Towards the effective action of Non-perturbative Gauge-Higgs Unification

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Workshop on the Standard Model and Beyond, Corfu, 9 Sept. 2017

Based on

- **N.I. and F. Knechtli (NP B719, 121, 2005), F. Knechtli, B. Bunk and N.I. (LAT2005), N.I. and F. Knechtli (hep-lat/0604006), N.I. and F. Knechtli (NP B775, 283, 2007), N.I., F. Knechtli and M. Luz (JHEP 0708, 028), N.I., F. Knechtli and K. Yoneyama (NP B865, 541, 2012), N.I., F. Knechtli and K. Yoneyama (PL B722, 378, 2013)**
- **N. I. and F. Knechtli, JHEP 1406 (2014) 070**
- **M. Alberti, N.I., F. Knechtli and G. Moir, JHEP 1509 (2015) 159 and work in progress**
- **N.I. and F. Koutroulis, arXiv:1703.10369 [hep-ph] and work in progress**
- **Work in progress with A. Chatziagapiou**
- **N.I., arXiv:1611.00157 [hep-th]**

- The quantum Higgs mechanism in 4d
- Putting things together: NPGHU
- Towards an effective action

The Standard Model

$SU(3) \times SU(2) \times U(1)$
Quantum gauge fields coupled to fermionic matter and Higgs field(s) in a spontaneously broken EW symmetry phase in 4 space-time dimensions.

The Higgs sector has a naturalness issue that can be resolved by extra symmetry (susy, compositeness, 5d gauge symmetry, etc) or dynamically (e.g. simply by a low cut-off and/or by weird cancellations) or by a combination-correlation of both.
Behind its innocent perturbative nature, subtle non-perturbative effects may be hiding in the details (such as the origin of the relative sign in the Higgs potential):

$$V = -m_0^2 H^2 + \frac{\lambda_0}{6} H^4$$

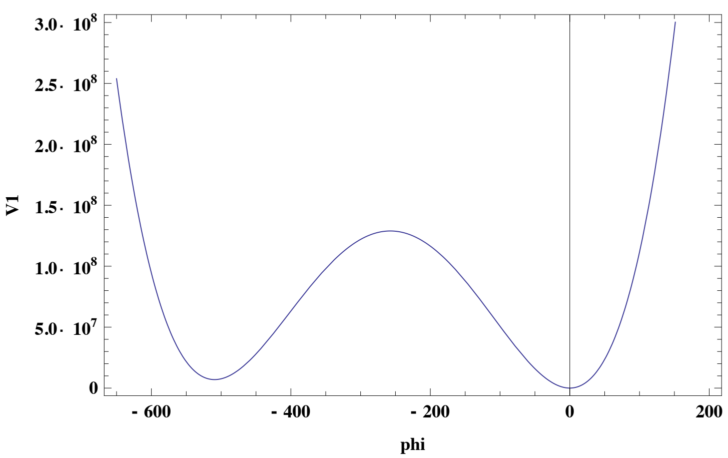
Let us look a bit closer at the Higgs mechanism in the simplest possible 4d context…

A toy model for the EW sector: the Abelian-Higgs model in 4d

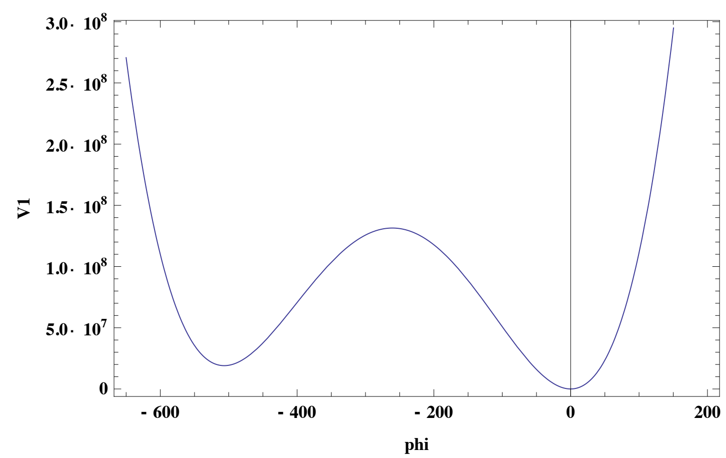
$$\mathcal{L}_{\rm AH} = -\frac{1}{4}F_{\mu\nu}^2 - \frac{1}{2\xi}\left(\partial_\mu A^\mu\right)^2 + |D_\mu H|^2 + m_0^2|H|^2 - \frac{\lambda_0}{6}|H|^4 + \text{const.}$$

Gauge invariant 1-loop AHiggs potential

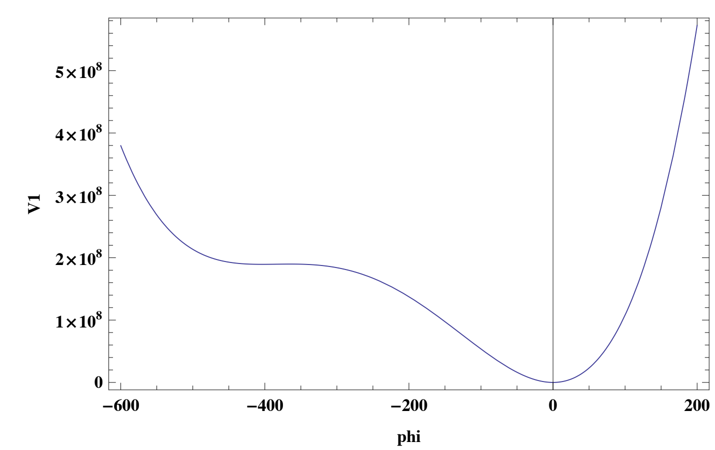
N.I. and F. Koutroulis, arXiv:1703.10369



