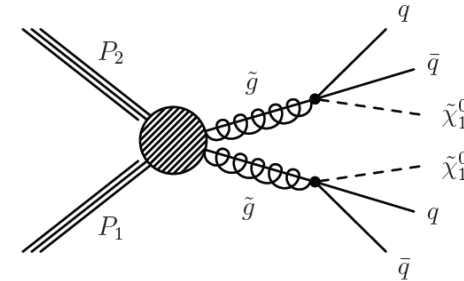


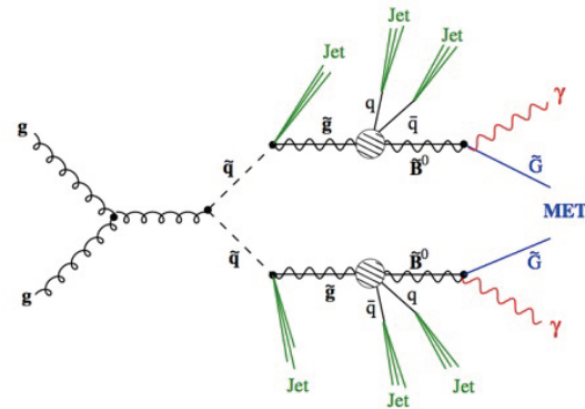
# SUSY searches at the LHC

Purely hadronic:  
Jets + missing energy

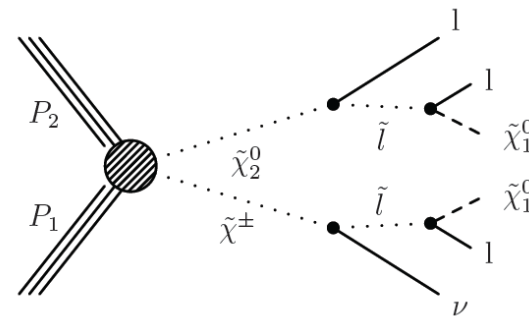


Photons:

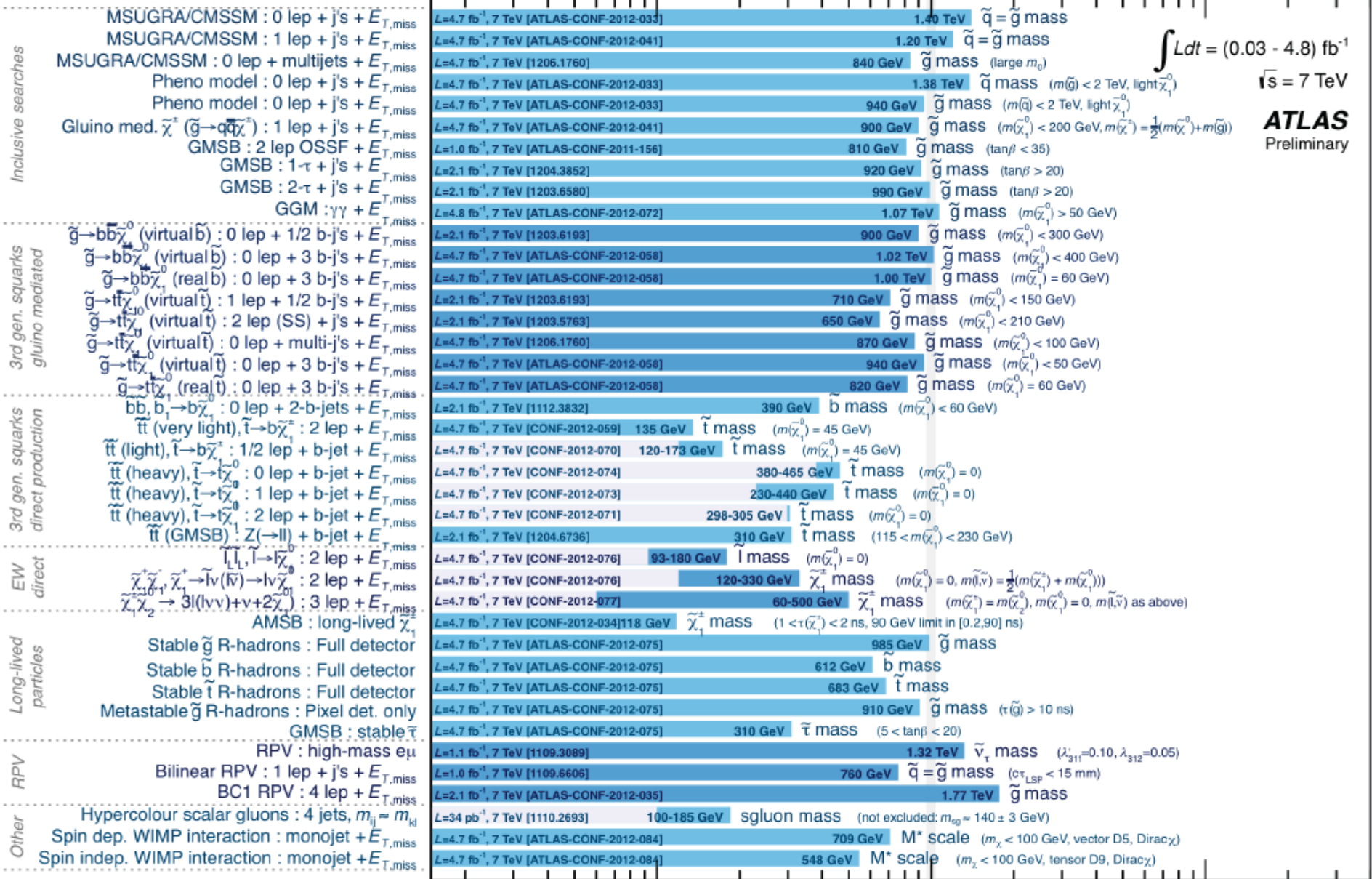
- targets:
  - > gauge mediated SUSY
  - > dark matter
  - > large extra dimensions



Leptonic:



# ATLAS SUSY Searches\* - 95% CL Lower Limits (Status: ICHEP 2012)



\*Only a selection of the available mass limits on new states or phenomena shown

Mass scale [TeV]

# ATLAS

## ATLAS SUSY Searches\* - 95% CL Lower Limits (Status: ICHEP 2012)

Search Category	Search Description	Lower Limit	Notes
Inclusive searches	MSUGRA/CMSSM : 0 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-033]	1.40 TeV $\tilde{q} = \tilde{g}$ mass
	MSUGRA/CMSSM : 1 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-041]	1.20 TeV $\tilde{q} = \tilde{g}$ mass
	MSUGRA/CMSSM : 0 lep + multijets + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [1206.1760]	840 GeV $\tilde{g}$ mass (large $m_0$ )
	Pheno model : 0 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-033]	1.38 TeV $\tilde{q}$ mass ( $m(\tilde{g}) < 2 \text{ TeV}$ , light $\tilde{\chi}_1^0$ )
	Pheno model : 0 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-033]	940 GeV $\tilde{g}$ mass ( $m(\tilde{g}) < 2 \text{ TeV}$ , light $\tilde{\chi}_1^0$ )
	Gluino med. $\tilde{\chi}^\pm (\tilde{g} \rightarrow q\tilde{q}\tilde{\chi}^\pm)$ : 1 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-041]	900 GeV $\tilde{g}$ mass ( $m(\tilde{\chi}_1^0) < 200 \text{ GeV}$ , $m(\tilde{\chi}^\pm) = \frac{1}{2}(m(\tilde{\chi}_1^0) + m(\tilde{g}))$ )
	GMSB : 2 lep OSSF + $E_{T,miss}$	$L=1.0 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2011-156]	810 GeV $\tilde{g}$ mass ( $\tan\beta < 35$ )
	GMSB : 1- $\tau$ + j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1204.3852]	920 GeV $\tilde{g}$ mass ( $\tan\beta > 20$ )
	GMSB : 2- $\tau$ + j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1203.6580]	990 GeV $\tilde{g}$ mass
	GGM : $\gamma\gamma$ + $E_{T,miss}$	$L=4.8 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-072]	1.07 TeV $\tilde{g}$ mass
3rd gen. squarks gluino mediated	$\tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$ (virtual $\tilde{b}$ ) : 0 lep + 1/2 b-j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1203.6193]	900 GeV $\tilde{g}$ mass
	$\tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$ (virtual $\tilde{b}$ ) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-058]	1.02 TeV $\tilde{g}$ mass
	$\tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$ (real $\tilde{b}$ ) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-058]	1.00 TeV $\tilde{g}$ mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (virtual $\tilde{t}$ ) : 1 lep + 1/2 b-j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1203.6193]	710 GeV $\tilde{g}$ mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (virtual $\tilde{t}$ ) : 2 lep (SS) + j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1203.5763]	650 GeV $\tilde{g}$ mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (virtual $\tilde{t}$ ) : 0 lep + multi-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [1206.1760]	870 GeV $\tilde{g}$ mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (virtual $\tilde{t}$ ) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-058]	940 GeV $\tilde{g}$ mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (real $\tilde{t}$ ) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-058]	820 GeV $\tilde{g}$ mass
	$\tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$ (real $\tilde{b}$ ) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1112.3832]	390 GeV $\tilde{b}$ mass ( $m(\tilde{\chi}_1^0) = 0 \text{ GeV}$ )
	$\tilde{t} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (very light), $\tilde{t} \rightarrow b\tilde{\chi}_1^\pm$ : 2 lep + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-059]	135 GeV $\tilde{t}$ mass ( $m(\tilde{\chi}_1^0) = 45 \text{ GeV}$ )
3rd gen. squarks direct production	$\tilde{t} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (light), $\tilde{t} \rightarrow b\tilde{\chi}_1^\pm$ : 1/2 lep + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-070]	120-173 GeV $\tilde{t}$ mass ( $m(\tilde{\chi}_1^0) = 45 \text{ GeV}$ )
	$\tilde{t} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (heavy), $\tilde{t} \rightarrow t\tilde{\chi}_1^0$ : 0 lep + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-074]	380-465 GeV $\tilde{t}$ mass ( $m(\tilde{\chi}_1^0) = 0$ )
	$\tilde{t} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (heavy), $\tilde{t} \rightarrow t\tilde{\chi}_1^0$ : 1 lep + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-073]	230-440 GeV $\tilde{t}$ mass ( $m(\tilde{\chi}_1^0) = 0$ )
	$\tilde{t} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (heavy), $\tilde{t} \rightarrow t\tilde{\chi}_1^0$ : 2 lep + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-071]	298-305 GeV $\tilde{t}$ mass ( $m(\tilde{\chi}_1^0) = 0$ )
	$\tilde{t} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (GMSB)!, $Z(\rightarrow ll) + b\text{-jet} + E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1204.6736]	310 GeV $\tilde{t}$ mass ( $115 < m(\tilde{\chi}_1^0) < 230 \text{ GeV}$ )
	$\tilde{t} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ : 2 lep + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-076]	93-180 GeV $\tilde{t}$ mass ( $m(\tilde{\chi}_1^0) = 0$ )
	$\tilde{\chi}_1^\pm \tilde{\chi}_1^\mp \rightarrow l\nu(\bar{\nu}) \rightarrow l\nu\tilde{\chi}_1^0$ : 2 lep + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-076]	120-330 GeV $\tilde{\chi}_1^\pm$ mass
	$\tilde{\chi}_1^\pm \tilde{\chi}_1^\mp \rightarrow 3l(l\nu\nu) + \nu + 2\tilde{\chi}_1^0$ : 3 lep + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-077]	118 GeV $\tilde{\chi}_1^\pm$ mass
	AMS $\tilde{b}$ : long-lived $\tilde{\chi}_1^\pm$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-034]	118 GeV $\tilde{\chi}_1^\pm$ mass
	Long-lived particles	Stable $\tilde{g}$ R-hadrons : Full detector	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]
Stable $\tilde{b}$ R-hadrons : Full detector		$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	
Stable $\tilde{t}$ R-hadrons : Full detector		$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	
Metastable $\tilde{g}$ R-hadrons : Pixel det. only		$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	
GMSB : stable $\tilde{\tau}$		$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	310 GeV $\tilde{\tau}$ mass ( $5 < \tan\beta < 10$ )
RPV	RPV : high-mass $e\mu$	$L=1.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1109.3089]	1.32 TeV $\tilde{\nu}_\tau$ mass ( $\lambda_{311}^2=0.10, \lambda_{312}^2=0.05$ )
	Bilinear RPV : 1 lep + j's + $E_{T,miss}$	$L=1.0 \text{ fb}^{-1}, 7 \text{ TeV}$ [1109.6606]	760 GeV $\tilde{q} = \tilde{g}$ mass ( $c\tau_{LSP} < 15 \text{ mm}$ )
	BC1 RPV : 4 lep + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-035]	1.7 TeV $\tilde{g}$ mass
Other	Hypercolour scalar gluons : 4 jets, $m_g = m_{kl}$	$L=34 \text{ pb}^{-1}, 7 \text{ TeV}$ [1110.2693]	100-185 GeV scalar mass (not excluded if $m_g = 140 \pm 3 \text{ GeV}$ )
	Spin dep. WIMP interaction : monojet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-084]	709 GeV $M^*$ scalar ( $m_\chi < 100 \text{ GeV}$ , vector D5, Dirac $\chi$ )
	Spin indep. WIMP interaction : monojet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-084]	548 GeV $M^*$ scalar ( $m_\chi < 100 \text{ GeV}$ , tensor D9, Dirac $\chi$ )

