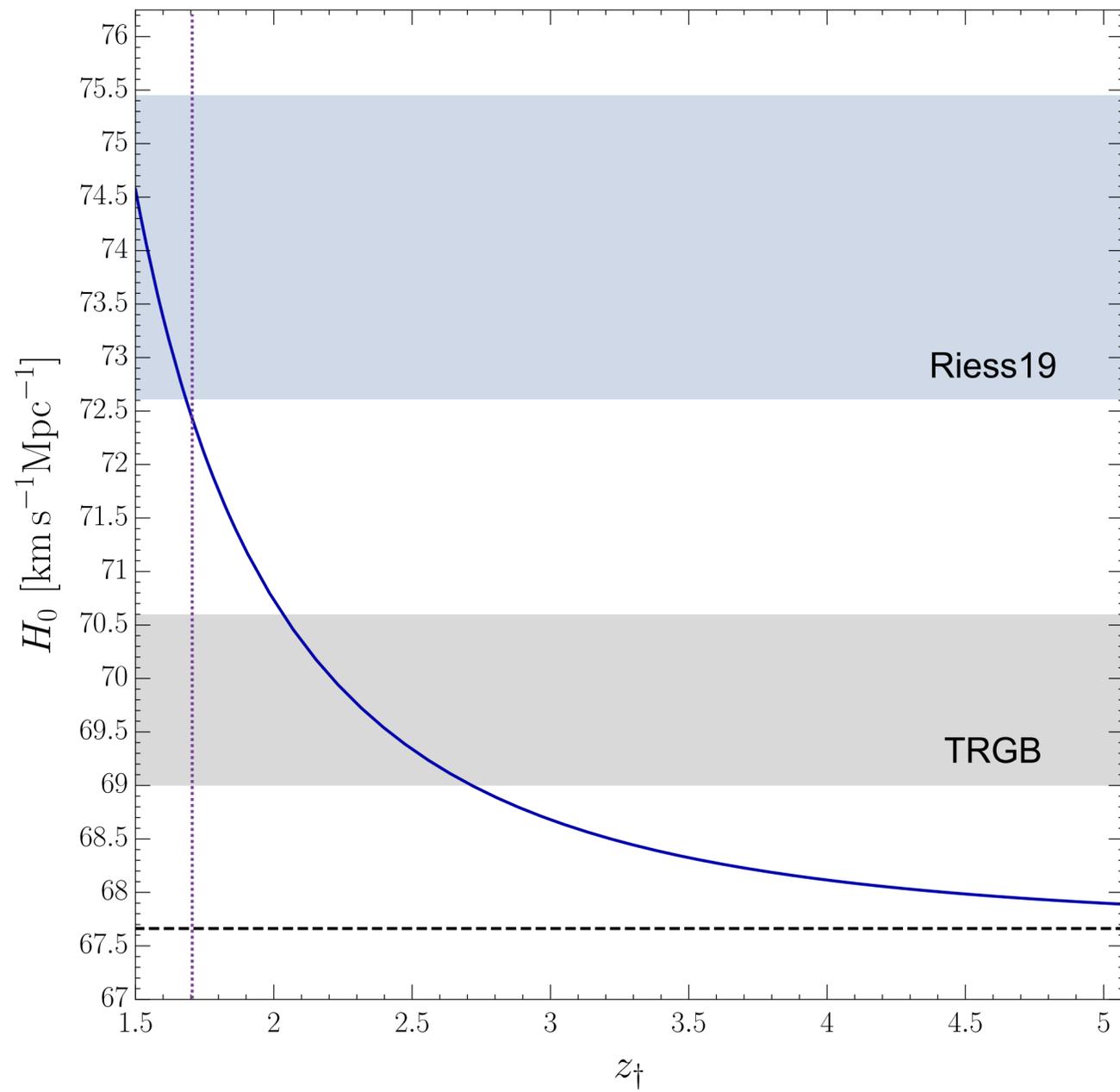
$$a(t) = \begin{cases} A^{\frac{1}{3}} \sin^{\frac{2}{3}} \left( \frac{3}{2} \sqrt{\frac{\Lambda_{s0}}{3}} t \right) & \text{for } t \leq t_{\dagger}, \\ A^{\frac{1}{3}} \sinh^{\frac{2}{3}} \left[ \frac{3}{2} \left( \sqrt{\frac{\Lambda_{s0}}{3}} t + B \right) \right] & \text{for } t \geq t_{\dagger}, \end{cases}$$

where

$$A = \sinh^{-2} \left[ \frac{3}{2} \left( \sqrt{\frac{\Lambda_{s0}}{3}} t_0 + B \right) \right],$$

$$B = \text{arcsinh} \left[ \sin \left( \frac{3}{2} \sqrt{\frac{\Lambda_{s0}}{3}} t_{\dagger} \right) - \frac{3}{2} \sqrt{\frac{\Lambda_{s0}}{3}} t_{\dagger} \right],$$





The figures are plotted by fixing  $D_M(z_*)$  and  $\rho_m(z_*)$  (and hence  $\rho_{m0}$ ) to that of  $\Lambda$ CDM using the mean values of the *Planck* 2018 TT,TE,EE+lowE+lensing results.

Angular scale of the sound horizon at last scattering

$$\theta_* = \frac{r_*}{D_M(z_*)}$$

Comoving sound horizon at last scattering

$$r_* = \int_{z_*}^{\infty} \frac{c_s(z)}{H_{\Lambda\text{CDM}}(z)} dz$$

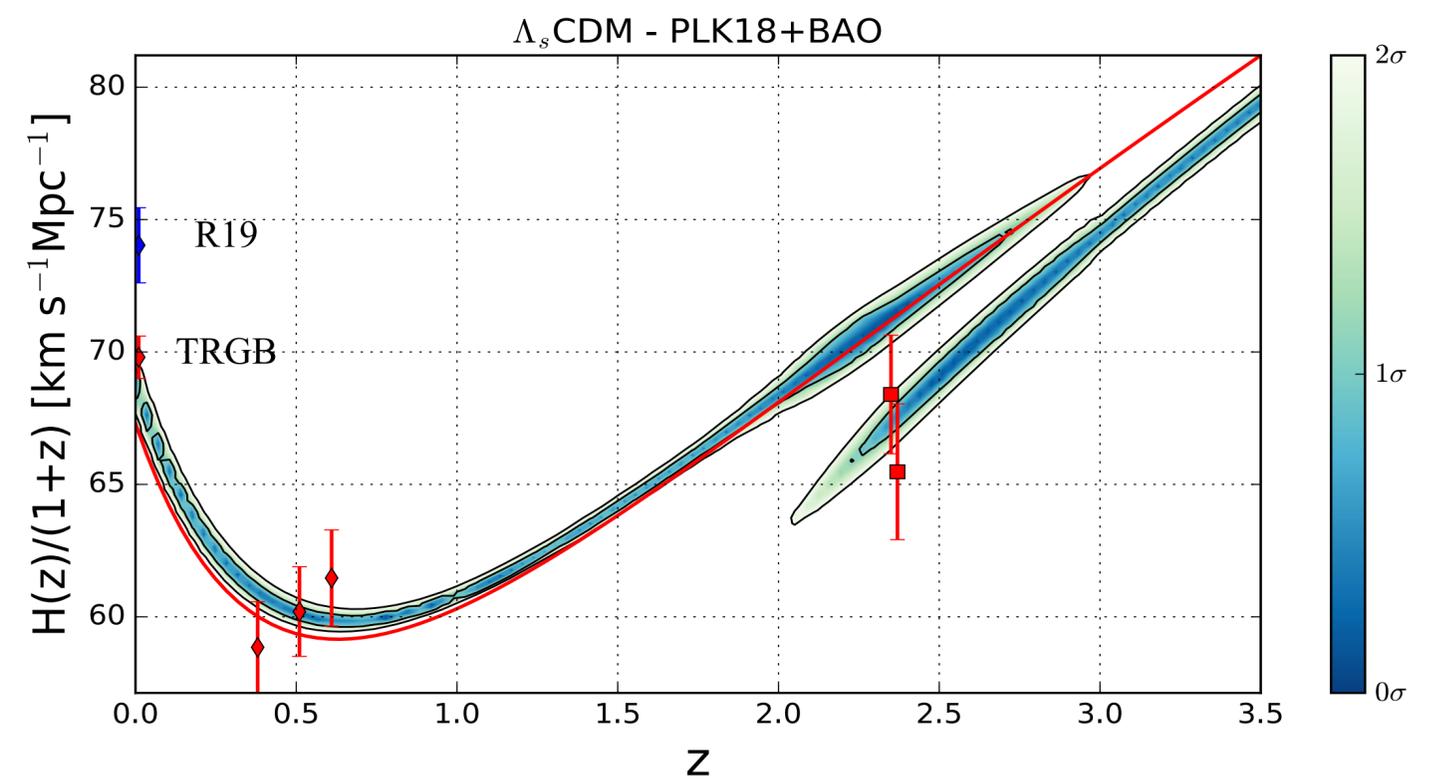
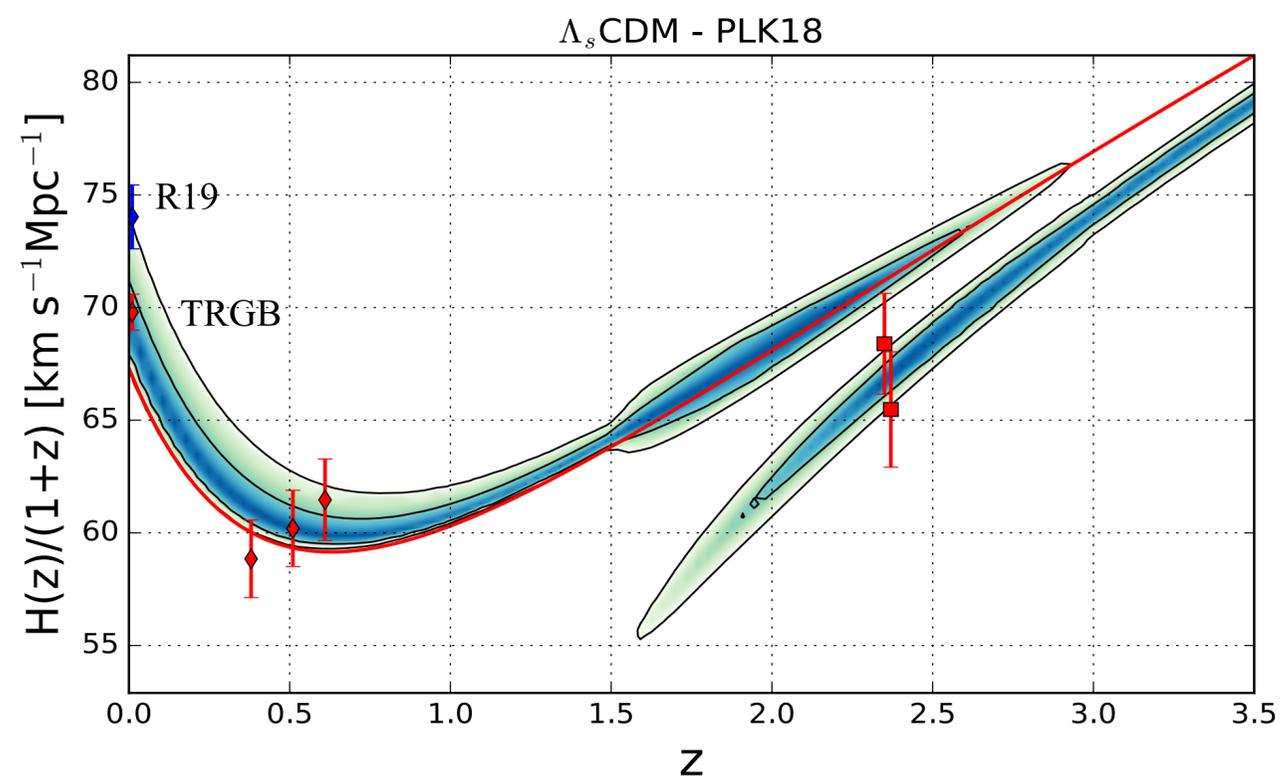
Comoving angular diameter distance out to last scattering

