

Particle Physics

The Standard Model

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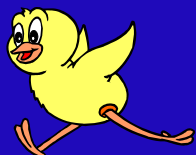
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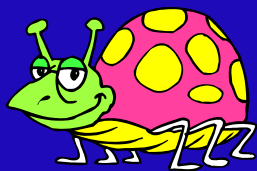
2. Quarks

- Quarks
- Colour
- Confinement
- Asymptotic Freedom

Quarks



up



down



charm



strange



top



beauty

Leptons



electron



neutrino e



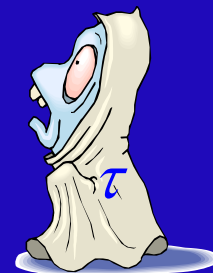
muon



neutrino μ

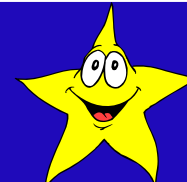


tau



neutrino τ

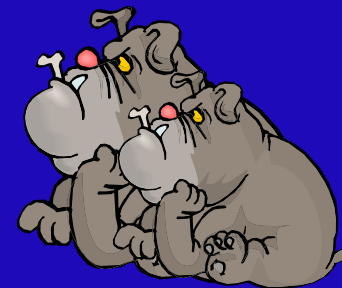
Bosons



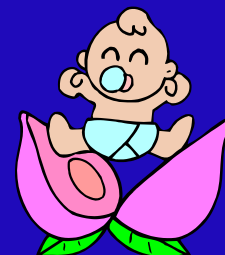
photon



gluon



Z⁰ W[±]



Higgs

QUARKS



- Strong Interactions bind them into hadrons
- Not Observed as Free Particles → Confinement
- Spin $\frac{1}{2}$; Pointlike ($r \leq \text{few} \times 10^{-17}$ cm)
- $Q_u = 2/3$; $Q_d = -1/3$

Family Structure:

$$\begin{pmatrix} u \\ d' \end{pmatrix}_L, \quad \begin{pmatrix} c \\ s' \end{pmatrix}_L, \quad \begin{pmatrix} t \\ b' \end{pmatrix}_L$$

Mass eigenstates \neq Flavour eigenstates

$$V_{\text{CKM}} \cdot V_{\text{CKM}}^\dagger = 1$$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = V_{\text{CKM}} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

Why 3?

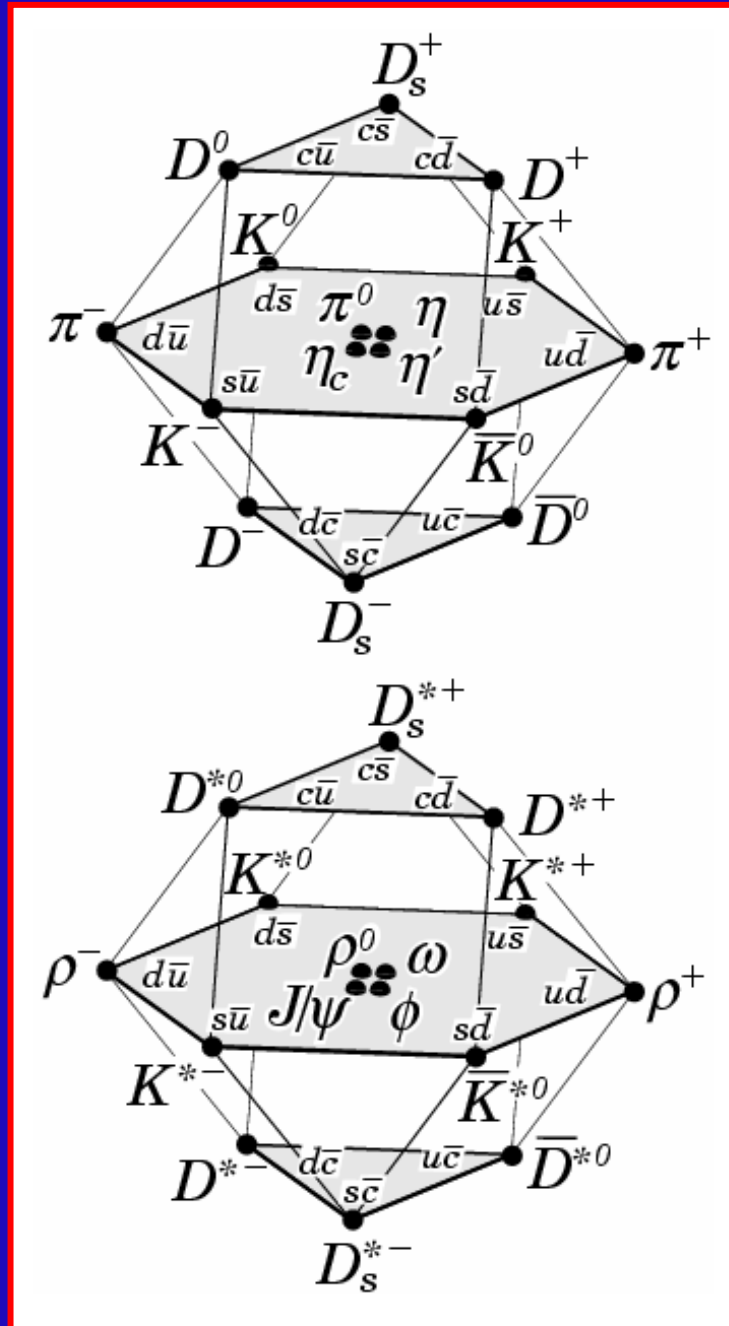
Light (MeV)	$m_u \sim 5$	$m_d \sim 8$	$m_s \sim 150$
Heavy (GeV)	$M_c \sim 1.2$	$M_b \sim 4.2$	$M_t \sim 178$