$\int L dt = (0.03 - 4.8) \text{ fb}^{-1}$   
 $\sqrt{s} = 7 \text{ TeV}$

**ATLAS Preliminary**

Limit 1 TeV strong interacting particles

Limit 300-400 GeV stop particles

And limits on WEAK INTERACTIONS

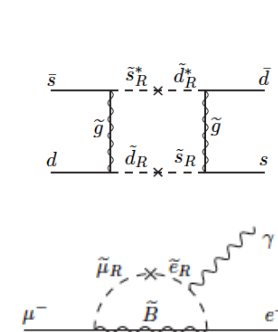
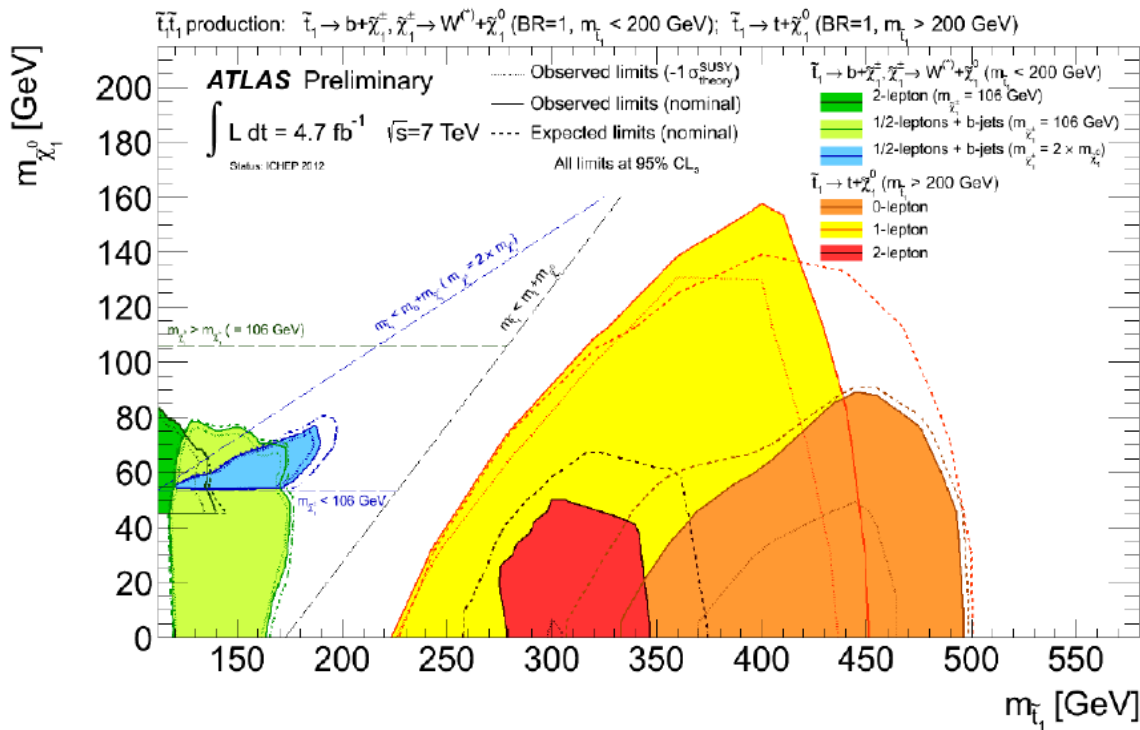
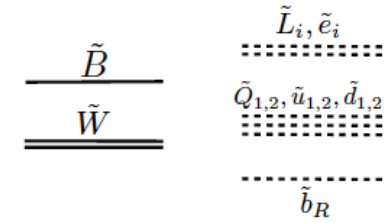
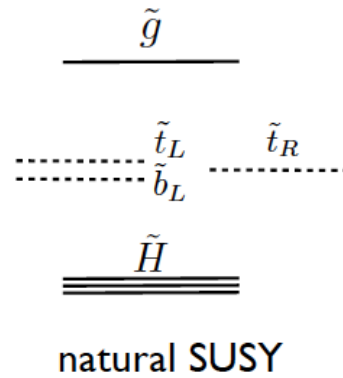
Mass scale [TeV]

\*Only a selection of the available searches

# An exception: "Natural" SUSY

FCNC: 1,2 sgenerations heavy

Hierarchy problem: 3<sup>rd</sup> sgeneration light



# Status of SUSY -little hierarchy problem

**MSSM:** 105 +(19) Parameters

$$M_Z^2 = \sum_{\tilde{q}, \tilde{l}} a_i \tilde{m}_i^2 + \sum_{\tilde{g}, \tilde{W}, \tilde{B}} \tilde{M}_i^2 + \dots$$

$$m_{\tilde{q}} > 0.6 - 1 \text{ TeV} \Rightarrow \Delta > a \frac{\tilde{m}^2}{M_Z^2} \sim 100 \quad (\text{Unless light stop } m_{t, \text{LHC}} > 250 \text{ GeV})$$

$\Rightarrow$  Correlations between SUSY breaking parameters  
and/or additional low-scale states

# Status of SUSY -little hierarchy problem

**MSSM:** 105 +(19) Parameters

$$M_Z^2 = \sum_{\tilde{q}, \tilde{l}} a_i \tilde{m}_i^2 + \sum_{\tilde{g}, \tilde{W}, \tilde{B}} \tilde{M}_i^2 + \dots$$

$$m_{\tilde{q}} > 0.6 - 1 \text{TeV} \Rightarrow \Delta > a \frac{\tilde{m}^2}{M_Z^2} \sim 100$$

(Unless light stop  $m_{t,LHC} > 250 \text{ GeV}$ )

$\Rightarrow$  Correlations between SUSY breaking parameters  
and/or additional low-scale states



definite SUSY structure

Fine Tuning measure:

$$\Delta(\gamma_i) = \left| \frac{\gamma_i}{M_Z} \frac{\partial M_Z}{\partial \gamma_i} \right|,$$

$$\Delta_{\max} = \text{Max}_{a_i} \Delta(\gamma_i)$$

$$\gamma_i = \{ \tilde{m}_i, \tilde{M}_i, \dots \}$$

Ellis, Enquist, Nanopoulos, Zwirner

Barbieri, Giudice



Fine Tuning measure:

$$\Delta(\gamma_i) = \left| \frac{\gamma_i}{M_Z} \frac{\partial M_Z}{\partial \gamma_i} \right|,$$

$$\Delta_{\max} = \text{Max}_{a_i} \Delta(\gamma_i)$$

Ellis, Enquist, Nanopoulos, Zwirner

Barbieri, Giudice

Likelihood:

$$L(\text{data}|\gamma_i^0) = \frac{1}{\Delta_q} L(\text{data}|\gamma_i; v_0, \beta, \tilde{y}_t(\beta), \tilde{y}_b(\beta)) \Big|_{\beta=\beta_0(\gamma_i); \gamma_i=\gamma_i^0}$$

$$\chi^2(\gamma_i) = -2\ln(L) = \chi_{old}^2(\gamma_i) + 2\ln \Delta_q$$

Ghilencea, Ross

$$\Delta_q = \left( \sum_i \Delta_{\gamma_i}^2 \right)^{1/2}$$

$$\Delta_q = 100, \quad \delta\chi^2 / d.o.f. \sim 1$$

$$\Delta_q = 1000, \quad \delta\chi^2 / d.o.f. \sim 1.5$$

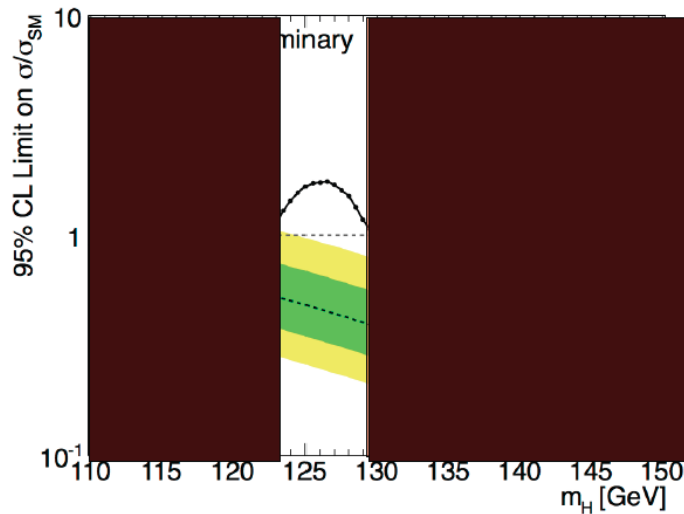
$$\chi^2 / d.o.f. = 2(2.5), \quad P = 3(0.6)\%$$

# The Higgs mass in SUSY ?

$$M_S^2 = m_{q_3} m_{U_3} \geq (500 \text{ GeV})^2$$

$$M_{h^0}^2 = M_Z^2 \cos^2 2\beta + \frac{3M_t^2 h_t^2}{4\pi^2} \left( \ln\left(\frac{M_S^2}{M_t^2}\right) + \delta_t \right) + \dots \approx 125 \text{ GeV (LHC)}$$

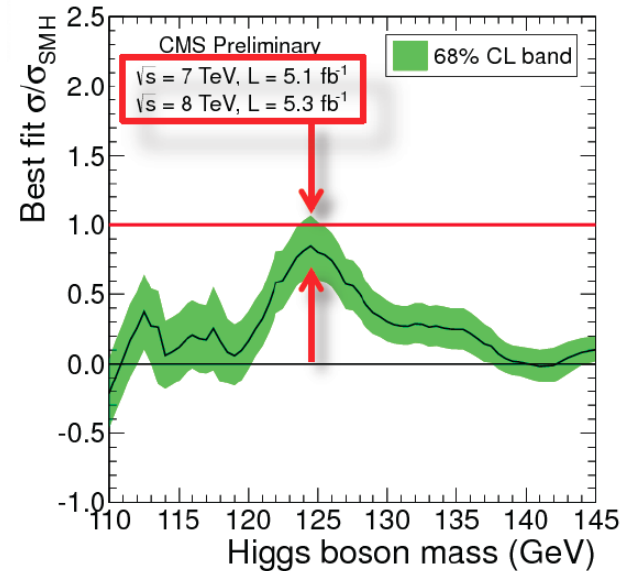
## Atlas



Excluded at 95% CL

110-122.7 129-557 GeV

## CMS





- The CMSSM

$$\mu_0, m_0, m_{1/2}, A_0, B_0$$



assume correlation between SUSY breaking parameters

# ● The CMSSM

$$\mu_0, m_0, m_{1/2}, A_0, B_0$$

$$V = m_1^2 |H_1|^2 + m_2^2 |H_2|^2 - (m_3^2 H_1 \cdot H_2 + h.c.) \\ + \frac{1}{2} \lambda_1 |H_1|^4 + \frac{1}{2} \lambda_2 |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1 \cdot H_2|^2 \\ + \left[ \frac{1}{2} \lambda_5 (H_1 \cdot H_2)^2 + \lambda_6 |H_1|^2 (H_1 \cdot H_2) + \lambda_7 |H_2|^2 (H_1 \cdot H_2) + h.c. \right]$$