$$D_M(z_*) = c \int_0^{z_*} \frac{dz}{H(z)}$$

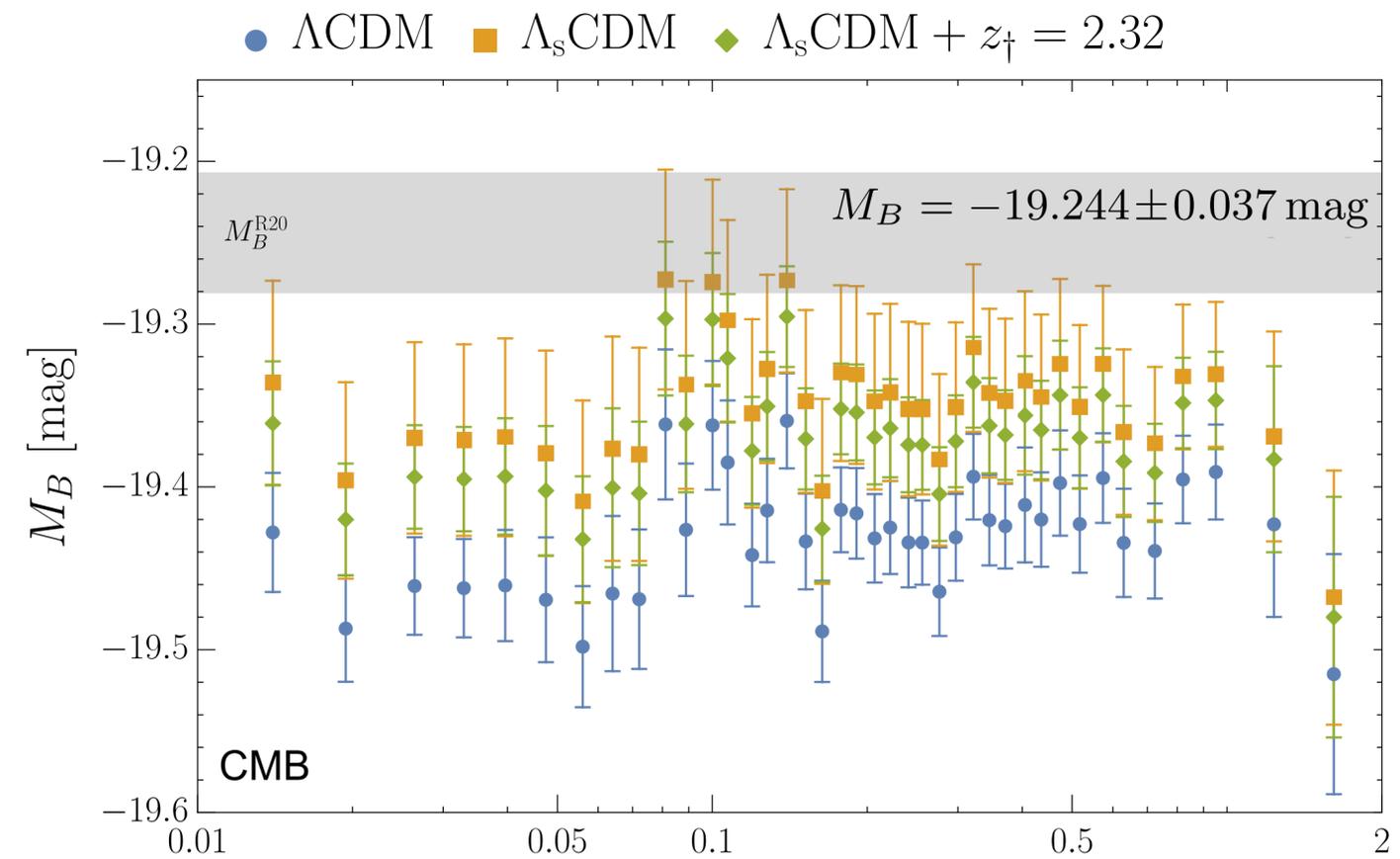
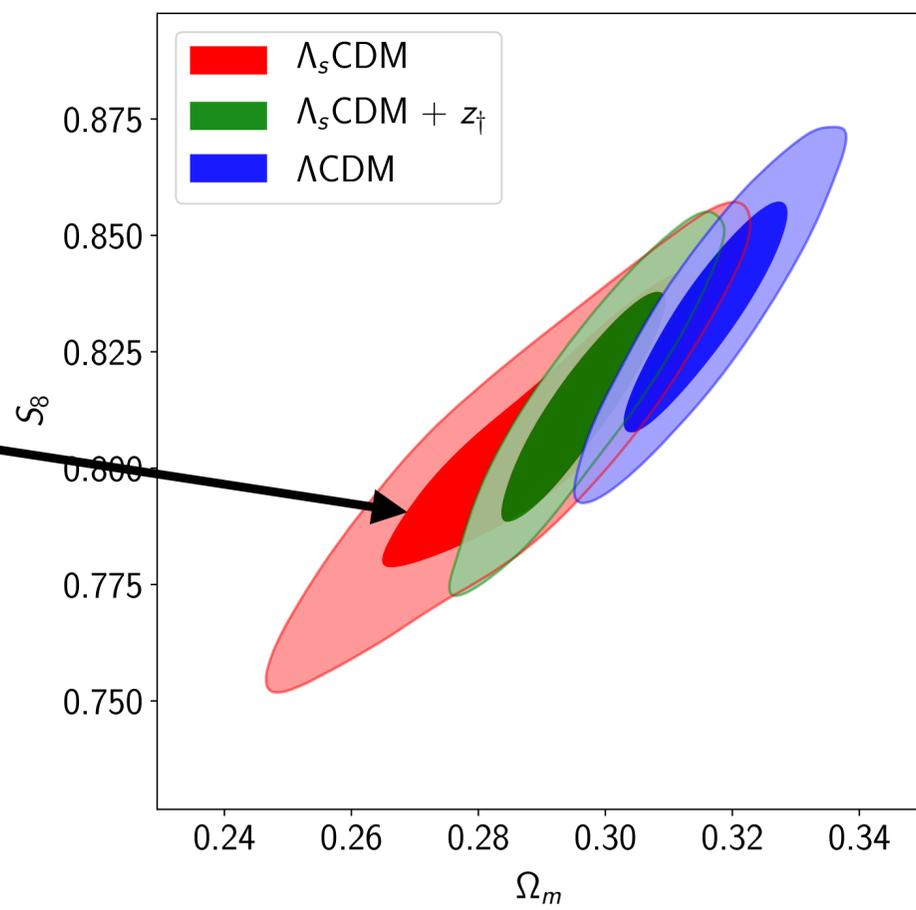
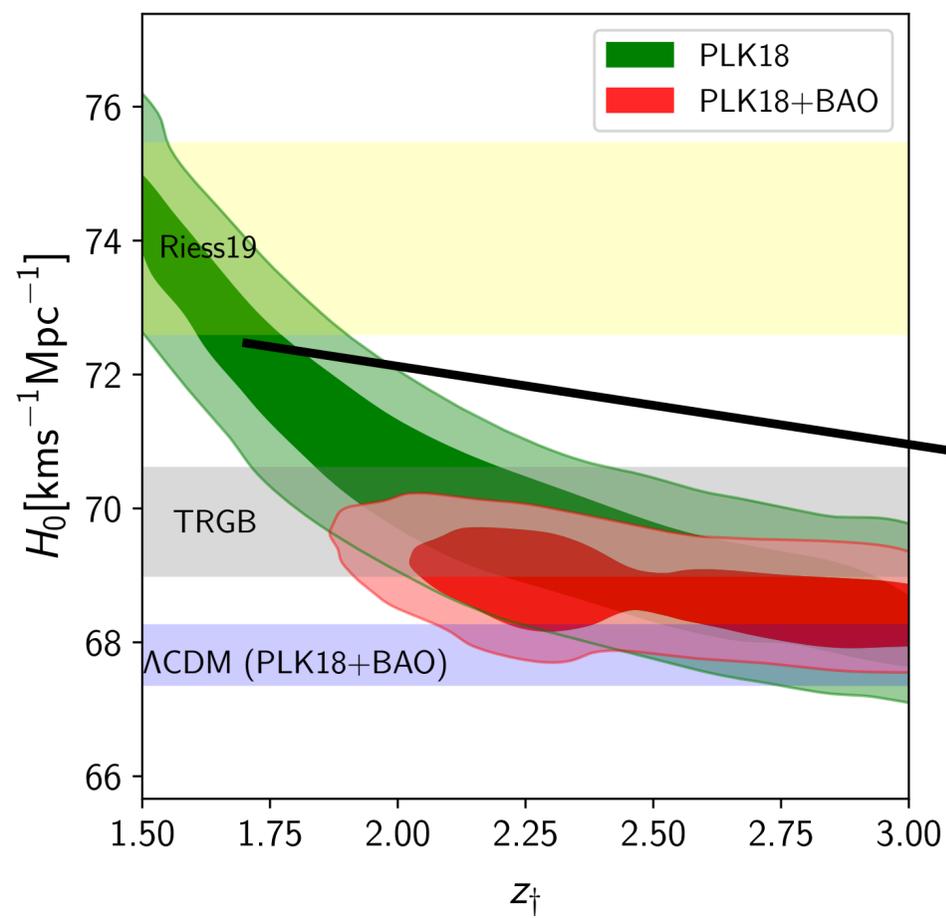
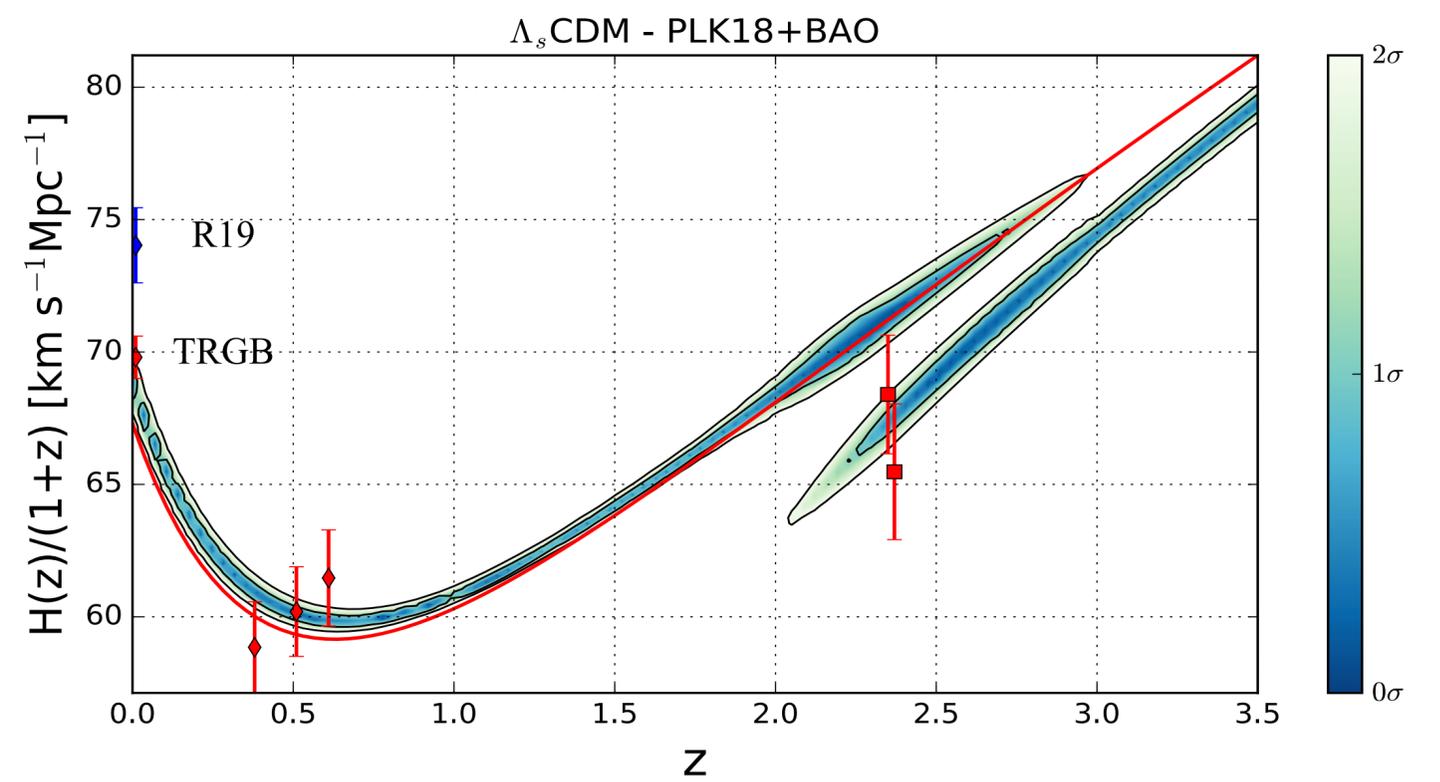
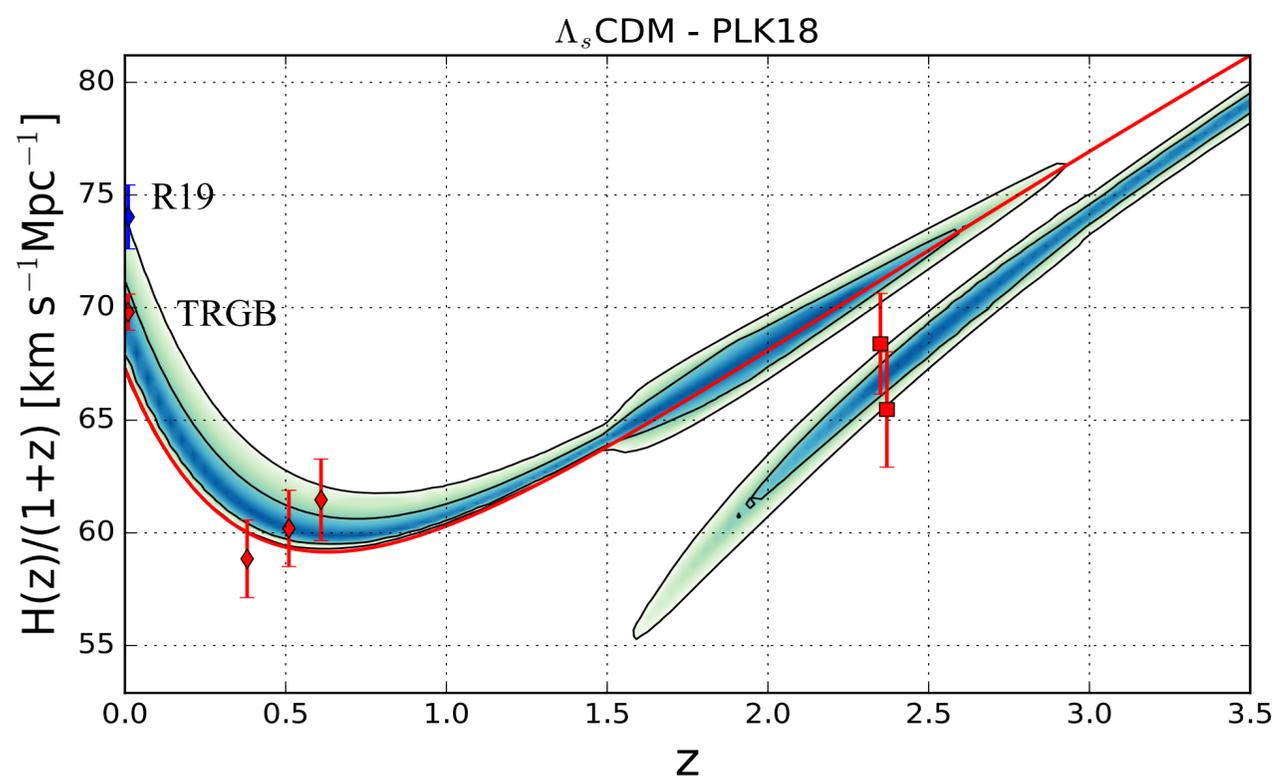
$100\theta_* = 1.04110 \pm 0.00031$  ( $\Lambda$ CDM PL18)

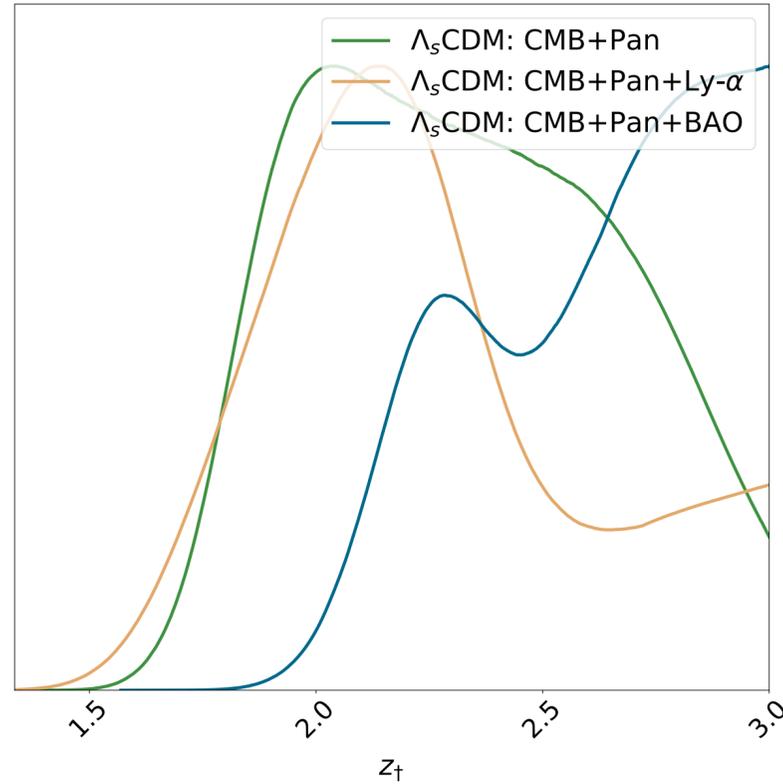
$r_* = 144.43 \pm 0.26$  Mpc ( $\Lambda$ CDM PL18)

$D_M(z_*) = 13872.83 \pm 25.31$  Mpc ( $\Lambda$ CDM PL18)

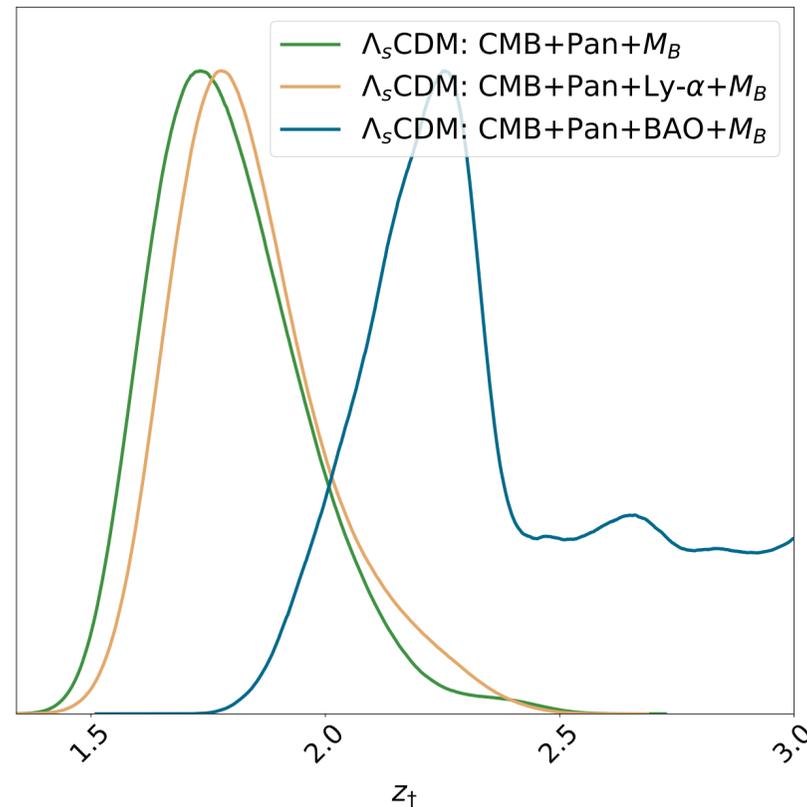


Data set	CMB			CMB+BAO		
	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda_s$ CDM+ $z_{\dagger} = 2.32$	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda_s$ CDM+ $z_{\dagger} = 2.32$
$10^2 \omega_b$	$2.235 \pm 0.015$	$2.238 \pm 0.015$	$2.238 \pm 0.015$	$2.244 \pm 0.013$	$2.231 \pm 0.014$	$2.230 \pm 0.013$
$\omega_c$	$0.1201 \pm 0.0014$	$0.1197 \pm 0.0013$	$0.1199 \pm 0.0013$	$0.1189 \pm 0.0009$	$0.1208 \pm 0.0011$	$0.1209 \pm 0.0009$
$100\theta_s$	$1.04090 \pm 0.00031$	$1.04093 \pm 0.00030$	$1.04091 \pm 0.00031$	$1.04102 \pm 0.00029$	$1.04081 \pm 0.00029$	$1.04080 \pm 0.00029$
$\ln(10^{10} A_s)$	$3.044 \pm 0.016$	$3.043 \pm 0.016$	$3.043 \pm 0.016$	$3.045 \pm 0.016$	$3.043 \pm 0.016$	$3.043 \pm 0.016$
$n_s$	$0.9646 \pm 0.0043$	$0.9657 \pm 0.0044$	$0.9655 \pm 0.0044$	$0.9673 \pm 0.0037$	$0.9633 \pm 0.0039$	$0.9632 \pm 0.0036$
$\tau_{\text{reio}}$	$0.0543 \pm 0.0078$	$0.0542 \pm 0.0078$	$0.0541 \pm 0.0078$	$0.0559 \pm 0.0078$	$0.0530 \pm 0.0077$	$0.0526 \pm 0.0075$
$z_{\dagger}$	—	unconstrained	[2.32]	—	$2.44 \pm 0.29$	[2.32]
$\Omega_m$	$0.3162 \pm 0.0084$	$0.2900 \pm 0.0160$	$0.2967 \pm 0.0086$	$0.3090 \pm 0.0059$	$0.3035 \pm 0.0062$	$0.3029 \pm 0.0060$
$H_0$	$67.29 \pm 0.60$	$70.22 \pm 1.78$	$69.42 \pm 0.71$	$67.81 \pm 0.44$	$68.82 \pm 0.55$	$68.91 \pm 0.48$
$\sigma_8$	$0.8117 \pm 0.0076$	$0.8223 \pm 0.0098$	$0.8186 \pm 0.0074$	$0.8090 \pm 0.0073$	$0.8207 \pm 0.0080$	$0.8215 \pm 0.0071$
$S_8$	$0.8332 \pm 0.0163$	$0.8071 \pm 0.0210$	$0.8138 \pm 0.0166$	$0.8219 \pm 0.0127$	$0.8255 \pm 0.0128$	$0.8264 \pm 0.0126$
$-2 \ln \mathcal{L}_{\text{max}}$	1386.52	1385.73	1386.56	1394.32	1393.77	1393.54
$\ln \mathcal{Z}$	-1424.19	-1424.22	-1423.50	-1431.46	-1432.77	-1431.89
$\Delta \ln \mathcal{Z}$	0.69	0.72	0	0	1.31	0.43