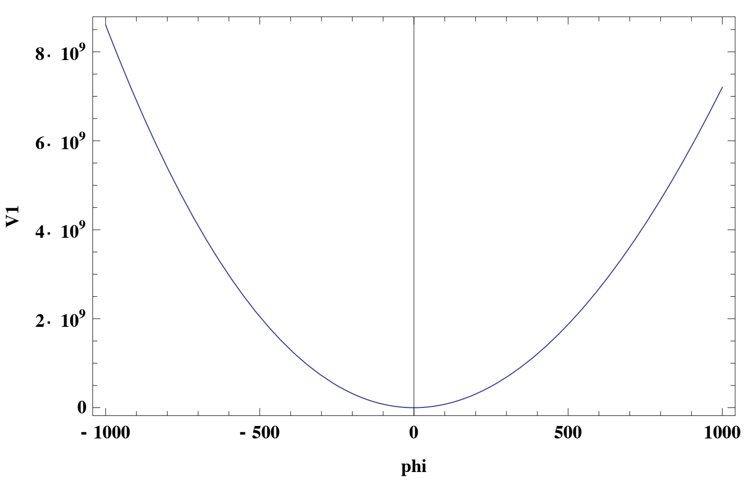
$125\ GeV$



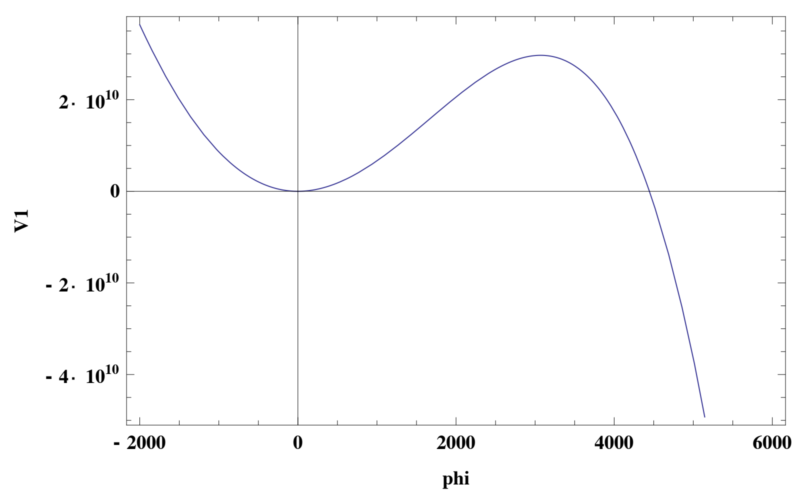
$10^{19}\ GeV$



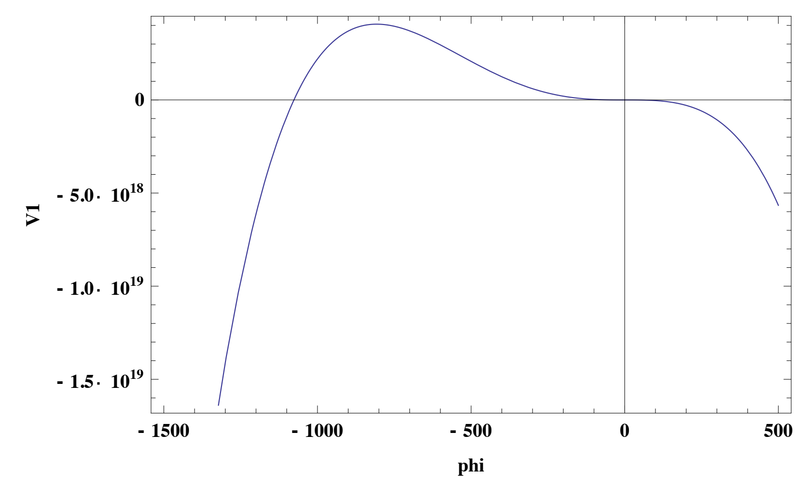
$10^{40}\ GeV$



$3 \cdot 10^{46}\ GeV$



$3.1 \cdot 10^{46}\ GeV$



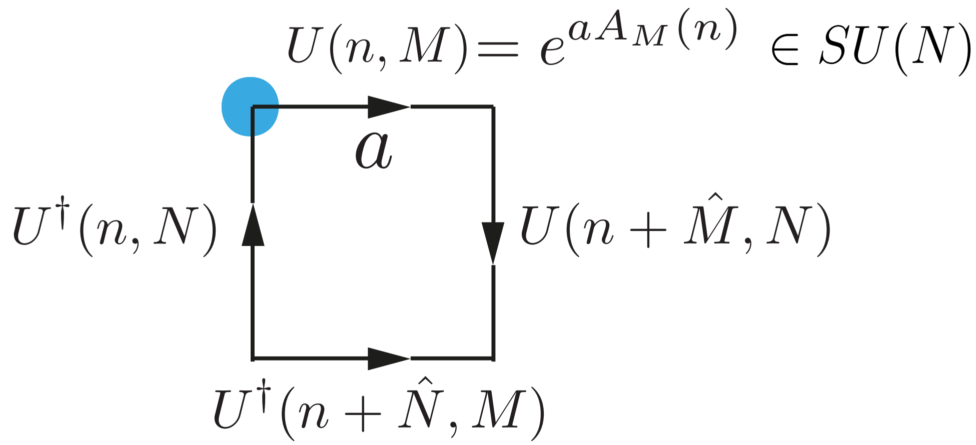
$4.3 \cdot 10^{49}\ GeV$

Instability scale Non-perturbative domain Landau Pole Phase transition?

The lattice regularization

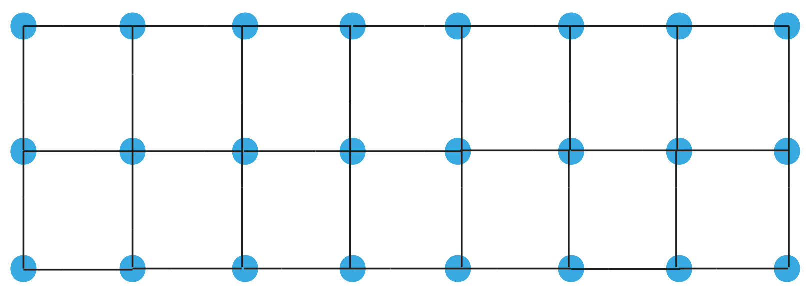
$x \to n \to$ ●

plaquette $U_{\mu\nu}(n)$:

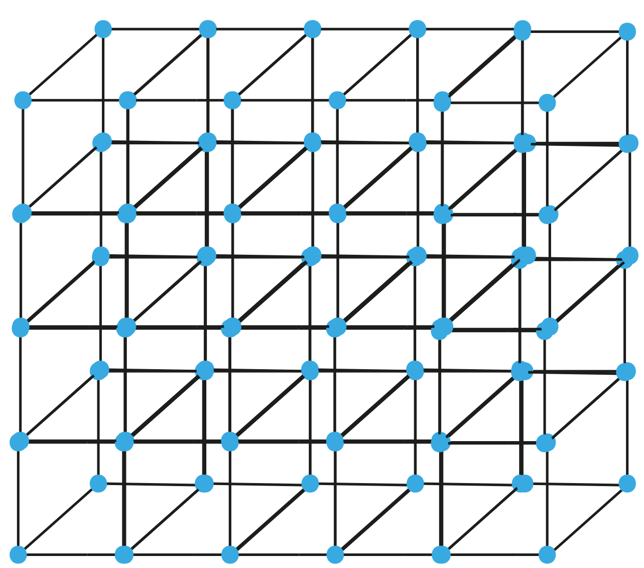


$\to -\frac{1}{4}a^2 F_{MN}^2 + O(a^4)$

$2d$



$3d$



$\cdots 4d, 5d, \cdots$

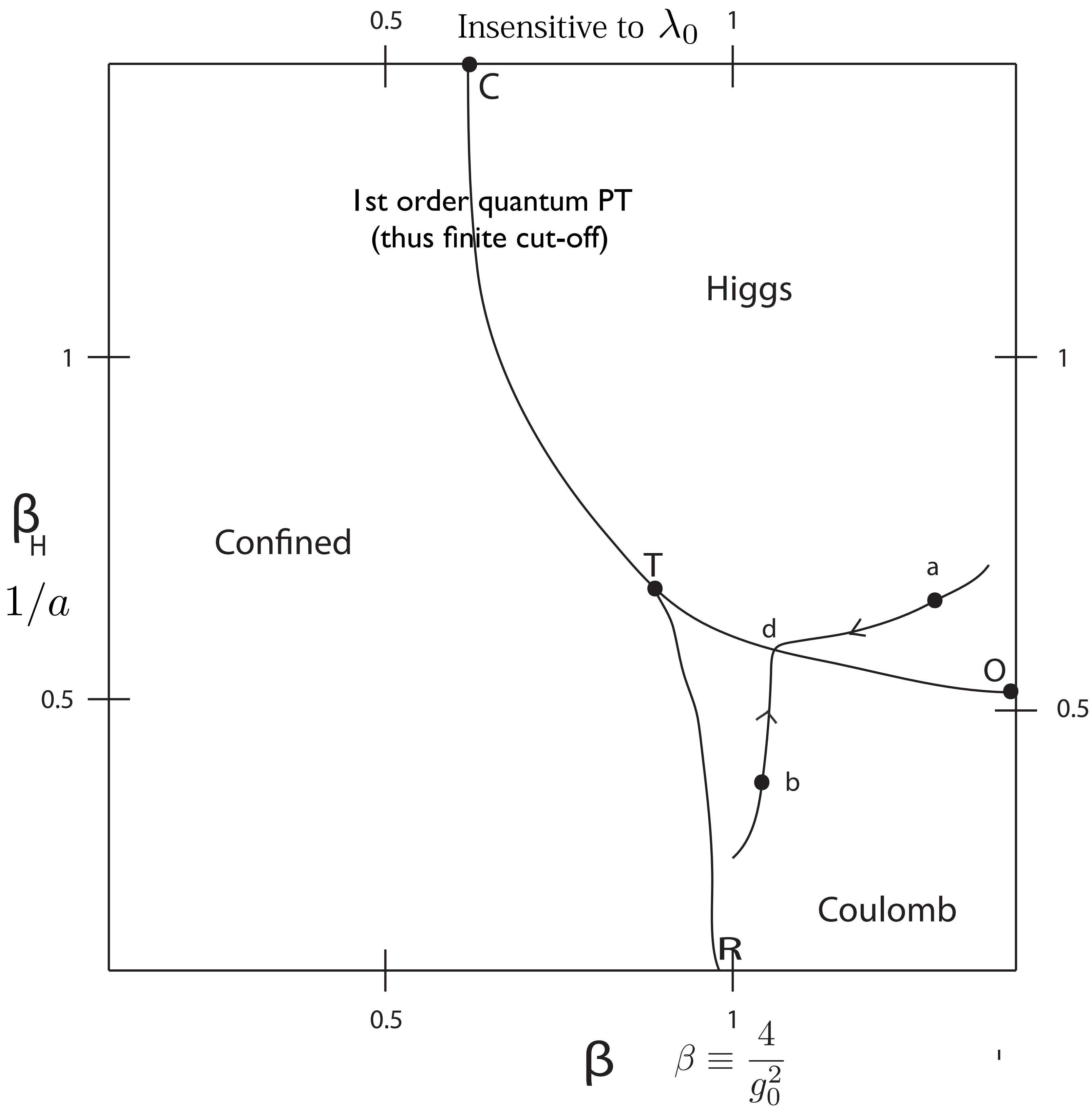
Now we can approach safely the phase transition

