

Workshop on Testing Fundamental Physics Principles, Corfu2017

Test of hypothetical forces at short range

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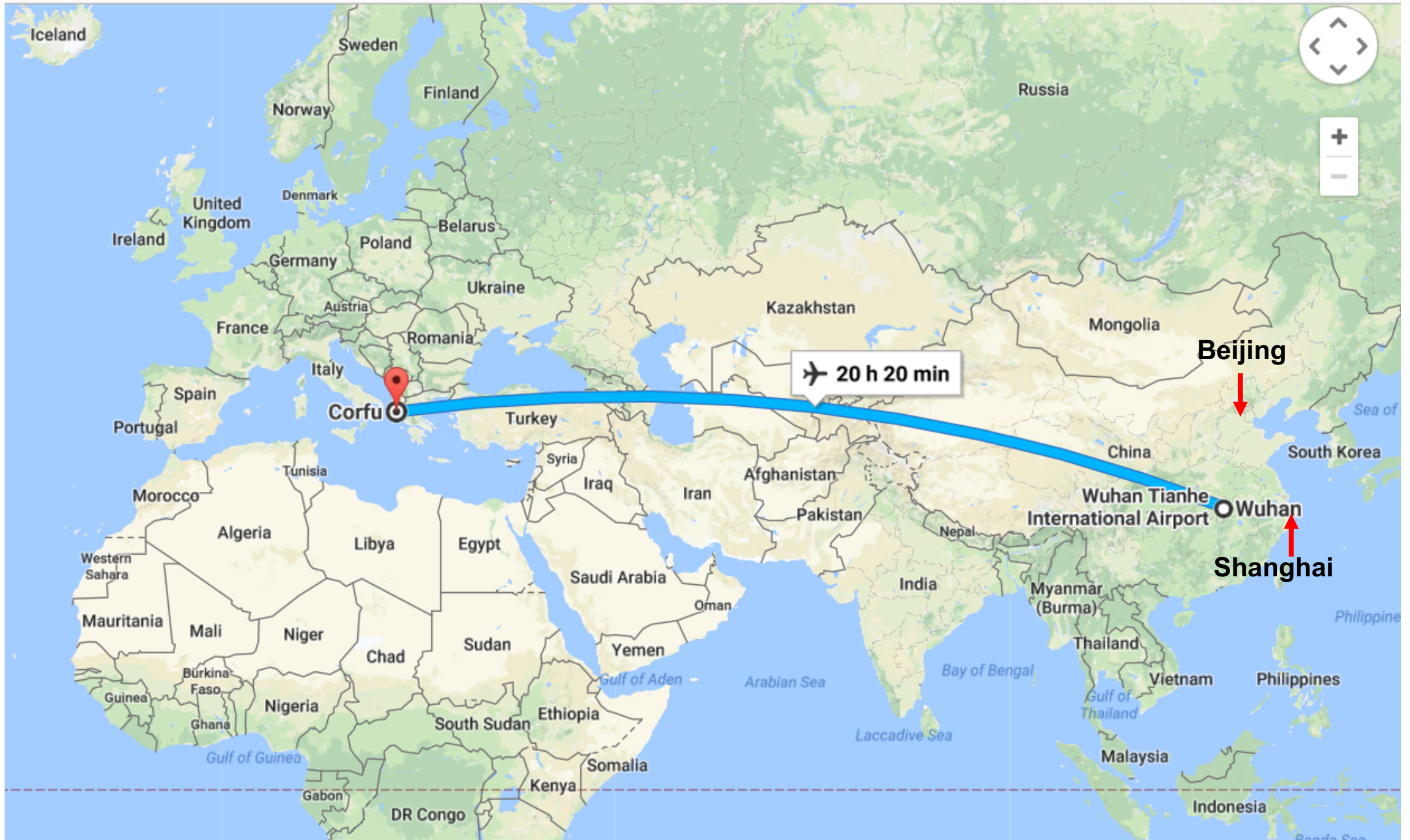


華中科技大學 物理學院

SCHOOL OF PHYSICS . HUAZHONG UNIVERSITY OF SCIENCE AND TECHNOLOGY



Where are we from?



Center for gravitational experiments, HUST



- **Precision Gravity Measurement National Facility**
 - > Inertial Sensor, Geophysics,
- **Test of fundamental principles by precision measurements**
 - > Big G measurement
 - > Test of Newton's inverse law (hypothetical forces)
 - > Test of equivalent principle
 - > Test of Lorentz violation
 - > Cold atoms and optical clocks
 - >



Center for gravitational experiments, HUST



- Precision Gravity Measurement National Facility
 - > Inertial Sensor, Geophysics,
- Test of fundamental principles by precision measurements
 - > Big G measurement
 - > **Test of Newton's inverse square law (hypothetical forces)**
 - > Test of equivalent principle
 - > Test of Lorentz violation (**Shao's talk**)
 - > Cold atoms and optical clocks
 - >



- Gravity with n extra dimensions

Yukawa correction

$$V(r) = \begin{cases} -\frac{G_4 m_1 m_2}{r} (1 + \alpha e^{-r/\lambda}) & (r \gg R) \\ -\frac{G_{4+n} m_1 m_2}{r^{n+1}} & (r \leq R) \end{cases}$$

Large extra dimensions: N. Arkani-Hamed, S. Dimopoulos, G. Dvali, PLB 429(1998) 263

- Forces mediated by new light bosons

$$V(r) = -g^2 \frac{e^{-r/\lambda}}{r}$$

New light bosons: moduli, dilatons, scalar axions, ...

$$\lambda = h / (mc)$$

$$\begin{aligned} \lambda \sim 1 \mu\text{m}: m \sim 0.2 \text{ eV} \\ \lambda \sim 1 \text{ nm}: m \sim 200 \text{ eV} \end{aligned}$$

Hypothetical short-ranged forces



Single Boson Exchange Potentials

Spin-independent

$$V_1 \propto f \frac{1}{r} e^{-r/\lambda}$$

B. Dobrescu and I. Mocioiu,
J. High Energy Phys. 11 (2006) 005.

Monopole-dipole:

$$V_{4+5} = -Z \left[f_{\perp}^{ee} + f_{\perp}^{ep} + \left(\frac{A-Z}{Z} \right) f_{\perp}^{en} \right] \frac{\hbar^2}{8\pi m_e c} [\hat{\sigma}_1 \cdot (\vec{v} \times \hat{r})] \left(\frac{1}{\lambda r} + \frac{1}{r^2} \right) e^{-r/\lambda}$$

$$V_{9+10} = Z \left[f_r^{ee} + f_r^{ep} + \left(\frac{A-Z}{Z} \right) f_r^{en} \right] \frac{\hbar^2}{8\pi m_e} (\hat{\sigma}_1 \cdot \hat{r}) \left(\frac{1}{\lambda r} + \frac{1}{r^2} \right) e^{-r/\lambda} \quad \text{Axion, axion-like particle}$$

$$V_{12+13} = Z \left[f_v^{ee} + f_v^{ep} + \left(\frac{A-Z}{Z} \right) f_v^{en} \right] \frac{\hbar}{8\pi} (\hat{\sigma}_1 \cdot \vec{v}) \left(\frac{1}{r} \right) e^{-r/\lambda},$$

Static, dipole-dipole:

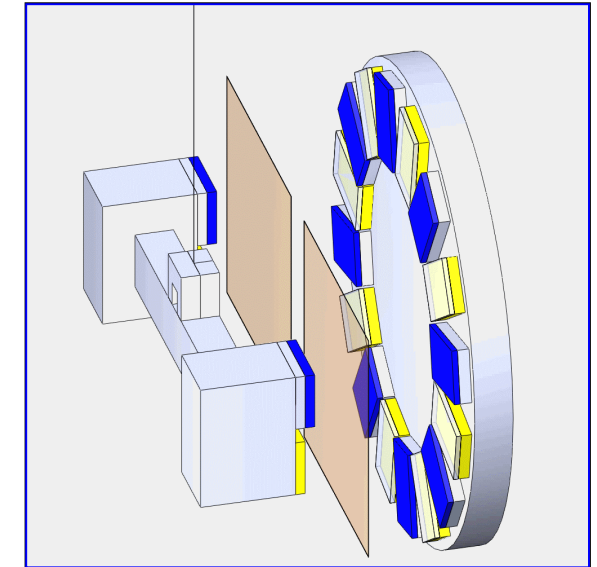
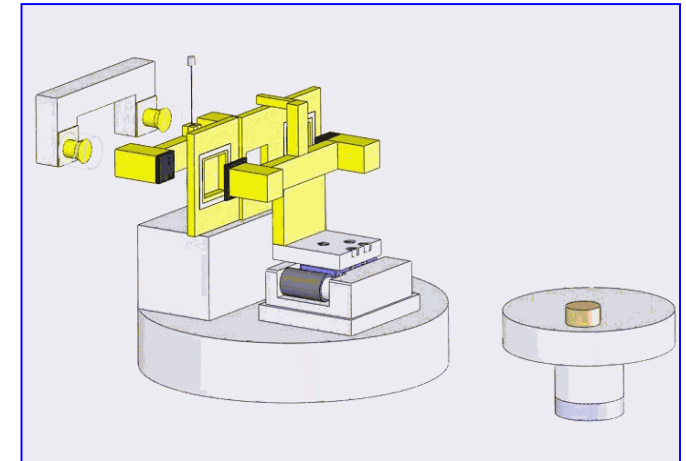
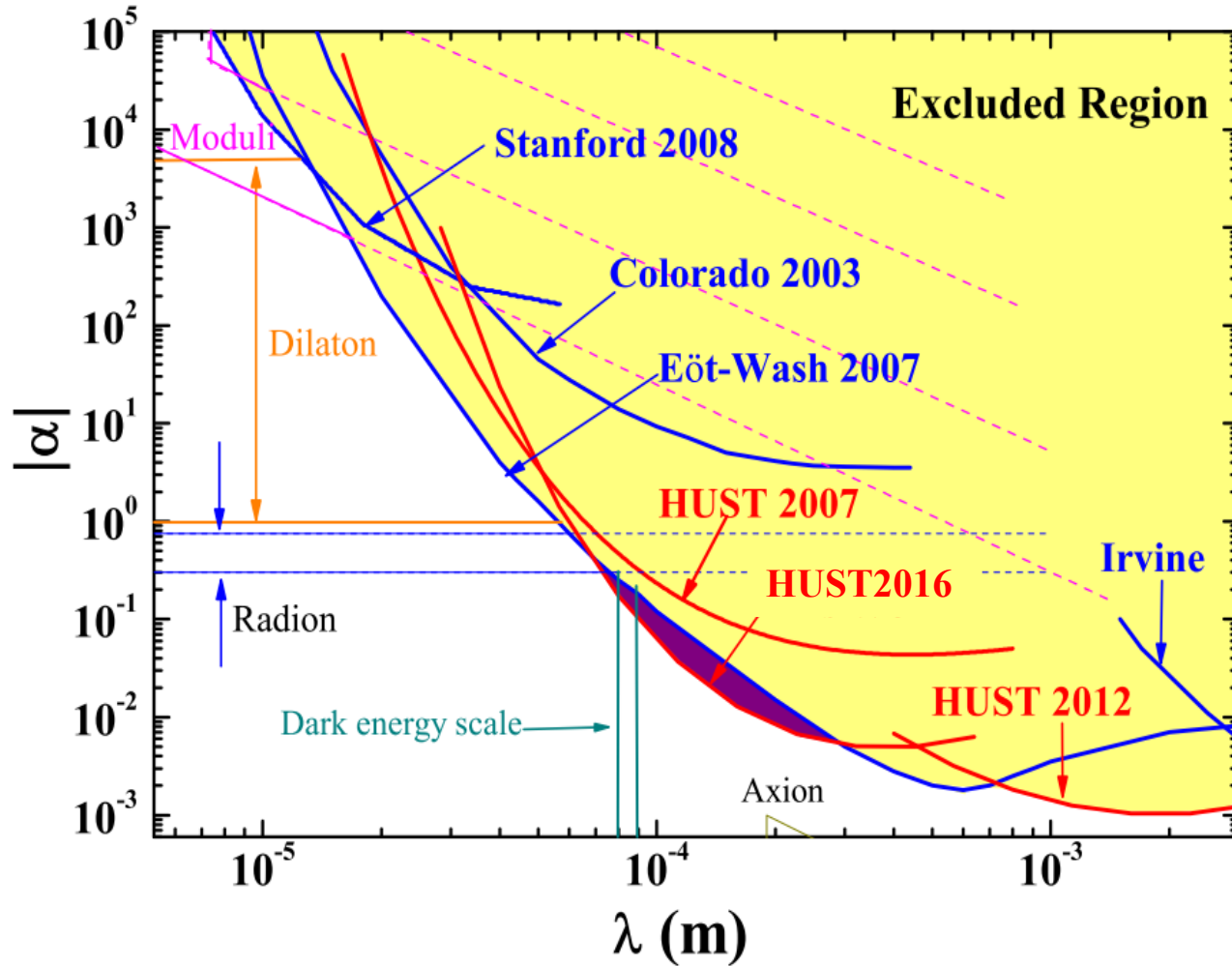
$$V_2 = f_2^{ee} \frac{\hbar c}{4\pi} (\hat{\sigma}_1 \cdot \hat{\sigma}_2) \left(\frac{1}{r} \right) e^{-r/\lambda}$$

$$V_3 = f_3^{ee} \frac{\hbar^3}{4\pi m_e^2 c} \left[(\hat{\sigma}_1 \cdot \hat{\sigma}_2) \left(\frac{1}{\lambda r^2} + \frac{1}{r^3} \right) - (\hat{\sigma}_1 \cdot \hat{r})(\hat{\sigma}_2 \cdot \hat{r}) \left(\frac{1}{\lambda^2 r} + \frac{3}{\lambda r^2} + \frac{3}{r^3} \right) \right] e^{-r/\lambda} \quad \text{Axion, axion-like particle}$$

$$V_{11} = -f_{11}^{ee} \frac{\hbar^2}{4\pi m_e} [(\hat{\sigma}_1 \times \hat{\sigma}_2) \cdot \hat{r}] \left(\frac{1}{\lambda r} + \frac{1}{r^2} \right) e^{-r/\lambda}.$$

Velocity dependent, dipole-dipole: ...