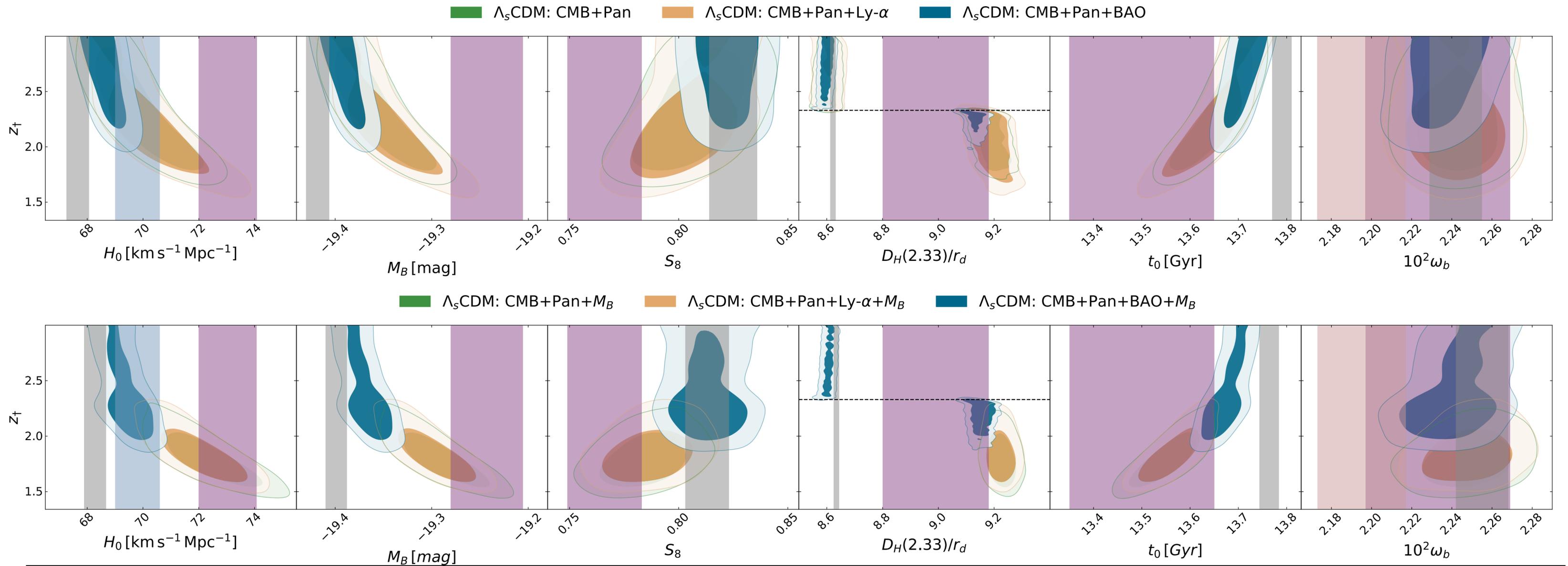




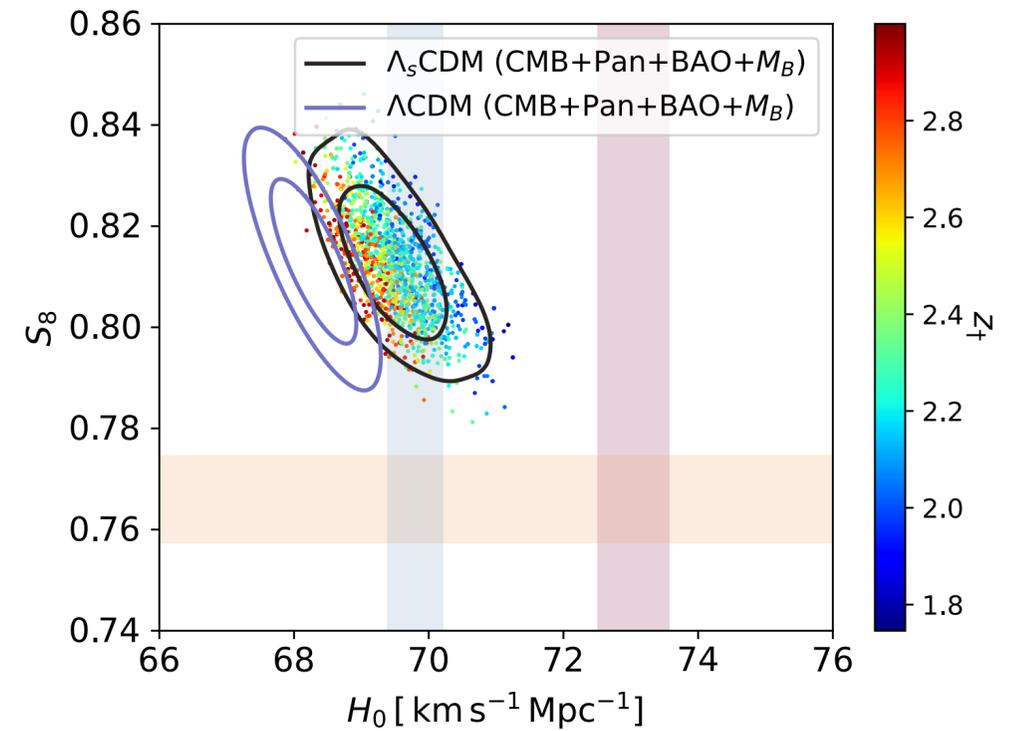
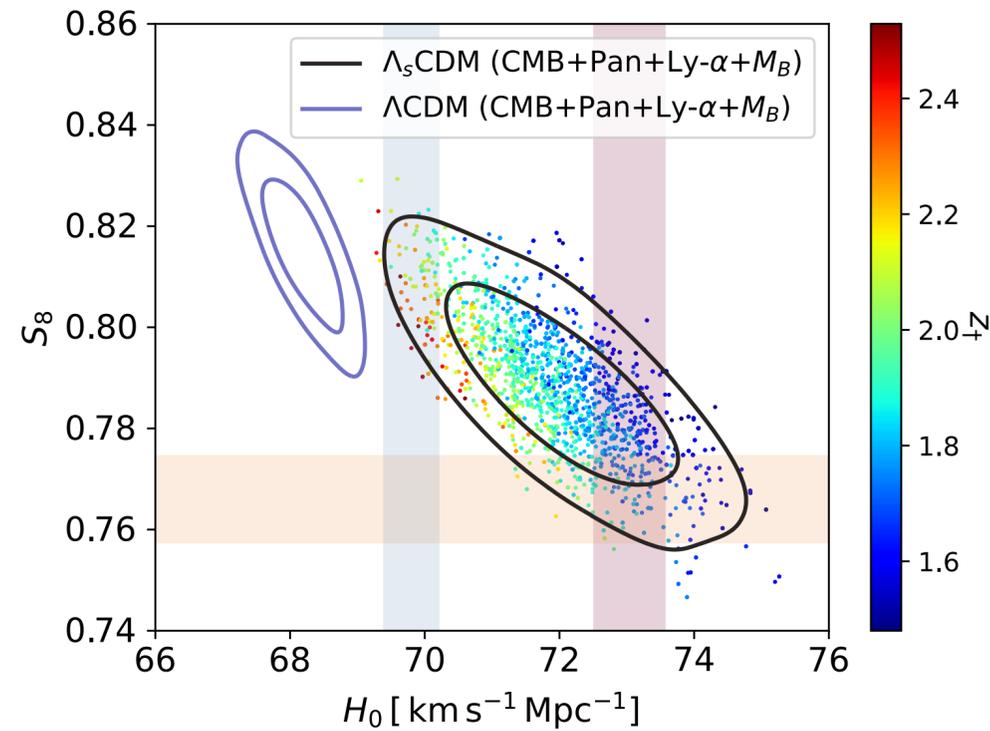
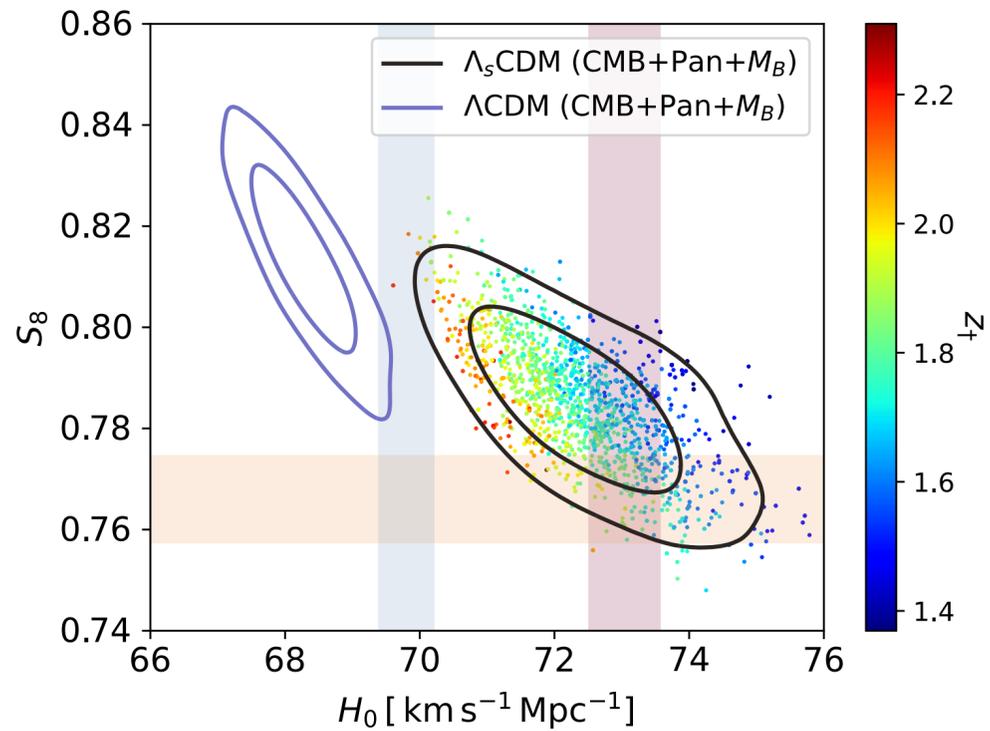
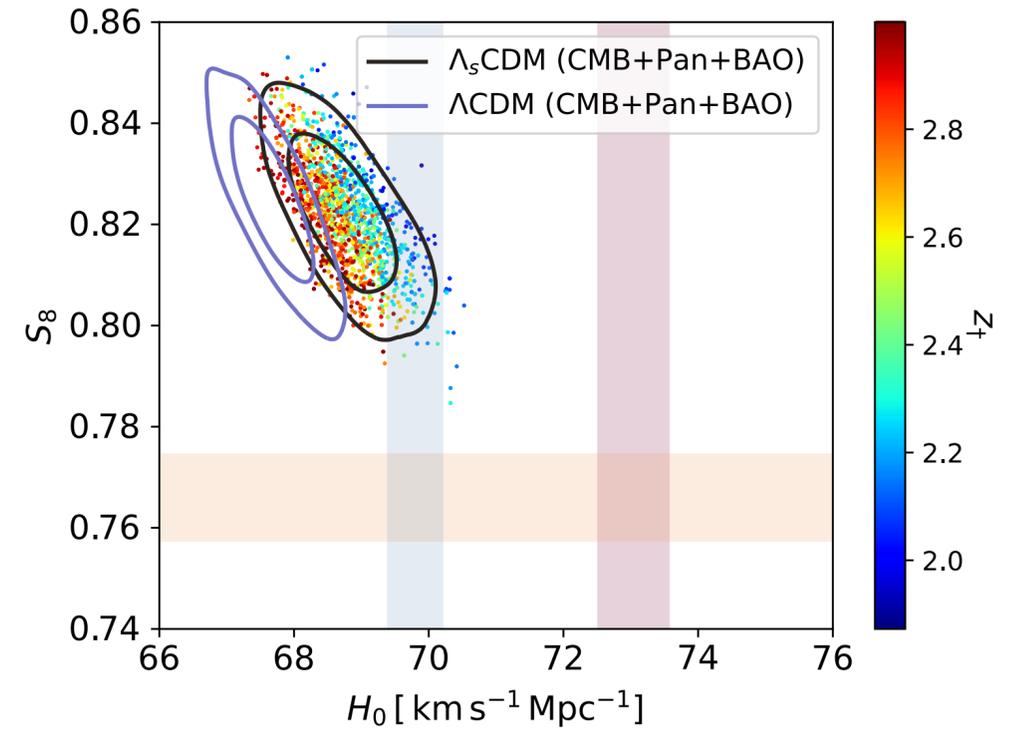
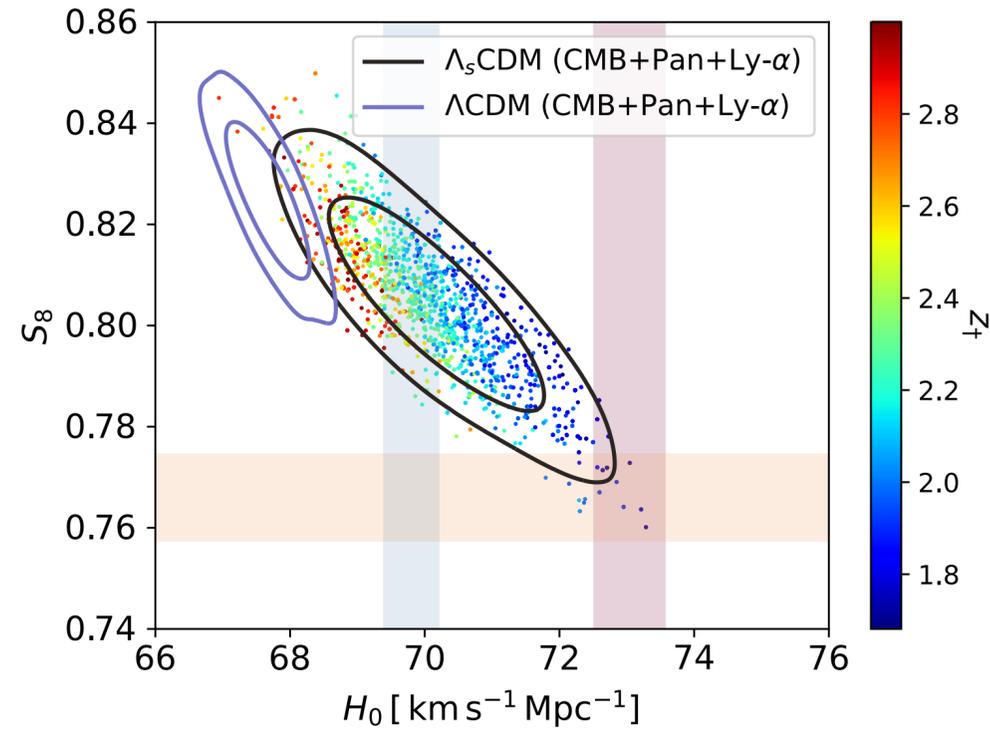
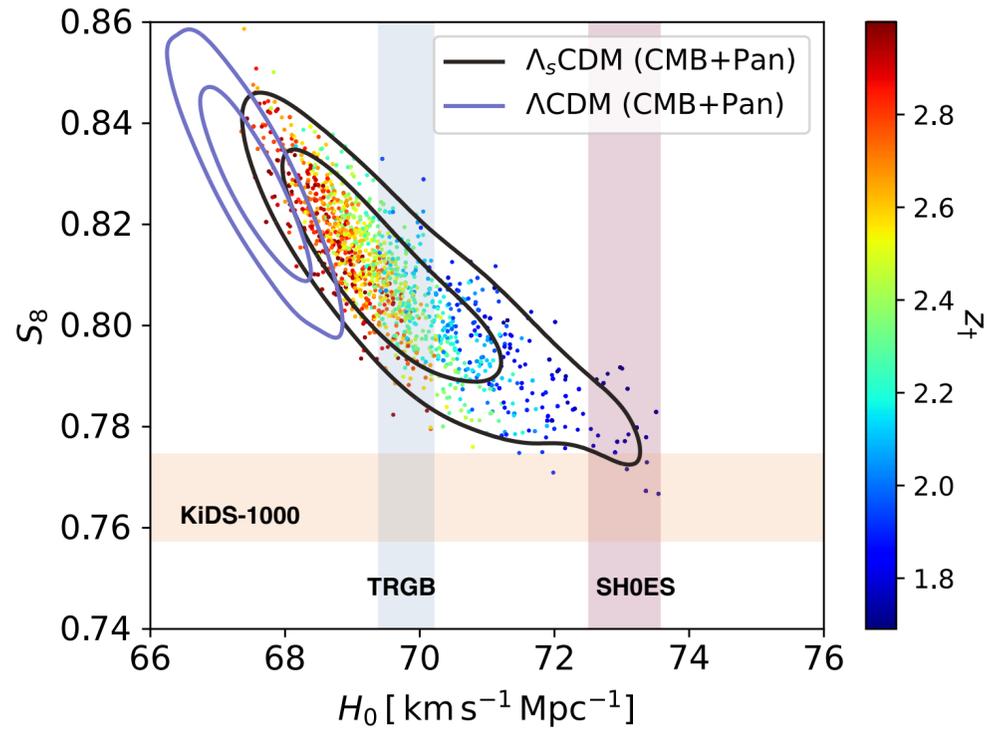
Data set	CMB+Pan		CMB+Pan+Ly- $\alpha$		CMB+Pan+BAO	
	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM
$10^2 \omega_b$	$2.240 \pm 0.015$	$2.241 \pm 0.014$	$2.242 \pm 0.013$	$2.241 \pm 0.015$	$2.242 \pm 0.013$	$2.235 \pm 0.014$
$\omega_c$	$0.1197 \pm 0.0012$	$0.1196 \pm 0.0011$	$0.1193 \pm 0.0009$	$0.1196 \pm 0.0011$	$0.1193 \pm 0.0009$	$0.1206 \pm 0.0010$
$100\theta_s$	$1.04191 \pm 0.00029$	$1.04190 \pm 0.00028$	$1.04191 \pm 0.00029$	$1.04190 \pm 0.00029$	$1.04194 \pm 0.00028$	$1.04180 \pm 0.00030$
$\ln(10^{10} A_s)$	$3.047 \pm 0.015$	$3.041 \pm 0.014$	$3.047 \pm 0.014$	$3.040 \pm 0.015$	$3.047 \pm 0.015$	$3.040 \pm 0.014$
$n_s$	$0.9662 \pm 0.0042$	$0.9668 \pm 0.0040$	$0.9669^{+0.0039}_{-0.0036}$	$0.9668 \pm 0.0041$	$0.9665 \pm 0.0037$	$0.9644 \pm 0.0037$
$\tau_{\text{reio}}$	$0.0556 \pm 0.0075$	$0.0533 \pm 0.0075$	$0.0560 \pm 0.0069$	$0.0528 \pm 0.0077$	$0.0561 \pm 0.0076$	$0.0515 \pm 0.0073$
$z_{\dagger}$	—	$> 1.80$ (95% CL)	—	$2.21^{+0.16}_{-0.38}$	—	$> 2.13$ (95% CL)
$M_B$ [mag]	$-19.421 \pm 0.014$	$-19.363^{+0.021}_{-0.037}$	$-19.418 \pm 0.011$	$-19.349 \pm 0.028$	$-19.418 \pm 0.012$	$-19.387 \pm 0.015$
$\Omega_m$	$0.3129 \pm 0.0071$	$0.2940^{+0.0120}_{-0.0093}$	$0.3110 \pm 0.0053$	$0.2899 \pm 0.0097$	$0.3109 \pm 0.0056$	$0.3039 \pm 0.0058$
$\omega_m$	$0.1427 \pm 0.0011$	$0.1427 \pm 0.0010$	$0.1424 \pm 0.0008$	$0.1426 \pm 0.0010$	$0.1424 \pm 0.0009$	$0.1436 \pm 0.0010$
$H_0$ [km/s/Mpc]	$67.55 \pm 0.53$	$69.68^{+0.77}_{-1.40}$	$67.68 \pm 0.40$	$70.17^{+0.96}_{-1.10}$	$67.69^{+0.38}_{-0.43}$	$68.74^{+0.49}_{-0.55}$
$t_0$ [Gyr]	$13.79 \pm 0.02$	$13.65^{+0.06}_{-0.04}$	$13.79 \pm 0.02$	$13.62^{+0.09}_{-0.03}$	$13.79 \pm 0.02$	$13.71^{+0.03}_{-0.02}$
$\sigma_8$	$0.8111^{+0.0056}_{-0.0063}$	$0.8167^{+0.0059}_{-0.0067}$	$0.8104 \pm 0.0060$	$0.8182 \pm 0.0066$	$0.8101 \pm 0.0063$	$0.8167 \pm 0.0062$
$S_8$	$0.828 \pm 0.013$	$0.809 \pm 0.015$	$0.825 \pm 0.010$	$0.804 \pm 0.014$	$0.825 \pm 0.011$	$0.822 \pm 0.010$
$-2 \ln \mathcal{L}_{\text{max}}$	1903.62	1902.50	1909.68	1903.44	1909.63	1909.53
$\ln \mathcal{Z}$	-1937.82	-1938.02	-1944.53	-1939.75	-1944.51	-1944.76
$\Delta \ln \mathcal{Z}$	0	0.20	4.78	0	0	0.25