Minimisation conditions:

$$\underline{v^2 = -m^2/\lambda}, \quad 2\lambda \frac{\partial m^2}{\partial \beta} = m^2 \frac{\partial \lambda}{\partial \beta}$$

$$m^2 = m_1^2 \cos^2 \beta + m_2^2 \sin^2 \beta - m_3^2 \sin 2\beta$$

$$\lambda = \frac{\lambda_1}{2} \cos^4 \beta + \frac{\lambda_2}{2} \sin^4 \beta + \frac{\lambda_{345}}{4} \sin^2 2\beta + \sin 2\beta (\lambda_6 \cos^2 \beta + \lambda_7 \sin^2 \beta)$$

$$\Delta \equiv \max \left| \Delta_p \right|_{p=\{\mu_0^2, m_0^2, m_{1/2}^2, A_0^2, B_0^2\}}, \quad \Delta_p \equiv \frac{\partial \ln v^2}{\partial \ln p}$$

Couplings and masses evaluated to two loop (leading log) order

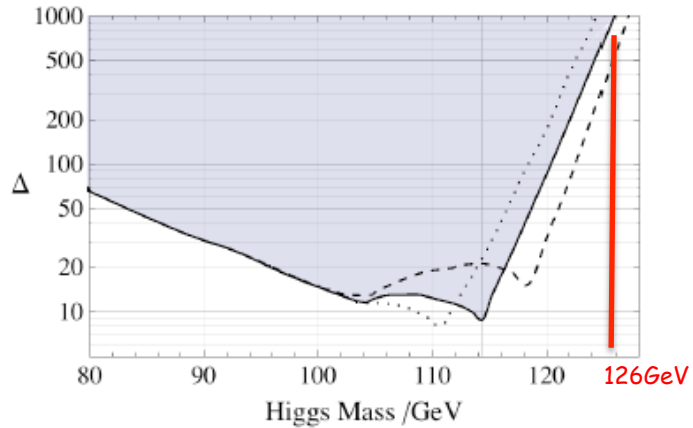
...enhanced sensitivity due to small tree-level  $\lambda = \frac{1}{8} (g_1^2 + g_2^2) \cos^2 2\beta$

Cassel, Ghilencea, GGR  
c.f. earlier work : Dimopoulos, Giudice  
Chankowski, Ellis, Olechowski, Pokorski

# ● The CMSSM

$$\mu_0, m_0, m_{1/2}, A_0, B_0$$

## Constraints



SUSY particle masses

$$3.20 < 10^4 \text{ Br}(b \rightarrow s\gamma) < 3.84$$

$$\text{Br}(b \rightarrow \mu\mu) < 1.8 \times 10^{-8}$$

$$\delta a_\mu < 292 \times 10^{-11}$$

$$-0.0007 < \delta\rho < 0.0012$$

Radiative EW breaking

Relic density unrestricted

$$\Delta \equiv \max |\Delta_p|_{p=\{\mu_0^2, m_0^2, m_{1/2}^2, A_0^2, B_0^2\}}, \quad \Delta_p \equiv \frac{\partial \ln v^2}{\partial \ln p}$$

$$\Delta_{Min} = 9, \quad m_h = 114 \pm 2 \text{ GeV}$$

(No Higgs bound applied)

# ● The CMSSM

## Constraints

SUSY particle masses

$$3.20 < 10^4 \text{Br}(b \rightarrow s\gamma) < 3.84$$

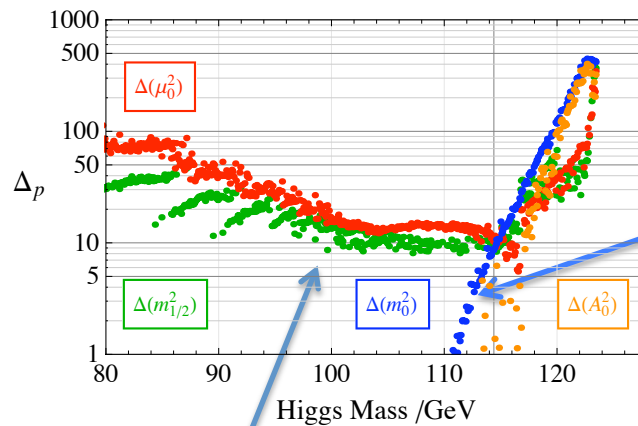
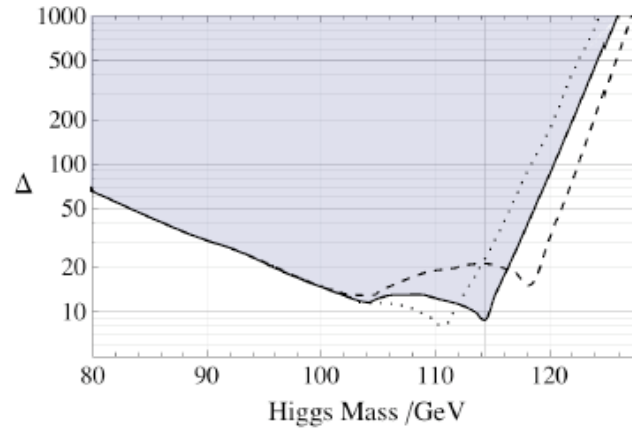
$$\text{Br}(b \rightarrow \mu\mu) < 1.8 \times 10^{-8}$$

$$\delta a_\mu < 292 \times 10^{-11}$$

$$-0.0007 < \delta\rho < 0.0012$$

Radiative EW breaking

Relic density unrestricted



Limit of focus point

$\lambda$  increase with  $m_H$

$$v^2 = -\frac{m^2}{\lambda}$$

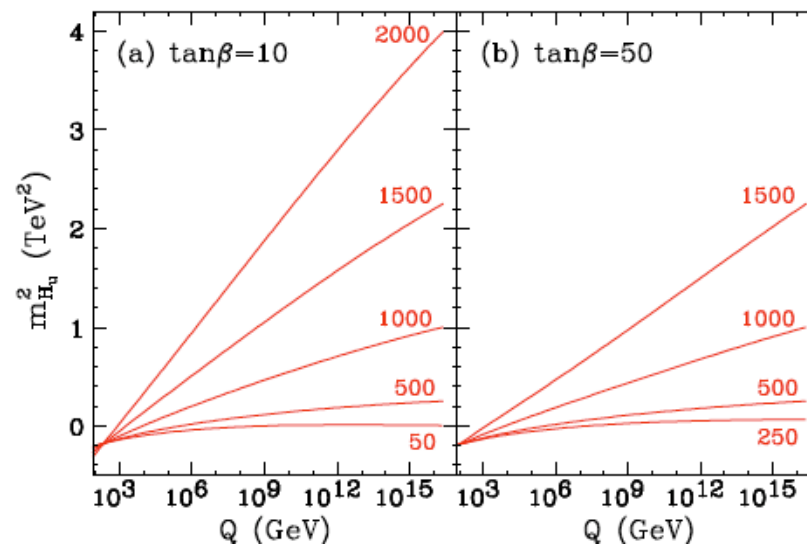
# Focus Point

$$2|y_t|^2(m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2|a_t|^2$$

$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3X_t - 6g_2^2 |M_2|^2 - \frac{6}{5}g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{Q_3}^2 = X_t + X_b - \frac{32}{3}g_3^2 |M_3|^2 - 6g_2^2 |M_2|^2 - \frac{2}{15}g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{u_3}^2 = 2X_t - \frac{32}{3}g_3^2 |M_3|^2 - \frac{32}{15}g_1^2 |M_1|^2$$



$$m_{H_u}^2(Q^2) = m_{H_u}^2(M_P^2) + \frac{1}{2} \left( m_{H_u}^2(M_P^2) + m_{Q_3}^2(M_P^2) + m_{u_3}^2(M_P^2) \right) \left[ \left( \frac{Q^2}{M_P^2} \right)^{\frac{3y_t^2}{4\pi^2}} - 1 \right]$$

$m_0^2$

$3m_0^2$

$\approx -\frac{2}{3}, Q^2 \approx M_Z^2$

“Focus point”:  $m_{H_u}^2(0) = m_{Q_3}^2(0) = m_{u_3}^2(0) \equiv m^2$

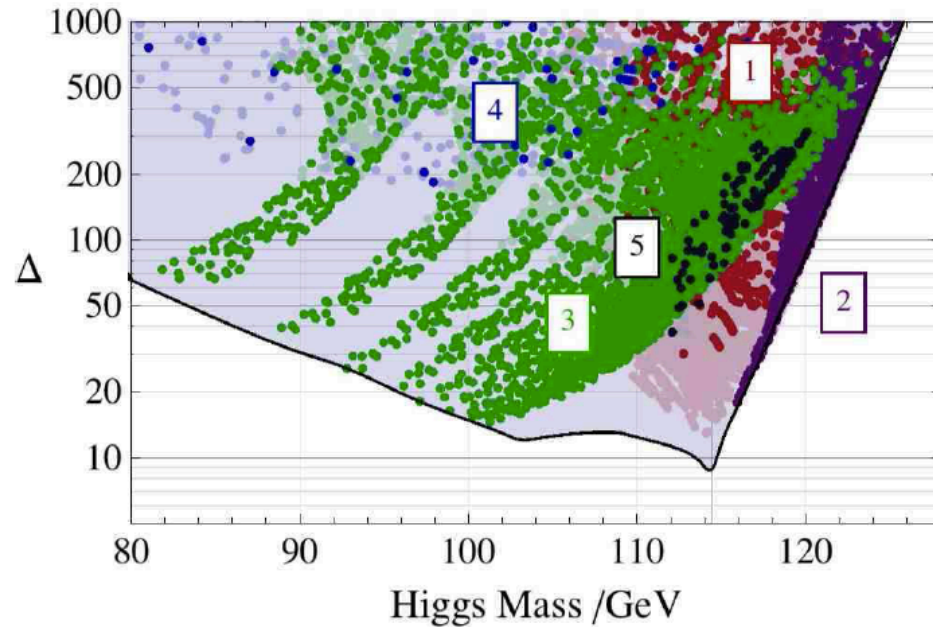
$$m_{H_u}^2(t_0) = a_0 m^2 + \dots, a_0 \leq 0.1$$

i.e.  $m_{Q_3}^2, m_{u_3}^2 \gg M_Z^2$  possible

Natural choice

Feng, Matchev, Moroi  
 Chan, Chattopadhyay, Nath  
 Barbieri, Giudice  
 Feng, Sanford

# Dark Matter structure



Relic density restricted

- 1  $h^0$  resonant annihilation
- 2  $\tilde{h}$  t-channel exchange
- 3  $\tilde{\tau}$  co-annihilation
- 4  $\tilde{t}$  co-annihilation
- 5  $A^0 / H^0$  resonant annihilation

Within  $3\sigma$  WMAP:

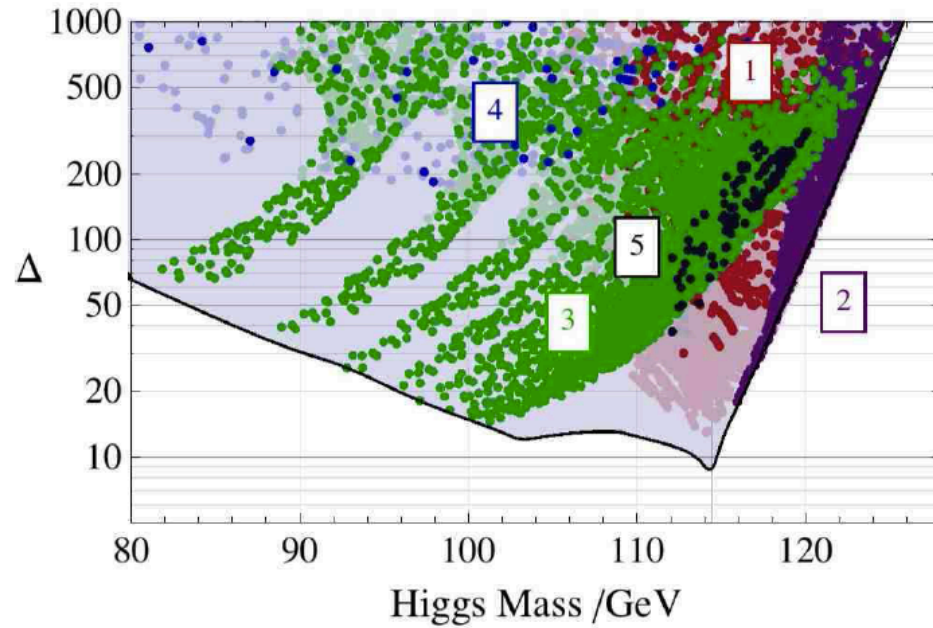
$$\Delta_{Min} = 15, \quad m_h = 114.7 \pm 2 GeV$$