Phase diagram of the Abelian-Higgs model in 4d

Fradkin & Shenker (1979), Callaway & Carson (1982),
Evertz et al (1987), Khodayari (2016)

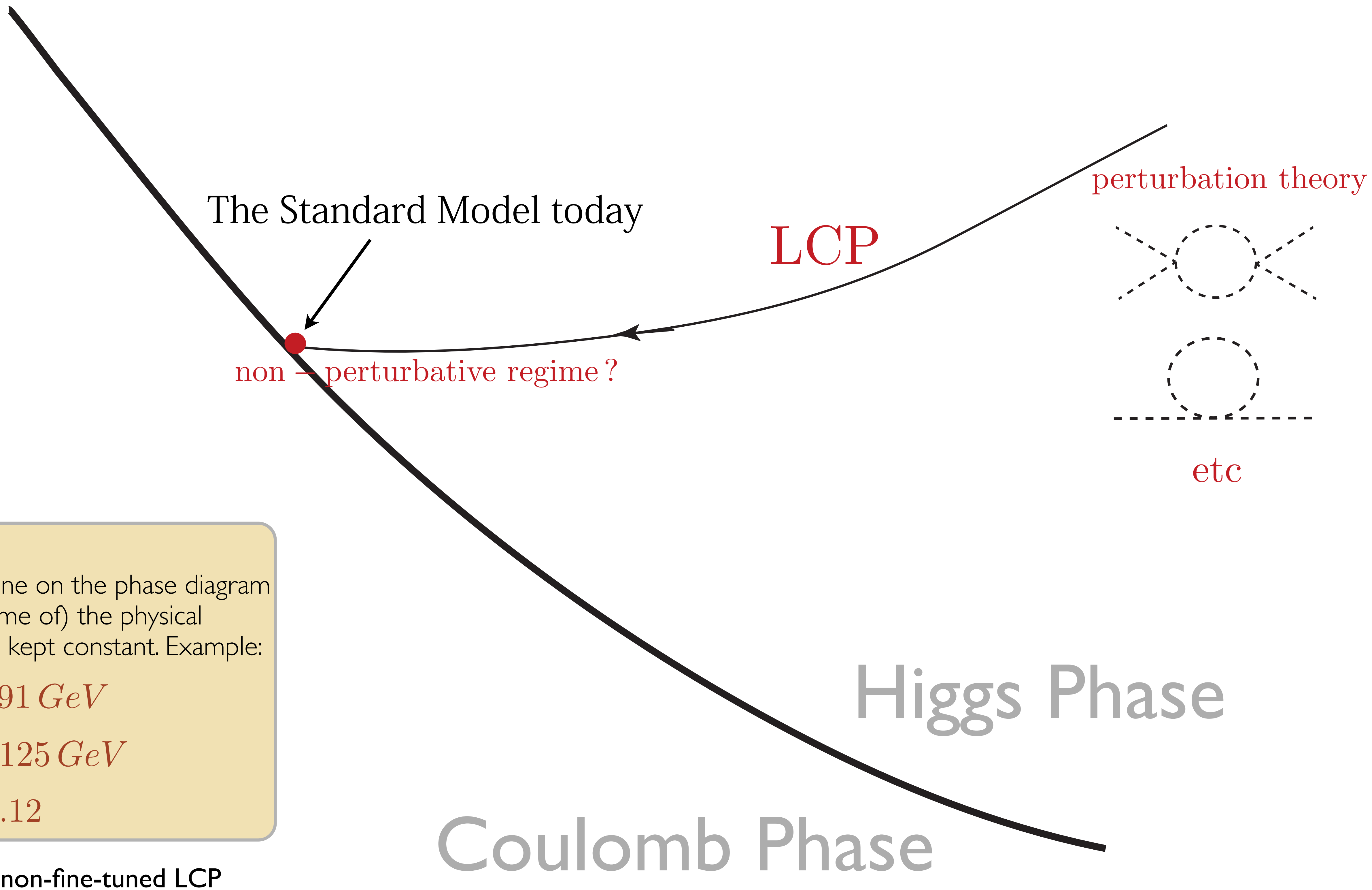
$\beta_H \equiv \frac{v_0^2}{\Lambda^2}$

$\Lambda = \text{cutoff} \sim 1/a$



$\beta \equiv \frac{4}{g_0^2}$

Let us **assume** that the AH model describes the observed Higgs mechanism and that we are sitting near a 1st order quantum phase transition.
Along the LCP the cut-off increases as the phase transition is approached and the LCP terminates on the phase transition at a value of the cut-off that may be lower than its maximal allowed value by perturbation theory (N.I. and F. Koutroulis, arXiv:1703.10369). It is like trying to launch a rocket from inside a room.



Definition:
An LCP is a line on the phase diagram on which (some of) the physical quantities are kept constant. Example:

- $m_Z = 91\, GeV$
- $m_H = 125\, GeV$
- $\lambda_R = 0.12$

Existence of non-fine-tuned LCP equivalent to stabilising the Higgs

Tentative lesson from 4d:
If you want to generate a SM-like Higgs potential without putting it by hand, hope for a solution to the naturalness problem with the SM sitting on the brink of a "bulk" or "quantum" phase transition then find some UV completion without elementary scalars that possesses such phase transition and it has a (dimensionally reduced) Higgs phase where the hierarchy is somehow protected.
Here we have in mind a framework where the mechanism is purely bosonic, that is, not of the susy or technicolor type.