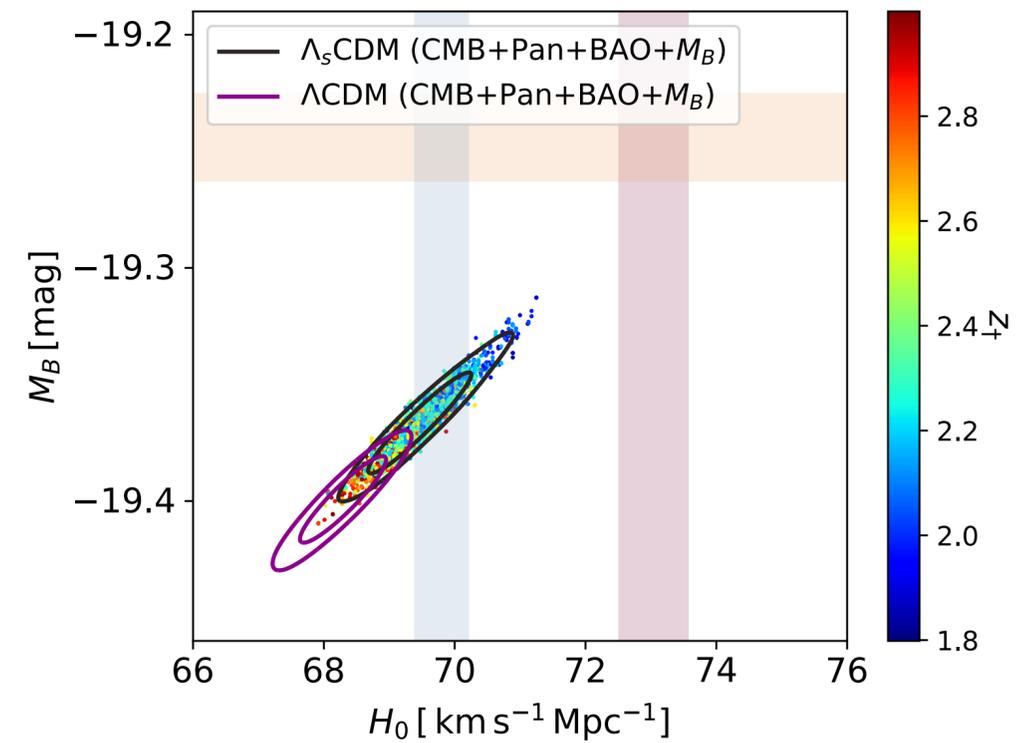
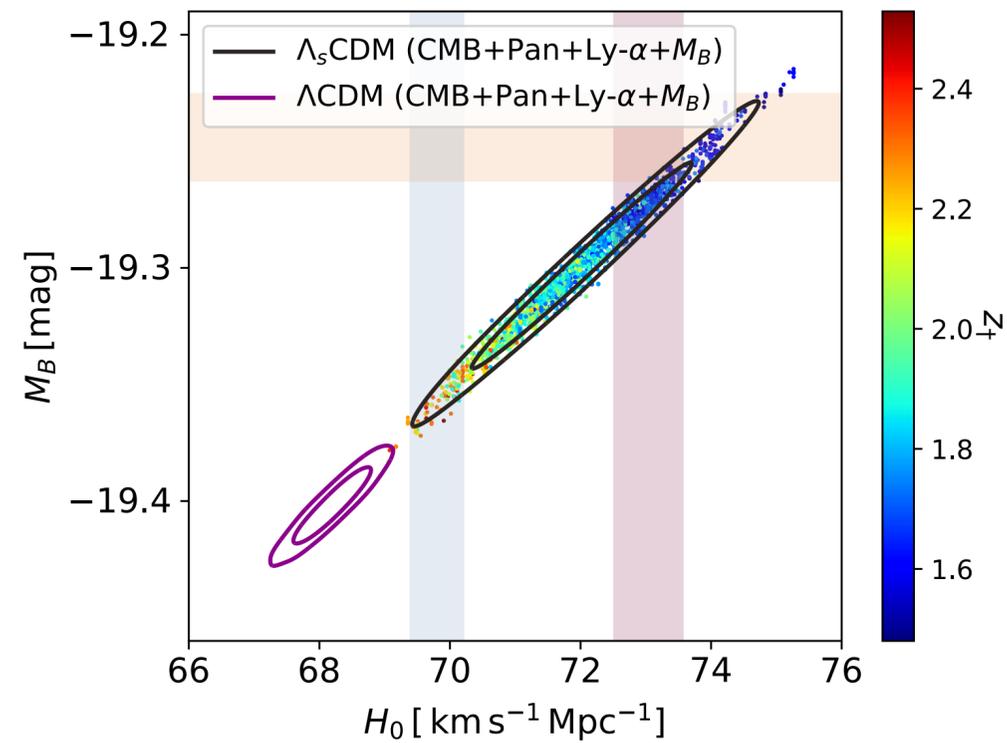
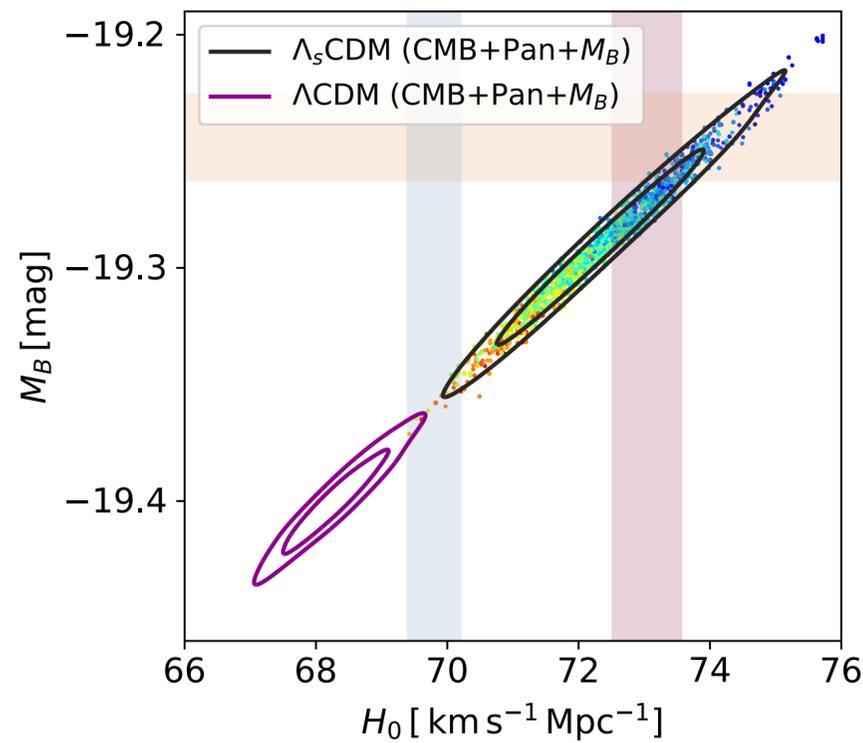
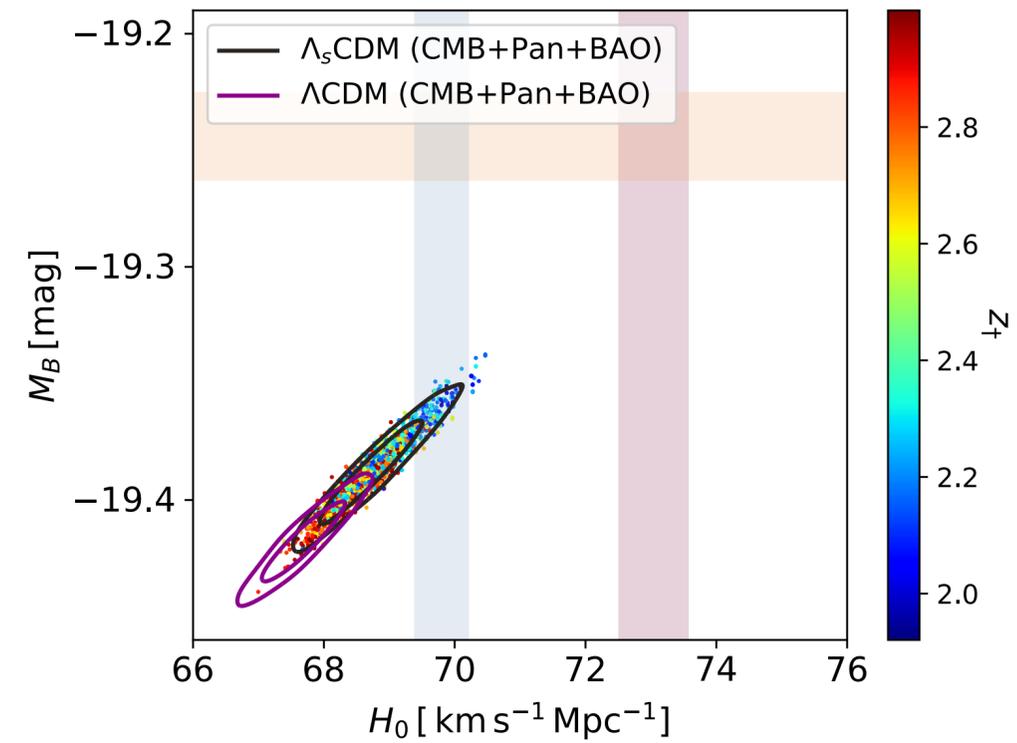
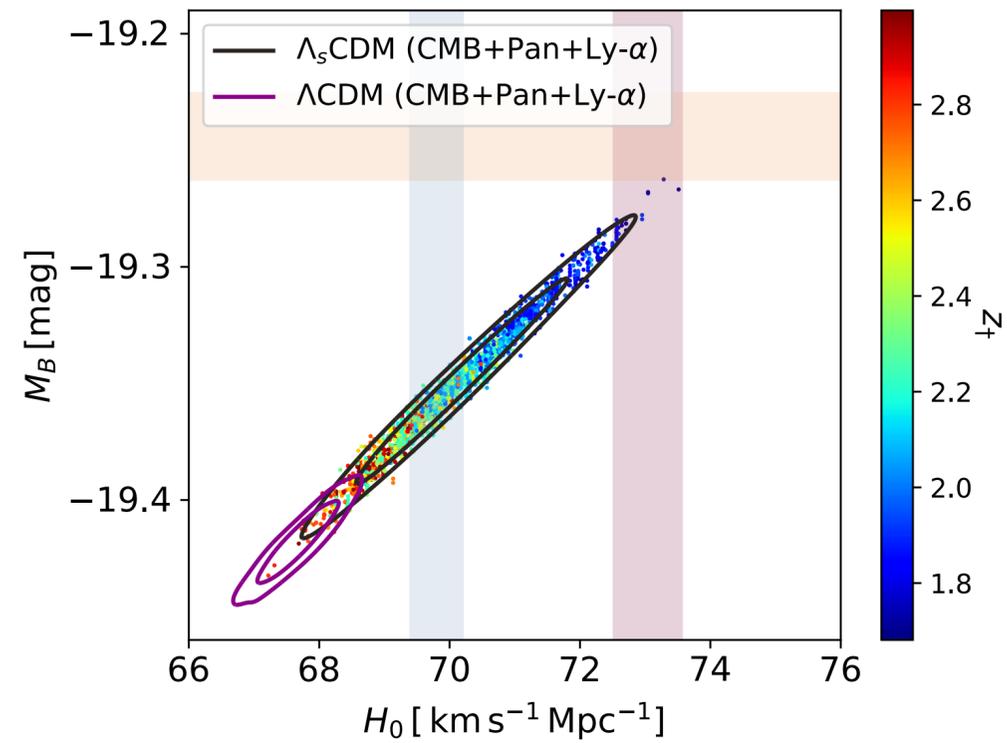
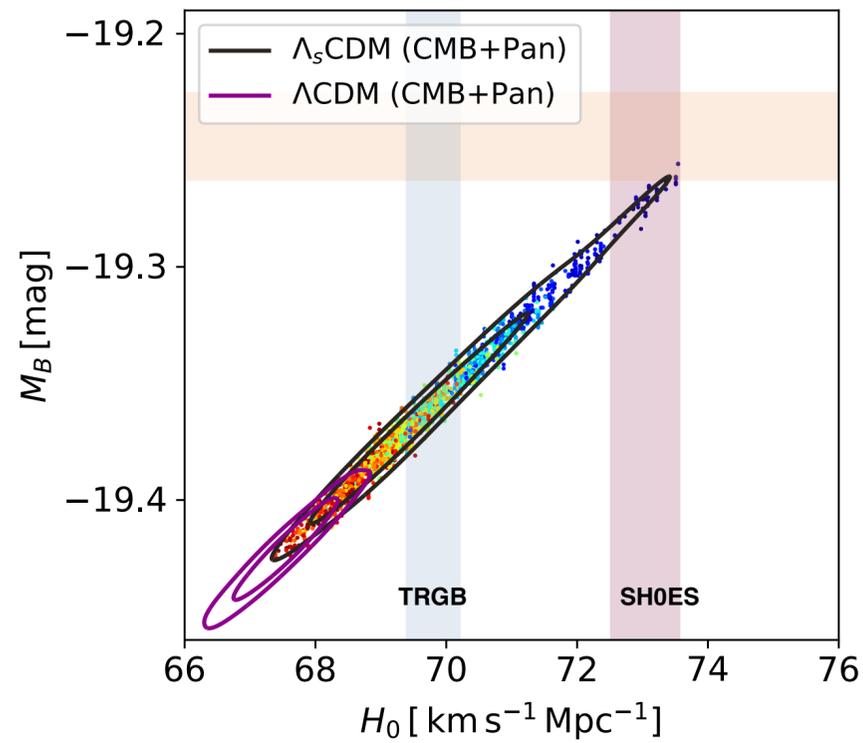