MESONS $\equiv q_1 \bar{q}_2$

Spin:

$$\frac{1}{2} \otimes \frac{1}{2} \rightarrow J = 0, 1$$

SU(4): u, d, s, c



(L=0)

J=0

J=1

BARYONS

$$\equiv q_1 q_2 q_3$$

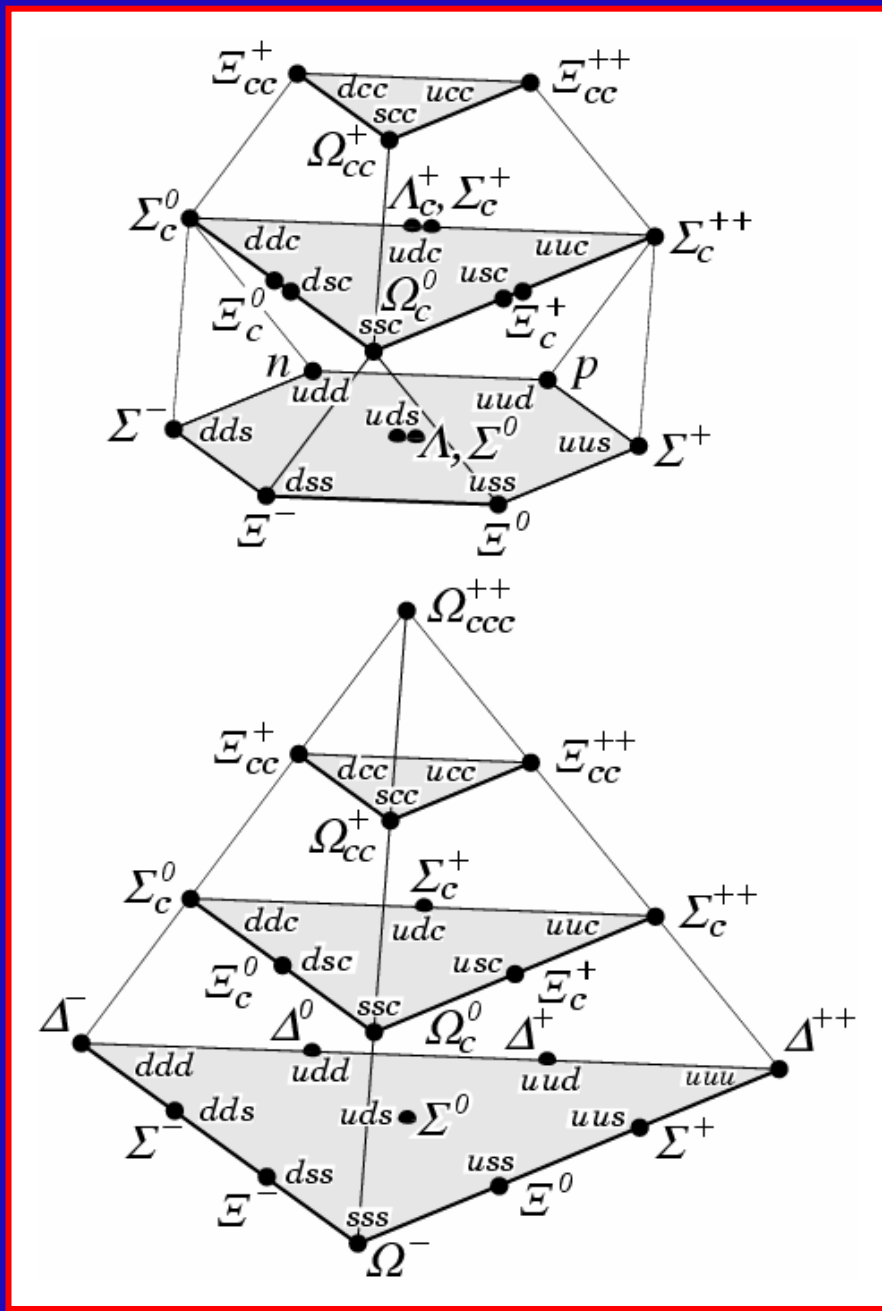
Baryon Number:

$$B(q_i) = \frac{1}{3}$$

Spin:

$$\frac{1}{2} \otimes \frac{1}{2} \otimes \frac{1}{2} \longrightarrow J = \frac{1}{2}, \frac{3}{2}$$