Short range gravity experiments



Liang-Cheng Tu, Jun Luo *et al.*, PRL 98, 201101 (2007)
Shan-Qing Yang, Jun Luo *et al.*, PRL 108, 081101 (2012)
Wen-Hai Tan, Jun Luo *et al.*, PRL 116, 131101 (2016)

- **Experimental Search for Yukawa-type forces at the micrometer range**
- **Constraints on the spin-spin interactions at the nanometer range**

- **Experimental Search for Yukawa-type forces at the micrometer scale**
- Constraints on the spin-spin interactions at the nanometer scale

Search for Yukawa forces at micrometer range

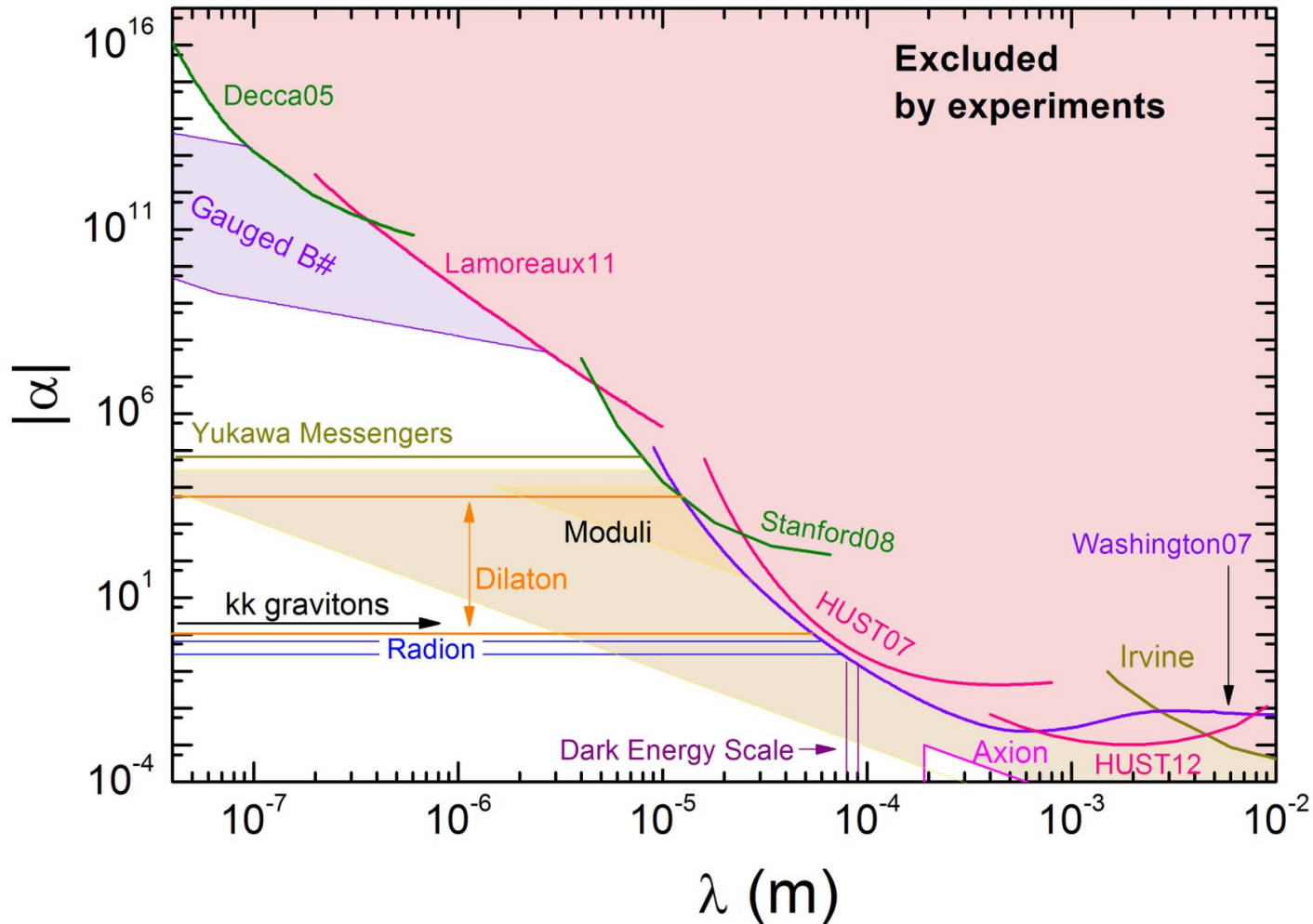


$$V(r) = -\frac{Gm_1m_2}{r} (1 + \alpha e^{-r/\lambda})$$

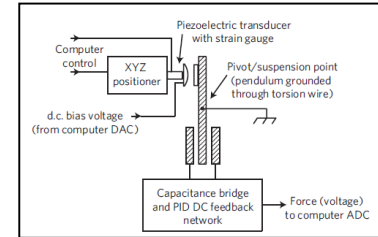
- To be sensitive to forces of range λ , $r \sim \lambda \sim \mu m$
- The force would be small if exists: size of the two interacting bodies $\sim \lambda$
- The disturbance is expected to be large: at such short range, the Casimir force and electrostatic forces contribute
- Approach and alignments: usually adopt a sphere-plate geometry

Constraints at micrometer range

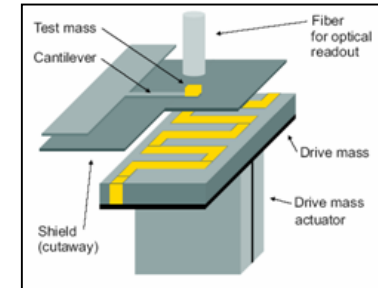
Yukawa Potential:
$$V(r) = \frac{Gm_1m_2}{r} (1 + \alpha e^{-r/\lambda})$$



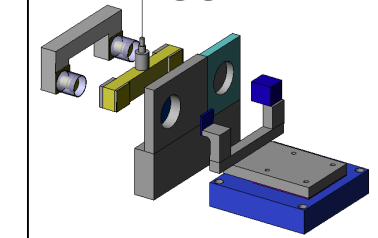
Lamoreaux



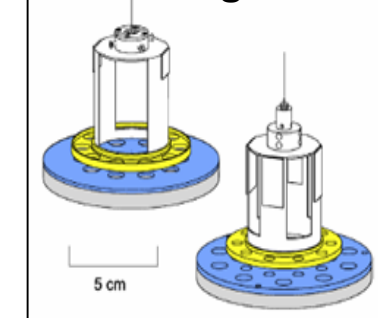
Stanford



HUST



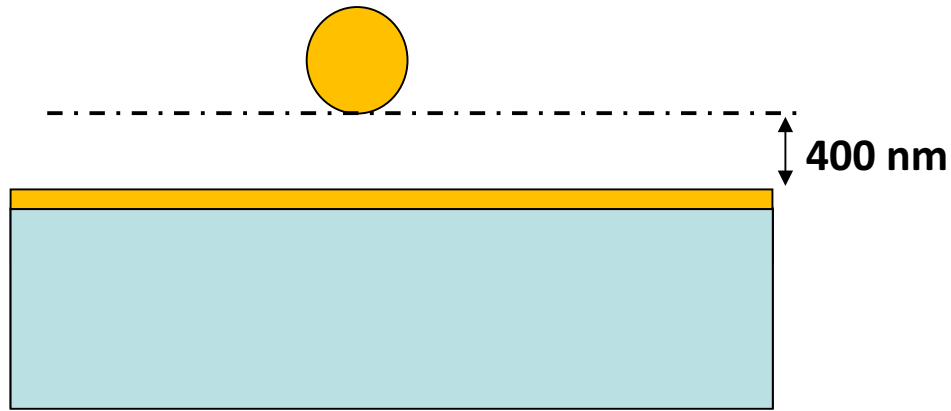
Washington



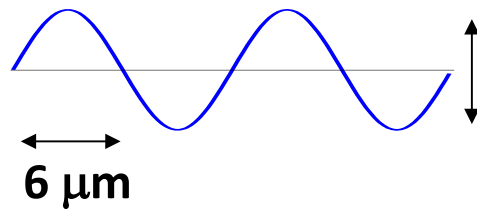
Experimental Scheme



$(d_t = 25 \mu\text{m})$



**Lateral
Yukawa Force**



$\sim 1.7 \times 10^{-16} \text{ N}$ ($\alpha = 3.0 \times 10^8$ $\lambda = 1 \mu\text{m}$)

Casimir : $\sim 4.3 \times 10^{-13} \text{ N}$

**Electrostatic : $\sim 3.3 \times 10^{-15} \text{ N}$
($\Delta V = 2 \text{ mV}$)**

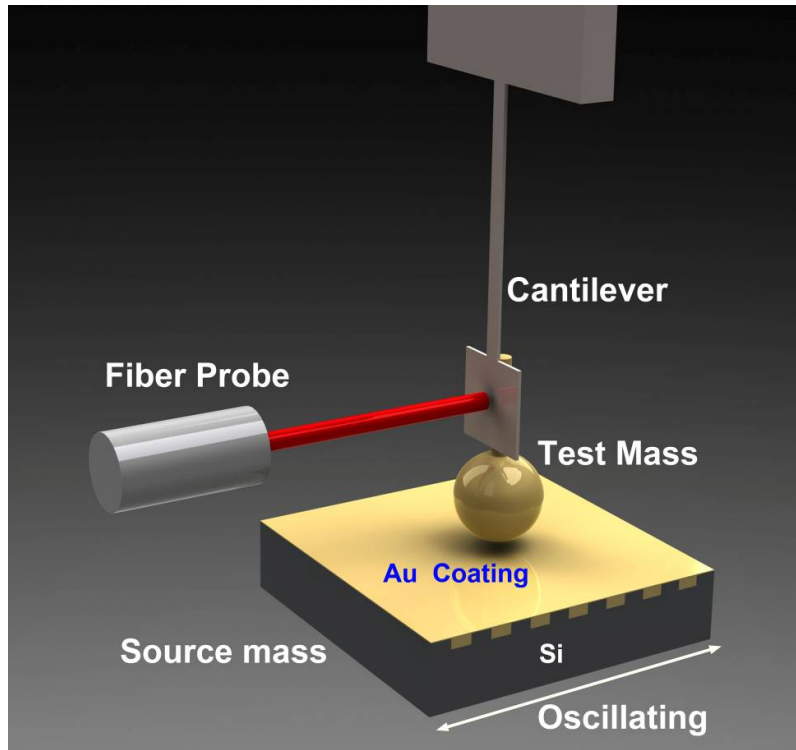
Projected: $1.0 \times 10^{-16} \text{ N}$



Density modulation



Signal of interest @ $n \times f_d$



- Cantilever: $\sim \text{mN/m}$
 - Pendulum-like: sensitive to lateral force
 - Laser interferometer:
 $\sim 2 \text{ pm/Hz}^{1/2}$ @ 16.8 Hz
 - Density modulation: period $\sim 12 \mu\text{m}$
 - Isoelectronic surface: gold coating
- make the Casimir & electrostatic forces constant