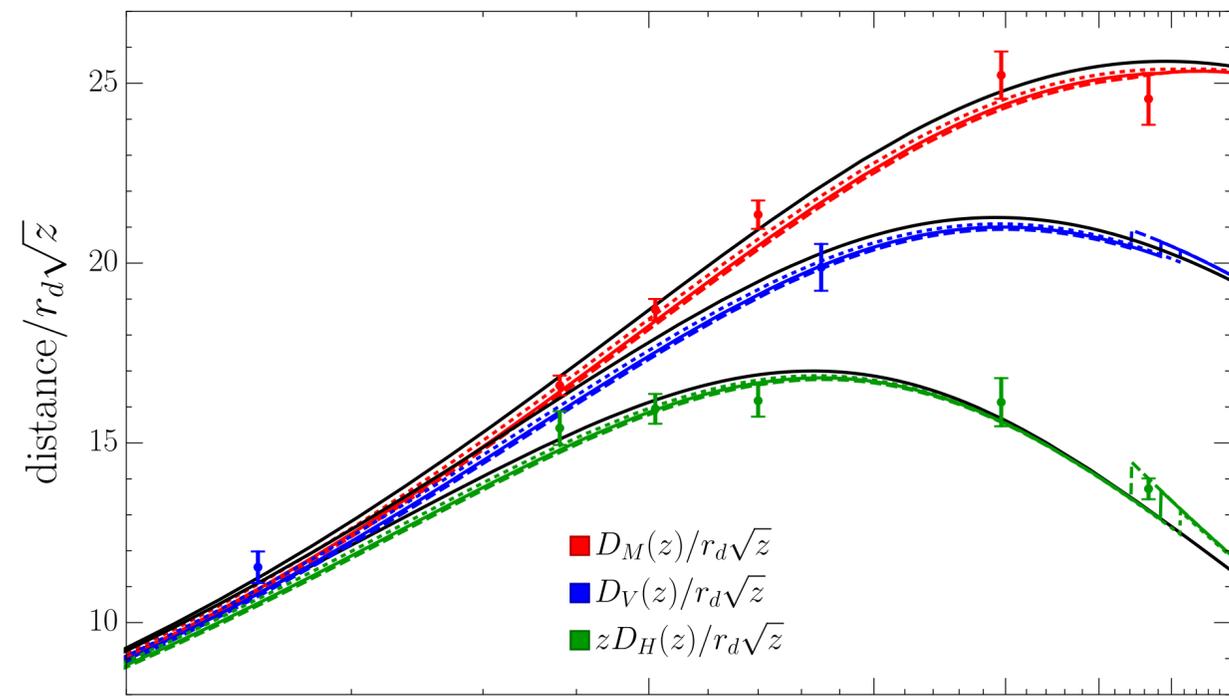
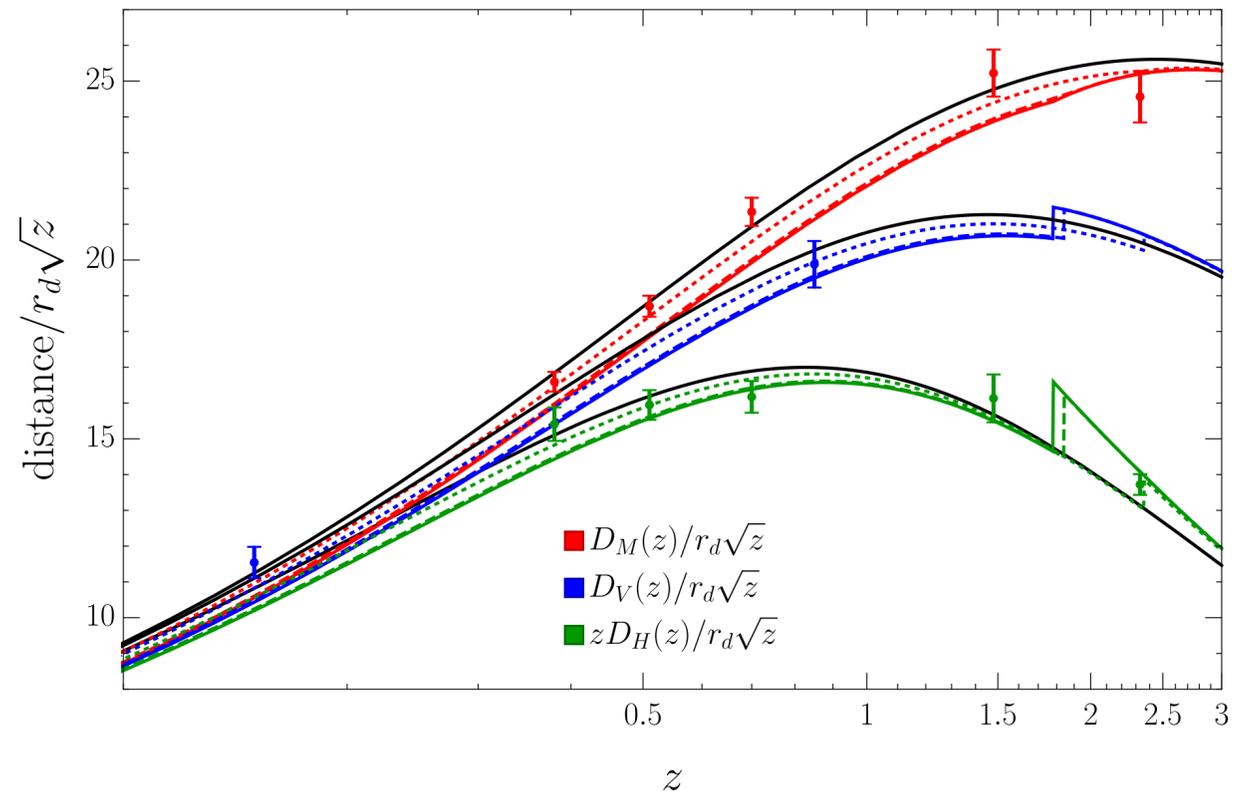
Data set	CMB+Pan+ $M_B$		CMB+Pan+Ly- $\alpha$ + $M_B$		CMB+Pan+BAO+ $M_B$	
	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM
$10^2 \omega_b$	$2.256 \pm 0.015$	$2.248 \pm 0.014$	$2.253 \pm 0.013$	$2.247^{+0.014}_{-0.013}$	$2.255 \pm 0.013$	$2.242 \pm 0.014$
$\omega_c$	$0.1181 \pm 0.0011$	$0.1191 \pm 0.0011$	$0.1183 \pm 0.0008$	$0.1191 \pm 0.0011$	$0.1181 \pm 0.0009$	$0.1200^{+0.0010}_{-0.0011}$
$100\theta_s$	$1.04208 \pm 0.00029$	$1.04197 \pm 0.00031$	$1.04204 \pm 0.00028$	$1.04196 \pm 0.00028$	$1.04207^{+0.00029}_{-0.00026}$	$1.04186 \pm 0.00028$
$\ln(10^{10} A_s)$	$3.053^{+0.014}_{-0.017}$	$3.039 \pm 0.014$	$3.052^{+0.013}_{-0.016}$	$3.041 \pm 0.015$	$3.053^{+0.014}_{-0.016}$	$3.041 \pm 0.015$
$n_s$	$0.9701 \pm 0.0040$	$0.9687^{+0.0043}_{-0.0038}$	$0.9697 \pm 0.0035$	$0.9684 \pm 0.0041$	$0.9702 \pm 0.0035$	$0.9661 \pm 0.0037$
$\tau_{\text{reio}}$	$0.0601^{+0.0072}_{-0.0085}$	$0.0526 \pm 0.0074$	$0.0593^{+0.0064}_{-0.0079}$	$0.0535 \pm 0.0077$	$0.0603^{+0.0070}_{-0.0078}$	$0.0524 \pm 0.0076$
$z_{\dagger}$	—	$1.78^{+0.14}_{-0.18}$	—	$1.84^{+0.13}_{-0.21}$	—	$2.36 \pm 0.28$
$M_B$ [mag]	$-19.399 \pm 0.014$	$-19.290^{+0.026}_{-0.029}$	$-19.402 \pm 0.011$	$-19.299 \pm 0.028$	$-19.399 \pm 0.011$	$-19.366^{+0.013}_{-0.015}$
$\Omega_m$	$0.3028 \pm 0.0068$	$0.2716 \pm 0.0084$	$0.3043 \pm 0.0050$	$0.2743^{+0.0086}_{-0.0097}$	$0.3030 \pm 0.0051$	$0.2965 \pm 0.0055$
$\omega_m$	$0.1413 \pm 0.0011$	$0.1422 \pm 0.0010$	$0.1415 \pm 0.0008$	$0.1422 \pm 0.0011$	$0.1413 \pm 0.0008$	$0.1431 \pm 0.0010$
$H_0$ [km/s/Mpc]	$68.31 \pm 0.52$	$72.38^{+0.98}_{-1.10}$	$68.19 \pm 0.38$	$72.0 \pm 1.1$	$68.29 \pm 0.39$	$69.48^{+0.48}_{-0.55}$
$t_0$ [Gyr]	$13.76 \pm 0.02$	$13.55 \pm 0.05$	$13.76 \pm 0.02$	$13.56^{+0.04}_{-0.04}$	$13.76 \pm 0.02$	$13.67 \pm 0.03$
$\sigma_8$	$0.8090 \pm 0.0064$	$0.8255^{+0.0072}_{-0.0081}$	$0.8091^{+0.0054}_{-0.0063}$	$0.8243 \pm 0.0076$	$0.8092^{+0.0057}_{-0.0061}$	$0.8176 \pm 0.0063$
$S_8$	$0.813 \pm 0.012$	$0.785 \pm 0.012$	$0.815 \pm 0.010$	$0.788^{+0.012}_{-0.014}$	$0.813 \pm 0.010$	$0.813 \pm 0.010$
$-2 \ln \mathcal{L}_{\text{max}}$	1913.28	1904.29	1918.68	1905.88	1919.85	1915.57
$\ln \mathcal{Z}$	-1947.83	-1940.06	-1954.17	-1941.85	-1955.02	-1951.79
$\Delta \ln \mathcal{Z}$	7.77	0	12.32	0	3.23	0



Data set	CMB+Pan		CMB+Pan+Ly- $\alpha$		CMB+Pan+BAO		CMB+Pan+ $M_B$		CMB+Pan+Ly- $\alpha$ + $M_B$		CMB+Pan+BAO+ $M_B$	
	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM
$H_0^{\text{R21}}$	4.7 $\sigma$	2.2 $\sigma$	4.8 $\sigma$	2.0 $\sigma$	4.8 $\sigma$	3.7 $\sigma$	4.1 $\sigma$	0.4 $\sigma$	4.4 $\sigma$	0.7 $\sigma$	4.3 $\sigma$	3.1 $\sigma$
$H_0^{\text{TRGB}}$	2.3 $\sigma$	0.1 $\sigma$	2.8 $\sigma$	0.3 $\sigma$	2.4 $\sigma$	1.1 $\sigma$	1.6 $\sigma^*$	2.0 $\sigma^*$	1.8 $\sigma^*$	1.6 $\sigma^*$	1.7 $\sigma^*$	0.3 $\sigma^*$
$M_B$ (SHOES)	4.5 $\sigma$	2.5 $\sigma$	4.5 $\sigma$	2.3 $\sigma$	4.5 $\sigma$	3.6 $\sigma$	3.9 $\sigma$	1.0 $\sigma$	4.1 $\sigma$	1.2 $\sigma$	4.0 $\sigma$	3.1 $\sigma$
$S_8$ (KiDS)	2.9 $\sigma$	1.9 $\sigma$	3.0 $\sigma$	1.7 $\sigma$	2.9 $\sigma$	2.8 $\sigma$	2.3 $\sigma$	0.9 $\sigma$	2.5 $\sigma$	1.0 $\sigma$	2.4 $\sigma$	2.4 $\sigma$
$D_H(2.33)/r_d$	2.0 $\sigma$	0.2 $\sigma$	1.9 $\sigma$	0.1 $\sigma$	1.9 $\sigma$	1.1 $\sigma$	1.9 $\sigma$	1.2 $\sigma$	1.8 $\sigma$	1.2 $\sigma$	1.9 $\sigma$	0.1 $\sigma$
$t_u$	1.9 $\sigma$	1.0 $\sigma$	1.9 $\sigma$	0.8 $\sigma$	1.9 $\sigma$	1.4 $\sigma$	1.7 $\sigma$	0.3 $\sigma$	1.7 $\sigma$	0.4 $\sigma$	1.7 $\sigma$	1.1 $\sigma$
$\omega_b^{\text{PCUV21}}$	1.7 $\sigma$	1.8 $\sigma$	1.8 $\sigma$	1.7 $\sigma$	1.8 $\sigma$	1.5 $\sigma$	2.3 $\sigma$	2.0 $\sigma$	2.3 $\sigma$	2.0 $\sigma$	2.3 $\sigma$	1.8 $\sigma$
$\omega_b^{\text{LUNA}}$	0.2 $\sigma$	0.2 $\sigma$	0.2 $\sigma$	0.2 $\sigma$	0.2 $\sigma$	0.1 $\sigma$	0.6 $\sigma$	0.4 $\sigma$	0.5 $\sigma$	0.4 $\sigma$	0.6 $\sigma$	0.2 $\sigma$



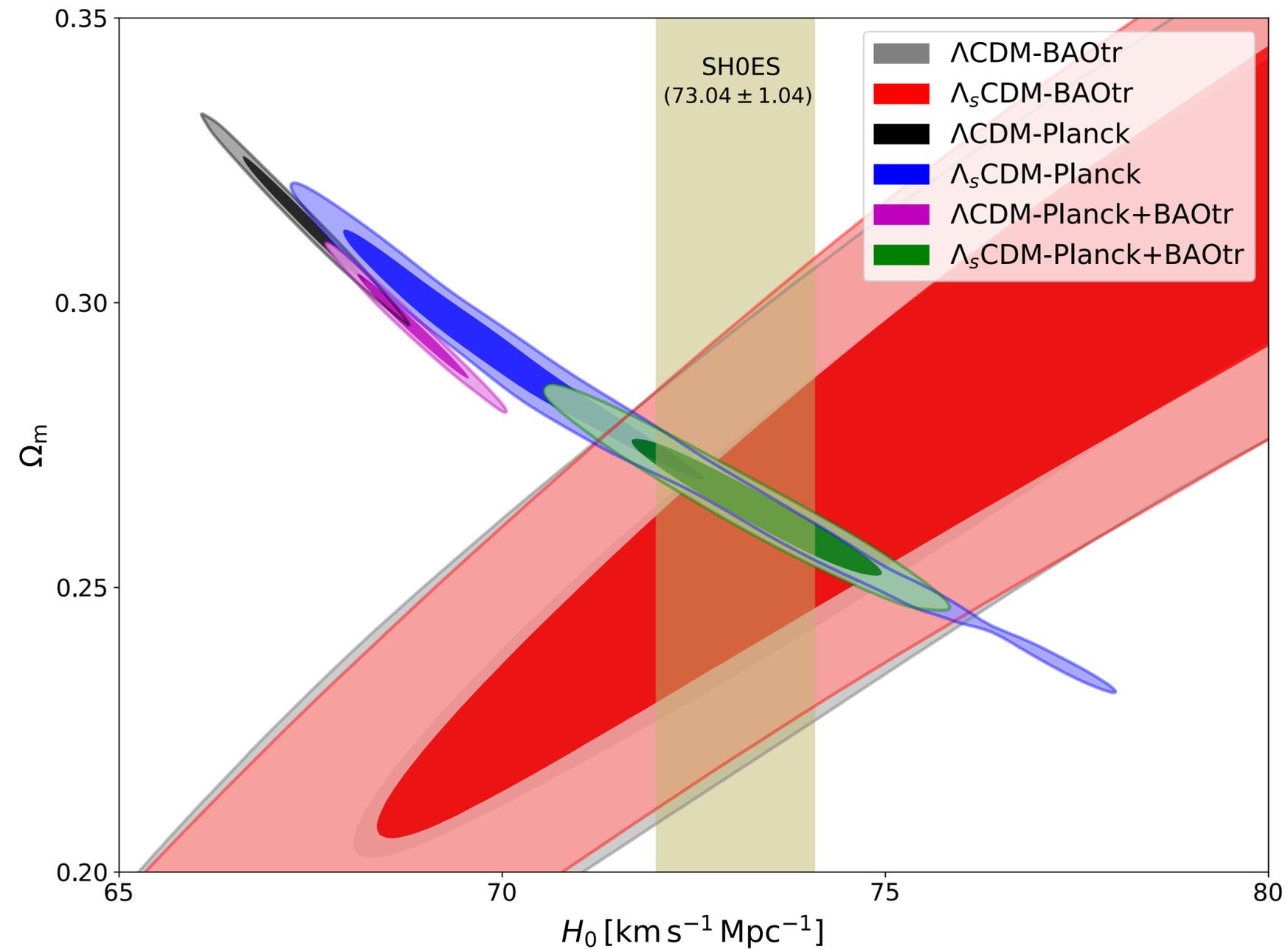




Data set	CMB+Pan		CMB+Pan+Ly- $\alpha$		CMB+Pan+BAO		CMB+Pan+ $M_B$		CMB+Pan+Ly- $\alpha$ + $M_B$		CMB+Pan+BAO+ $M_B$	
	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM	$\Lambda$ CDM	$\Lambda_s$ CDM
$D_V(0.15)/r_d$	$0.9\sigma$	$1.7\sigma$	$1.0\sigma$	$1.8\sigma$	$1.0\sigma$	$0.7\sigma$	$1.2\sigma$	$2.4\sigma$	$1.3\sigma$	<b><math>2.3\sigma</math></b>	$1.2\sigma$	$1.6\sigma$
$D_V(0.85)/r_d$	$0.7\sigma$	$0.0\sigma$	$0.6\sigma$	$0.1\sigma$	$0.6\sigma$	$0.3\sigma$	$0.5\sigma$	$0.6\sigma$	$0.4\sigma$	$0.5\sigma$	$0.5\sigma$	$0.2\sigma$
$D_M(0.38)/r_d$	$0.9\sigma$	$0.6\sigma$	$0.9\sigma$	$0.9\sigma$	$0.8\sigma$	$0.2\sigma$	$0.3\sigma$	$2.0\sigma$	$0.3\sigma$	<b><math>1.8\sigma</math></b>	$0.4\sigma$	$0.3\sigma$
$D_M(0.51)/r_d$	$0.5\sigma$	$0.9\sigma$	$0.4\sigma$	$1.2\sigma$	$0.4\sigma$	$0.3\sigma$	$0.1\sigma$	$2.3\sigma$	$0.1\sigma$	<b><math>2.2\sigma</math></b>	$0.0\sigma$	$0.8\sigma$
$D_M(0.70)/r_d$	$0.9\sigma$	$1.9\sigma$	$0.9\sigma$	$2.1\sigma$	$1.0\sigma$	$1.5\sigma$	$1.3\sigma$	$3.1\sigma$	$1.4\sigma$	<b><math>3.0\sigma</math></b>	$1.3\sigma$	$2.0\sigma$
$D_M(1.48)/r_d$	$0.6\sigma$	$1.3\sigma$	$0.6\sigma$	$1.5\sigma$	$0.7\sigma$	$1.0\sigma$	$0.8\sigma$	$1.9\sigma$	$0.9\sigma$	<b><math>1.9\sigma</math></b>	$0.8\sigma$	$1.2\sigma$
$D_M(2.33)/r_d$	$1.5\sigma$	$1.0\sigma$	$1.5\sigma$	$1.0\sigma$	$1.5\sigma$	$1.2\sigma$	$1.3\sigma$	$0.9\sigma$	$1.3\sigma$	$0.9\sigma$	$1.4\sigma$	$1.1\sigma$
$D_H(0.38)/r_d$	$0.6\sigma$	$1.3\sigma$	$0.6\sigma$	$1.4\sigma$	$0.6\sigma$	$0.9\sigma$	$0.8\sigma$	$2.0\sigma$	$0.9\sigma$	<b><math>1.9\sigma</math></b>	$0.8\sigma$	$1.2\sigma$
$D_H(0.51)/r_d$	$0.7\sigma$	$0.1\sigma$	$0.6\sigma$	$0.3\sigma$	$0.6\sigma$	$0.3\sigma$	$0.4\sigma$	$0.8\sigma$	$0.4\sigma$	$0.8\sigma$	$0.4\sigma$	$0.0\sigma$
$D_H(0.70)/r_d$	$1.7\sigma$	$1.0\sigma$	$1.7\sigma$	$0.9\sigma$	$1.7\sigma$	$1.4\sigma$	$1.5\sigma$	$0.5\sigma$	<b><math>1.5\sigma</math></b>	$0.5\sigma$	<b><math>1.5\sigma</math></b>	$1.2\sigma$
$D_H(1.48)/r_d$	$0.6\sigma$	$0.8\sigma$	$0.6\sigma$	$0.8\sigma$	$0.6\sigma$	$0.7\sigma$	$0.6\sigma$	$0.9\sigma$	$0.6\sigma$	$0.9\sigma$	$0.6\sigma$	$0.8\sigma$
$D_H(2.33)/r_d$	$2.0\sigma$	$0.2\sigma$	$1.9\sigma$	$0.1\sigma$	$1.9\sigma$	$1.1\sigma$	$1.9\sigma$	$1.2\sigma$	<b><math>1.8\sigma</math></b>	$1.2\sigma$	<b><math>1.9\sigma</math></b>	$0.1\sigma$

?

?