SU(4): u, d, s, c



(L = 0)

$J = \frac{1}{2}$

$J = \frac{3}{2}$

Hadronization Scale

$$\Lambda_\chi \sim 1 \text{ GeV}$$

ISOSPIN: u, d $M_p = 938.3 \text{ MeV}$; $M_n = 939.6 \text{ MeV}$ $m_{u,d} \ll \Lambda_\chi$

SU(3): u, d, s $M_\Lambda = 1115.7 \text{ MeV}$; $M_{\Xi^0} = 1314.8 \text{ MeV}$ $m_s < \Lambda_\chi$

SU(4): u, d, s, c $\Sigma_c = 2453 \text{ MeV}$; $\Omega_c^0 = 2704 \text{ MeV}$ $M_c \approx \Lambda_\chi$

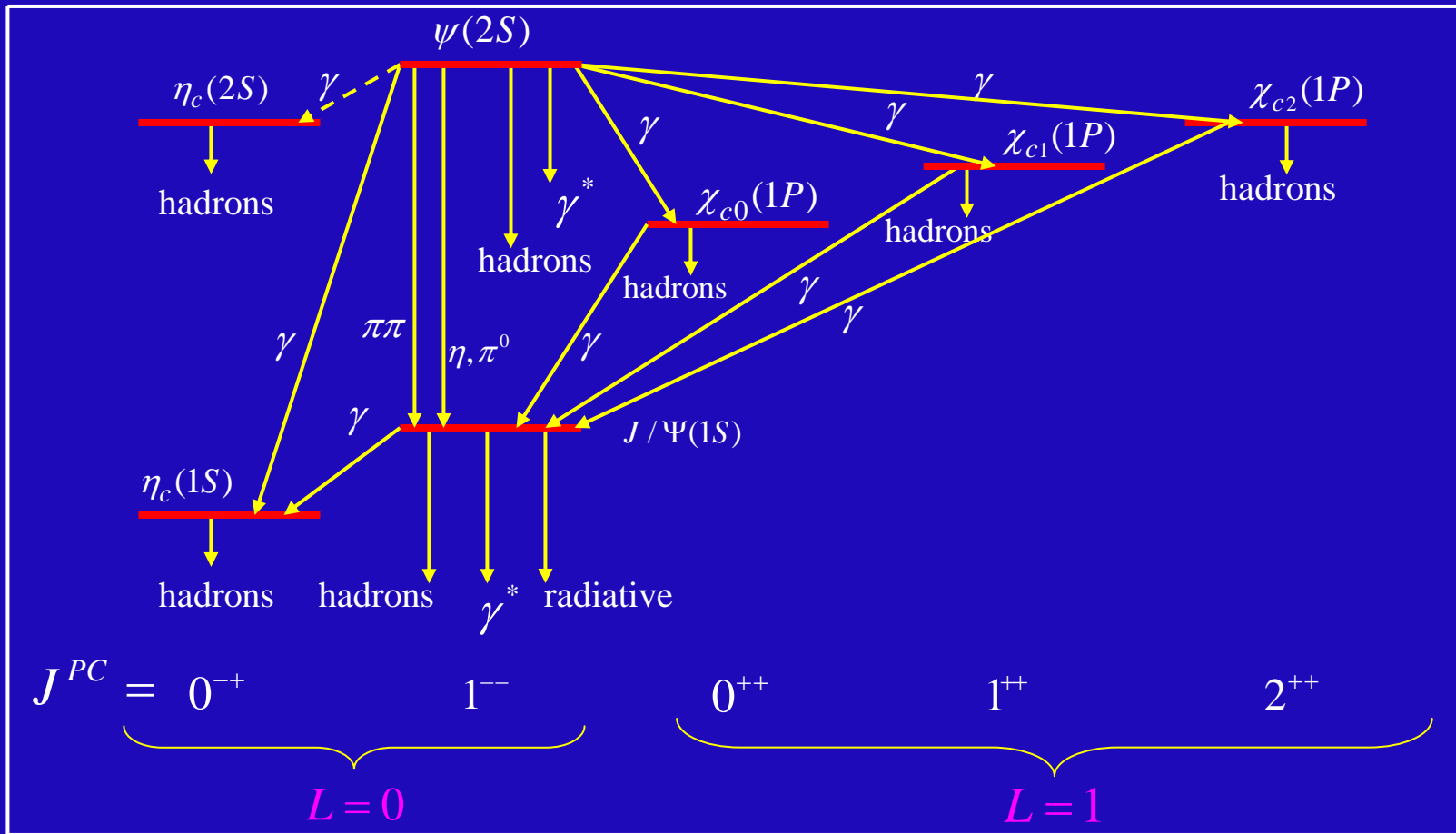
SU(5): u, d, s, c, b $M_{\Lambda_b^0} = 5624 \text{ MeV}$ $M_b > \Lambda_\chi$