→ “null” test

Density modulation

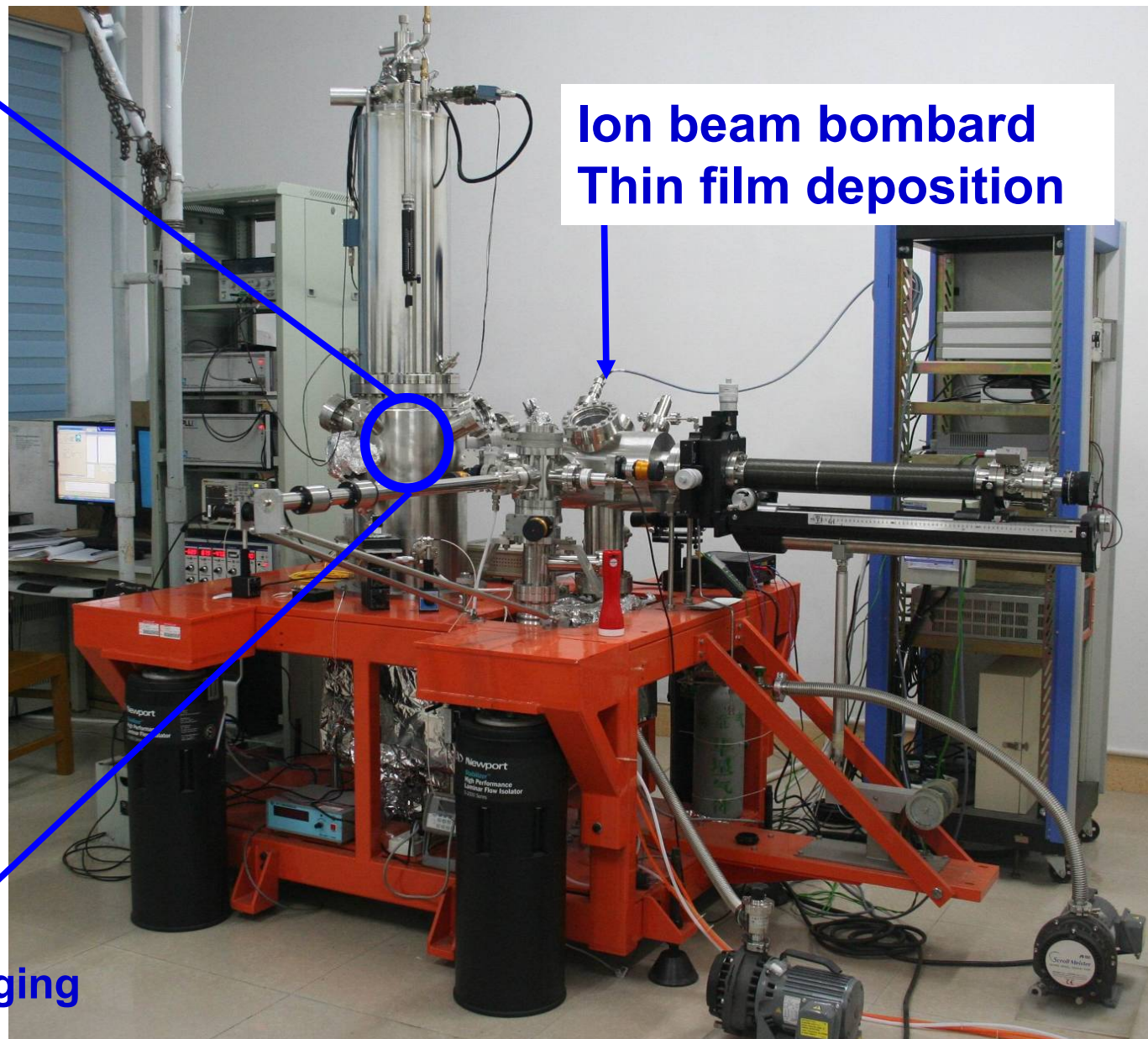
↓ Oscillating
amplitude: $18.4 \mu\text{m}$

Signal frequency : $8f_d$

Apparatus

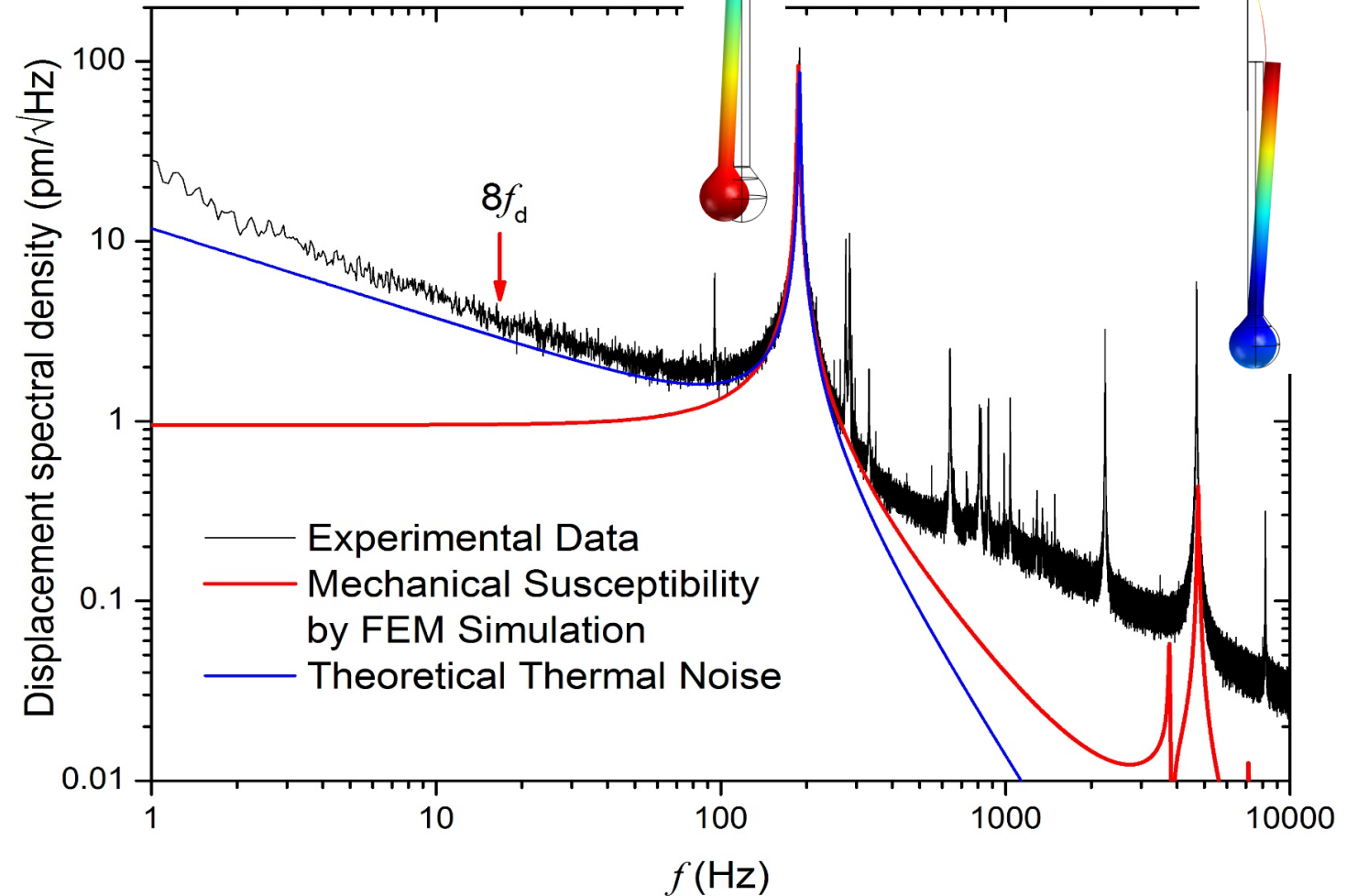
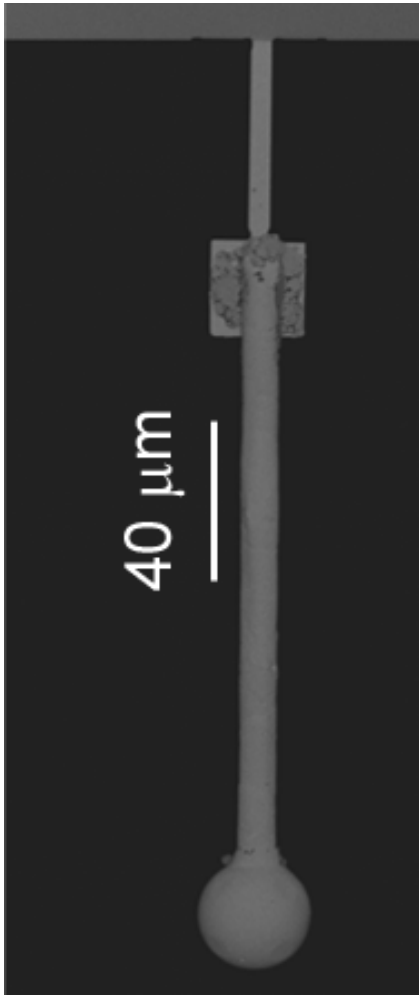


Surface imaging
Surface potential imaging
ISL exp.



Ion beam bombard
Thin film deposition

Cantilever: force sensitivity



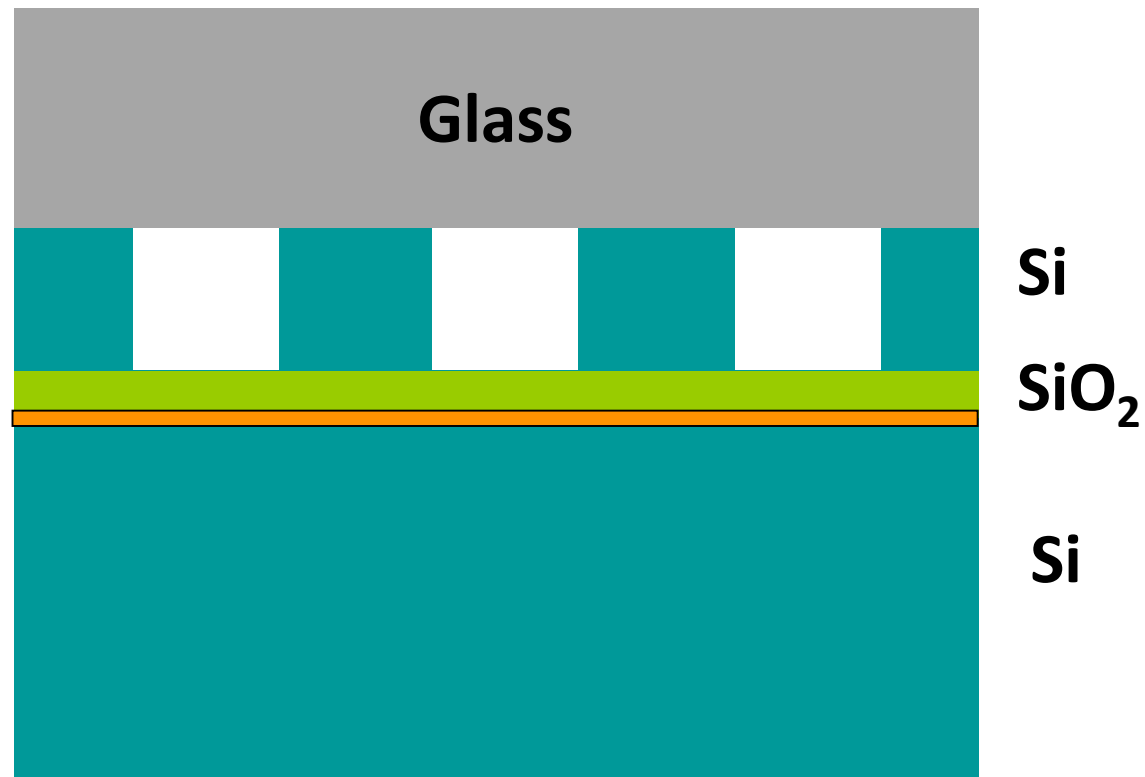
$$k = 1.3 (2) \text{ mN/m}$$

$$\text{Force noise level: } 6 \times 10^{-15} \text{ N/} \sqrt{\text{Hz}}$$

Density modulated source mass



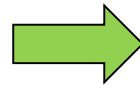
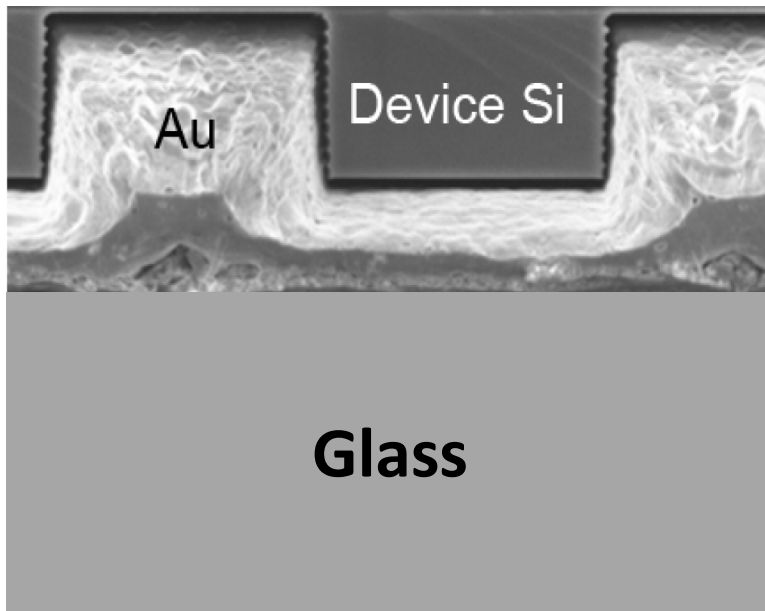
Density modulation + Flat + isoelectronic