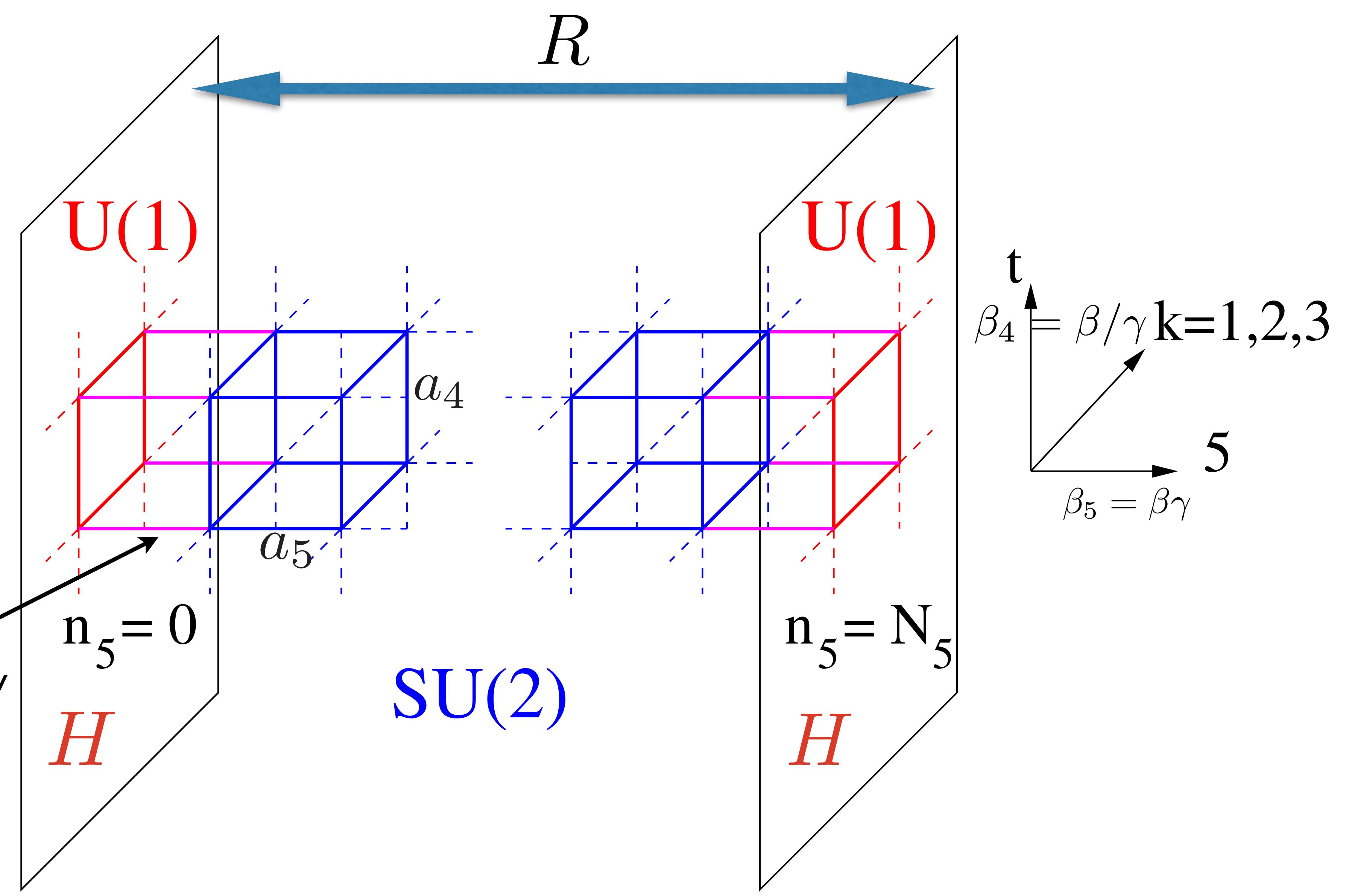
Higher than 4d gauge theories with appropriate boundary conditions turn out to have such properties.

Now let us put everything together

The model

Let us consider now an anisotropic SU(2) ‘lattice orbifold’. On the boundaries we have the spectrum of a 4d (Abelian-Higgs) model U(1) + H + excited states. Local and global symmetries are just ‘right’ so that all phases can be described in a gauge invariant way. We call this new version of GHU, “Non-Perturbative Gauge-Higgs Unification”, or NPGHU.

N. I., F. Knechtli (2005, 2007, 2014)



The Higgs mechanism is ensured by the breaking of a global “stick” symmetry, acting on these “hybrid” links.

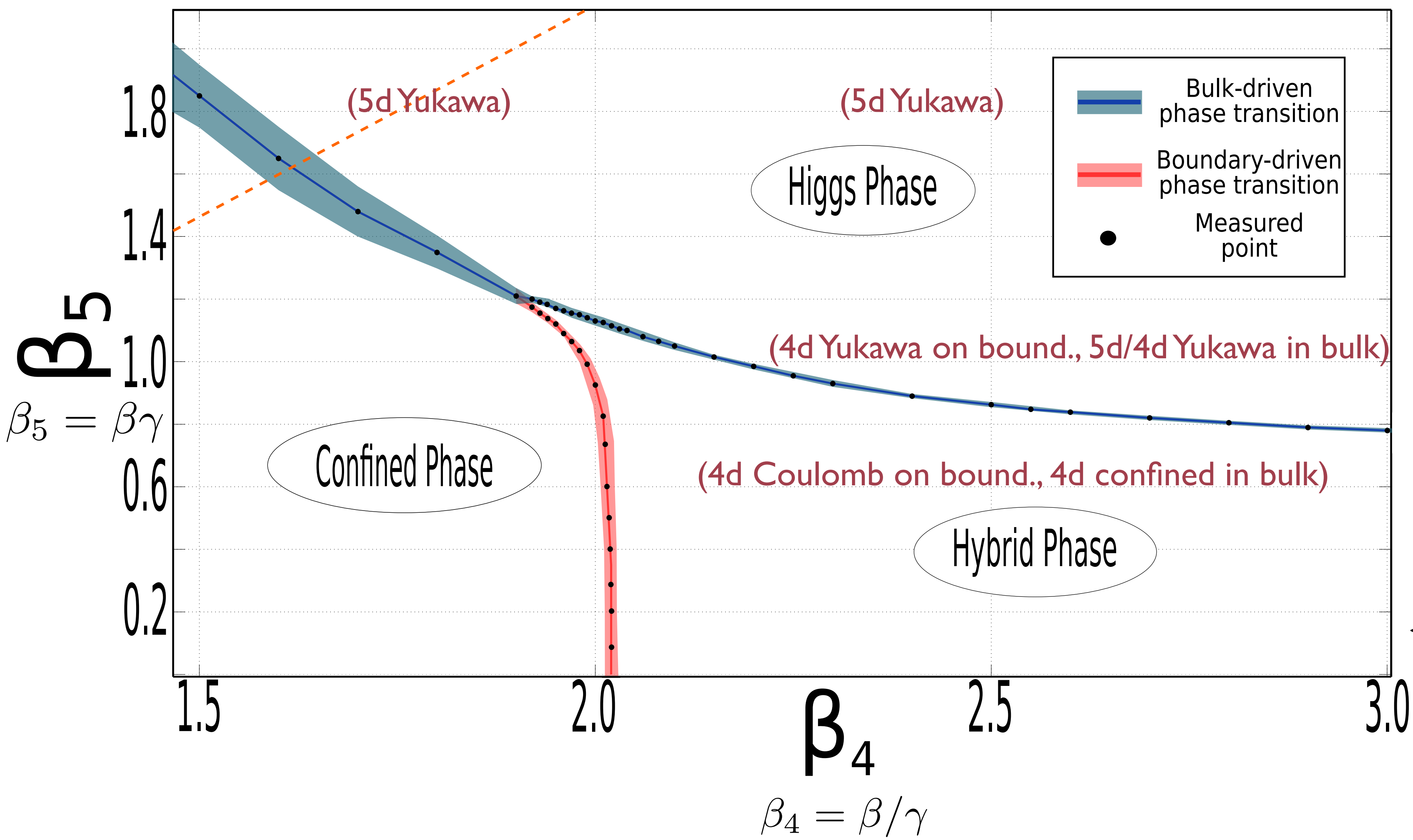
dimension-ful parameters: a_4, a_5, R, g_5