<  $3\sigma$  WMAP:

$$\Delta_{Min} = 18, \quad m_h = 115.9 \pm 2 GeV$$

Cassel, Ghilencea, GGR

Relic density restricted



- 1  $h^0$  resonant annihilation
- 2  $\tilde{h}$  t-channel exchange
- 3  $\tilde{\tau}$  co-annihilation
- 4  $\tilde{t}$  co-annihilation
- 5  $A^0 / H^0$  resonant annihilation

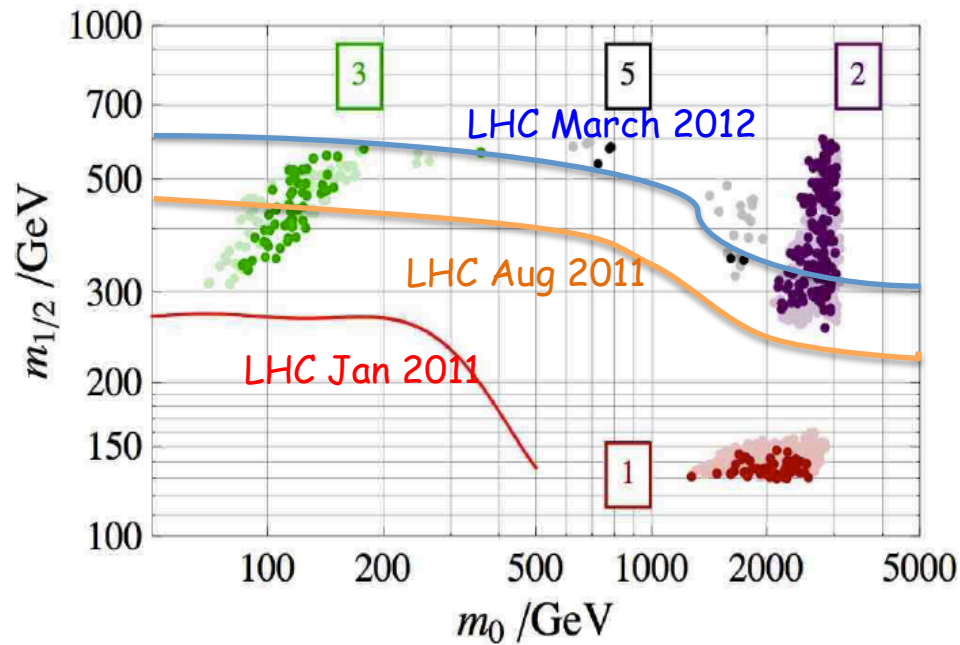
Within  $3\sigma$  WMAP:

$$\Delta_{Min} = 15, \quad m_h = 114.7 \pm 2 GeV$$

$< 3\sigma$  WMAP:

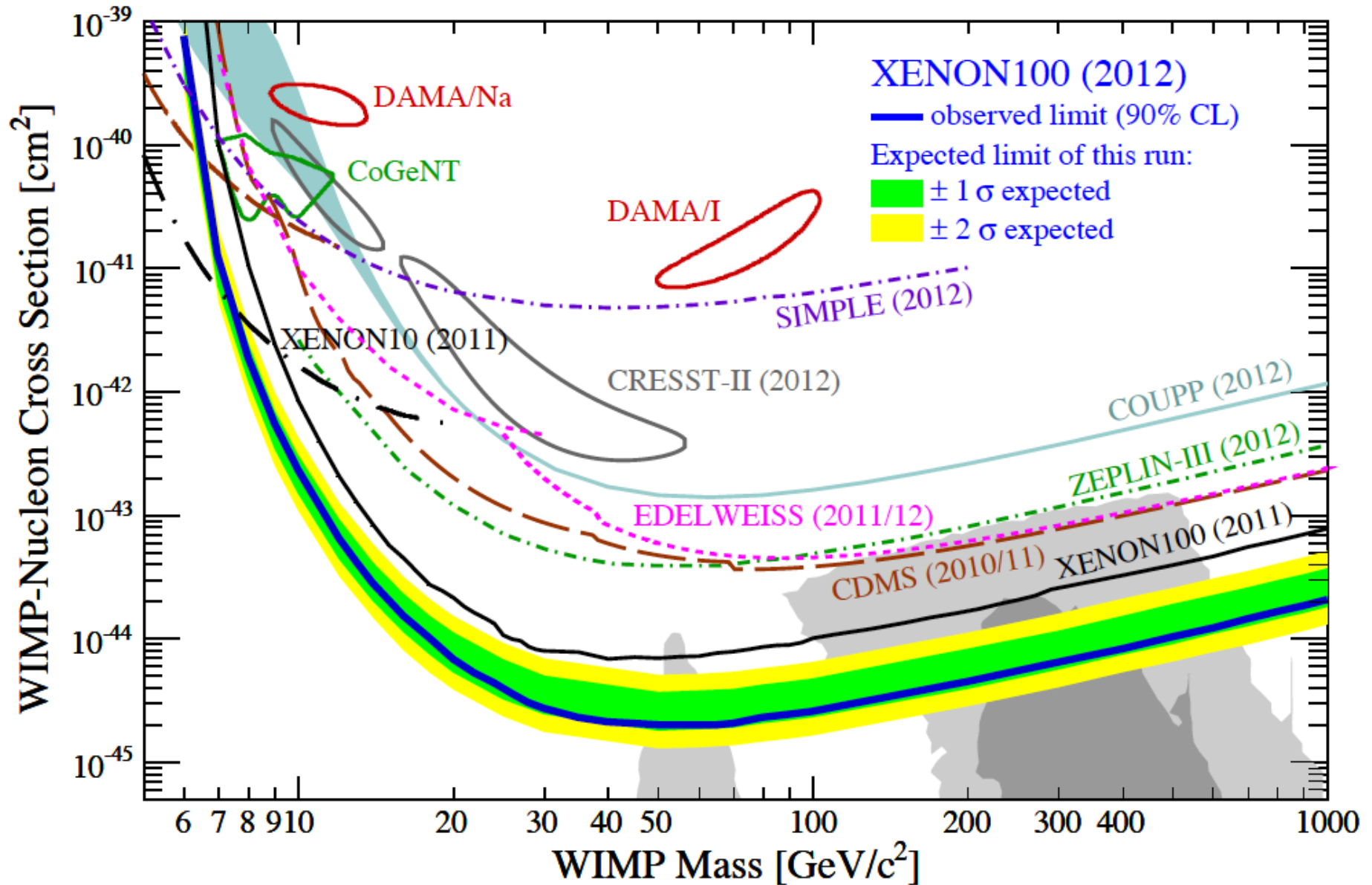
$$\Delta_{Min} = 18, \quad m_h = 115.9 \pm 2 GeV$$

Cassel, Ghilencea, GGR

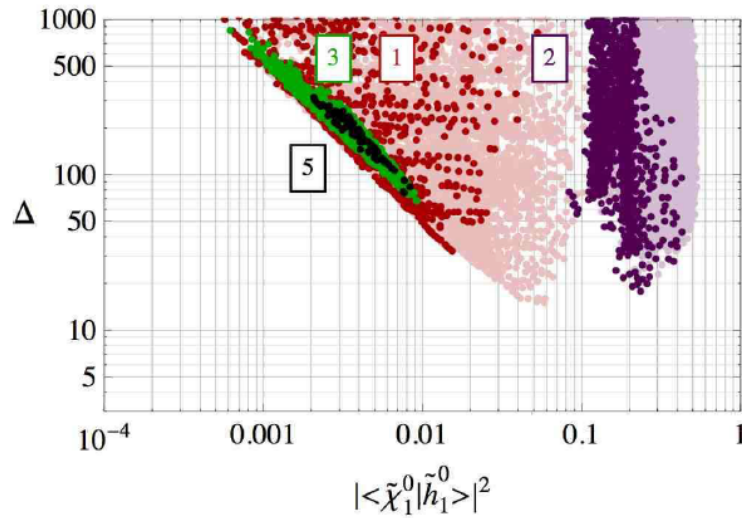




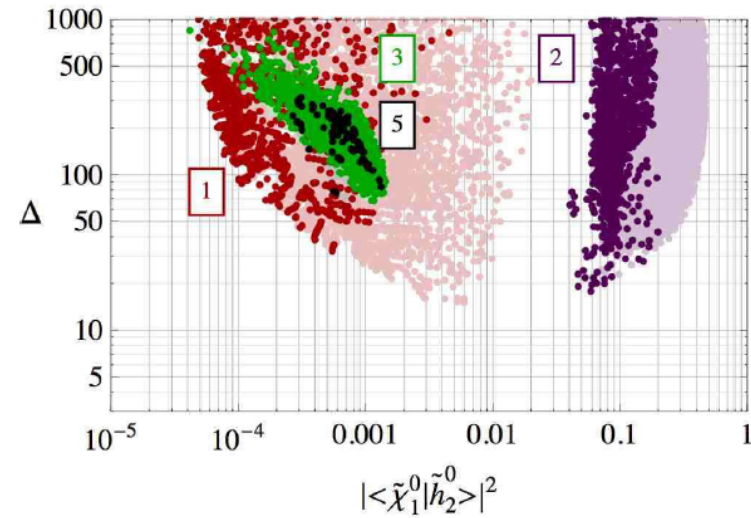
# Direct dark matter searches: (spin independent)



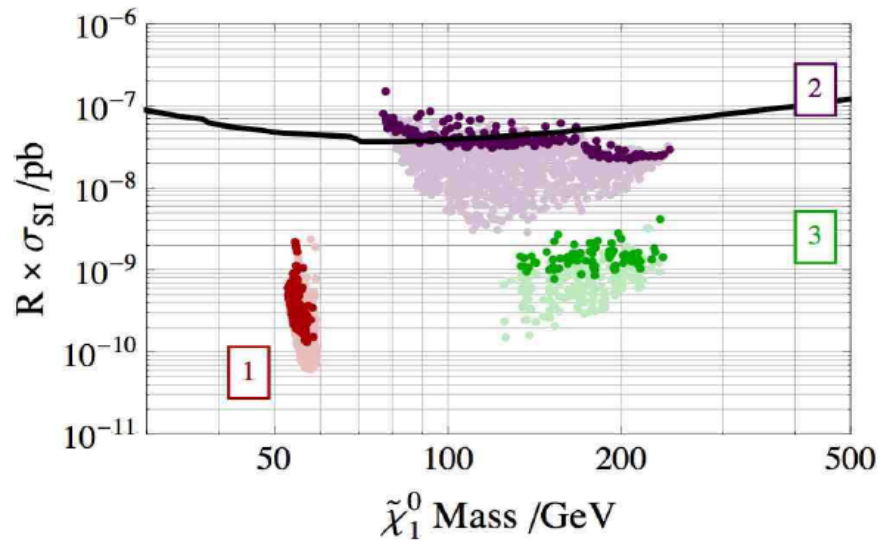
# DM - Scaled spin independent cross section for LSP-proton scattering:



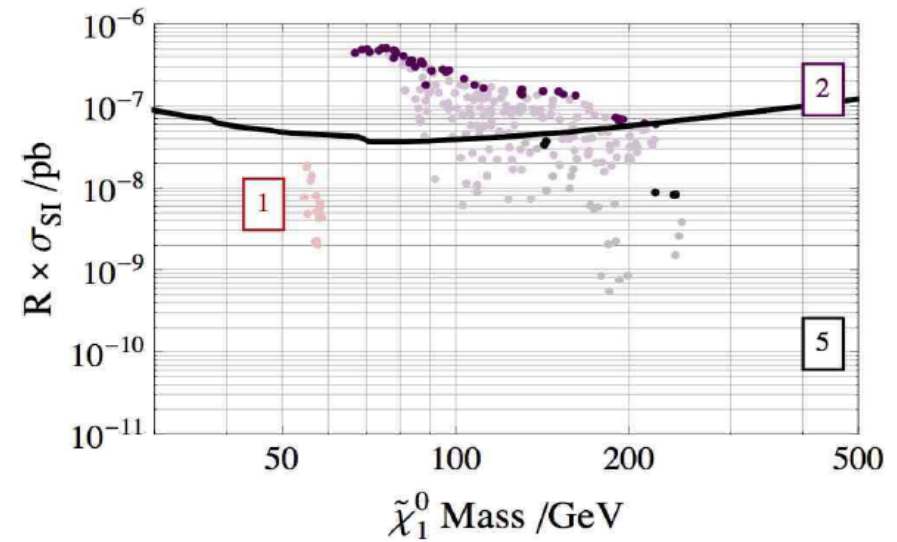
(a) LSP  $\tilde{h}_1^0$  component



(b) LSP  $\tilde{h}_2^0$  component



(a)  $\tan \beta \leq 45$   
 $\Delta < 100$



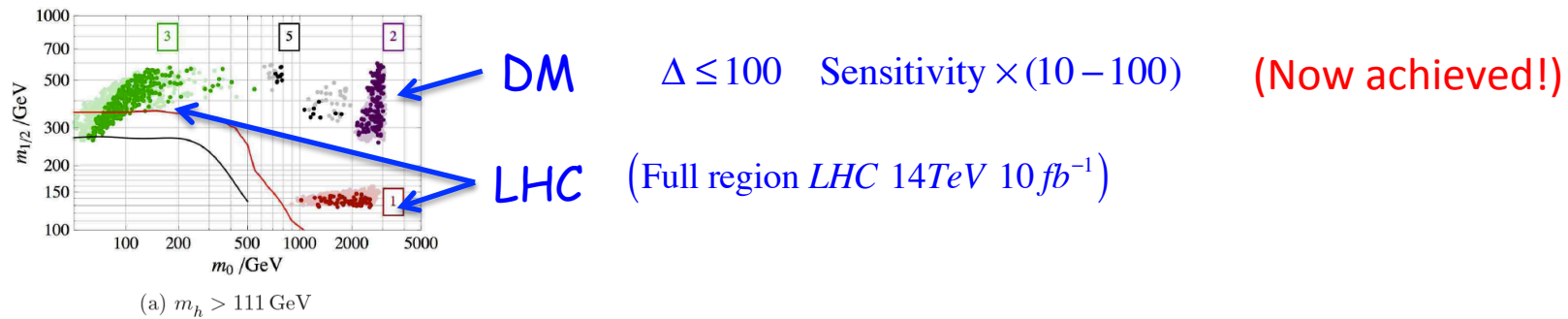
(b)  $50 \leq \tan \beta \leq 55$   
 $\Delta < 100$

# CMSSM summary:

- Minimises MSSM fine tuning (focus point)

$$\text{Max}[\Delta_{EW}, \Delta_{\Omega}] = 15(29), \quad m_h = 114(116) \pm 2 \text{ GeV}$$

- Complementary DM & LHC searches



- **BUT**  $\Delta > 300$  for  $m_H = 126 \text{ GeV}$

- (General) Gauge mediation in the MSSM

$$M_{\tilde{\lambda}_i}(M_{mess}) = k_i \frac{\alpha_i(M_{mess})}{4\pi} \Lambda_G$$

$$m_{\tilde{f}}^2(M_{mess}) = 2 \sum_{i=1}^3 C_i k_i \frac{\alpha_i^2(M_{mess})}{(4\pi)^2} \Lambda_S^2$$

$$k_i = \left(\frac{5}{3}, 1, 1\right)$$

$$k_i \alpha_i(M_{GUT}) = 1, \quad i = 1, 2, 3$$

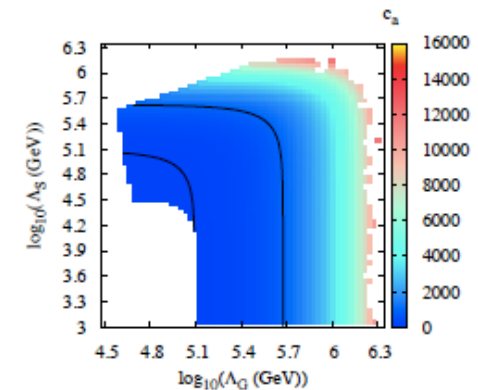
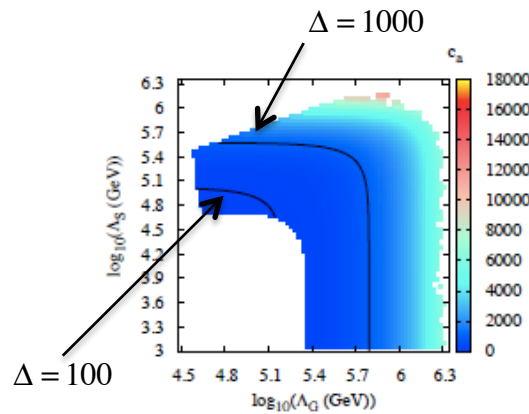
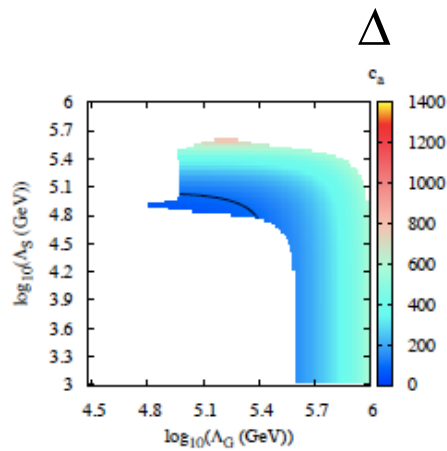
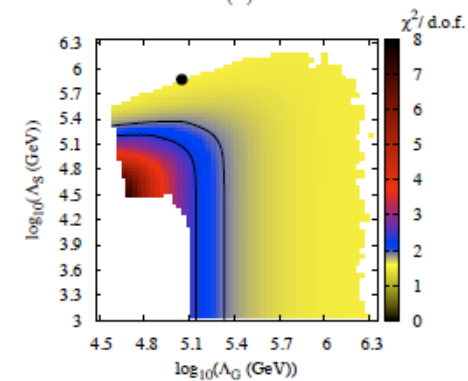
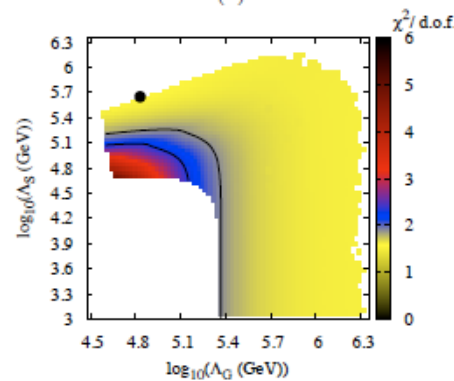
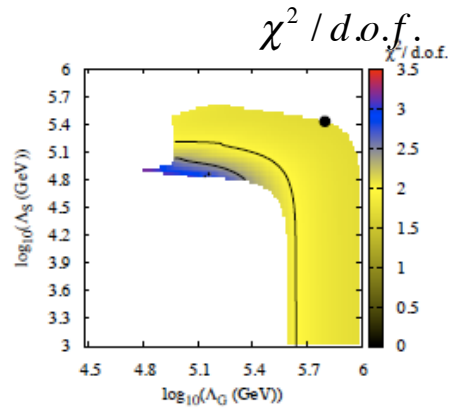
(Ordinary gauge mediation  $\Lambda_G = \Lambda_S$ )



No focus point

# Fine tuning in General Gauge Mediation

$B \rightarrow X_s \gamma, B \rightarrow \tau \mu, B \rightarrow \mu^+ \mu^-, B \rightarrow D \tau \mu,$   
 $D_s \rightarrow \mu \nu, D_s \rightarrow \tau \nu, K \rightarrow \mu \nu / \pi \rightarrow \mu \nu, \Delta_{0-}$



$M_{\text{Messenger}}$

$10^6 \text{ GeV}$

$10^{10} \text{ GeV}$

$10^{14} \text{ GeV}$

$\Delta \gg 100$  no focus point

Abel, Dolan, Jaeckel, Khoze  
 (Giusti, Romanino, Strumia)

# Reduced fine tuning (c.f. CMSSM)

- New degrees of freedom
- New focus points?

Gauginos:

$$M_{\tilde{g}, \tilde{W}, \tilde{B}}$$

Non-universal gaugino correlations

Kane, King  
Lebedev, Nilles, Ratz...  
Horton, GGR

...

Scalars:

$$M_0, A_0$$

correlations?

Feldman, Kane, Kuflik, Lu

$$M_0, A_0, B_0 \gg \mu, m_a$$

$$m_{h_u}^2(t) = f_{M_0} M_0^2 - f_{A_0} A_0^2$$

$$f_{M_0} \sim f_{A_0} \sim 0.1 \quad + \quad M_0 \sim A_0 \quad \Rightarrow$$

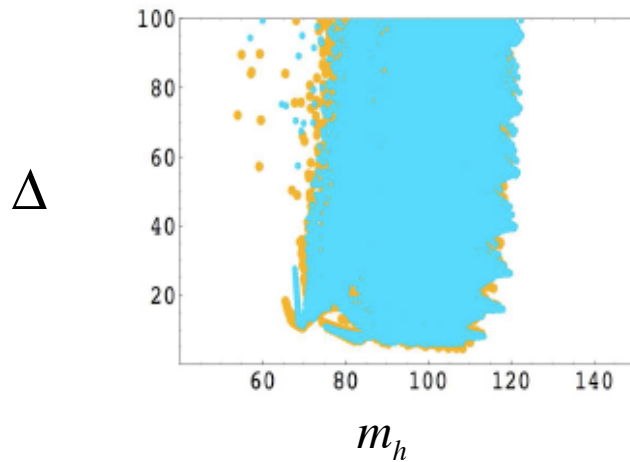
$$m_{h_u}^2 \sim 10^{-2} m_{3/2}^2$$

$$\Delta_{h_t} \sim 10^4, \quad M_0 \sim 10 \text{ TeV}$$

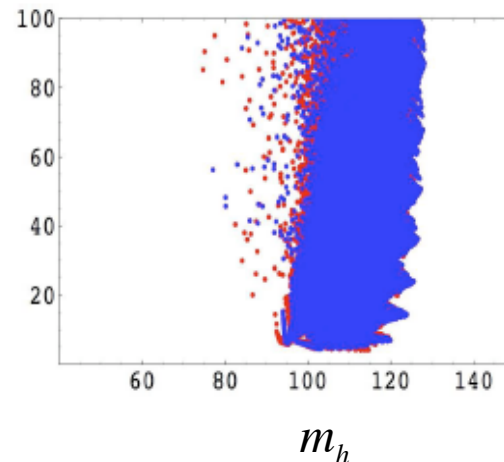
# I. Reduced fine tuning : New heavy states - higher dimension operators

$$\delta L = \int d^2\theta \frac{1}{M_*} (\mu_0 + c_0 S) (H_1 H_2)^2, \quad S = m_0 \theta \theta \quad \text{Dimension 5}$$

$$\delta V = \varsigma_1 (|h_1|^2 + |h_2|^2) h_1 h_2 + \varsigma_2 (h_1 h_2)^2; \quad \varsigma_1 = \frac{\mu_0}{M_*}, \quad \varsigma_2 = \frac{c_0 m_0}{M_*}$$



MSSM



+ dim 5 operators

Cassel, Ghilencea, GGR  
Casas, Espinosa, Hidalgo  
Dine, Seiberg, Thomas  
Batra, Delgado, Tait  
Kaplan,

Even for  $M_* = 65 \mu_0$  a significant shift of  $m_h$  for constant  $\Delta$

...effect mainly comes from  $\varsigma_1$  term ... origin?