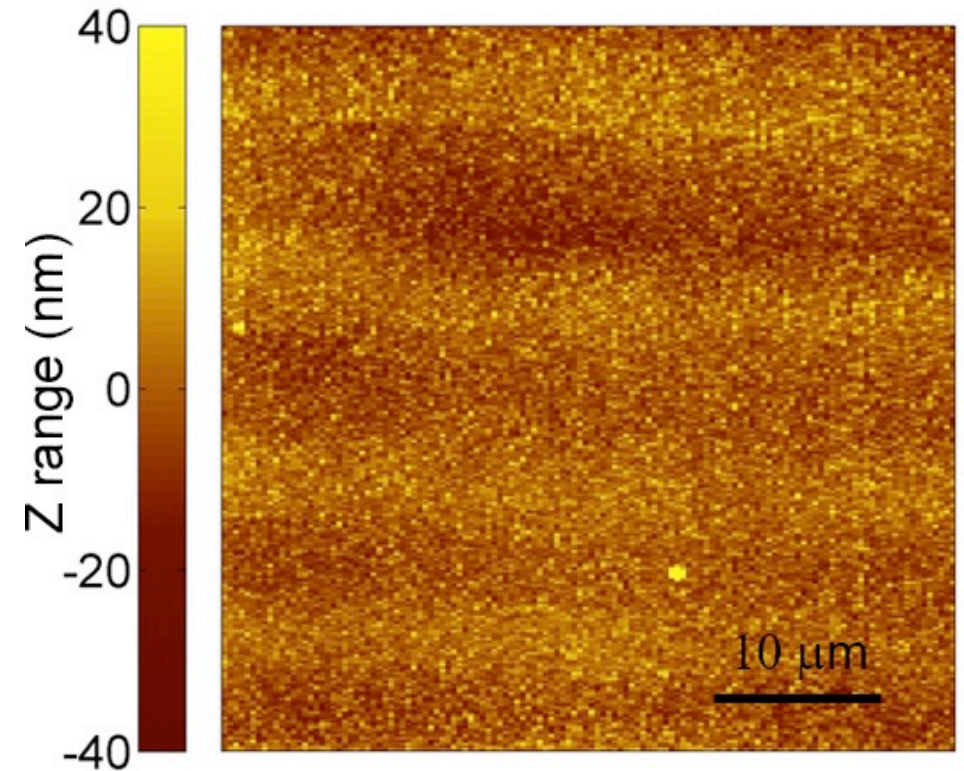
Process based on silicon on insulator (SOI) wafer

Density modulated source mass

SEM Image

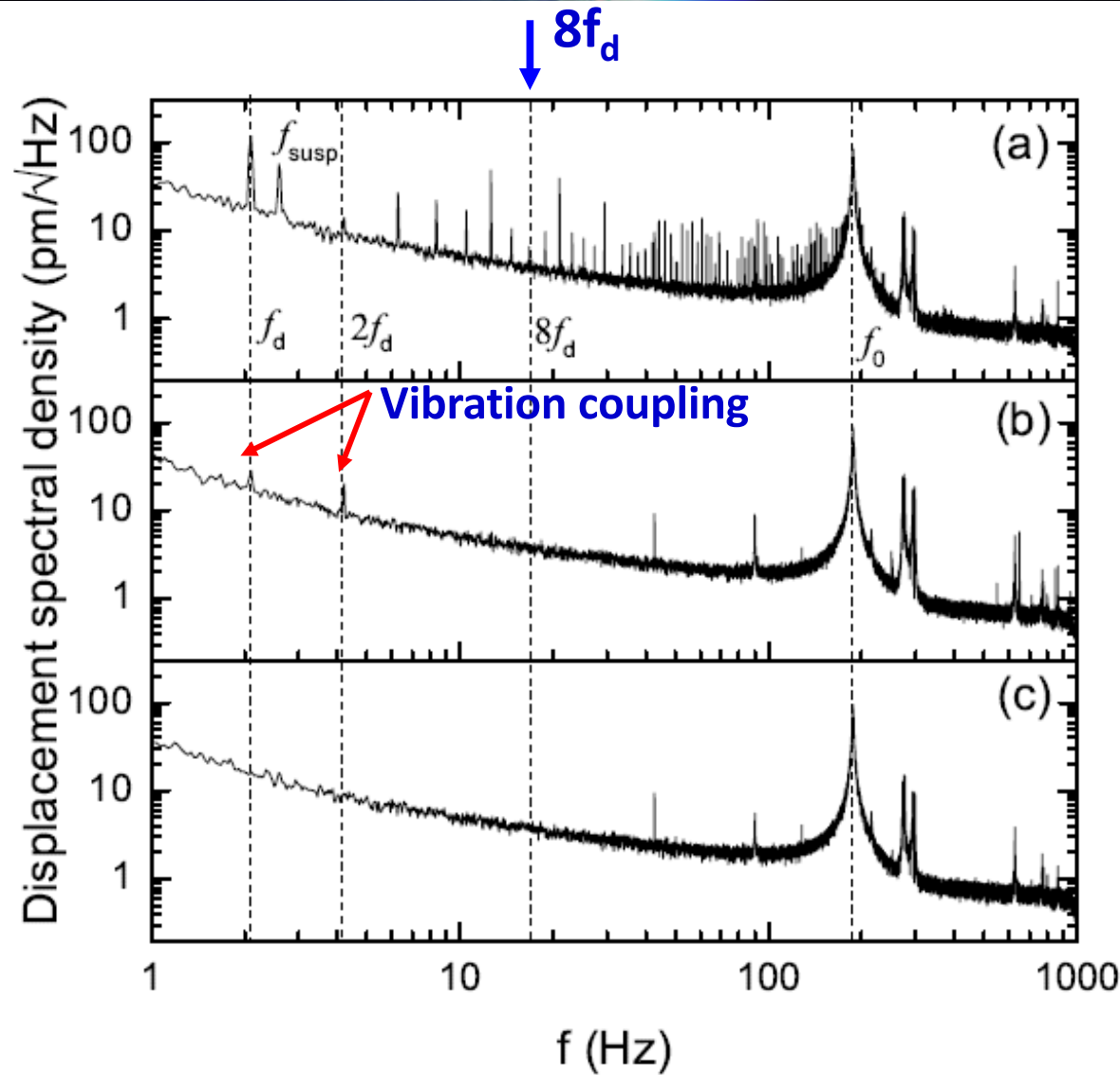


AFM Image



Averaged corrugation: ~3 nm

Control experiments



Oscillating
 $d \sim 640 \text{ nm}$

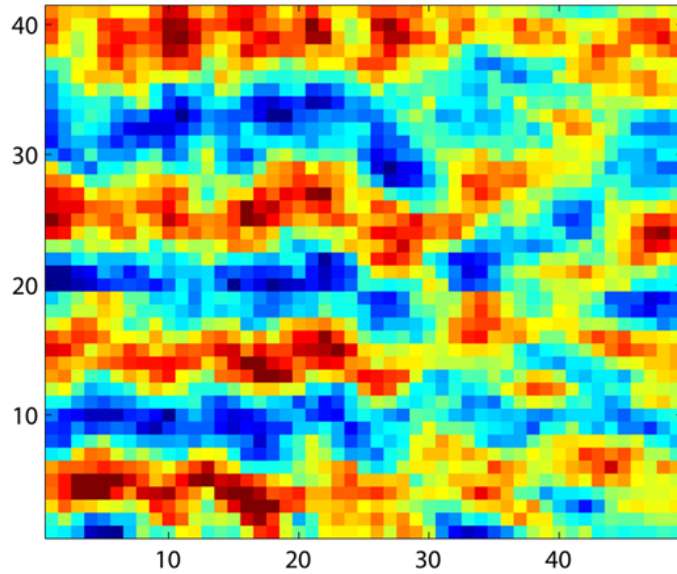
Oscillating
 $d \sim 3 \mu\text{m}$

at rest

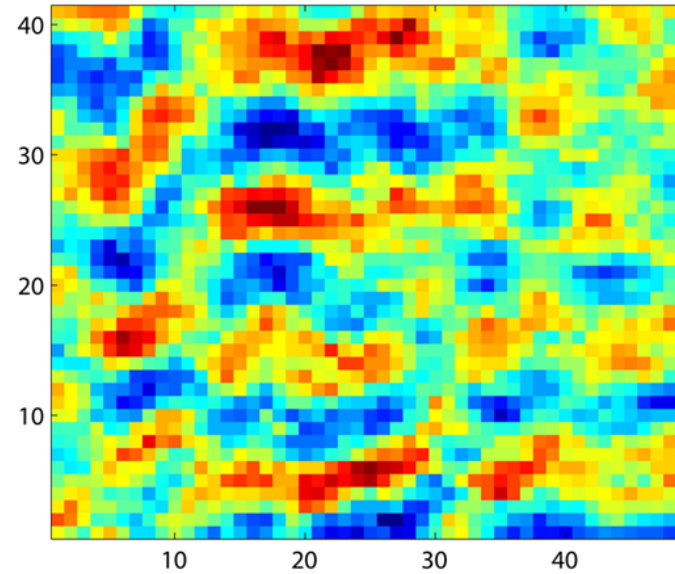
Observed non-zero signal at $8f_d$ where signal of interest is expected.

Mapping the force at $8f_d$

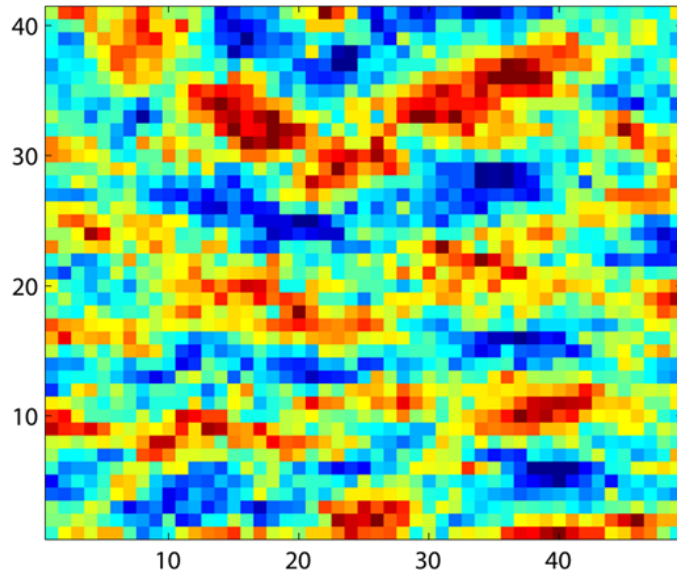
150 nm gold coating



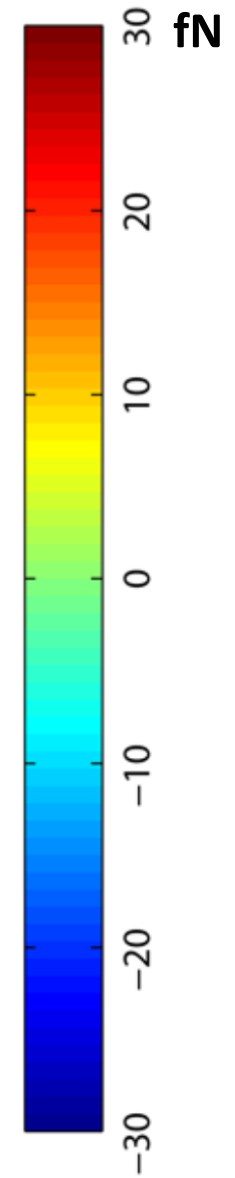
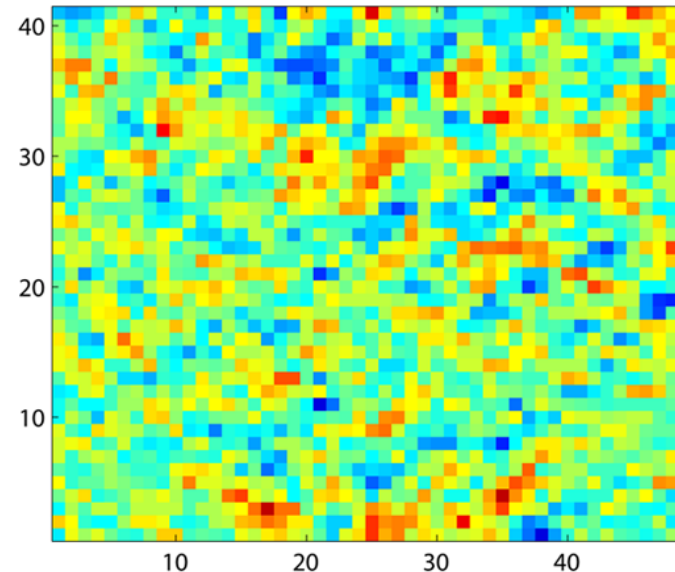
300 nm gold coating