SU(6): u, d, s, c, b, t $M_t = 178 \text{ GeV}$ $M_t \gg \Lambda_\chi$

$$\tau(t)^{-1} \equiv \Gamma(t \rightarrow \text{all}) \approx \Gamma(t \rightarrow b W^+) \gg \Lambda_\chi$$

The Top Quark has no time to Hadronize

CHARMONIUM



Bound $c\bar{c}$ States

$M_{\eta_c(1S)} = 2.980 \text{ GeV}$; $M_{\eta_c(2S)} = 3.594 \text{ GeV}$

$M_{J/\Psi(1S)} = 3.097 \text{ GeV}$; $M_{\Psi(2S)} = 3.686 \text{ GeV}$

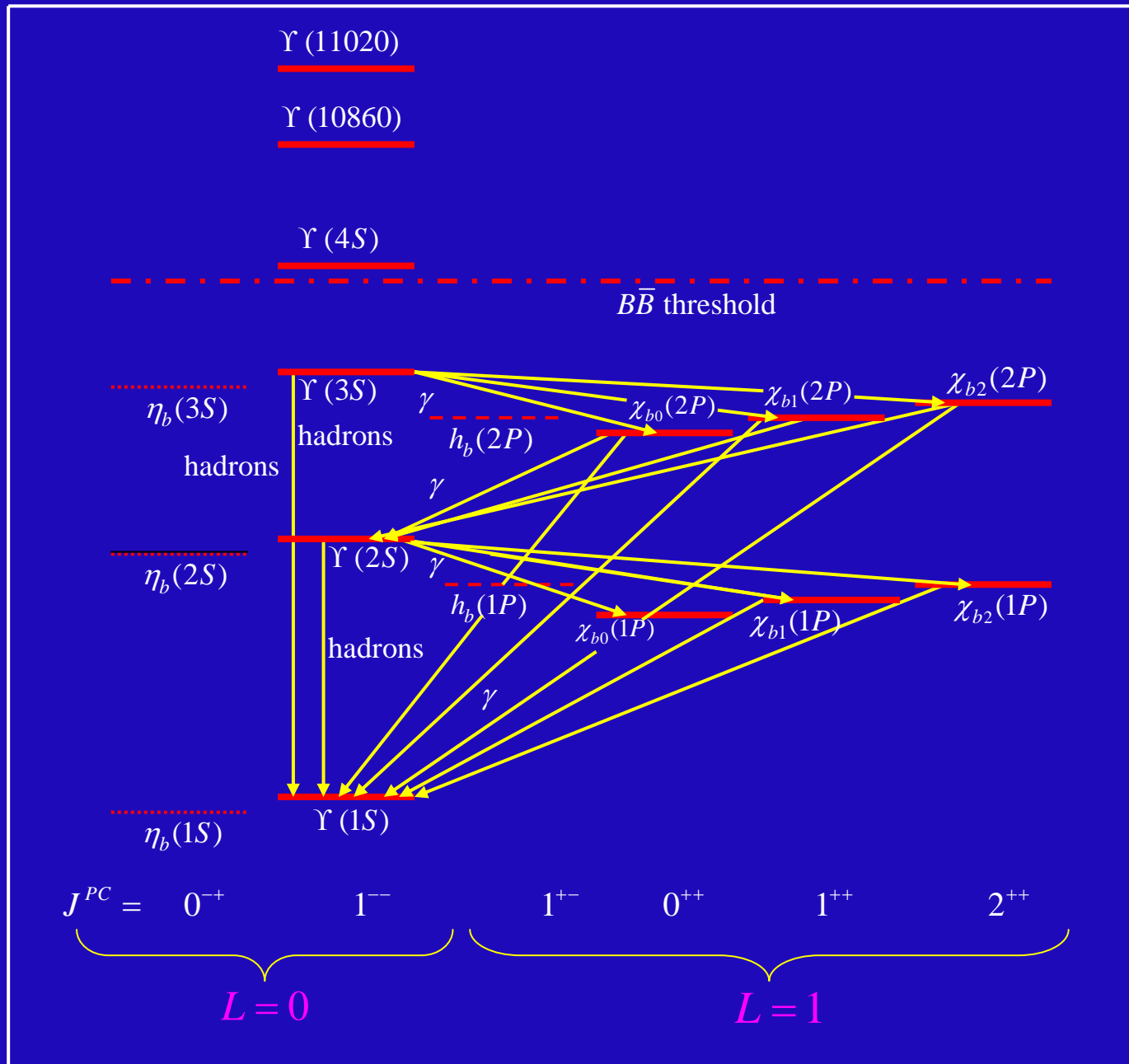
$$V_{c\bar{c}}(r) = -C_F \frac{\alpha_s}{r} + k r$$