# Reduced fine tuning : singlet extensions

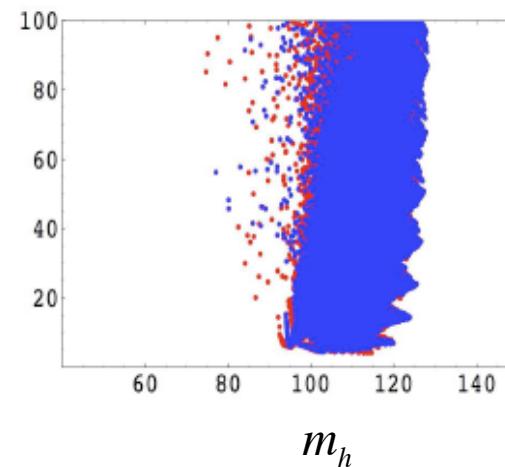
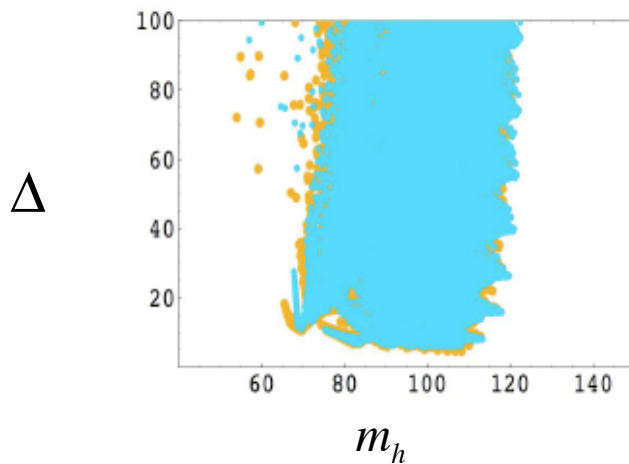
$$W = W_{\text{Yukawa}} + (\mu + \lambda S)H_u H_d + \frac{\mu S}{2}S^2 + \frac{\kappa}{3}S^3 + \xi S \quad \text{GNMSSM}$$

$$\mu_s \gg m_{3/2} \quad \dagger$$

$$\text{c.f. } W = W_{\text{Yukawa}} + \lambda S H_u H_d + \frac{\kappa}{3}S^3 \quad \text{NMSSM}$$

$$W_{\text{eff}}^{\text{GNMSSM}} = (H_u H_d)^2 / \mu_s + \mu H_u H_d$$

$$\frac{\mu}{\mu_s} (|H_u|^2 + |H_d|^2) H_u H_d \quad \xrightarrow{\nu^2 = -\frac{m^2}{\lambda}}$$



Reduced fine tuning in GNMSSM (but not NMSSM) †

# SUSY extensions of the Standard Model

R-symmetry ensures Singlet extensions natural

# SUSY extensions of the Standard Model

**NMSSM spectrum**  
 No perturbative  $\mu$  term  
 Commutes with  $SO(10)$   
 Anomaly cancellation

$N$	$q_{10}$	$q_{\bar{5}}$	$q_{H_u}$	$q_{H_d}$	$q_S$
4	1	1	0	0	2
8	1	5	0	4	6

Can be embedded in  $SO(10)$

R-symmetry ensures singlets light

## D=5 operators

up and down Yukawas allowed

$$3q_{10} + q_{\bar{5}} + q_{H_u} + q_{H_d} = 4 \pmod{N} \Rightarrow 3q_{10} + q_{\bar{5}} = 0 \pmod{N} \Rightarrow \frac{1}{M} \cancel{QQQL} \quad \frac{1}{M} LLH_u H_u$$

Weinberg operator

## SUSY breaking

$\langle W \rangle, \langle \lambda \lambda \rangle$  R=2 non-perturbative breaking

Domain walls and tadpoles safe      Abelian

$$Z_{4,8}^R \rightarrow Z_2^R \quad R\text{-parity}$$

$$\mu \sim m_{3/2}, \quad O\left(\frac{m_{3/2}}{M^2} QQQL\right)$$

# SUSY extensions of the Standard Model

## NMSSM spectrum

No perturbative  $\mu$  term

Commutates with  $SO(10)$

Anomaly cancellation

$N$	$q_{10}$	$q_{\bar{5}}$	$q_{H_u}$	$q_{H_d}$	$q_S$
4	1	1	0	0	2
8	1	5	0	4	6

R-symmetry ensures singlets light

## D=5 operators

up and down Yukawas allowed

$$3q_{10} + q_{\bar{5}} + q_{H_u} + q_{H_d} = 4 \pmod{N} \Rightarrow 3q_{10} + q_{\bar{5}} = 0 \pmod{N} \Rightarrow \frac{1}{M} \cancel{QQQL} \quad \frac{1}{M} LLH_u H_u$$

Weinberg operator

## SUSY breaking

$\langle W \rangle, \langle \lambda \lambda \rangle$  R=2 non=perturbative breaking

Domain walls and tadpoles safe Abel

$$Z_{4,8}^R \rightarrow Z_2^R \quad R\text{-parity}$$

$$\mu \sim m_{3/2}, \quad O\left(\frac{m_{3/2}}{M^2} QQQL\right)$$

$$W = W_{MSSM} + \lambda S H_u H_d + \kappa S^3 + \Delta W$$

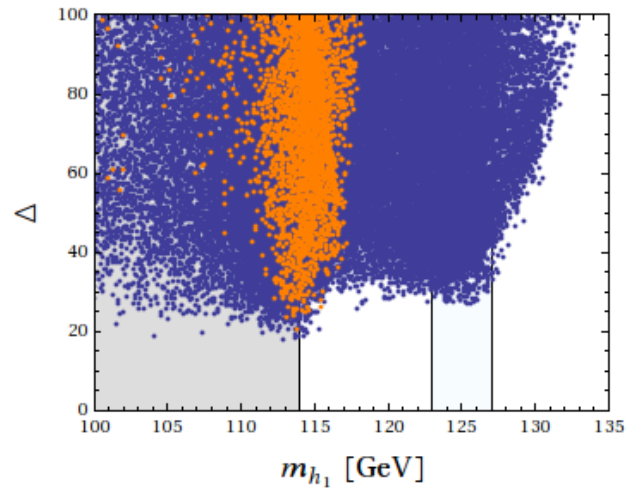
$$\Delta W_{Z_4^R} \sim m_{3/2} H_u H_d + m_{3/2}^2 S + m_{3/2} S^2$$

$$\Delta W_{Z_8^R} \sim m_{3/2}^2 S$$

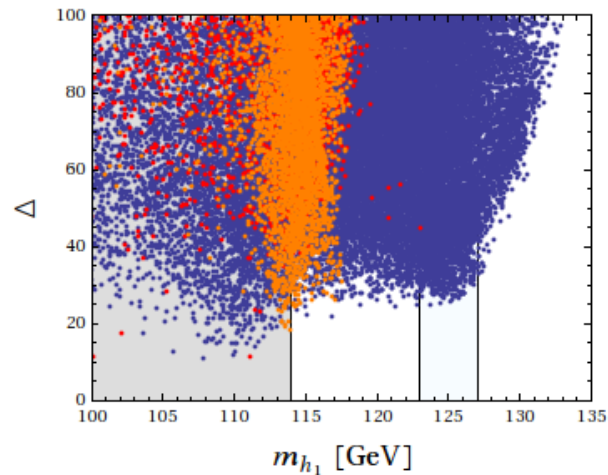
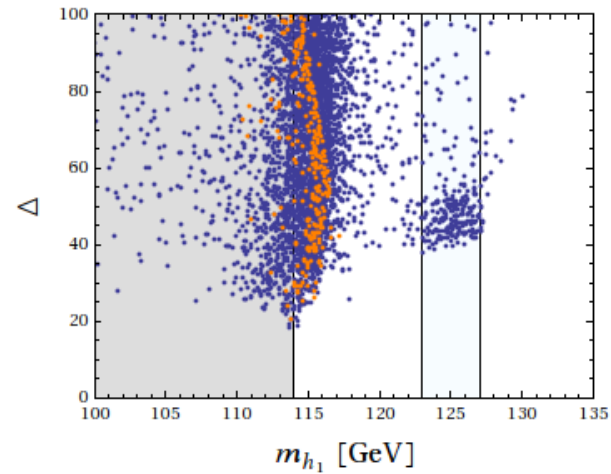
←  $\mu$  term and mass terms “natural”

GNMSSM (c.f. NMSSM)

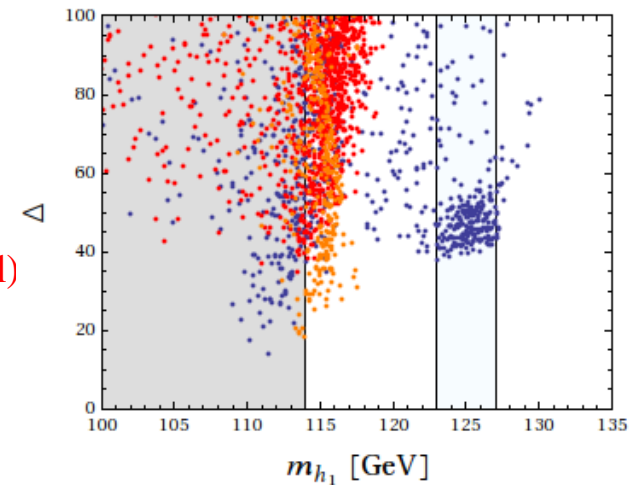
# Fine tuning in the GNMSSM $(\lambda \leq 0.7^\dagger)$



- CMSSM
- CGNMSSM  
(universal masses)



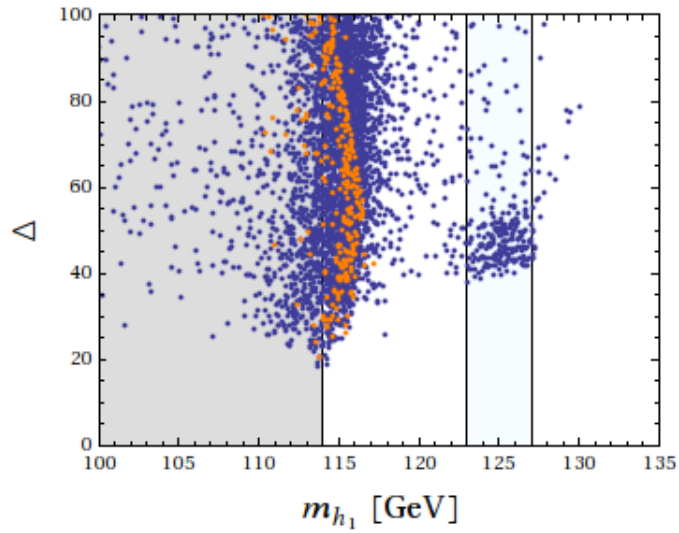
- CMSSM
- CGNMSSM
- CNMSSM  
(Higgs not universal)