500 nm gold coating



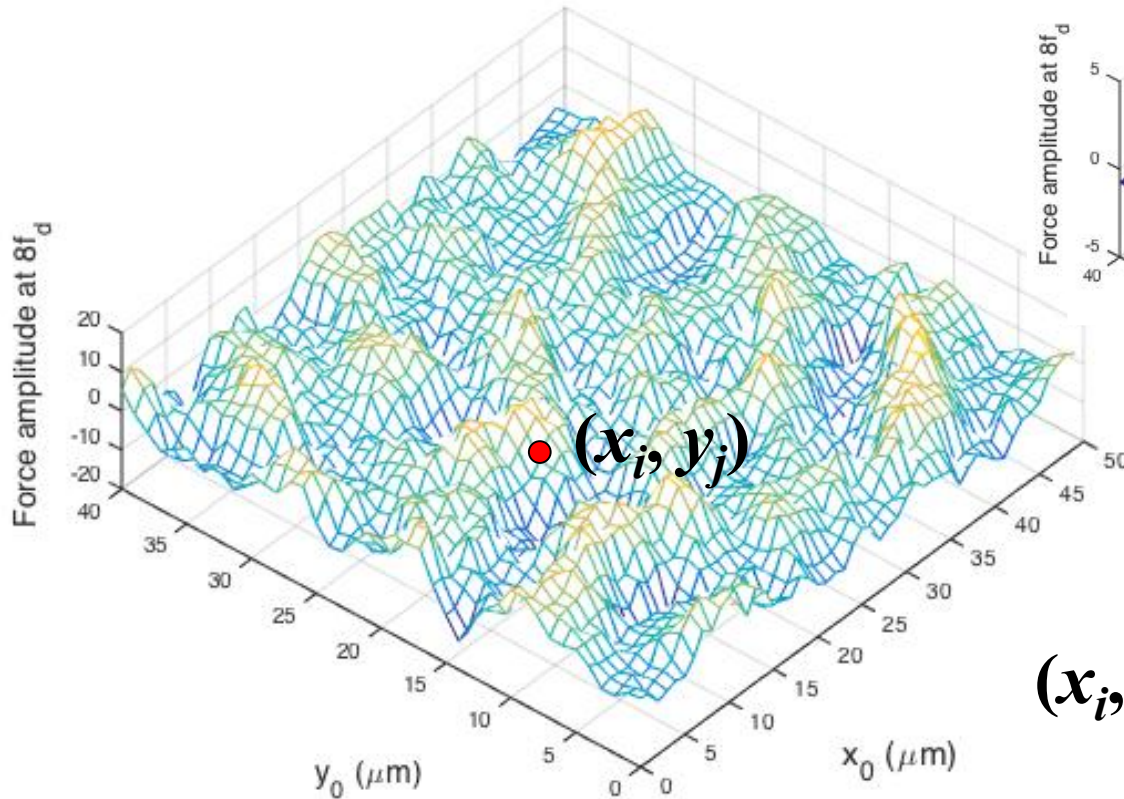
500 nm + annealing @150°C, 12hr



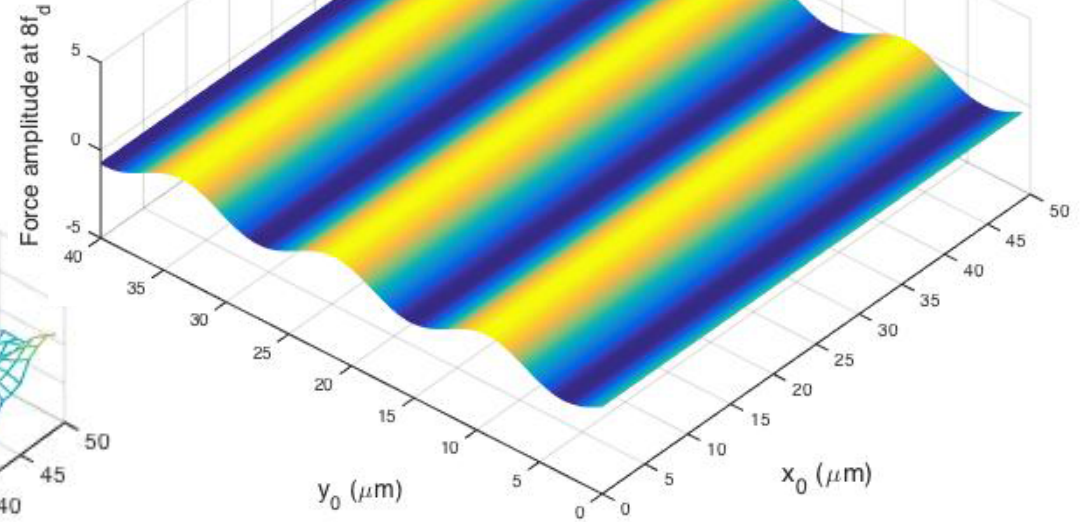
Maximum likelihood estimation



What we observed



What we expect
(α, λ, y_{00})



$$(x_i, y_j): P_{i,j}(F_{i,j}^{\text{exp}} | y_{00}, \alpha) = \frac{1}{\sqrt{2\pi}\sigma_{i,j}} e^{-\frac{F_{i,j}^{\text{exp}} - F_{i,j}^T}{\sigma_{i,j}}}$$

$$\sigma_{i,j} = \sqrt{(\delta F_{i,j}^{\text{exp}})^2 + (\delta F_{i,j}^T)^2}$$

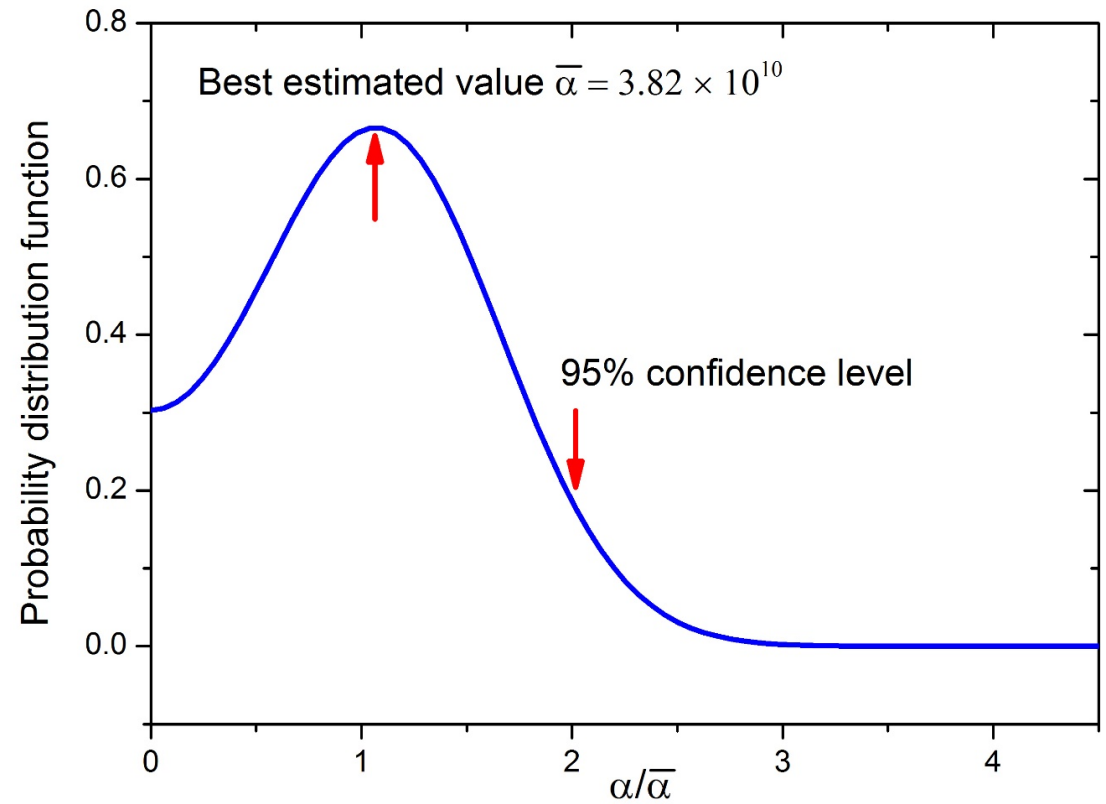
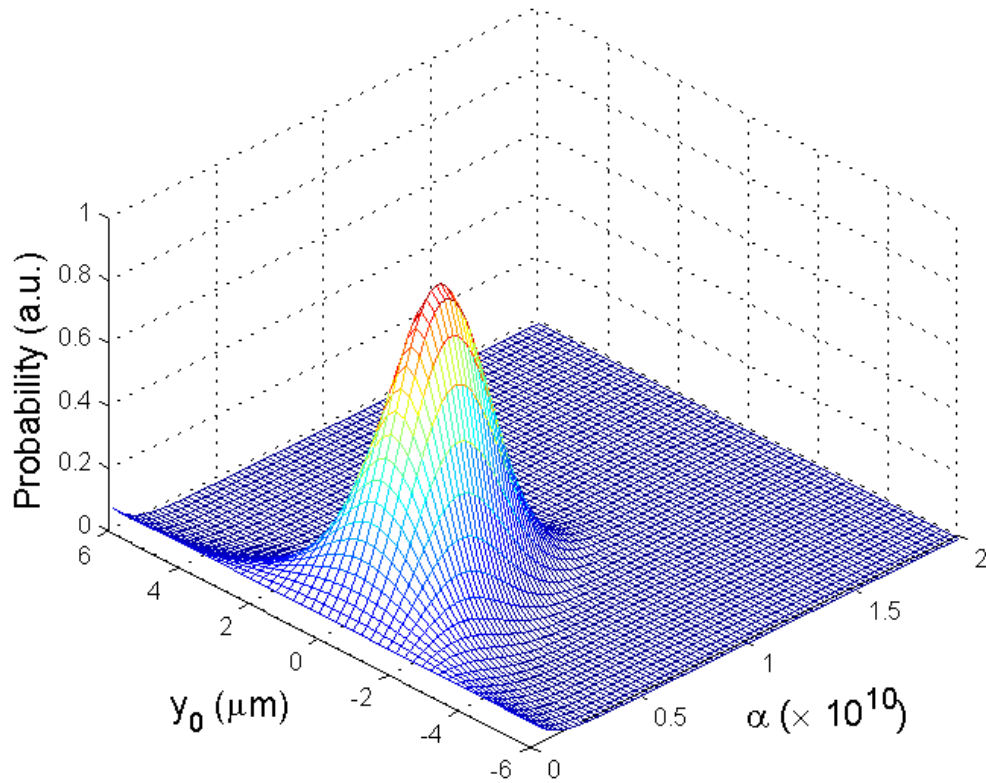
Conditional probability:
(for a fixed λ)

$$P(y_{00}, \alpha) = \frac{1}{A} \prod_{i,j} P_{i,j}(F_{i,j}^{\text{exp}} | y_{00}, \alpha)$$