Here **BAOtr** dataset is the **2D BAO** dataset (less model independent) compiled in arXiv:2002.09293 (Nunes, Yadav, Jesus, Bernui, MNRAS 2020) and arXiv:2103.14121 (Carvalho, Bernui, Avila, Novaes, Nogueira-Cavalcante, A&A 2021)

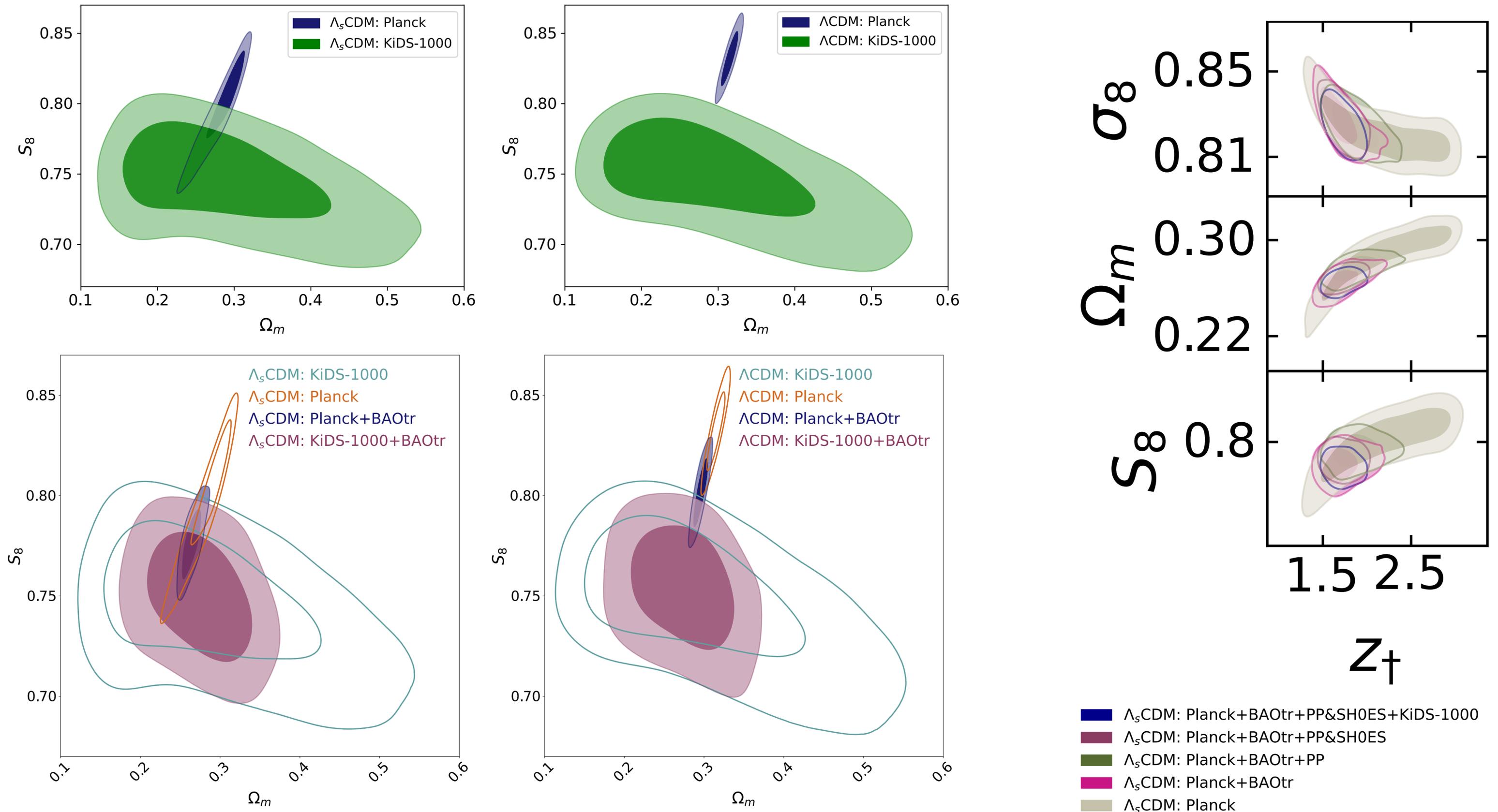
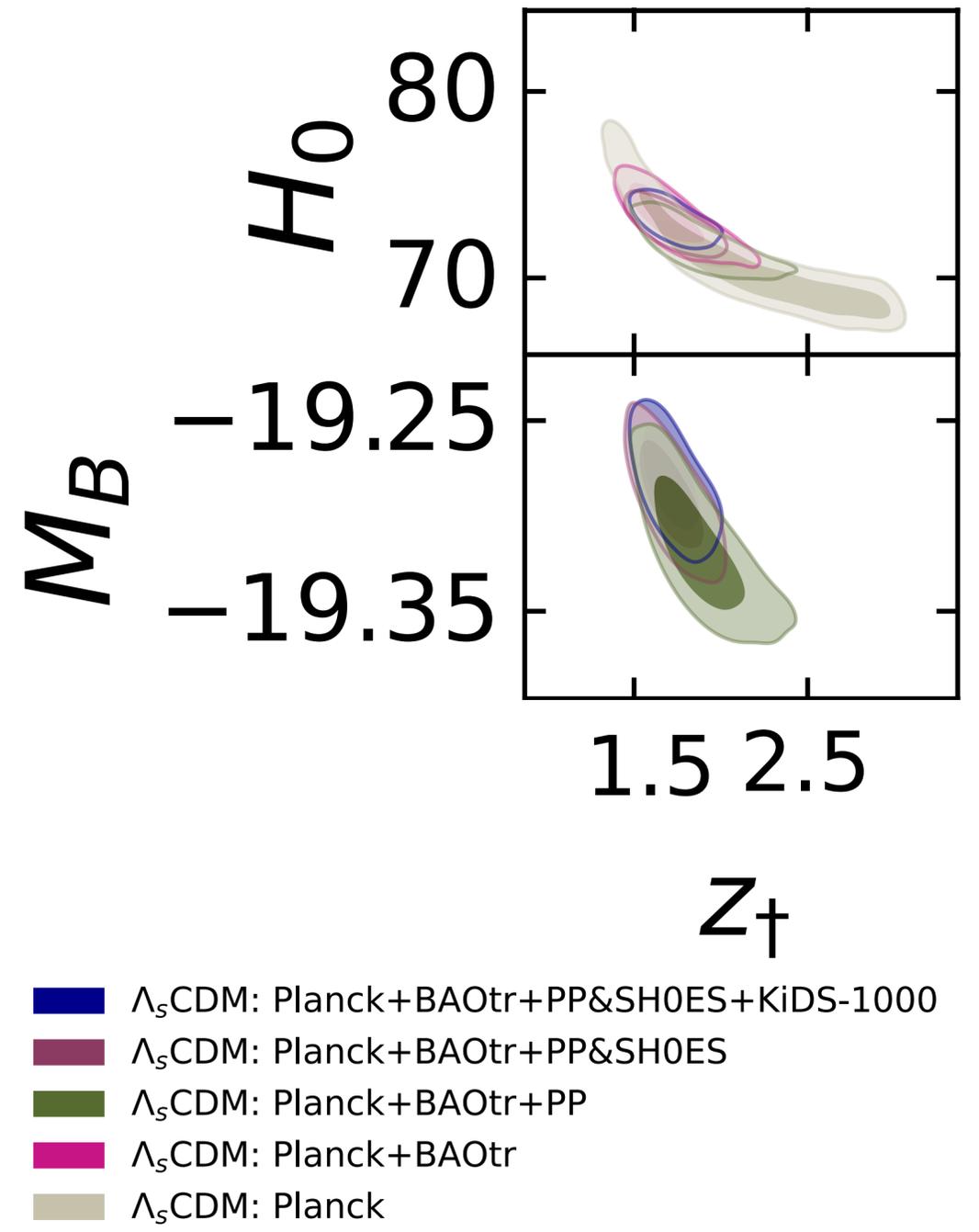
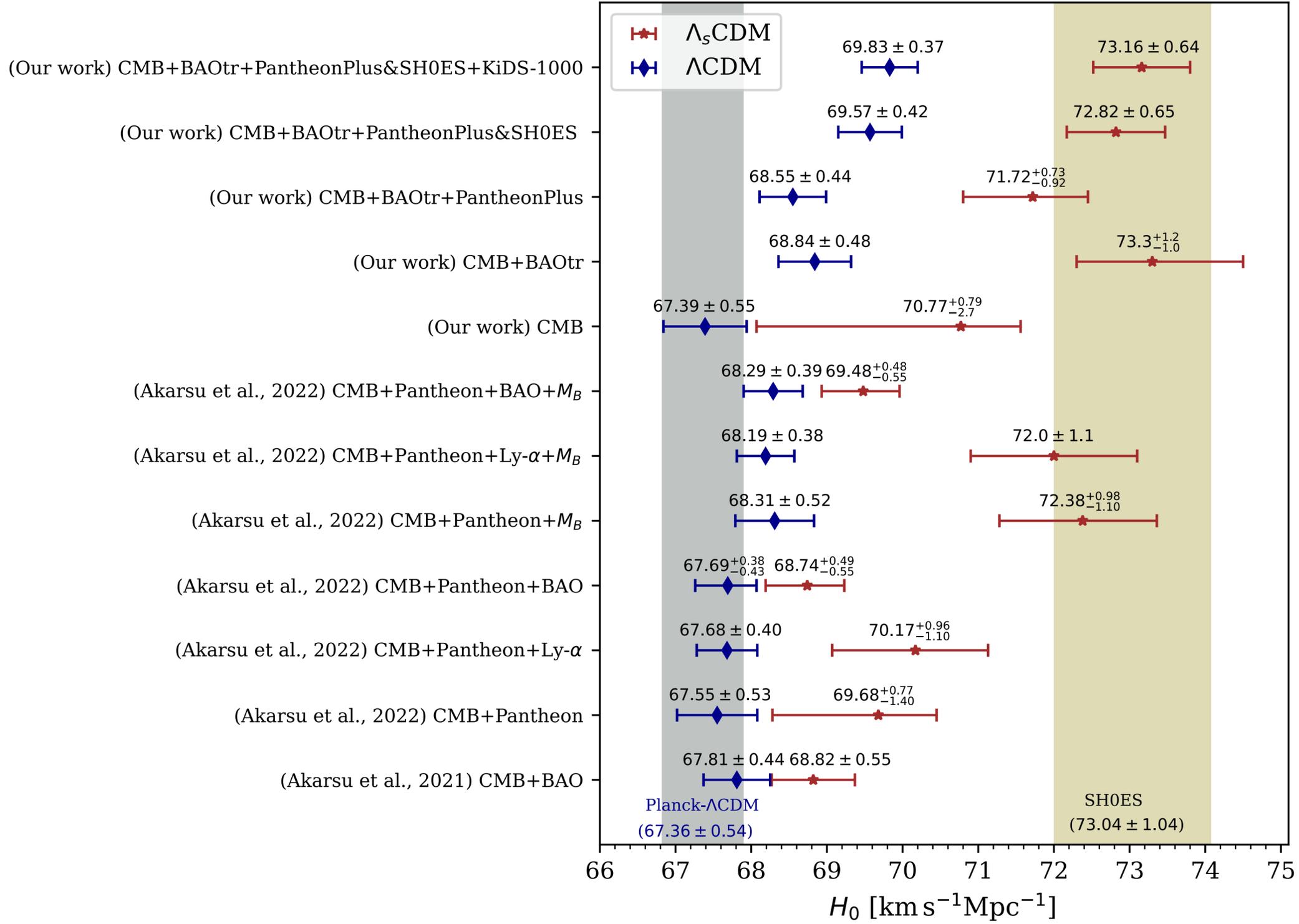
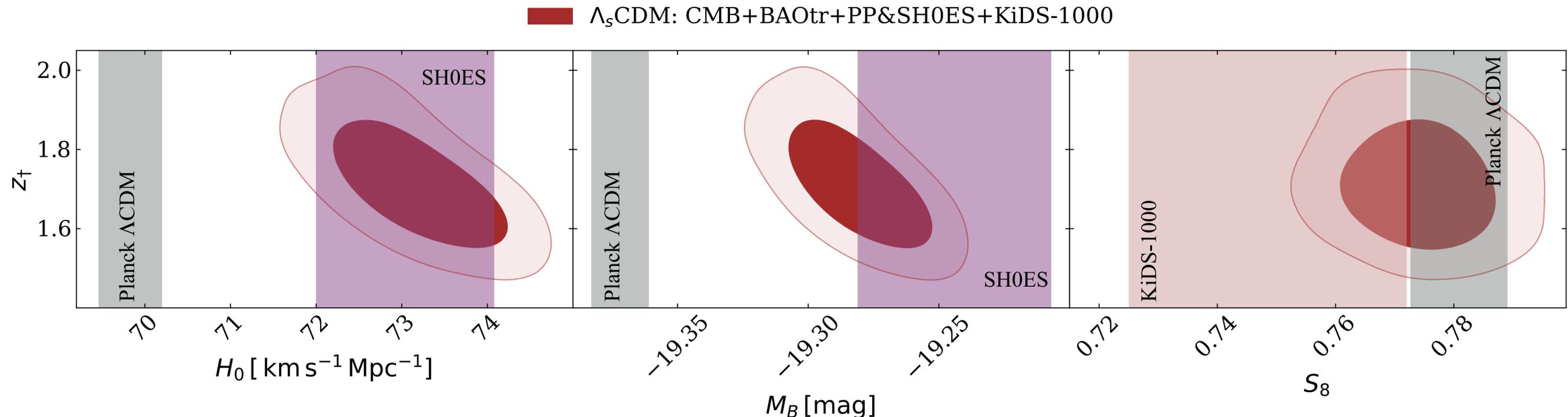


FIG. 1. 2D contours at 68%, and 95% CLs in the  $\Omega_m$ - $S_8$  plane for the  $\Lambda_s$ CDM and  $\Lambda$ CDM models.  $S_8 = 0.801^{+0.026}_{-0.016}$  ( $\Lambda_s$ CDM: Planck),  $S_8 = 0.746^{+0.026}_{-0.021}$  ( $\Lambda_s$ CDM: KiDS),  $S_8 = 0.832 \pm 0.012$  ( $\Lambda$ CDM: Planck),  $S_8 = 0.749^{+0.027}_{-0.020}$  ( $\Lambda$ CDM: KiDS) at 68% CL.

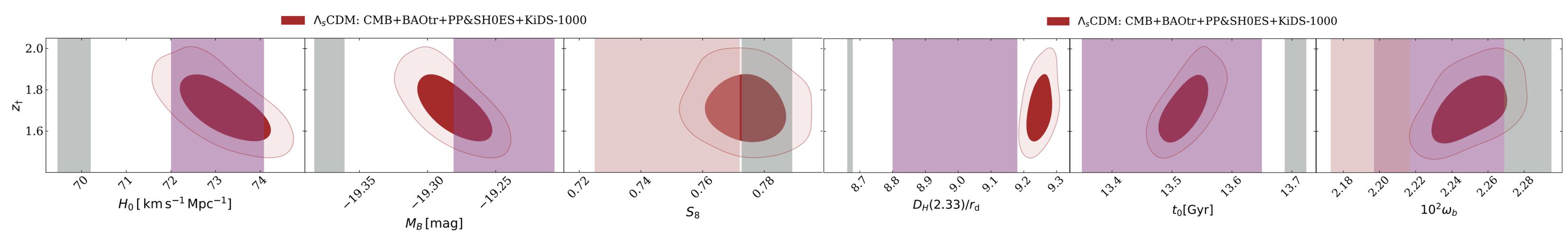


Data set	Planck	Planck+BAOtr	Planck+BAOtr +PP	Planck+BAOtr +PP&SH0ES	Planck+BAOtr +PP&SH0ES+KiDS-1000
Model	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM
$z_{\dagger}$	unconstrained	$1.70^{+0.09}_{-0.19}(1.65)$	$1.87^{+0.13}_{-0.21}(1.75)$	$1.70^{+0.10}_{-0.13}(1.67)$	$1.72^{+0.09}_{-0.12}(1.70)$
	--	--	--	--	--
$M_B$ [mag]	--	--	$-19.317^{+0.021}_{-0.025}(-19.311)$	$-19.290 \pm 0.017(-19.278)$	$-19.282 \pm 0.017(-19.280)$
	--	--	$-19.407 \pm 0.013(-19.411)$	$-19.379 \pm 0.012(-19.373)$	$-19.372 \pm 0.011(-19.369)$
$H_0$ [km/s/Mpc]	$70.77^{+0.79}_{-2.70}(71.22)$	$73.30^{+1.20}_{-1.00}(73.59)$	$71.72^{+0.73}_{-0.92}(71.97)$	$72.82 \pm 0.65(73.20)$	$73.16 \pm 0.64(73.36)$
	$67.39 \pm 0.55(67.28)$	$68.84 \pm 0.48(68.61)$	$68.55 \pm 0.44(68.54)$	$69.57 \pm 0.42(69.73)$	$69.83 \pm 0.37(69.96)$
$\Omega_m$	$0.2860^{+0.0230}_{-0.0099}(0.2796)$	$0.2643^{+0.0072}_{-0.0090}(0.2618)$	$0.2768^{+0.0072}_{-0.0063}(0.2759)$	$0.2683 \pm 0.0052(0.2646)$	$0.2646 \pm 0.0052(0.2622)$
	$0.3151 \pm 0.0075(0.3163)$	$0.2958 \pm 0.0061(0.2984)$	$0.2995 \pm 0.0056(0.2992)$	$0.2869 \pm 0.0051(0.2849)$	$0.2837 \pm 0.0045(0.2816)$
$S_8$	$0.801^{+0.026}_{-0.016}(0.791)$	$0.777 \pm 0.011(0.772)$	$0.791 \pm 0.011(0.794)$	$0.783 \pm 0.010(0.777)$	$0.774 \pm 0.009(0.773)$
	$0.832 \pm 0.013(0.835)$	$0.802 \pm 0.011(0.804)$	$0.808 \pm 0.010(0.804)$	$0.788 \pm 0.010(0.784)$	$0.781 \pm 0.008(0.782)$
$\chi^2_{\min}$	2778.06	2793.38	4219.68	4097.32	4185.34
	2780.52	2820.30	4235.18	4138.26	4226.50
$\ln\mathcal{B}_{ij}$	-1.28	-12.65	-7.52	-19.47	-19.77