$C_F = \frac{4}{3}$; $\alpha_s \simeq 0.21$; $k \simeq 1 \text{ GeV fm}^{-1}$

C-NON-C

$b\bar{b}$ States

$$\alpha_s \approx 0.18$$



QUARKS HAVE COLOUR

$$\Delta^{++} = u^\uparrow u^\uparrow u^\uparrow \quad (J = \frac{3}{2}, J_3 = \frac{3}{2})$$

Fermi Statistics



$$\Delta^{++} \approx \varepsilon^{\alpha\beta\gamma} u_\alpha^\uparrow u_\beta^\uparrow u_\gamma^\uparrow$$

$$B \approx \varepsilon^{\alpha\beta\gamma} q_\alpha^i q_\beta^j q_\gamma^k \quad ; \quad M \approx \delta^{\alpha\beta} q_\alpha^i \bar{q}_\beta^j \quad (i, j, k = u, d, s, \dots \ ; \ \alpha, \beta, \gamma = 1, \dots, N_c)$$

$$N_c = 3$$



$$q^i q^i q^i$$

We don't see Colour Multiplets



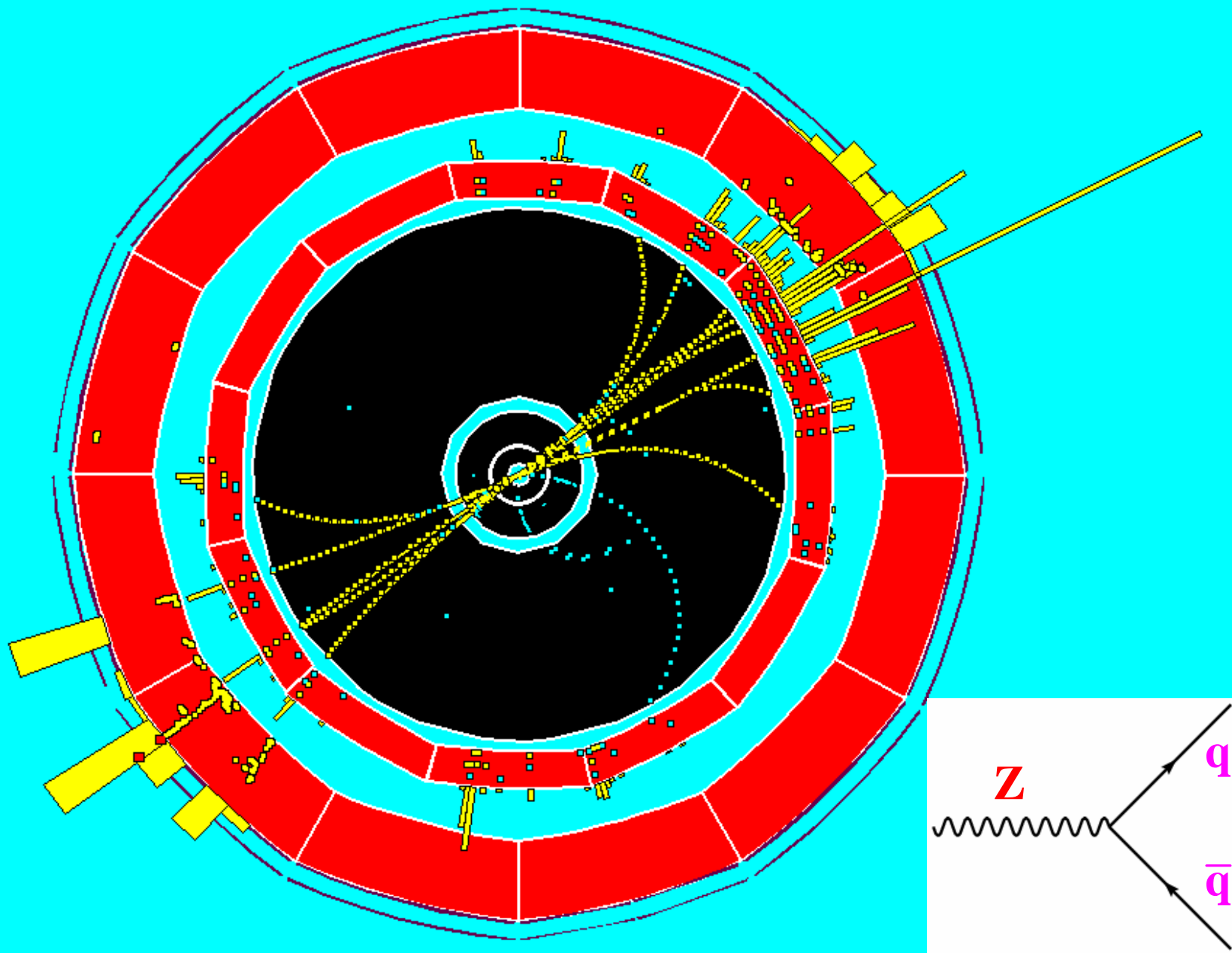
Hadrons are Colour Singlets

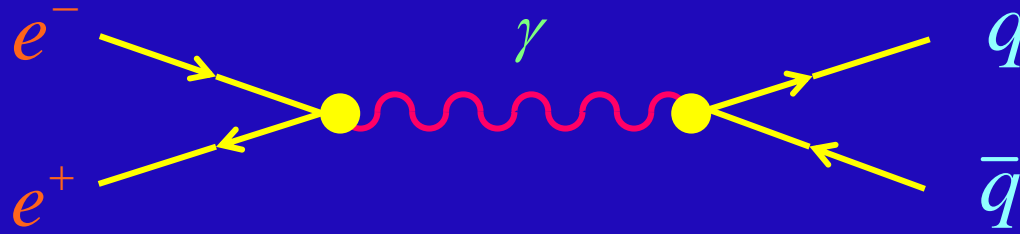
(qqq , $\bar{q}\bar{q}\bar{q}$ and $q\bar{q}$; BUT NOT qq and $qqqq$)

We don't see Quarks



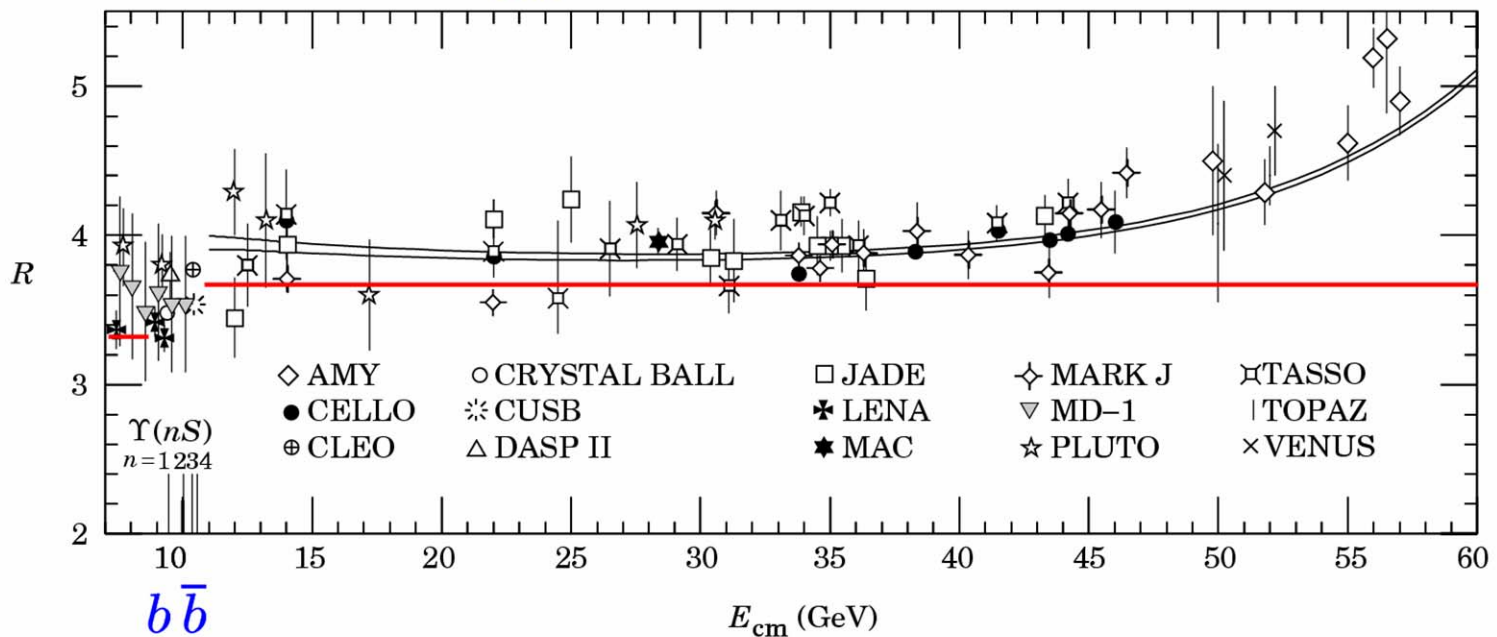
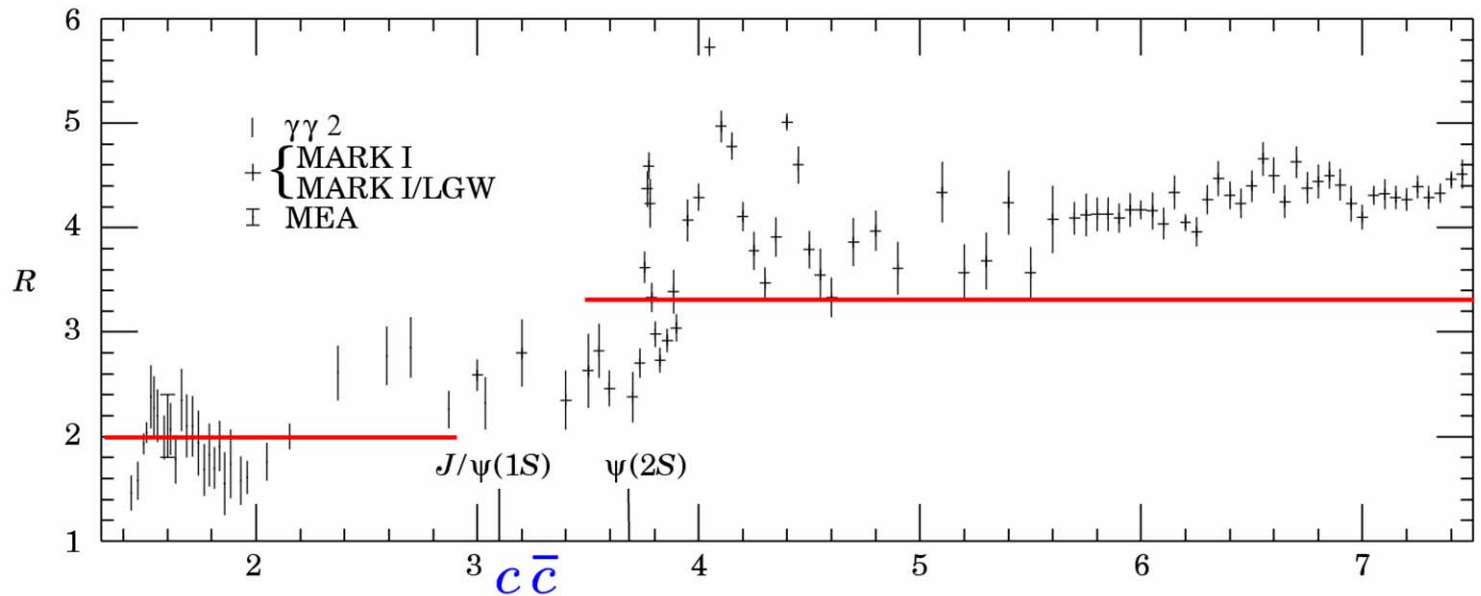
- ◆ Don't exist ?
- ◆ **CONFINEMENT**