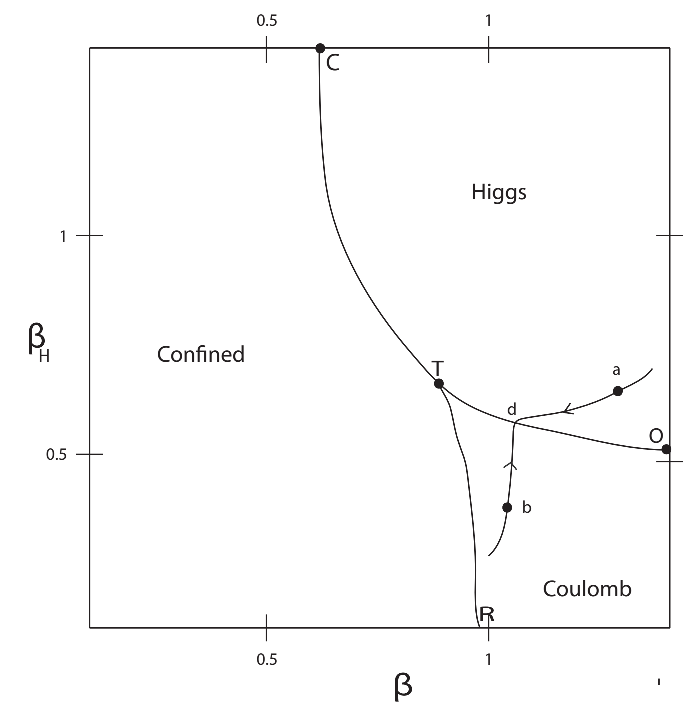
dimensionless parameters: $\beta = 4a_4^2/g_5^2$, $\gamma = a_4/a_5$, $N_5 = \pi R/a_5$

The phase diagram

G. Moir, M. Alberti, N. I., F. Knechtli (2015)

dynamics: phases + dimensional reduction (N5 dependence is weak)



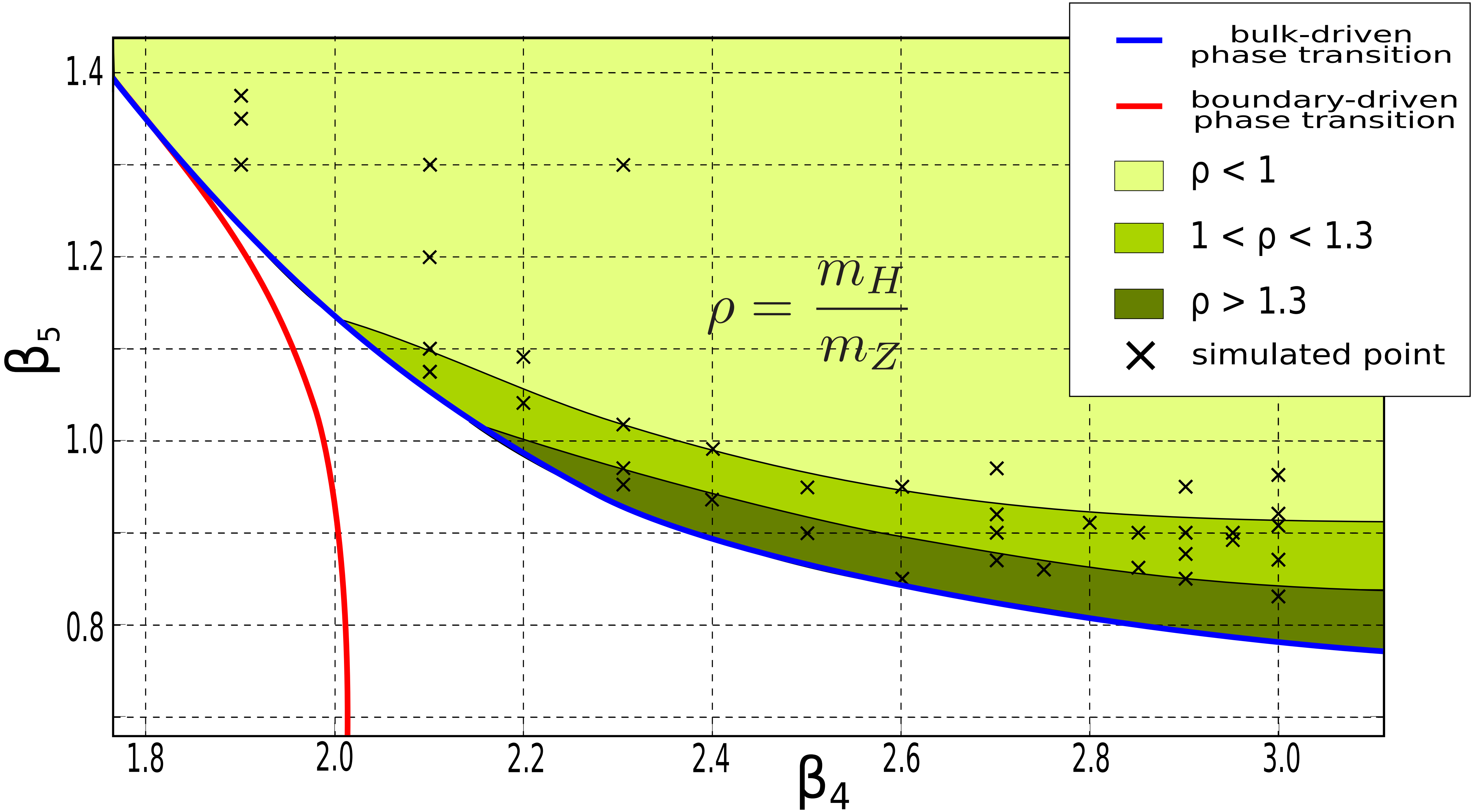


Note: this part of the phase diagram is reminiscent of the phase diagram of the (q=2) 4d Abelian-Higgs model, which is not unexpected since the two models have identical low lying spectra.

All phase transitions 1st order, effective theories must have a finite cut-off.

More dynamics:
Standard Model-like spectrum near the phase transition,
precisely in the 4d Yukawa regime, where the 5d space breaks into an array
of weakly interacting 4d planes. The lattice spacing decreases as the PT is approached from either sides.

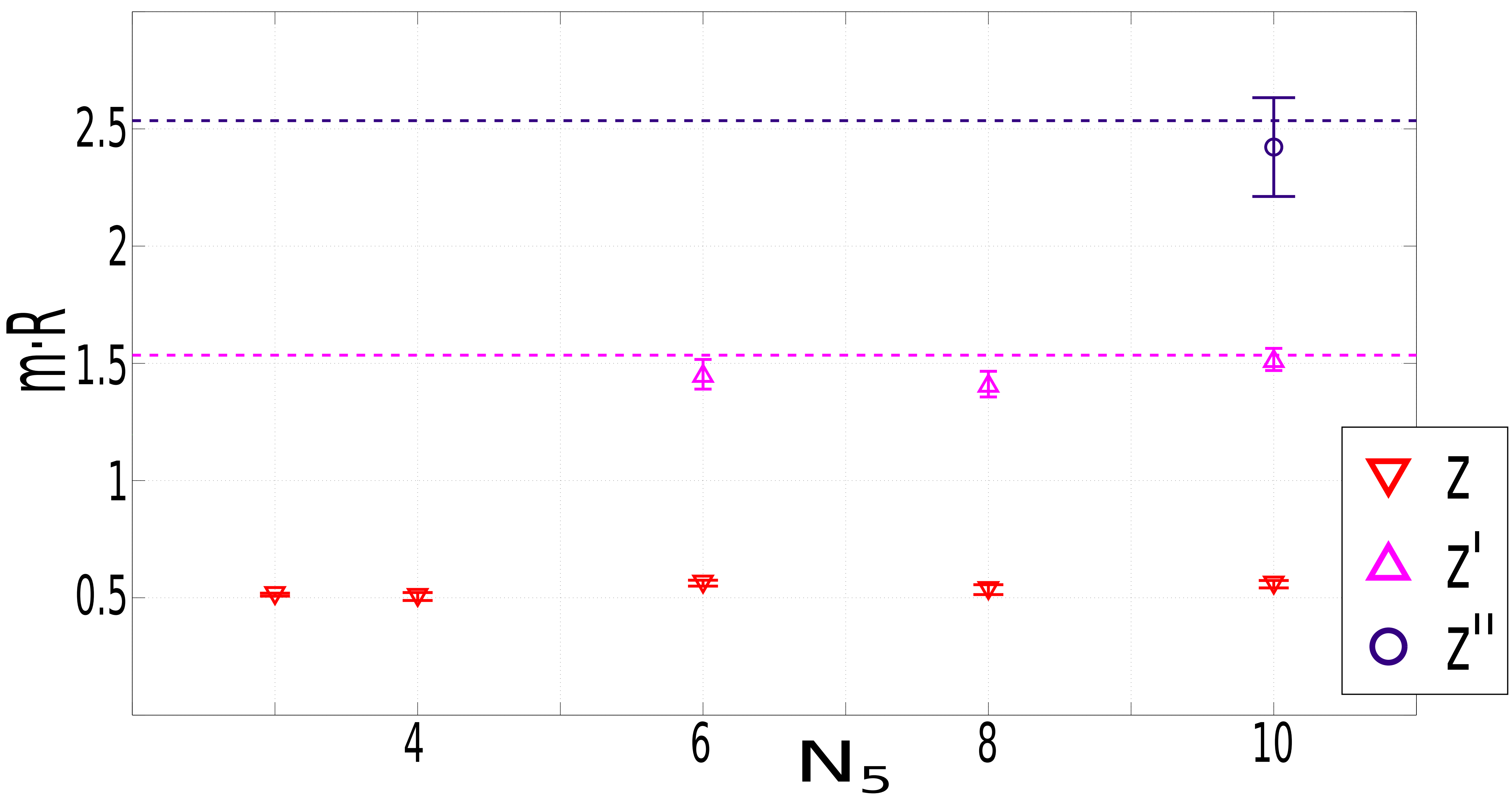
G. Moir, M. Alberti, N. I., F. Knechtli (2015)