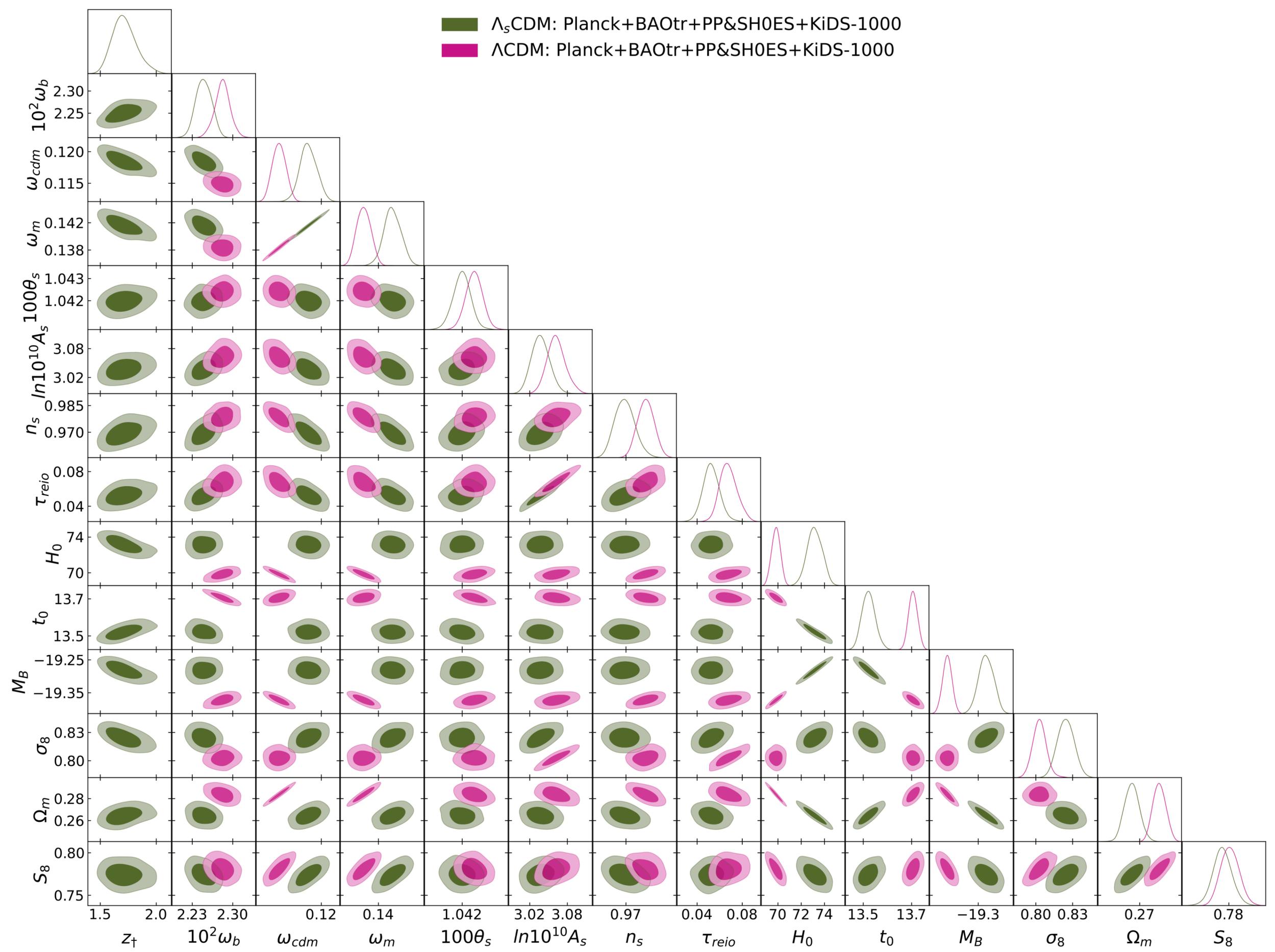


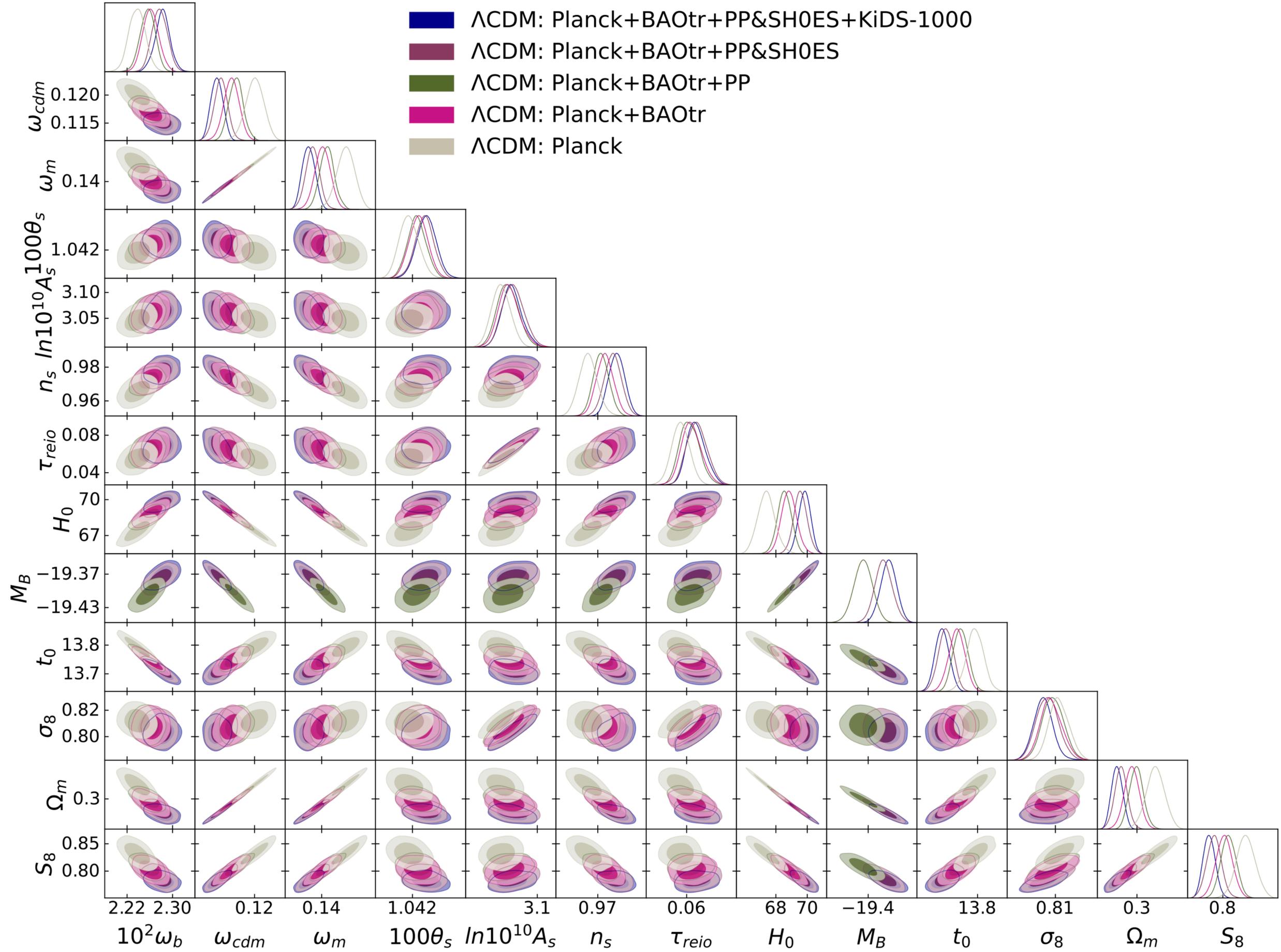
Data set	Planck	Planck+BAOtr	Planck+BAOtr +PP	Planck+BAOtr +PP&SH0ES	Planck+BAOtr +PP&SH0ES+KiDS-1000
Model	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM
$10^2 \omega_b$	$2.241 \pm 0.015(2.252)$ $2.238 \pm 0.014(2.235)$	$2.249 \pm 0.014(2.251)$ $2.262 \pm 0.014(2.255)$	$2.245 \pm 0.014(2.247)$ $2.256 \pm 0.013(2.248)$	$2.246 \pm 0.014(2.249)$ $2.277 \pm 0.013(2.280)$	$2.250 \pm 0.013(2.252)$ $2.282 \pm 0.013(2.283)$
$\omega_{cdm}$	$0.1195 \pm 0.0012(0.1187)$ $0.1200 \pm 0.0012(0.1202)$	$0.1187 \pm 0.0012(0.1186)$ $0.1169 \pm 0.0010(0.1173)$	$0.1192 \pm 0.0011(0.1198)$ $0.1175 \pm 0.0010(0.1174)$	$0.1192^{+0.0010}_{-0.0012}(0.1186)$ $0.1154 \pm 0.0009(0.1151)$	$0.1184 \pm 0.0010(0.1180)$ $0.1149 \pm 0.0008(0.1143)$
$100\theta_s$	$1.04189 \pm 0.00029(1.04207)$ $1.04190^{+0.00027}_{-0.00031}(1.04178)$	$1.04199 \pm 0.00030(1.04194)$ $1.04218 \pm 0.00028(1.04211)$	$1.04196 \pm 0.00029(1.04181)$ $1.04213 \pm 0.00027(1.04225)$	$1.04197 \pm 0.00029(1.04167)$ $1.04236 \pm 0.00028(1.04242)$	$1.04199 \pm 0.00031(1.04168)$ $1.04242 \pm 0.00029(1.04218)$
$\ln(10^{10} A_s)$	$3.040 \pm 0.014(3.046)$ $3.046 \pm 0.014(3.049)$	$3.039 \pm 0.015(3.034)$ $3.058^{+0.014}_{-0.017}(3.053)$	$3.042 \pm 0.014(3.044)$ $3.056 \pm 0.016(3.047)$	$3.039 \pm 0.014(3.038)$ $3.064^{+0.015}_{-0.017}(3.063)$	$3.037 \pm 0.014(3.045)$ $3.062^{+0.013}_{-0.016}(3.079)$
$n_s$	$0.9669 \pm 0.0043(0.9664)$ $0.9657 \pm 0.0041(0.9658)$	$0.9695 \pm 0.0041(0.9692)$ $0.9733 \pm 0.0039(0.9706)$	$0.9679 \pm 0.0039(0.9644)$ $0.9715 \pm 0.0035(0.9728)$	$0.9682 \pm 0.0040(0.9711)$ $0.9768 \pm 0.0038(0.9801)$	$0.9695 \pm 0.0043(0.9701)$ $0.9786 \pm 0.0035(0.9797)$
$\tau_{reio}$	$0.0528 \pm 0.0073(0.0569)$ $0.0550 \pm 0.0072(0.5488)$	$0.0532 \pm 0.0077(0.0515)$ $0.0639^{+0.0073}_{-0.0087}(0.0608)$	$0.0534 \pm 0.0073(0.0544)$ $0.0624^{+0.0074}_{-0.0086}(0.0586)$	$0.0522 \pm 0.0073(0.0555)$ $0.0684^{+0.0076}_{-0.0089}(0.0685)$	$0.0525 \pm 0.0074(0.0584)$ $0.0678^{+0.0067}_{-0.0085}(0.0771)$
$z_{\dagger}$	unconstrained --	$1.70^{+0.09}_{-0.19}(1.65)$ --	$1.87^{+0.13}_{-0.21}(1.75)$ --	$1.70^{+0.10}_{-0.13}(1.67)$ --	$1.72^{+0.09}_{-0.12}(1.70)$ --
$\chi^2_{\min}$	2778.06 2780.52	2793.38 2820.30	4219.68 4235.18	4097.32 4138.26	4185.34 4226.50
$\ln \mathcal{Z}$	-1423.17 -1424.45	-1432.71 -1445.36	-2144.75 -2152.27	-2084.37 -2103.84	-2133.85 -2153.62
$\ln \mathcal{B}_{ij}$	-1.28	-12.65	-7.52	-19.47	-19.77

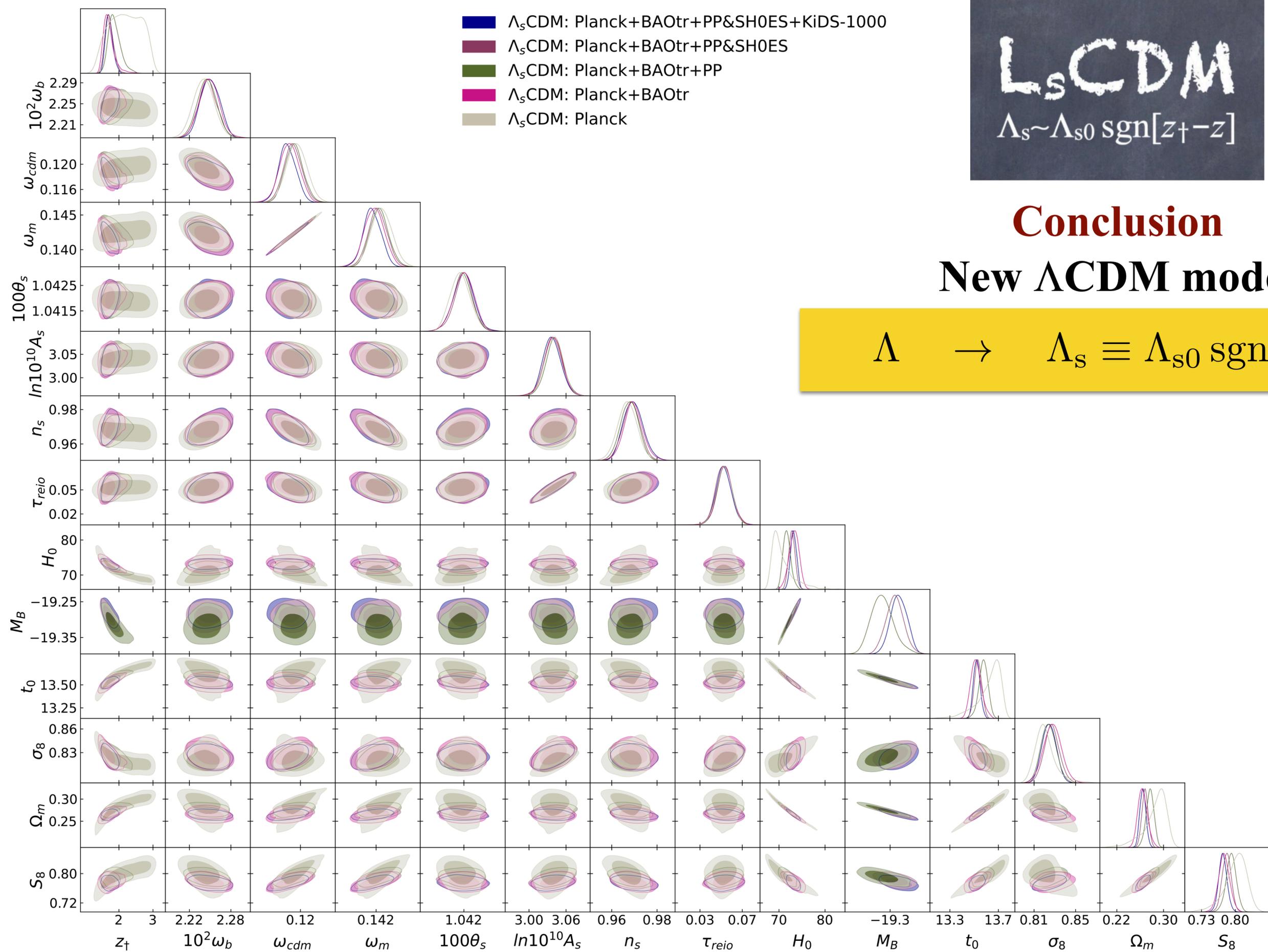
Data set	Planck	Planck+BAOtr	Planck+BAOtr +PP	Planck+BAOtr +PP&SH0ES	Planck+BAOtr +PP&SH0ES+KiDS-1000
Model	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM
$z_{reio}$	$7.43^{+0.78}_{-0.67}(7.83)$ $7.75 \pm 0.72(7.76)$	$7.42 \pm 0.78(7.25)$ $8.52 \pm 0.76(8.25)$	$7.47 \pm 0.74(7.59)$ $8.39 \pm 0.76(8.05)$	$7.34 \pm 0.76(7.67)$ $8.87 \pm 0.75(8.88)$	$7.34 \pm 0.74(7.94)$ $8.79^{+0.64}_{-0.75}(9.64)$
$Y_P$	$0.247856 \pm 0.000063(0.247905)$ $0.247842 \pm 0.000062(0.247832)$	$0.247889 \pm 0.000060(0.247901)$ $0.247944 \pm 0.000059(0.247914)$	$0.247876 \pm 0.000058(0.247881)$ $0.247921^{+0.000059}_{-0.000053}(0.247888)$	$0.247877 \pm 0.000061(0.247887)$ $0.248010 \pm 0.000056(0.248020)$	$0.247895 \pm 0.000057(0.247903)$ $0.248031 \pm 0.000055(0.248034)$
$z_d$	$1060.03 \pm 0.29(1060.22)$ $1059.99 \pm 0.28(1059.95)$	$1060.15 \pm 0.29(1060.22)$ $1060.28 \pm 0.28(1060.16)$	$1060.12 \pm 0.29(1060.19)$ $1060.21 \pm 0.27(1060.03)$	$1060.12 \pm 0.30(1060.15)$ $1060.52 \pm 0.28(1060.55)$	$1060.15 \pm 0.27(1060.16)$ $1060.59 \pm 0.29(1060.56)$
$r_d$ [Mpc]	$147.17 \pm 0.27(147.28)$ $147.07^{+0.24}_{-0.27}(147.06)$	$147.31 \pm 0.26(147.30)$ $147.65 \pm 0.25(147.63)$	$147.20 \pm 0.25(147.03)$ $147.55^{+0.24}_{-0.21}(147.65)$	$147.21 \pm 0.24(147.33)$ $147.87 \pm 0.23(147.93)$	$147.36 \pm 0.23(147.46)$ $147.96^{+0.25}_{-0.23}(148.10)$
$t_0$ [Gyr]	$13.620^{+0.120}_{-0.042}(13.596)$ $13.793 \pm 0.023(13.800)$	$13.517^{+0.038}_{-0.049}(13.502)$ $13.745 \pm 0.021(13.756)$	$13.576^{+0.039}_{-0.034}(13.560)$ $13.755 \pm 0.020(13.760)$	$13.531 \pm 0.028(13.524)$ $13.716 \pm 0.020(13.710)$	$13.522 \pm 0.027(13.521)$ $13.706 \pm 0.018(13.709)$
$M_B$ [mag]	-- --	-- --	$-19.317^{+0.021}_{-0.025}(-19.311)$ $-19.407 \pm 0.013(-19.411)$	$-19.290 \pm 0.017(-19.278)$ $-19.379 \pm 0.012(-19.373)$	$-19.282 \pm 0.017(-19.280)$ $-19.372 \pm 0.011(-19.369)$
$H_0$ [km/s/Mpc]	$70.77^{+0.79}_{-2.70}(71.22)$ $67.39 \pm 0.55(67.28)$	$73.30^{+1.20}_{-1.00}(73.59)$ $68.84 \pm 0.48(68.61)$	$71.72^{+0.73}_{-0.92}(71.97)$ $68.55 \pm 0.44(68.54)$	$72.82 \pm 0.65(73.20)$ $69.57 \pm 0.42(69.73)$	$73.16 \pm 0.64(73.36)$ $69.83 \pm 0.37(69.96)$
$\omega_m$	$0.1426 \pm 0.0011(0.1418)$ $0.1431 \pm 0.0011(0.1432)$	$0.1418 \pm 0.0011(0.1418)$ $0.1401 \pm 0.0010(0.1405)$	$0.1423 \pm 0.0010(0.1429)$ $0.1407 \pm 0.0010(0.1406)$	$0.1422 \pm 0.0010(0.1418)$ $0.1388 \pm 0.0009(0.1385)$	$0.1416 \pm 0.0010(0.1411)$ $0.1384 \pm 0.0008(0.1378)$
$\Omega_m$	$0.2860^{+0.0230}_{-0.0099}(0.2796)$ $0.3151 \pm 0.0075(0.3163)$	$0.2643^{+0.0072}_{-0.0090}(0.2618)$ $0.2958 \pm 0.0061(0.2984)$	$0.2768^{+0.0072}_{-0.0063}(0.2759)$ $0.2995 \pm 0.0056(0.2992)$	$0.2683 \pm 0.0052(0.2646)$ $0.2869 \pm 0.0051(0.2849)$	$0.2646 \pm 0.0052(0.2622)$ $0.2837 \pm 0.0045(0.2816)$
$\sigma_8$	$0.8210^{+0.0064}_{-0.0110}(0.8191)$ $0.8121^{+0.0055}_{-0.0061}(0.8136)$	$0.8278 \pm 0.0086(0.8260)$ $0.8076^{+0.0058}_{-0.0067}(0.8064)$	$0.8240 \pm 0.0074(0.8281)$ $0.8087 \pm 0.0062(0.8054)$	$0.8277 \pm 0.0075(0.8274)$ $0.8054 \pm 0.0064(0.8047)$	$0.8244 \pm 0.0067(0.8264)$ $0.8030 \pm 0.0055(0.8076)$
$S_8$	$0.801^{+0.026}_{-0.016}(0.791)$ $0.832 \pm 0.013(0.835)$	$0.777 \pm 0.011(0.772)$ $0.802 \pm 0.011(0.804)$	$0.791 \pm 0.011(0.794)$ $0.808 \pm 0.010(0.804)$	$0.783 \pm 0.010(0.777)$ $0.788 \pm 0.010(0.784)$	$0.774 \pm 0.009(0.773)(0.773)$ $0.781 \pm 0.008(0.782)$
$D_H(2.33)/r_d$	$8.960^{+0.280}_{-0.380}(9.218)$ $8.615 \pm 0.013(8.614)$	$9.240^{+0.035}_{-0.025}(9.252)$ $8.648 \pm 0.011(8.643)$	$9.201^{+0.041}_{-0.017}(9.222)$ $8.641 \pm 0.010(8.639)$	$9.232 \pm 0.025(9.242)$ $8.664 \pm 0.008(8.667)$	$9.249 \pm 0.025(9.261)$ $8.670 \pm 0.008(8.675)$
$\chi^2_{\min}$	2778.06 2780.52	2793.38 2820.30	4219.68 4235.18	4097.32 4138.26	4185.34 4226.50
$\ln \mathcal{Z}$	-1423.17 -1424.45	-1432.71 -1445.36	-2144.75 -2152.27	-2084.37 -2103.84	-2133.85 -2153.62
$\ln \mathcal{B}_{ij}$	-1.28	-12.65	-7.52	-19.47	-19.77