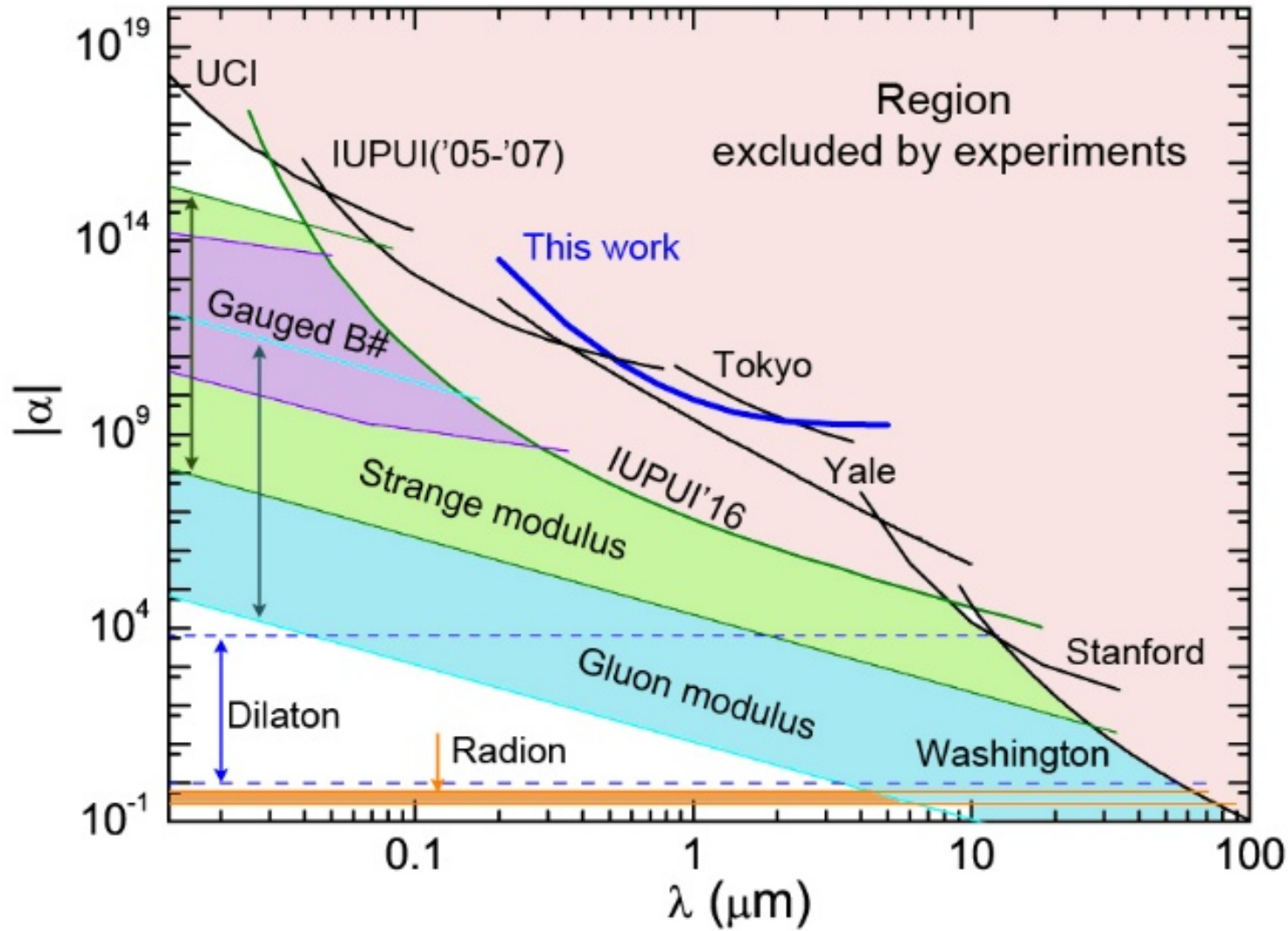
Maximum likelihood estimation



$$\lambda = 1 \mu\text{m}$$



Constraints on the Yukawa-type forces



Yale: derived from Casimir experiment

IUPUI'16: current strongest constraints

Jianbo Wang, Pengshun Luo et al., PRD 94, 122005 (2016)

- Experimental Search for Yukawa-type forces at the micrometer scale
- **Constraints on the spin-spin interactions at the nanometer scale**

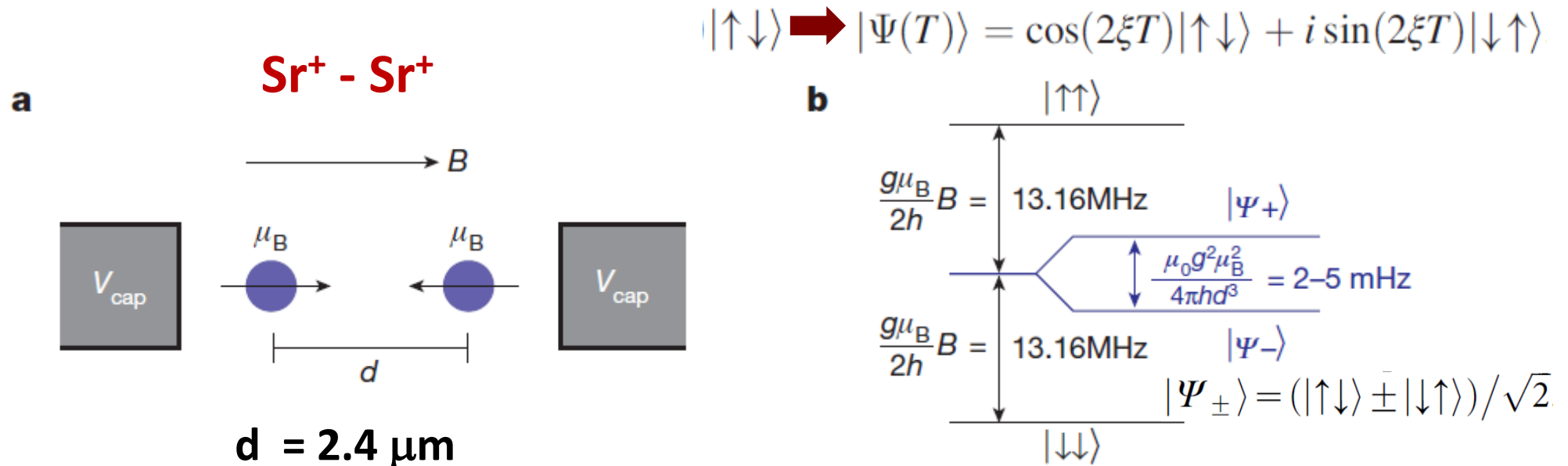
Constraints on Exotic Dipole-Dipole Couplings between Electrons at the Micrometer Scale

Shlomi Kotler,¹ Roei Ozeri,² and Derek F. Jackson Kimball³

¹National Institute of Standards and Technology, 325 Broadway Street, Boulder, Colorado 80305, USA

²Department of Physics of Complex Systems, Weizmann Institute of Science, P.O. Box 26, Rehovot 76100, Israel

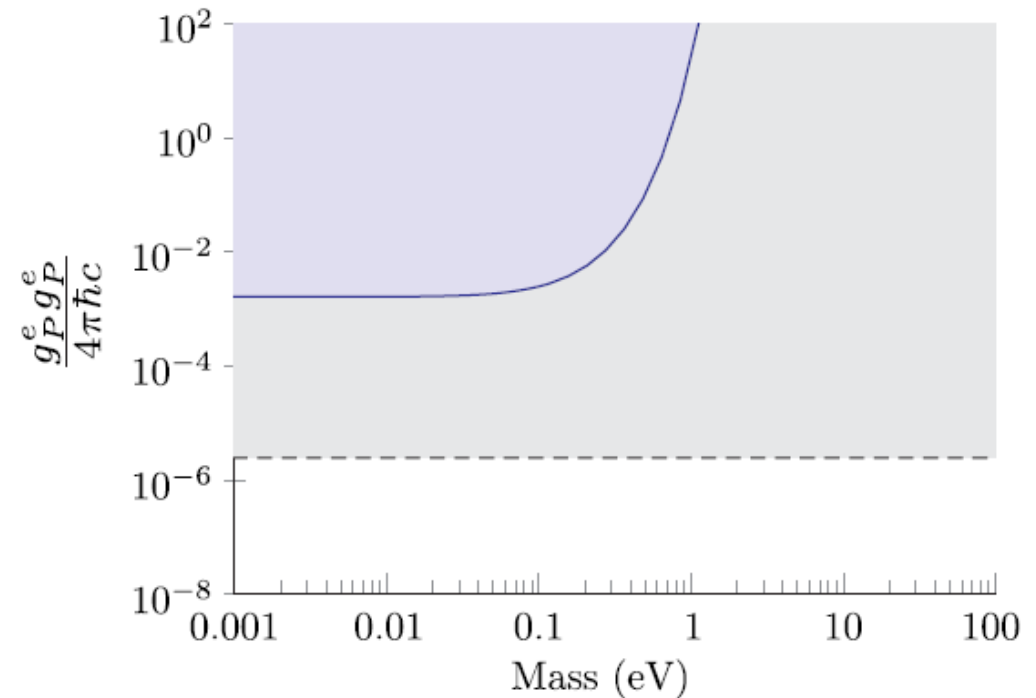
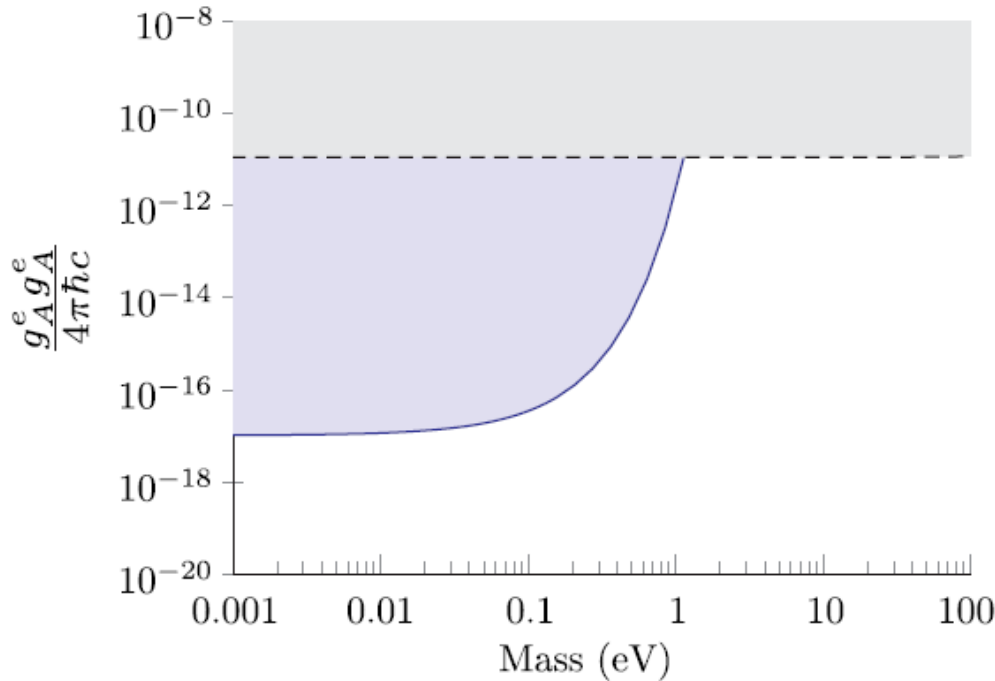
³Department of Physics, California State University, East Bay, Hayward, California 94542-3084, USA



Coupling strength: $\xi = 2\pi \times 1.020(95)_{\text{stat}} \text{ mHz}$

Constraints on hypothetical force: $\xi_h \leq 2\delta\xi$

Constraints on spin-spin interaction



Pseudovector coupling

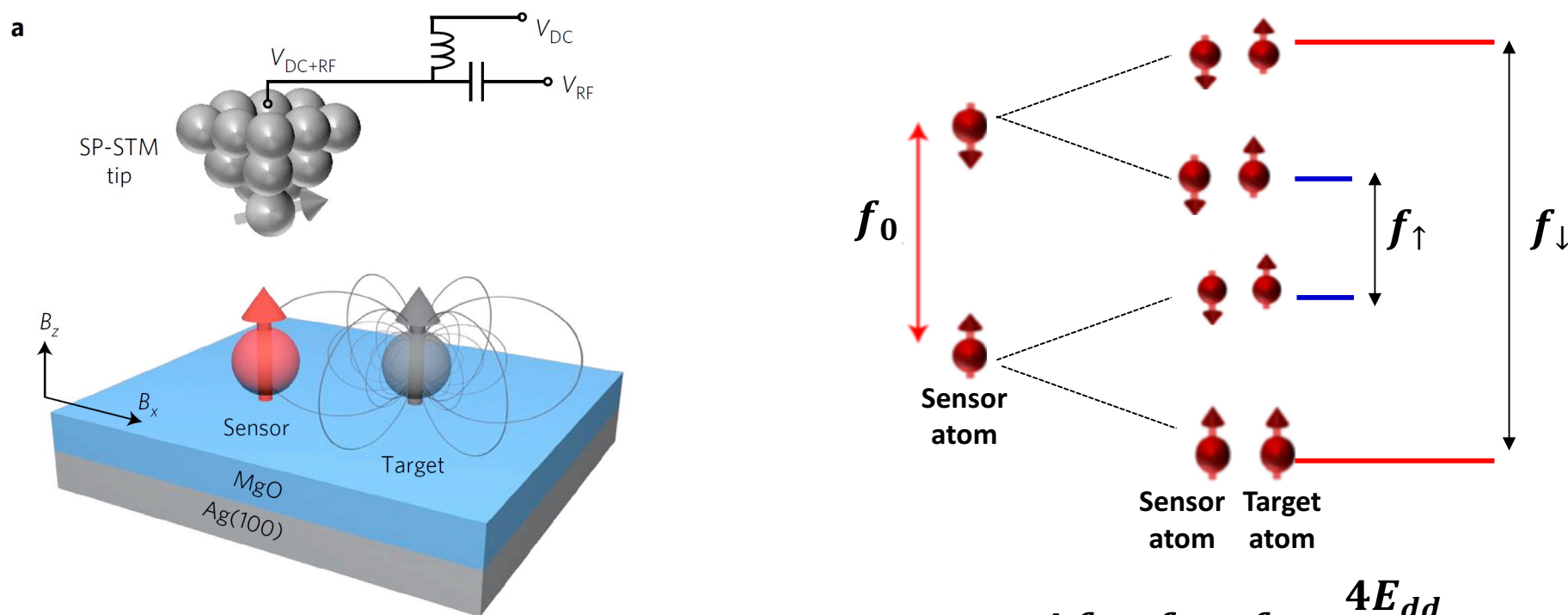
$$\mathcal{V}_A(r) = \frac{g_A^e g_A^e}{4\pi\hbar c} \frac{\hbar c}{r} \mathbf{S}_1 \cdot \mathbf{S}_2 e^{-r/\lambda}$$