quantum + bosonic Higgs mechanism…no other such mechanism in 4 (or higher) dimensions to our knowledge…

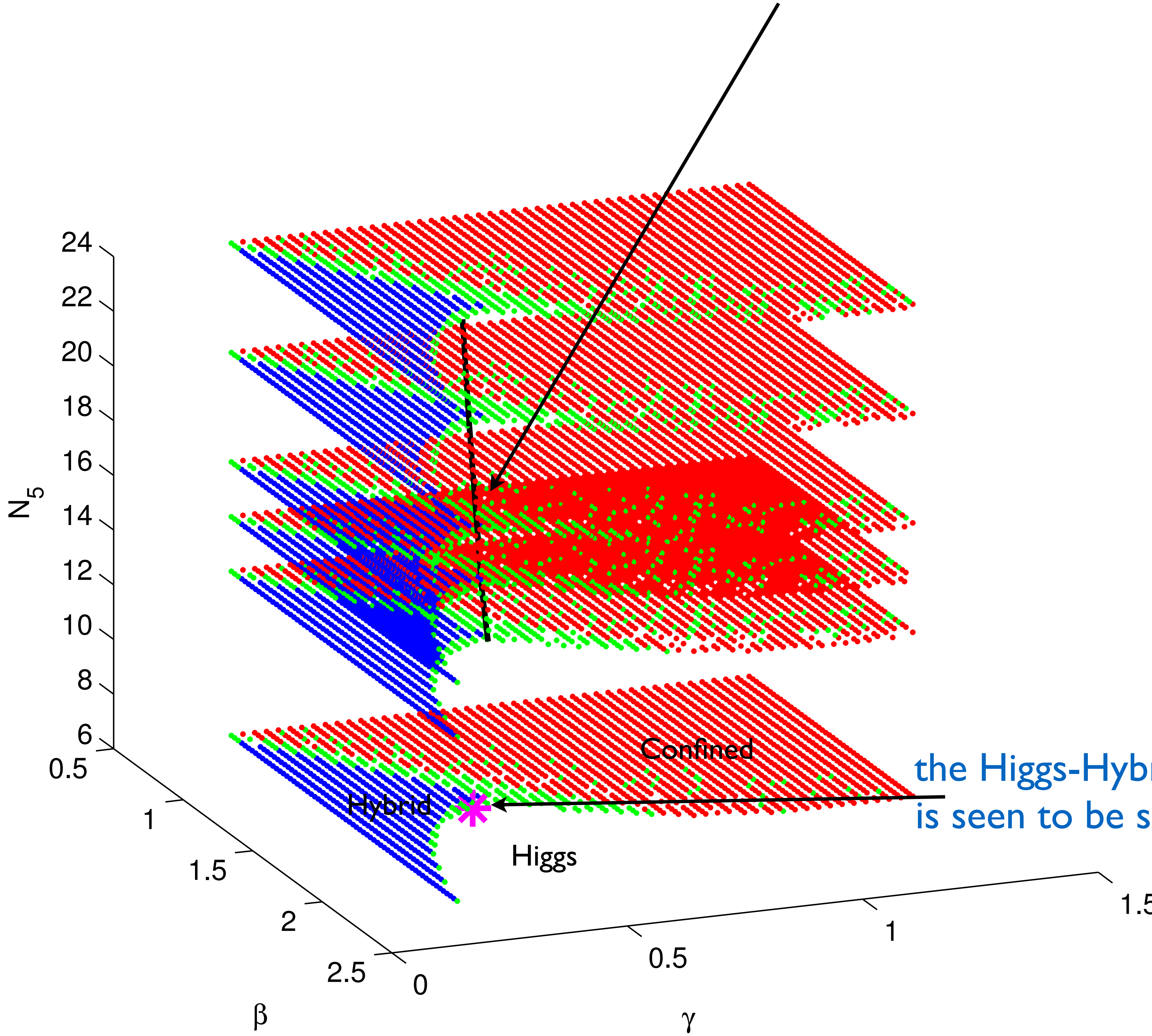
The spectrum in the gauge sector

G. Moir, M. Alberti, N. I., F. Knechtli (2015)



There is a vacuum shift of 1/2 wrt (1-loop) perturbation theory
to explain here…

A semi-analytical approach: The Mean-Field LCP (3d view)