Data set	Planck	Planck+BAOtr	Planck+BAOtr +PP	Planck+BAOtr +PP&SH0ES	Planck+BAOtr +PP&SH0ES+KiDS-1000
Model	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM	$\Lambda_s$ CDM $\Lambda$ CDM
$H_0$	$1.4\sigma$	$0.2\sigma$	$1.0\sigma$	$0.2\sigma$	$0.1\sigma$
	$4.8\sigma$	$3.7\sigma$	$4.3\sigma$	$3.1\sigma$	$2.9\sigma$
$M_B$	–	–	$1.7\sigma$	$1.1\sigma$	$0.9\sigma$
	–	–	$4.5\sigma$	$3.5\sigma$	$3.3\sigma$
$S_8$	$1.7\sigma$	$1.2\sigma$	$1.7\sigma$	$1.4\sigma$	$1.1\sigma$
	$3.1\sigma$	$2.0\sigma$	$2.3\sigma$	$1.5\sigma$	$1.3\sigma$
$t_0$	$1.0\sigma$	$0.1\sigma$	$0.5\sigma$	$0.2\sigma$	$0.1\sigma$
	$1.9\sigma$	$1.6\sigma$	$1.7\sigma$	$1.4\sigma$	$1.4\sigma$
$D_H(2.33)/r_d$	$0.2\sigma$	$1.3\sigma$	$1.1\sigma$	$1.3\sigma$	$1.4\sigma$
	$2.0\sigma$	$1.8\sigma$	$1.8\sigma$	$1.7\sigma$	$1.7\sigma$
$\omega_b^{\text{PCUV21}}$	$1.2\sigma$	$2.1\sigma$	$1.9\sigma$	$1.9\sigma$	$2.2\sigma$
	$1.6\sigma$	$2.6\sigma$	$2.4\sigma$	$3.1\sigma$	$3.4\sigma$
$\omega_b^{\text{LUNA}}$	$0.3\sigma$	$0.4\sigma$	$0.3\sigma$	$0.3\sigma$	$0.4\sigma$
	$0.1\sigma$	$0.8\sigma$	$0.6\sigma$	$1.1\sigma$	$1.3\sigma$







# Ho'oleilana: An Individual Baryon Acoustic Oscillation?

R. BRENT TULLY,<sup>1</sup> CULLAN HOWLETT,<sup>2</sup> AND DANIEL POMARÈDE<sup>3</sup>

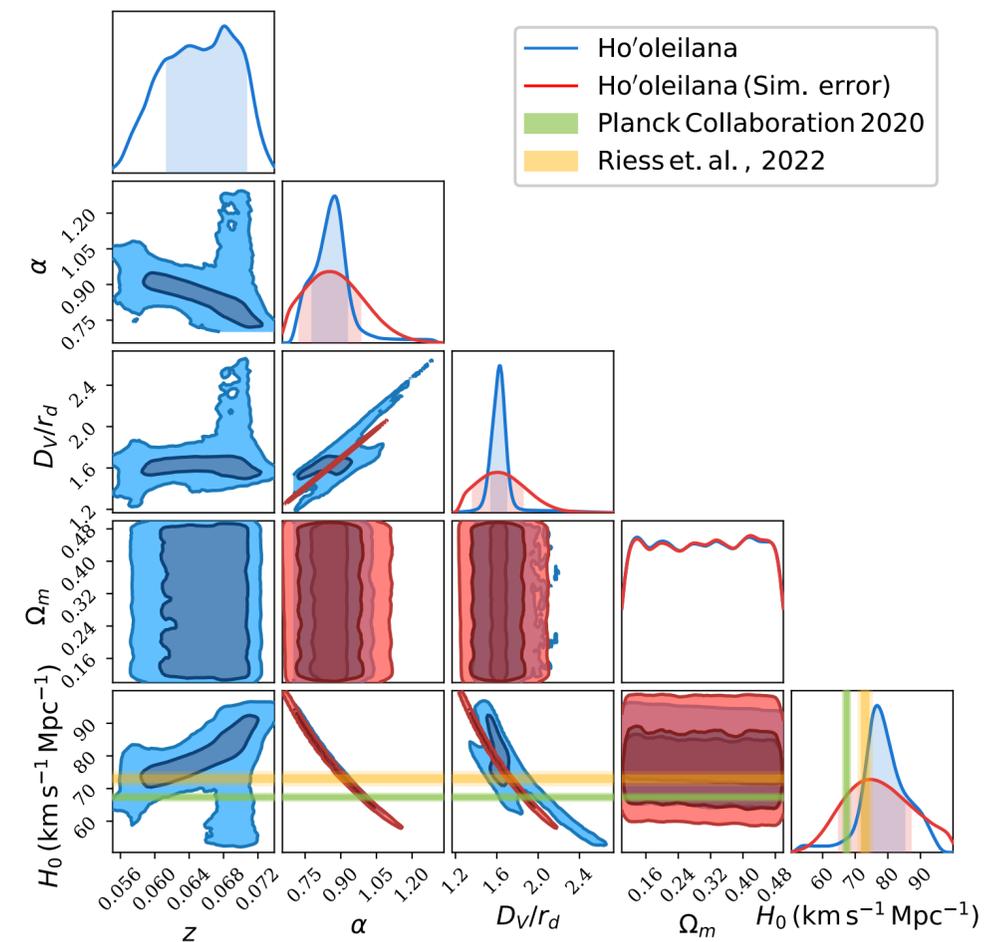
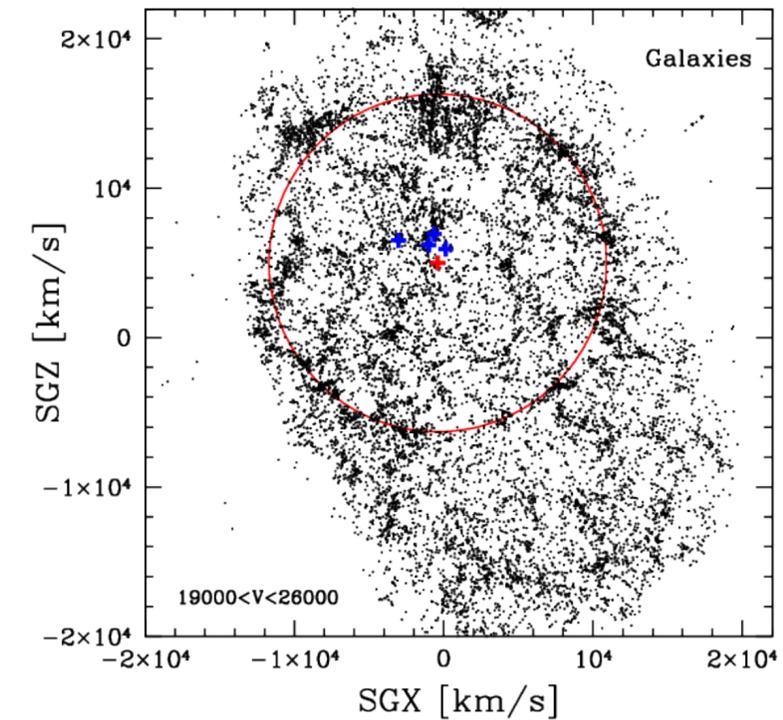
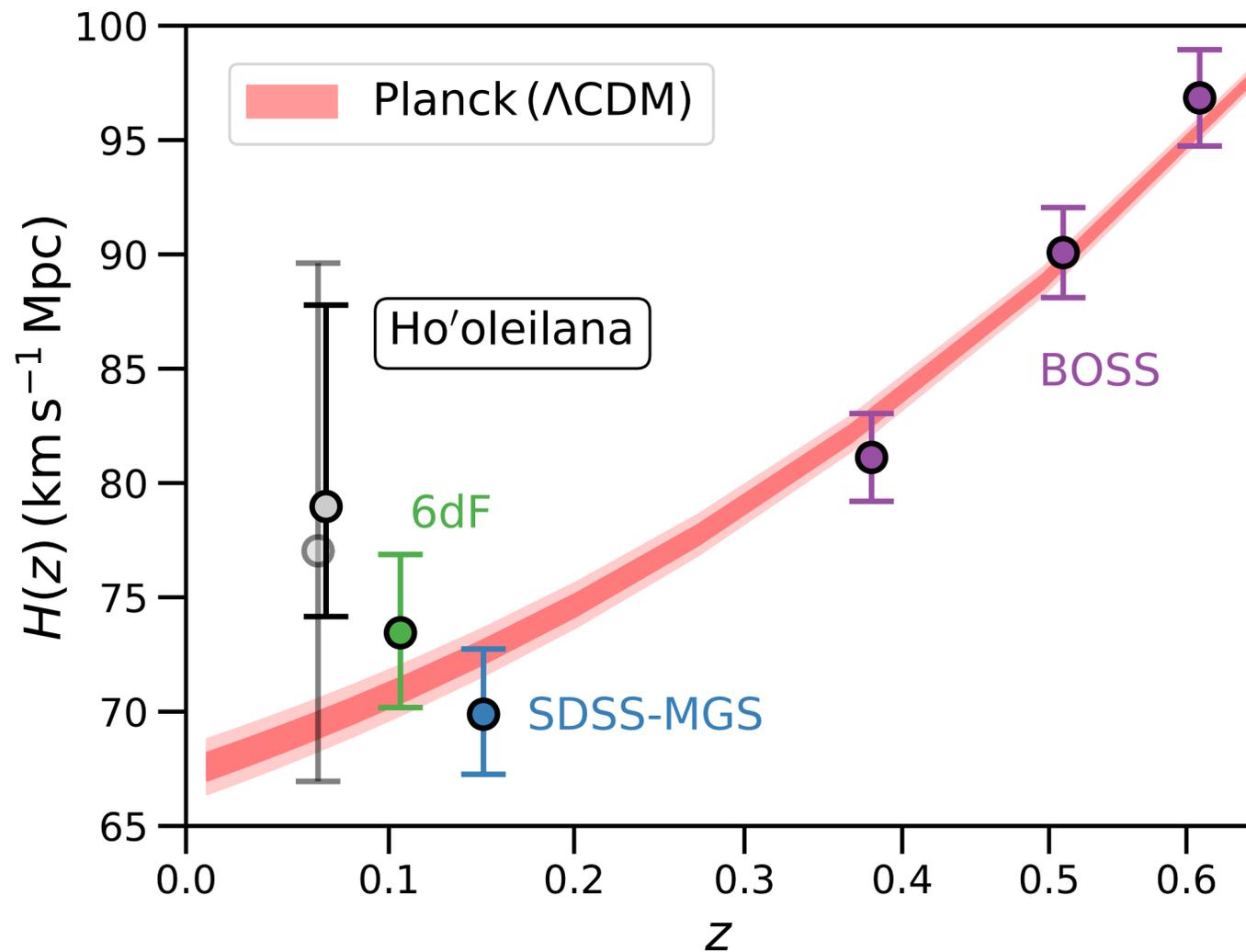
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## ABSTRACT

Theory of the physics of the early hot universe leads to a prediction of baryon acoustic oscillations that has received confirmation from the pair-wise separations of galaxies in samples of hundreds of thousands of objects. Evidence is presented here for the discovery of a remarkably strong *individual* contribution to the baryon acoustic oscillation (BAO) signal at  $z = 0.068$ , an entity that is given the name Ho'oleilana. The radius of the 3D structure is  $155 h_{75}^{-1}$  Mpc. At its core is the Boötes supercluster. The Sloan Great Wall, CfA Great Wall, and Hercules complex all lie within the BAO shell. The interpretation of Ho'oleilana as a BAO structure with our preferred analysis implies a value of the Hubble constant of  $76.9^{+8.2}_{-4.8} \text{ km s}^{-1} \text{ Mpc}^{-1}$ .



# The growth of structure of the minimally interacting pressureless sources (baryons and CDM) after decoupling

$$\partial_t^2 \delta_m = -2H \partial_t \delta_m + 4\pi G \bar{\rho}_m \delta_m$$

arXiv:2307.12763

## Dark energy in light of the early JWST observations: case for a negative cosmological constant?

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**Abstract.** Early data from the James Webb Space Telescope (JWST) has uncovered the existence of a surprisingly abundant population of very massive galaxies at extremely high redshift, which are hard to accommodate within the standard  $\Lambda$ CDM cosmology. We explore whether the JWST observations may be pointing towards more complex dynamics in the dark energy (DE) sector. Motivated by the ubiquity of anti-de Sitter vacua in string theory, we consider a string-inspired scenario where the DE sector consists of a negative cosmological constant (nCC) and a evolving component with positive energy density on top, whose equation of state is allowed to cross the phantom divide. We show that such a scenario can drastically alter the growth of structure compared to  $\Lambda$ CDM, and accommodate the otherwise puzzling JWST observations if the dynamical component evolves from the quintessence-like regime in the past to the phantom regime today: in particular, we demonstrate that the presence of a nCC (which requires a higher density for the evolving component) plays a crucial role in enhancing the predicted cumulative comoving stellar mass density. Our work reinforces the enormous potential held by observations of the abundance of high- $z$  galaxies in probing cosmological models and new fundamental physics, including string-inspired ingredients.

arXiv:2308.07046

## The density of virialized clusters as a probe of dark energy

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23 August 2023

### ABSTRACT

We use the spherical collapse model to demonstrate that the observable average density of virialized clusters depends on the properties of dark energy along with the properties of gravity on cluster scales and can therefore be used as a probe of these properties. As an application of this approach we derive the predicted virialized densities and radii of cluster mass structures for a wide range of values of the cosmological constant (including negative values) as a function of the turnaround redshift. For the value of  $\Omega_{\Lambda,0} = -0.7$  (with  $\Omega_{m,0} = 0.3$ ) preferred by  $\Lambda$  sign-switching models ( $\Lambda_s$ CDM) proposed for the resolution of the Hubble and  $S_8$  tensions, we find an amplification of the density of virialized clusters which can be as large as 80% compared to Planck18/ $\Lambda$ CDM for a turnaround redshift  $z_{\max} \gtrsim 2$ . Such an amplification may lead to more efficient early galaxy formation in this class of models in accordance with the recent findings of JWST.

**Key words:** Cosmology: Observations, Cosmology: Dark Energy