Pseudoscalar coupling

$$\mathcal{V}_P(\mathbf{r}) = \frac{g_P^e g_P^e}{4\pi\hbar c} \frac{\hbar^3}{4m_e^2 c} \left[\mathbf{S}_1 \cdot \mathbf{S}_2 \left(\frac{1}{\lambda r^2} + \frac{1}{r^3} + \frac{4\pi}{3} \delta^3(r) \right) - (\mathbf{S}_1 \cdot \hat{\mathbf{r}})(\mathbf{S}_2 \cdot \hat{\mathbf{r}}) \left(\frac{1}{\lambda^2 r} + \frac{3}{\lambda r^2} + \frac{3}{r^3} \right) \right] e^{-r/\lambda},$$

Atomic-scale sensing of the magnetic dipolar field from single atoms

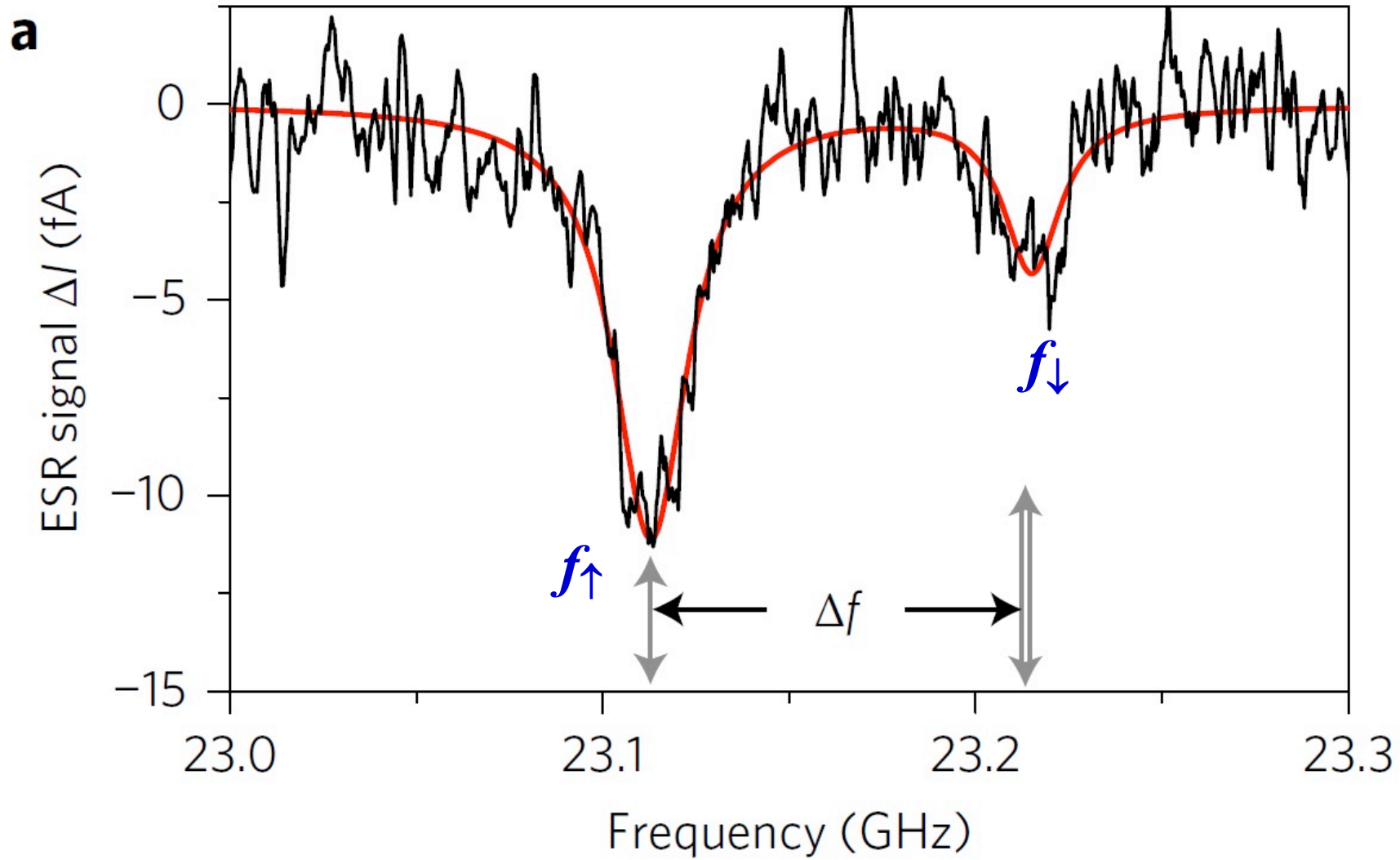
Taeyoung Choi^{1†}, William Paul¹, Steffen Rolf-Pissarczyk^{2,3}, Andrew J. Macdonald⁴,
Fabian D. Natterer^{1,5}, Kai Yang^{1,6}, Philip Willke^{1,7}, Christopher P. Lutz^{1*} and Andreas J. Heinrich^{8,9*}



$$\Delta f = f_{\downarrow} - f_{\uparrow} = \frac{4E_{dd}}{h}$$

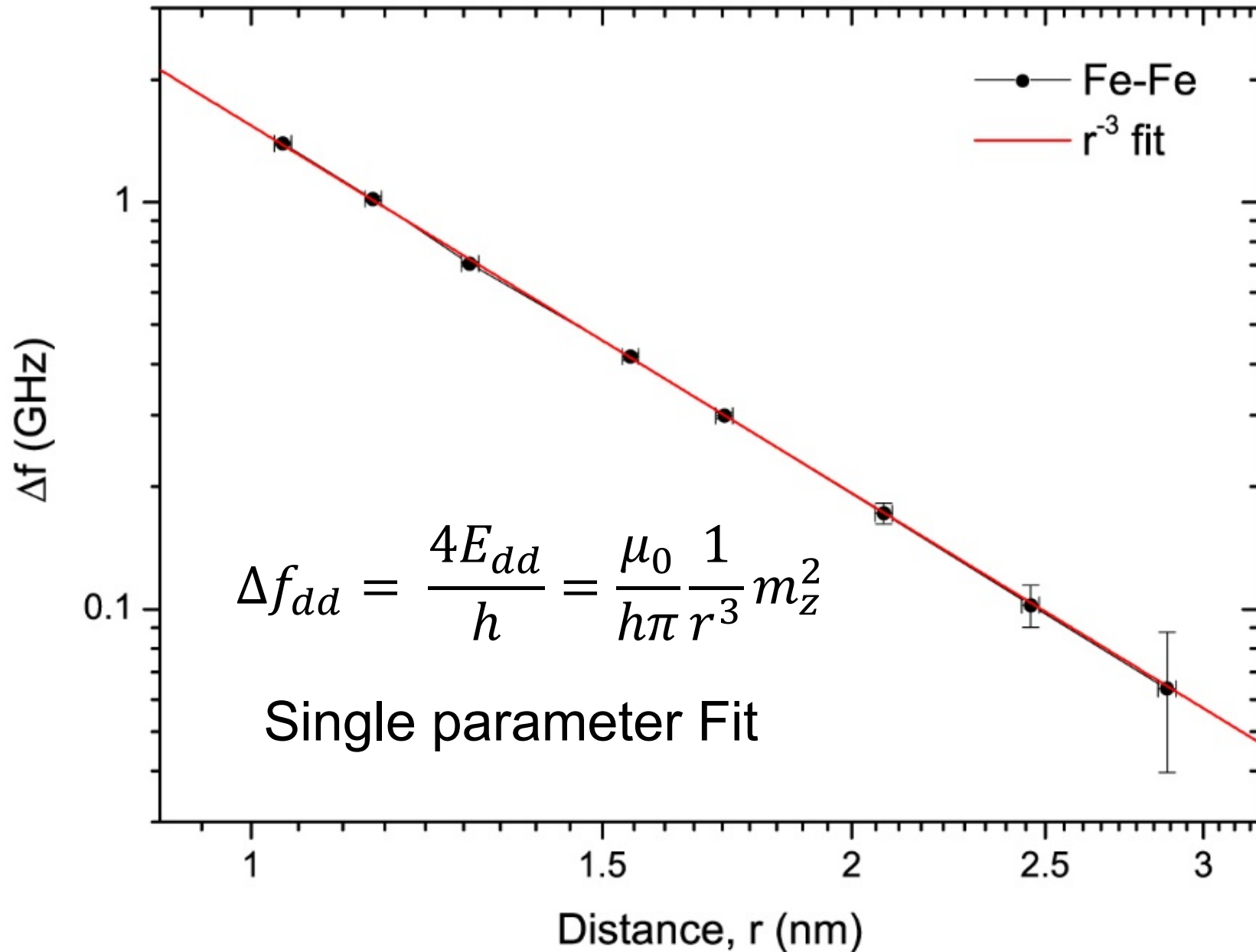
Dipole-dipole:
$$E_{dd} = \frac{\mu_0}{4\pi} \frac{1}{r^3} \left[(\vec{m}^{(1)} \cdot \vec{m}^{(2)}) - 3(\vec{m}^{(1)} \cdot \hat{r})(\vec{m}^{(2)} \cdot \hat{r}) \right] = \frac{\mu_0}{4\pi} \frac{1}{r^3} m_z^2$$