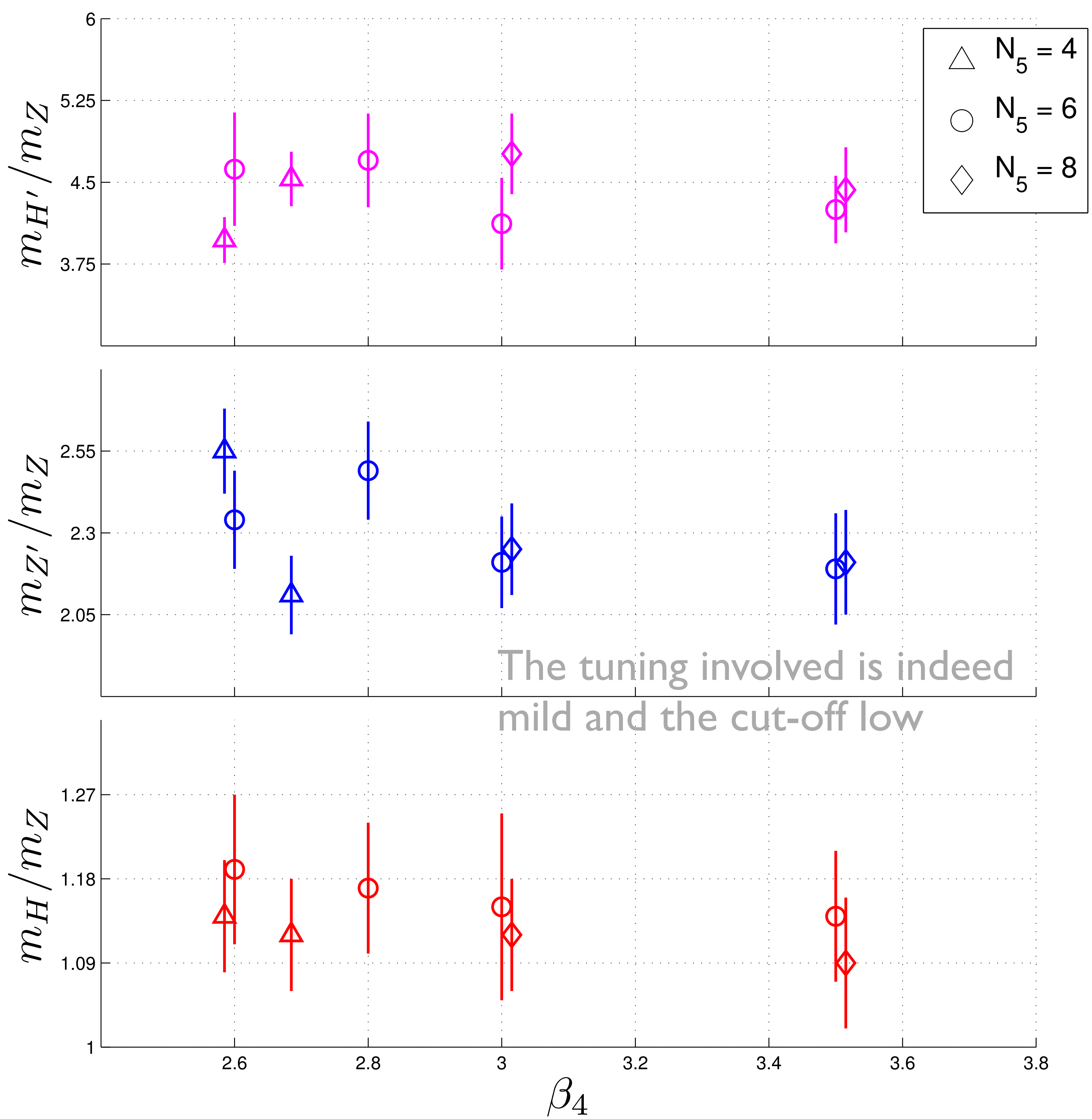


the Higgs-Hybrid phase transition is seen to be second order by MF!

N. I., F. Knechtli and K. Yoneyama (PL B722, 378, 2013)

A Monte Carlo LCP

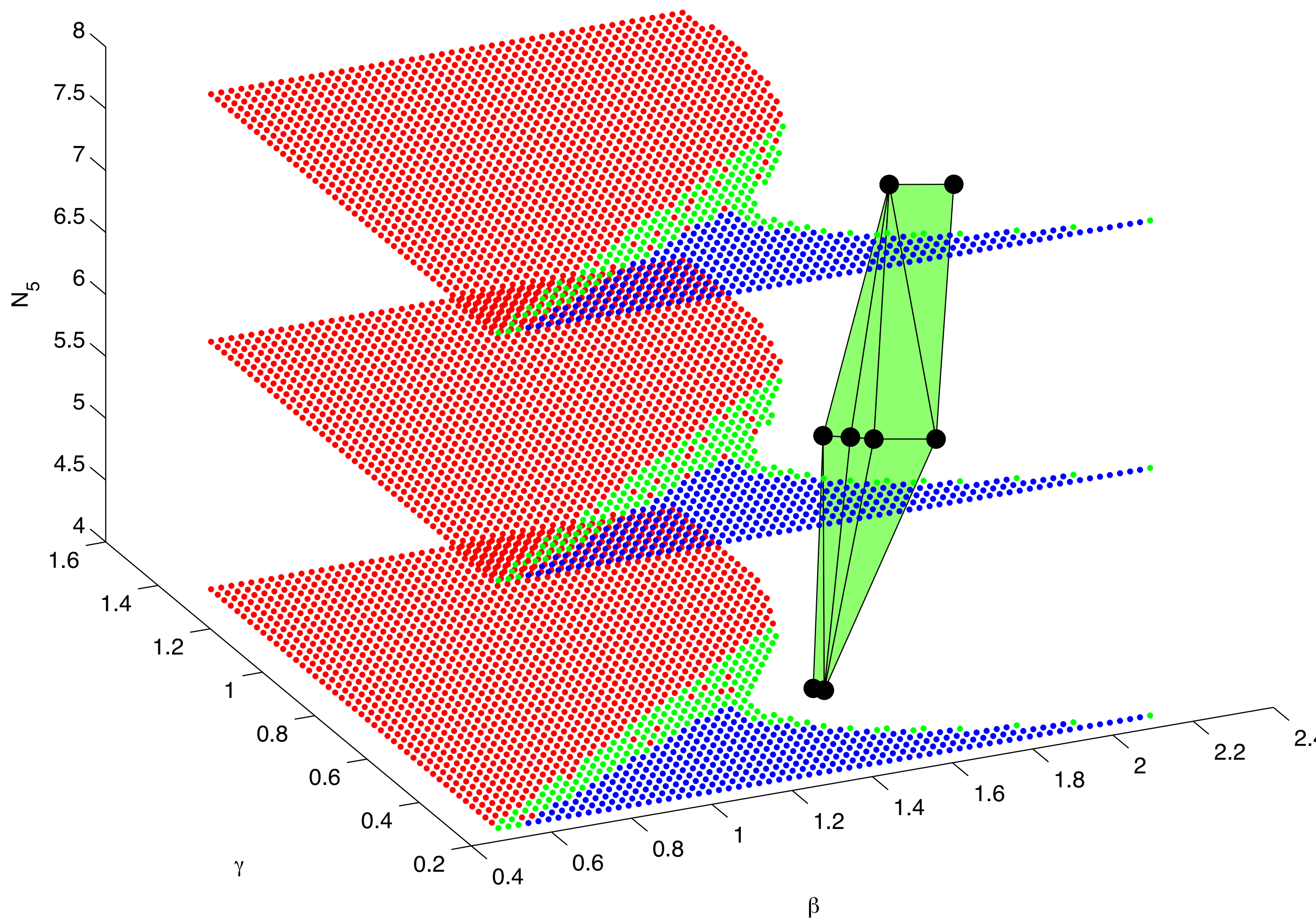
from M. Alberti's talk at the Lattice 2016 conference



The Monte Carlo LCP (3d view)