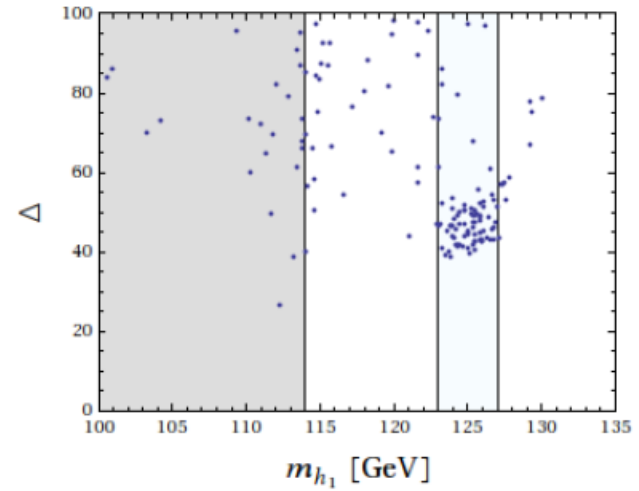
LHC constraints  
applied

LHC + DM constraints  
applied

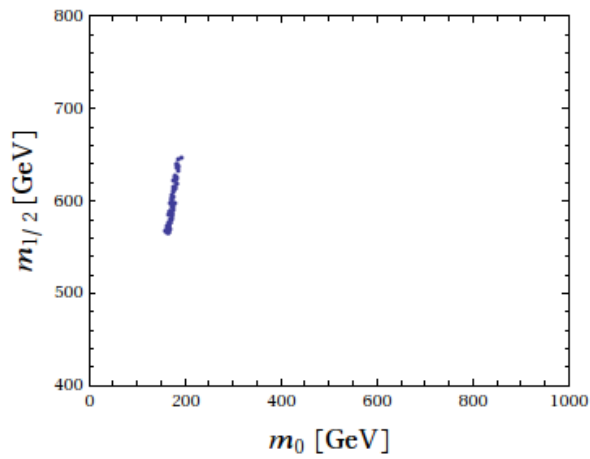
# Dark Matter structure



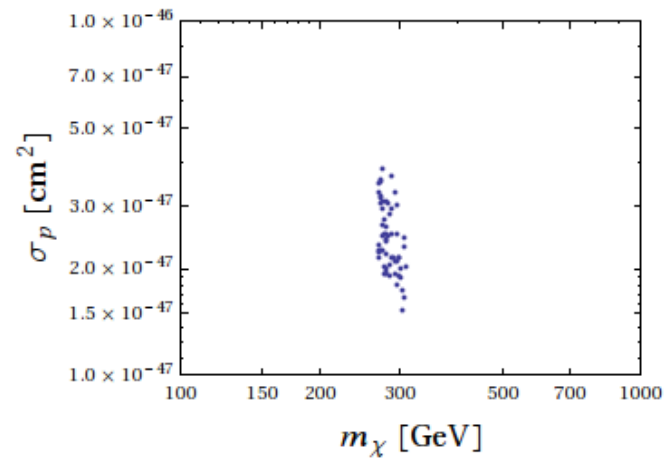
$$\rho_{LSP} \leq \rho_{DM}$$



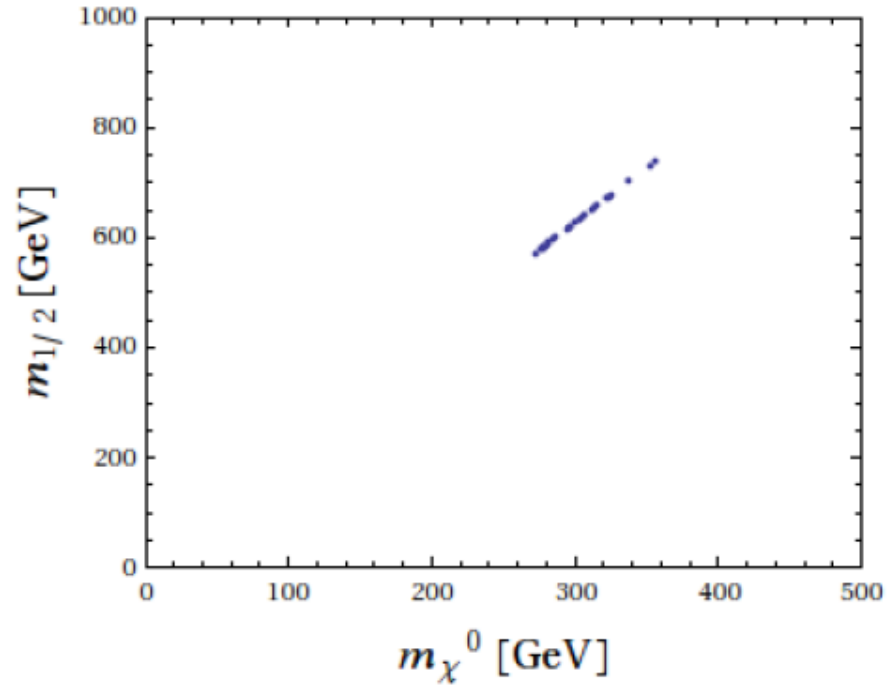
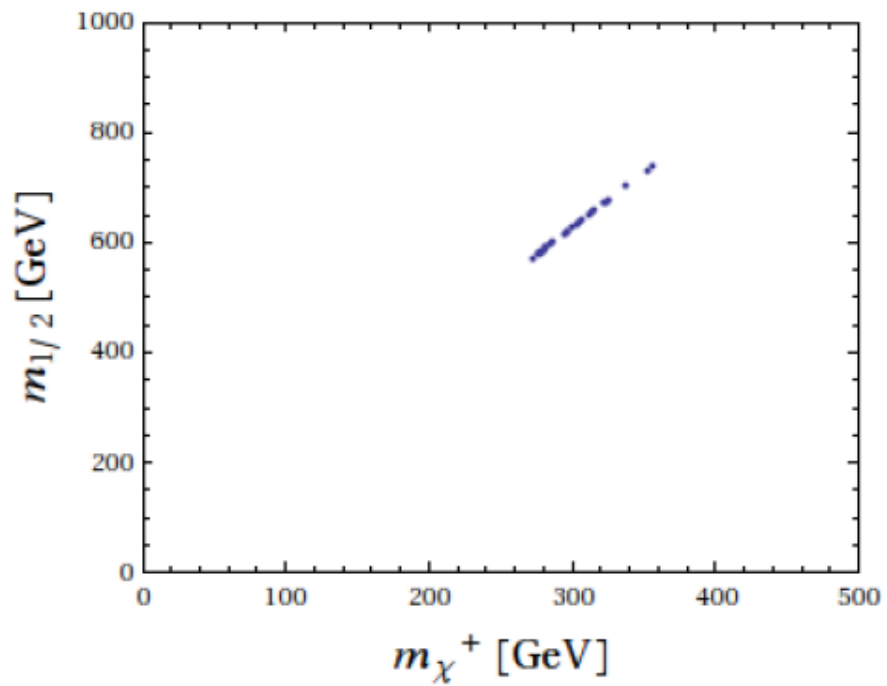
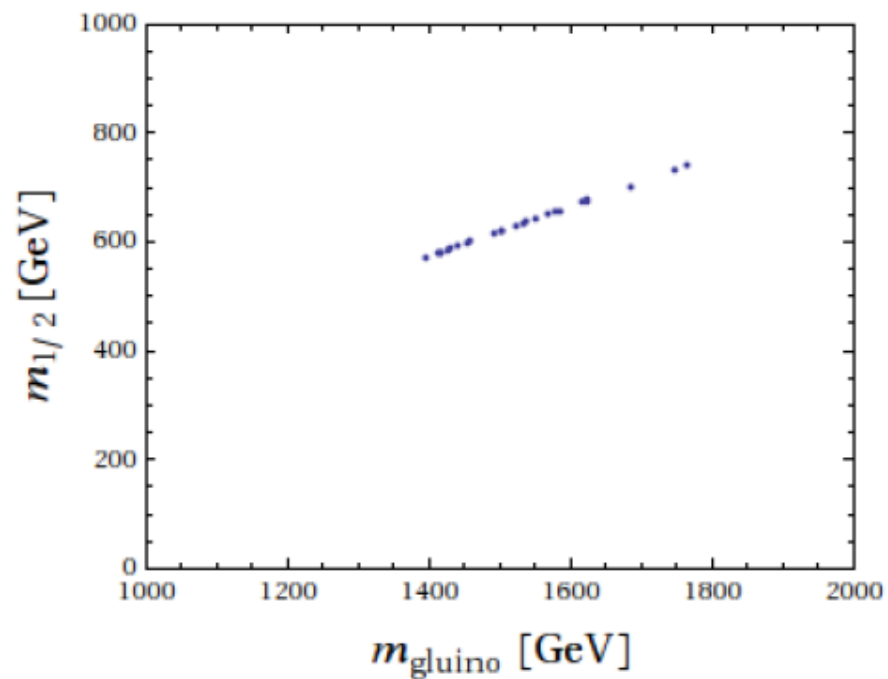
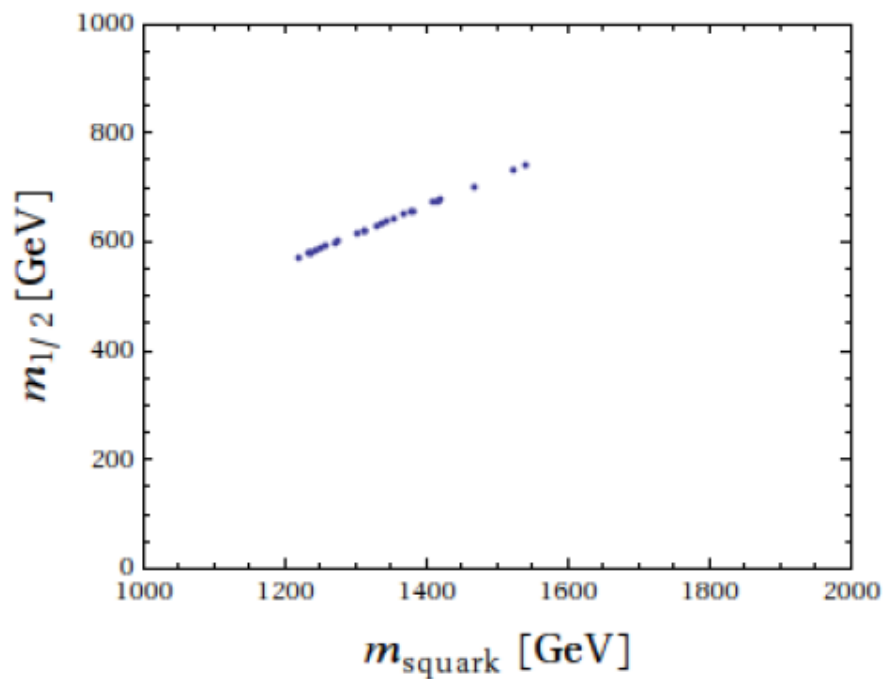
$$\rho_{LSP} \approx \rho_{DM}$$



Stau co-annihilation



DM searches insensitive



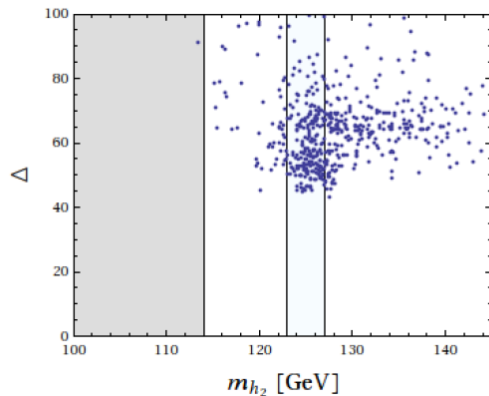
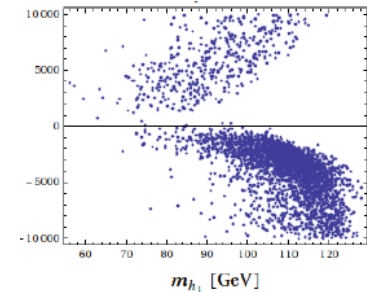


# GENERAL-NMSSM PHENOMENOLOGY

## Higgs structure $(h_u, h_d, s)$

- $\mu_s \gg \mu$  MSSM SUSY structure with heavy Higgs
- $\mu_s, m_s, b_s \sim \mu$   $h_1 \simeq H_{u,d} + \epsilon S, \quad h_2 = S - \epsilon H_{u,d}$

...  $h_2$  may be lighter than LEP bound



$m_{h_1} \text{ v/s } \Delta$  for the case  $m_{h_2} < m_{h_1}$

# Benchmark points

	BP1	BP2	BP3	BP4	BP5
$m_0$ [GeV]	746	163	957	573	752
$m_{1/2}$ [GeV]	476	568	557	482	472
$\tan \beta$	2.7	2.9	2.8	3.4	2.8
$A_0$ [GeV]	1433	1666	782	27	-198
$\lambda$	1.43	1.47	1.58	1.34	1.12
$\kappa$	-0.1	0.09	-0.005	1.52	1.03
$A_\lambda$ [GeV]	$A_0$	$A_0$	$A_0$	400	192
$A_\kappa$ [GeV]	$A_0$	$A_0$	$A_0$	-323	-326
$v_S$ [GeV]	-841	-190	-929	390	281
$\mu_S$ [GeV]	-5931	-5354	-5799	131	-37
$m_{h_d}^2$ [GeV <sup>2</sup> ]	$m_0^2$	$m_0^2$	$m_0^2$	$9.1 \cdot 10^5$	$5.4 \cdot 10^5$
$m_{h_u}^2$ [GeV <sup>2</sup> ]	$m_0^2$	$m_0^2$	$m_0^2$	$2.3 \cdot 10^6$	$2.4 \cdot 10^6$
$m_s^2$ [GeV <sup>2</sup> ]	$m_0^2$	$m_0^2$	$m_0^2$	$2.8 \cdot 10^6$	$1.7 \cdot 10^6$
$\mu$ [GeV]	-750	-1136	-934	-33	10
$b\mu$ [GeV <sup>2</sup> ]	$-2.4 \cdot 10^6$	$-1.2 \cdot 10^6$	$-2.3 \cdot 10^6$	147	26
$b_s$ [GeV <sup>2</sup> ]	$-1.9 \cdot 10^7$	$-5.4 \cdot 10^6$	$-1.4 \cdot 10^7$	326	144
$\xi_s$ [GeV <sup>3</sup> ]	$2.2 \cdot 10^9$	$1.5 \cdot 10^9$	$3.0 \cdot 10^9$	22	-8
$m_{\text{squark}}$ [GeV]	1256-1293	1207-1263	1507-1548	1211-1248	1280-1315
$m_{\tilde{g}}$ [GeV]	1219	1389	1416	1242	1235
$m_{h_1}$ [GeV]	124	123.5	125	93.5	78
$m_{h_2}$ [GeV]	1002	856	1257	125	124
$h_1$ singletfraction	$\mathcal{O}(10^{-4})$	$\mathcal{O}(10^{-6})$	$\mathcal{O}(10^{-4})$	0.8	0.85
$\text{Br}(h \rightarrow \gamma\gamma)$	$2.29 \cdot 10^{-3}$	$2.28 \cdot 10^{-3}$	$2.2 \cdot 10^{-3}$	$2.5 \cdot 10^{-3}$	$2.66 \cdot 10^{-3}$
$\text{Br}(b \rightarrow s\gamma)$	$3.1 \cdot 10^{-4}$	$3.1 \cdot 10^{-4}$	$3.1 \cdot 10^{-4}$	$3.1 \cdot 10^{-4}$	$3.3 \cdot 10^{-4}$
$\Delta a_\mu$	$-7.8 \cdot 10^{-11}$	$-2.5 \cdot 10^{-10}$	$-5.4 \cdot 10^{-11}$	$1.7 \cdot 10^{-10}$	$8 \cdot 10^{-11}$
$\delta\rho$	$6.2 \cdot 10^{-5}$	$6.6 \cdot 10^{-5}$	$7.5 \cdot 10^{-5}$	$1.9 \cdot 10^{-4}$	$3.1 \cdot 10^{-4}$
$m_{\tilde{\chi}_1^0}$ [GeV]	229	270	168	99	70
$\tilde{\chi}_1^0$ singlinofraction	$\mathcal{O}(10^{-5})$	$\mathcal{O}(10^{-5})$	$\mathcal{O}(10^{-5})$	0.1	0.2
$\Omega h^2$	7.5	0.10	7.4	0.017	0.11
$\sigma_p$ [cm <sup>2</sup> ]	$2.8 \cdot 10^{-47}$	$2.2 \cdot 10^{-47}$	$6 \cdot 10^{-47}$	$1.2 \cdot 10^{-44}$	$1.3 \cdot 10^{-45}$
$\Delta$ (Fine-tuning)	34.9	51.0	51.8	44.9	52.7