ESR Spectroscopy of Fe atom



$$\Delta f = 4 E_{dd}/h$$

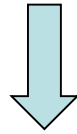
Magnetic dipole-dipole interaction



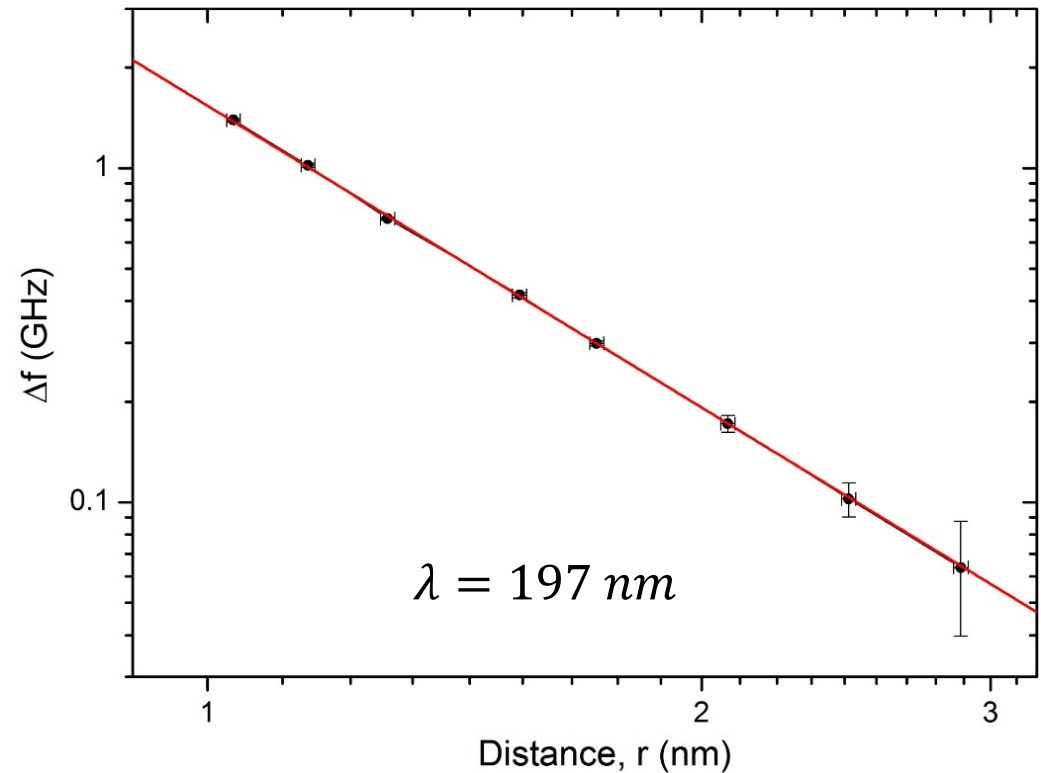
Constraints on pseudo-vector mediated force



$$V_A(r) = \frac{g_A^2}{4\pi\hbar c} \frac{\hbar c}{r} e^{-r/\lambda} \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2$$



$$\Delta f_A = \frac{g_A^2}{4\pi\hbar c} \frac{8c}{\pi r} S_Z^2 e^{-r/\lambda}$$



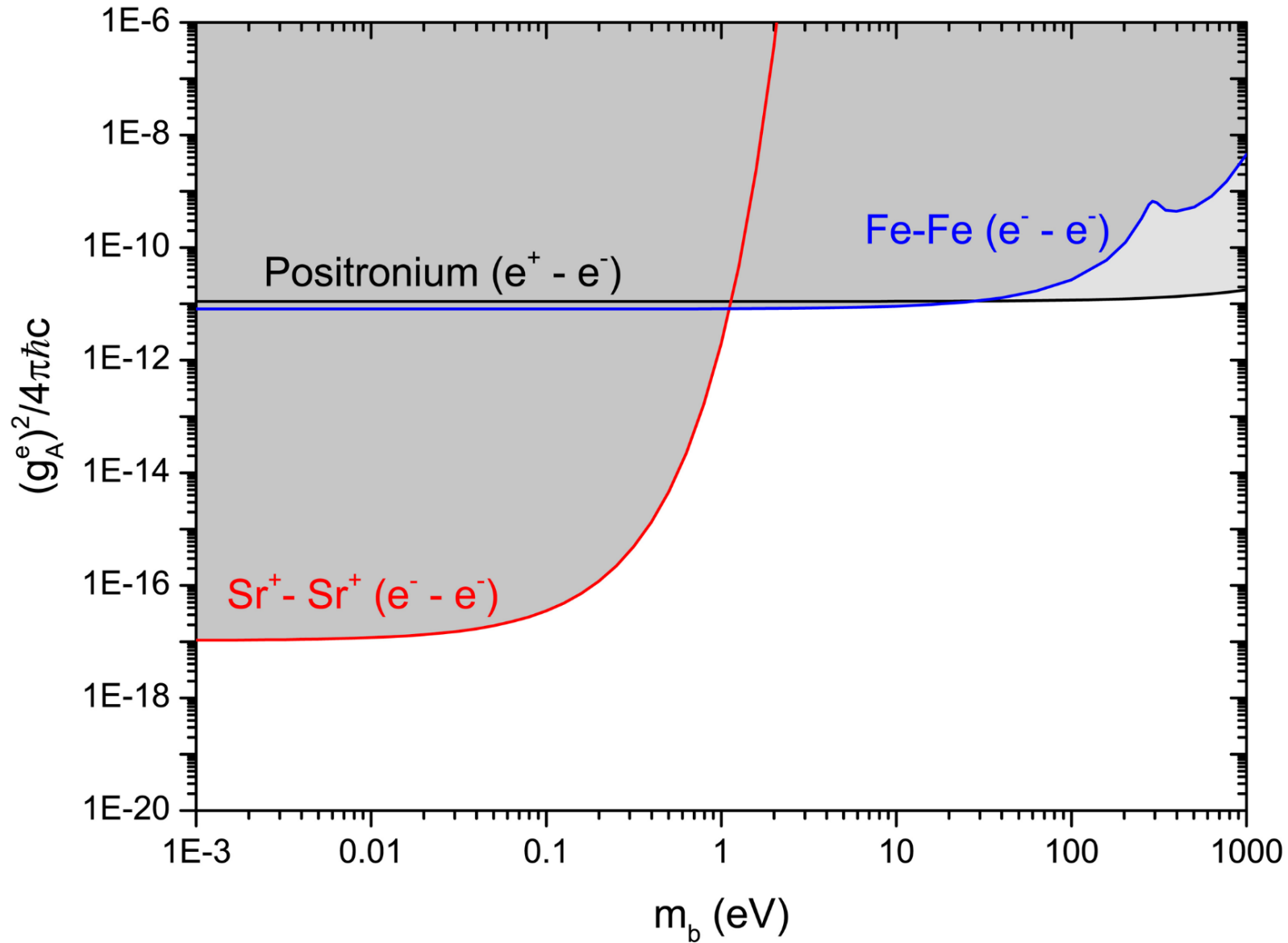
Assume

$$\Delta f_{exp} = \Delta f_{dd}(m_z) + \Delta f_{PP}(\lambda, g_p^2)$$

$$\frac{g_A^2}{4\pi\hbar c} = (0 \pm 4.1) \times 10^{-12}$$

$$\frac{g_A^2}{4\pi\hbar c} \leq 8.1 \times 10^{-12}$$

Constraints on pseudo-vector mediated force



$$m_b = \frac{\hbar}{\lambda c}$$

Constraints on pseudo-scalar mediated force



$$V_P(r) = -\frac{g_p^2}{4\pi\hbar c} \frac{\hbar^3}{4m_f^2 c} \left[\boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 \left(\frac{1}{\lambda r^2} + \frac{1}{r^3} \right) - (\boldsymbol{\sigma}_1 \cdot \hat{\mathbf{r}})(\boldsymbol{\sigma}_2 \cdot \hat{\mathbf{r}}) \left(\frac{1}{\lambda^2 r} + \frac{3}{\lambda r^2} + \frac{3}{r^3} \right) \right] e^{-r/\lambda}$$



$$V_P(r) = -\frac{g_p^2}{4\pi\hbar c} \frac{\hbar^3}{4m_f^2 c} \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 \left(\frac{1}{\lambda r^2} + \frac{1}{r^3} \right) e^{-r/\lambda}$$



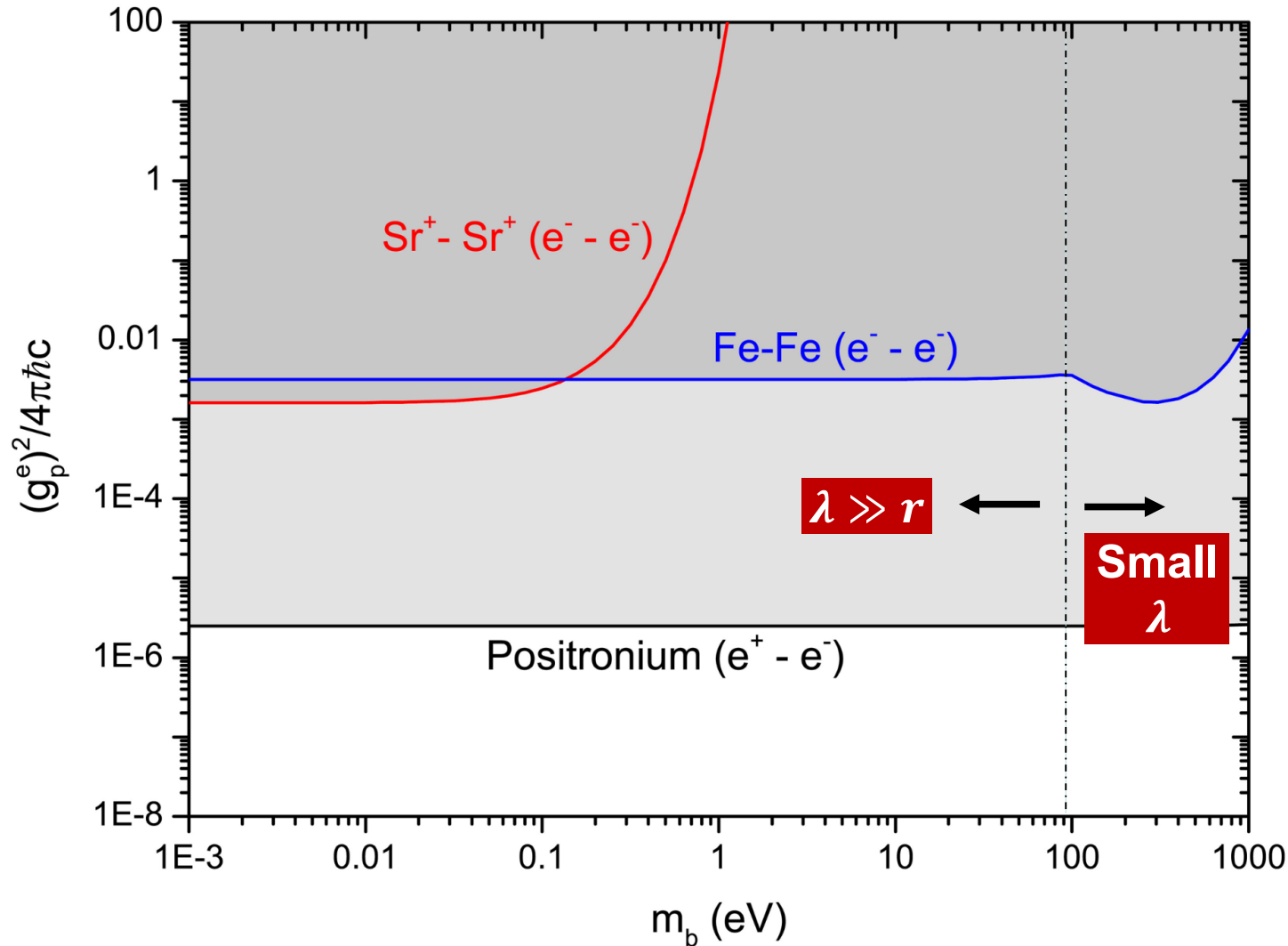
$$\Delta f_P = -\frac{g_p^2}{4\pi\hbar c} \frac{2\hbar^2}{\pi m_e^2 c} S_Z^2 \left(\frac{1}{\lambda r^2} + \frac{1}{r^3} \right) e^{-r/\lambda} \xrightarrow{\lambda \gg r} \propto \frac{1}{r^3}$$

Small λ : $\Delta f_{exp} = \Delta f_{dd}(m_Z) + \Delta f_A(\lambda, g_A^2)$

$\lambda \gg r$: $\Delta f_{exp} = \Delta f_{dd}(m_Z = 6\mu_B) + \Delta f_A(\lambda, g_A^2)$

Maximum DD contribution

Constraints on pseudo-scalar mediated force



$$m_b = \frac{\hbar}{\lambda c}$$

Stellar cooling rates imposed rather stronger constraints than laboratory experiments [G. Raffelt, Phys. Rev. D 86, 015001 (2012)].

- Performed an experimental search for the Yukawa-type forces at the micrometer range.
- Constraints were derived without the need to subtracting the Casimir and electrostatic force background.
- Derived the constraints on the pseudoscalar and pseudovector coupling between electrons by analyzing the ESR-STM data.
- The constraints on the pseudovector coupling are the strongest for bosons with mass range from 1 eV to 20 eV.

Acknowledgments



East Lake, Wuhan, 9/2017



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Dr. Shengguo Guan

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Dr. Wenjie Wu

Jihua Ding

Huixing Fu

Xiaofang Ren

Zhaoyang Tian

.....

Institute of Physics, CAS:

Dr. Aizi Jin

SPBSTU, Saint Petersburg:

Prof. G. Klimchitskaya

Prof. V. Mostepaneko



Micrometer range experiment



TABLE II. Table of the mean values and uncertainties of the main experimental parameters.

Parameter	Value	Error	Units
Parameters in force measurement			
Effective spring constant (k)	1.3	0.2	mN/m
Interferometer sensitivity (S_{int})	12.0	0.9	nm/V
Other parameters			
Separation (d)	905	54	nm
Test mass radius (R)	13.7	0.1	μm
Silicon mass width (W_{Si})	5.9	0.2	μm
Gold mass width (W_{Au})	6.3	0.2	μm
Electroplated gold density (ρ_{Au})	19.1	0.9	g/cm^3
Source mass depth (t)	3.3	0.1	μm
Drive amplitude (A_d)	18.4	0.1	μm
Tilt about the y -axis (θ_y)	0.0	0.7	mrad