courtesy of M. Alberti

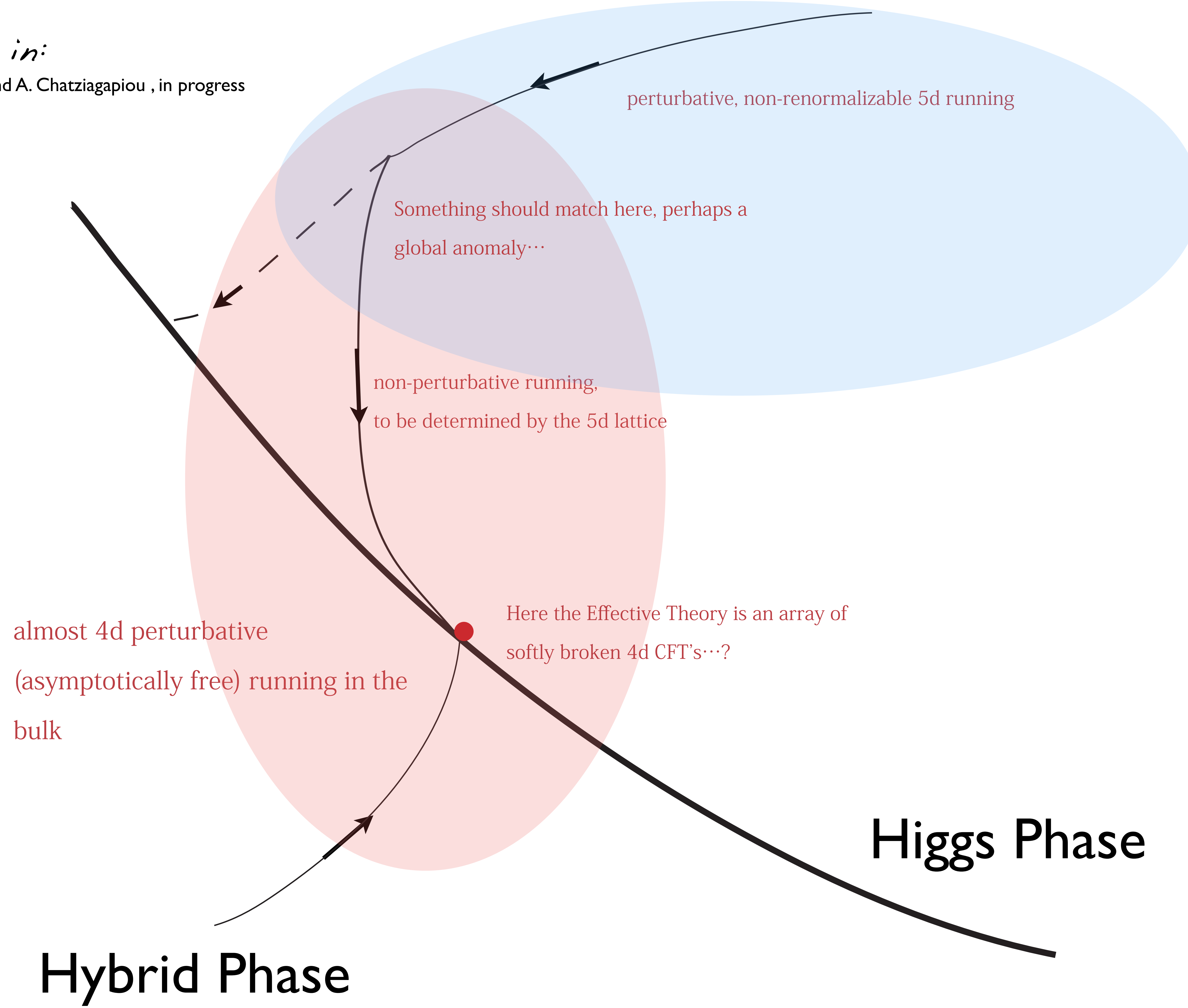
$$m_H/m_Z \simeq 1.15,\ m_{Z'}/m_Z \simeq 2.20$$



Towards an effective action

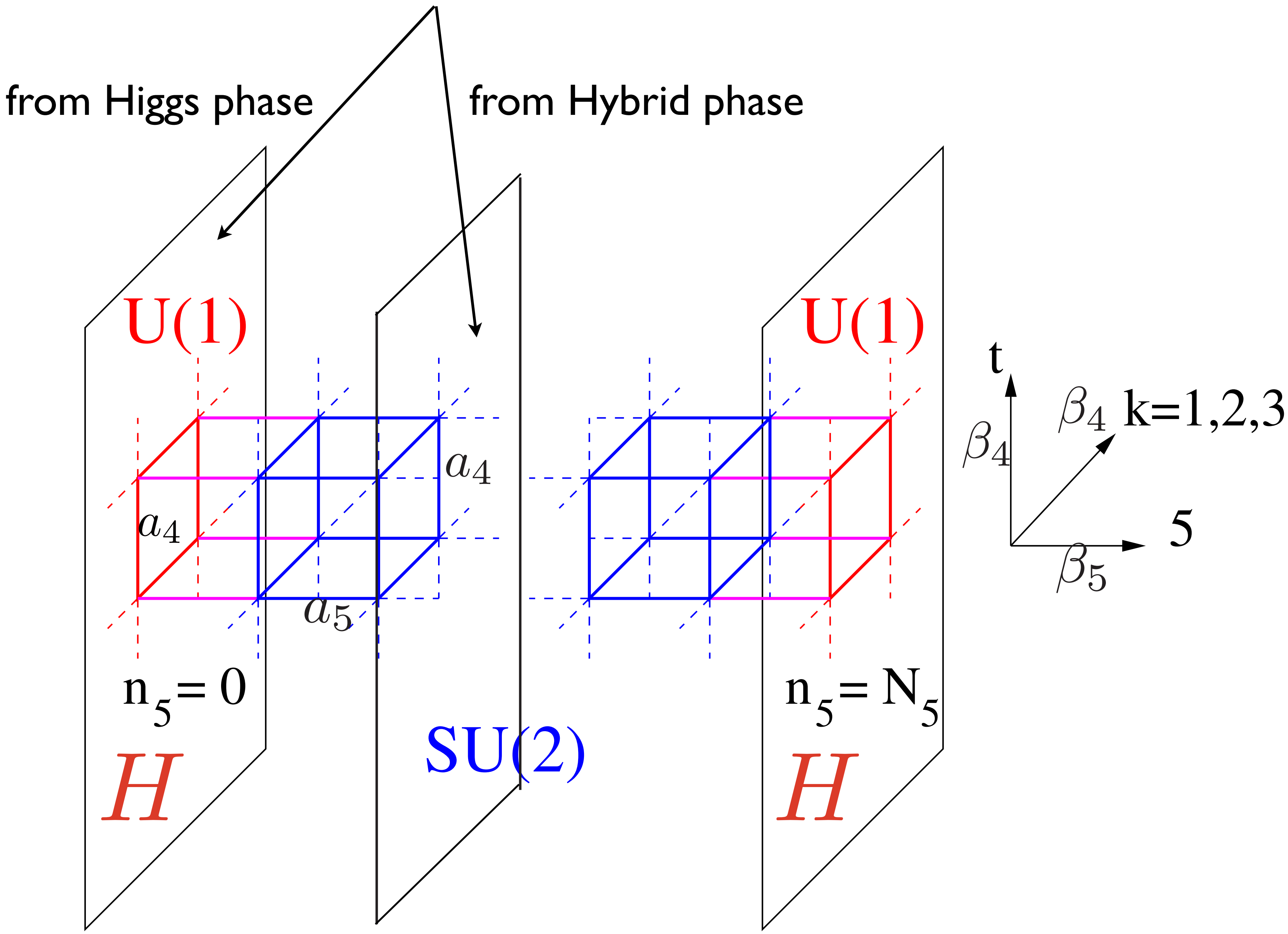
Zoom in:

with F. Koutroulis and A. Chatziagapiou , in progress



On the PT these two 4d slices are, to a good approximation, QFT's with the same cut-off,

$$\Lambda \sim 1/a_4$$



- This is a gauge invariant way to construct simultaneously two field theories, a confined non-Abelian theory and an Abelian gauge-scalar system with the same cut-off. As the boundary U(1) gauge-scalar theory in the Higgs phase becomes strongly coupled, the confining bulk SU(2) theory in the hybrid phase becomes asymptotically free. There exist LCP's from both sides, notably from the Higgs phase side, meaning that the spectrum, including the Higgs mass is stable as the cut-off varies. The matching of the LCPs on the PT determines the absolute scale, i.e. the cut-off. The "experimental" value of the Sommer scale does not allow the common cut-off to be large.

- There is a yet undetermined RG flow from the UV where the system is 5-dimensional to the IR where we expect to see a system of weakly interacting, softly broken 4d CFT's.

Conclusions and Outlook

- We presented a pure gauge 5d orbifold model where a Higgs mechanism is realised on the weakly coupled 4d boundary in a regime of its phase diagram close to the first order bulk phase transition where the fifth dimension is strongly coupled. Precisely and only in this regime, we simultaneously observe a Higgs slightly heavier than the Z boson and the system being dimensionally reduced to 4-dimensions via localization. The existence of an LCP points to a Higgs mass whose stability is somehow non-perturbatively guaranteed at least within a certain energy regime, by the higher dimensional gauge symmetry. We gave arguments for these statements analytically in the context of a Mean-Field expansion and numerically via extensive Monte Carlo simulations, both on the lattice.

- We described a plausible way to construct a continuum effective field theory (a system of spontaneously broken CFTs perhaps) that will allow us on one hand to answer the question whether this novel Higgs mechanism is in the same class where the Standard Model Higgs mechanism belongs and understand the details of the gauge hierarchy protection dynamics on the other.

Thank you!