$$R \equiv \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} \simeq \frac{\sum_q \sigma(e^+e^- \rightarrow q\bar{q})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} \simeq N_c \sum_q Q_q^2$$

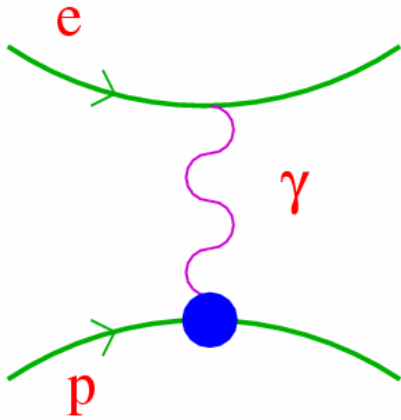
$$= \left\{ \begin{array}{l} \frac{2}{3} N_c \quad , \quad (u, d, s) \\ \frac{10}{9} N_c \quad , \quad (u, d, s, c) \\ \frac{11}{9} N_c \quad , \quad (u, d, s, c, b) \end{array} \right.$$



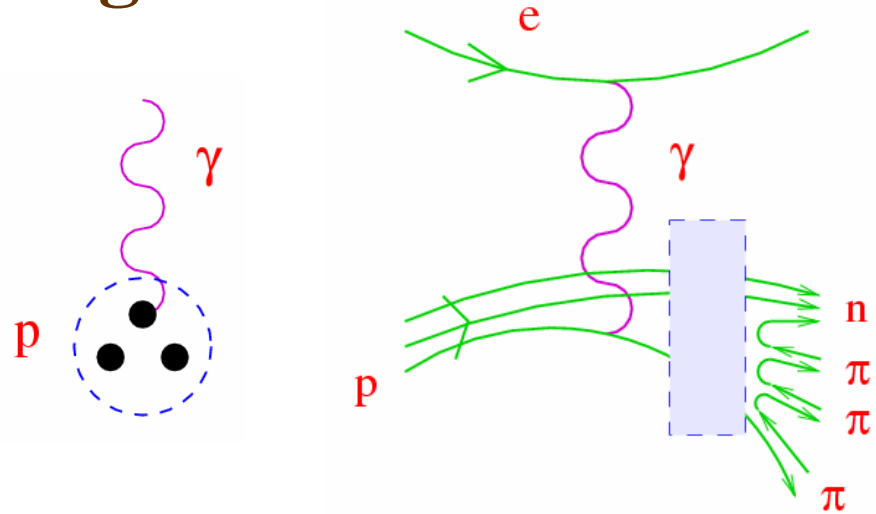
$e p$ Scattering

$$\lambda = h/q$$

Small E



High E



High-Energy hadronic processes are well described through the interactions of **free** constituent quarks

$$\sigma(e^- p \rightarrow e^- X) \approx \sum_q P_q \sigma(e^- q \rightarrow e^- q)$$

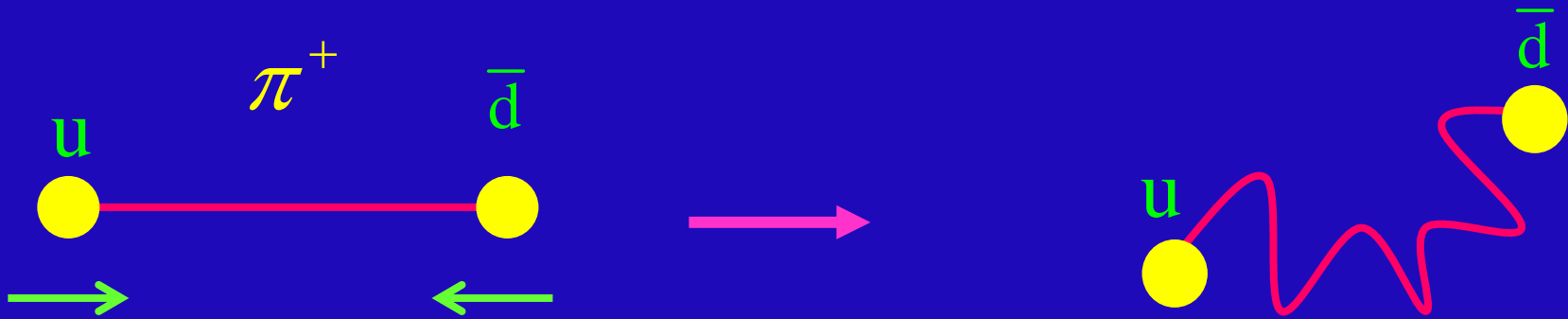
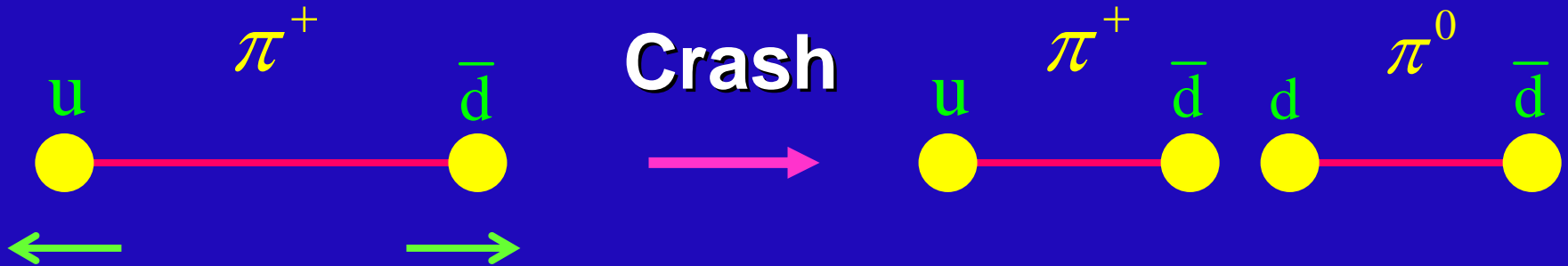
ASYMPTOTIC FREEDOM:

$\alpha_s \rightarrow 0$ at large E (short distances)

CONFINEMENT:

Large α_s at small E (large distances)

CONFINEMENT



ASYMPTOTIC

FREEDOM

ASYMPTOTIC FREEDOM:

$\alpha_s \rightarrow 0$ at large E (short distances)

CONFINEMENT:

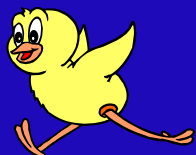
Large α_s at small E (large distances)

Quark Flavour (u, d, s, c, b, t)

Strong Interactions are $\left\{ \begin{array}{l} \text{Flavour Independent} \\ \text{Flavour Conserving} \end{array} \right\}$ COLOURDYNAMICS

Weak Interactions change the Quark Flavour: FLAVOURDYNAMICS

Quarks



up



down



charm



strange



top



beauty

Leptons



electron



neutrino e



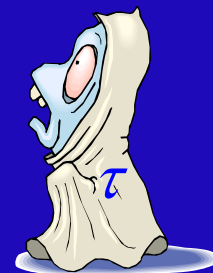
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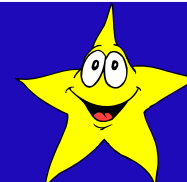


tau



neutrino τ

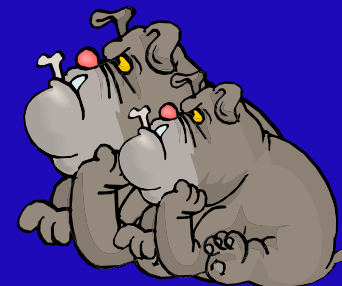
Bosons



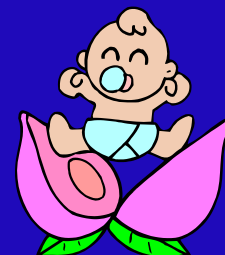
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$Z^0 W^\pm$



Higgs