Table 1: Benchmark scenarios for the GNMSSM for the universal (BP1-BP3) and the general (BP4-BP5) case.  $m_{\text{squark}}$  shows the range of squark masses of the first two generations. For the last two points the second lightest Higgs is mostly MSSM-like.

# GENERAL-NMSSM PHENOMENOLOGY

## Higgs structure $(h_u, h_d, s)$

- $\mu_s \gg \mu$  MSSM SUSY structure with heavy Higgs

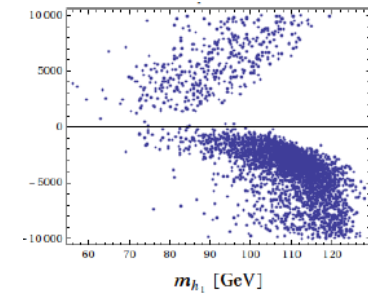
- $\mu_s, m_s, b_s \sim \mu$   $h_1 \simeq H_{u,d} + \epsilon S, \quad h_2 = S - \epsilon H_{u,d}$

...  $h_2$  may be lighter than LEP bound

$h_1 \rightarrow h_2 h_2$  large

...  $h_1$  may have enhanced  $\gamma\gamma$  rate (later)

... DM and SUSY phenomenology modified

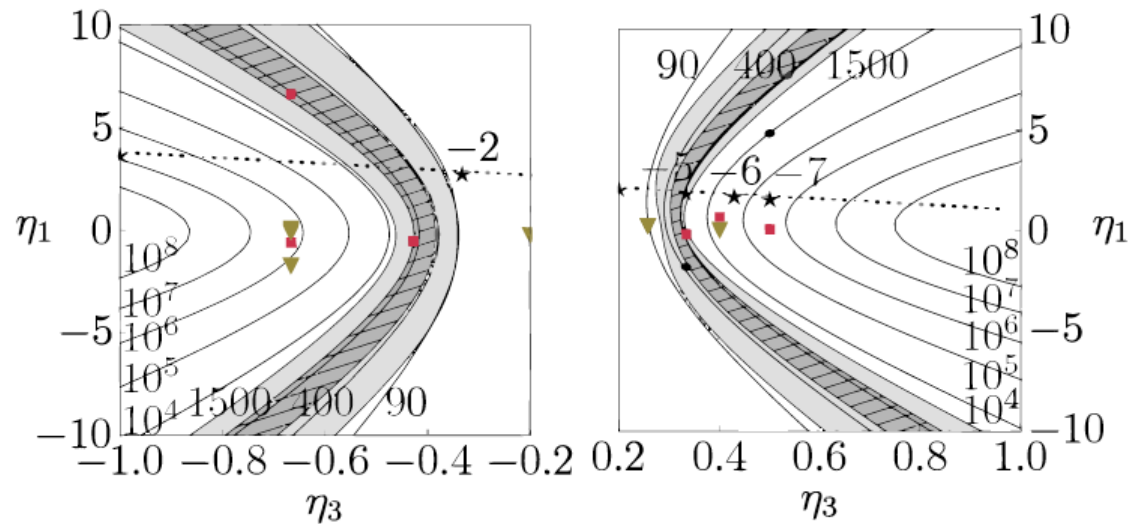


*II.* Reduced fine tuning : nonuniversal gaugino masses

# Reduced fine tuning: nonuniversal gaugino masses

$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3 \left( 2 |y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2 |a_t|^2 \right) - 6g_2^2 |M_2|^2 - \frac{6}{5} g_1^2 |M_1|^2$$

New focus point: cancellation between  $M_3$  and  $M_2$  contributions if  $|M_2|^2 \simeq |M_3|^2$  at  $M_{SUSY}$



$$M_3 : M_2 : M_1 = \eta_3 : 1 : \eta_1$$

# Reduced fine tuning: nonuniversal gaugino masses

$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3 \left( 2 |y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2 |a_t|^2 \right) - 6g_2^2 |M_2|^2 - \frac{6}{5} g_1^2 |M_1|^2$$

New focus point: cancellation between  $M_3$  and  $M_2$  contributions if  $|M_2|^2 \simeq |M_3|^2$  at  $M_{SUSY}$

Natural ratios? e.g.:

**GUT:**  $SU(5): \Phi^N \subset (24 \times 24)_{\text{symm}} = 1 + 24 + 75 + 200; \quad SO(10): (45 \times 45)_{\text{symm}} = 1 + 54 + 210 + 770$

	$\eta_3 : 1 : \eta_1$	$2.7\eta_3 : 1 : 0.5\eta_1$
Representation	$M_3 : M_2 : M_1$ at $M_{GUT}$	$M_3 : M_2 : M_1$ at $M_{EWSB}$
1	1:1:1	6:2:1
24	2:(-3):(-1)	12:(-6):(-1)
75	1:3:(-5)	6:6:(-5)
200	1:2:10	6:4:10

**String:**  $(3 + \delta_{GS}) : (-1 + \delta_{GS}) : \left( -\frac{33}{5} + \delta_{GS} \right)$  (OII, also mixed moduli anomaly)

# Phenomenology

- Gaugino mass ratios

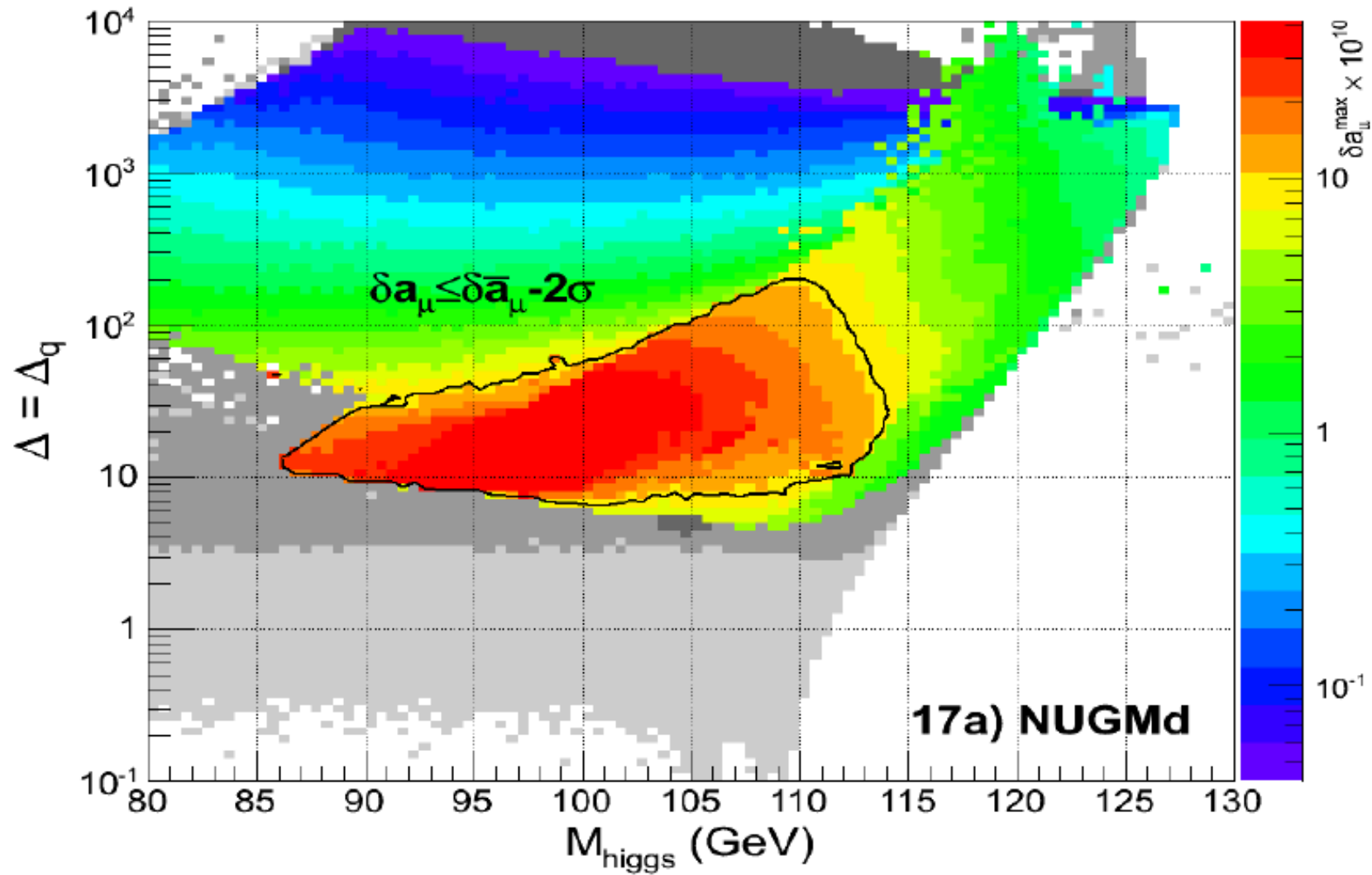
$$\frac{M_i(Q)}{M_{1/2}} = \eta_i \frac{\alpha_i(Q)}{\alpha_i(M_X)} \Rightarrow \begin{aligned} \frac{M_1(Q)}{M_2(Q)} &\approx 0.5\eta_1 \\ M_2(Q) &\approx 0.8M_{1/2} \\ \frac{M_3(Q)}{M_2(Q)} &\approx 2.7\eta_3 \end{aligned}$$

.... gauginos can be very heavy

- Light neutralino and 2 charginos nearly degenerate

$$\begin{aligned} m_{\chi_2^0} - m_{\chi_1^0} &= M_Z^2 \left( \frac{s_W^2}{M_1} + \frac{c_W^2}{M_2} \right) + \mathcal{O}\left(\frac{M_Z^3}{M_2^2}\right) \\ m_{\chi_1^\pm} - m_{\chi_1^0} &= \frac{1}{2}M_Z^2 \left( \frac{s_W^2}{M_1} + \frac{c_W^2}{M_2} \right) + \frac{1}{2}M_Z^2 \left( \frac{s_W^2}{M_1} - \frac{c_W^2}{M_2} \right) \epsilon \sin 2\beta + \mathcal{O}\left(\frac{M_Z^3}{M_2^2}\right) \end{aligned}$$

+ for  $|M_1| < \mu$ , Bino or Higgsino LSP candidate



2-loop fine tuning in 75 case

Ghilenca, Lee, Park



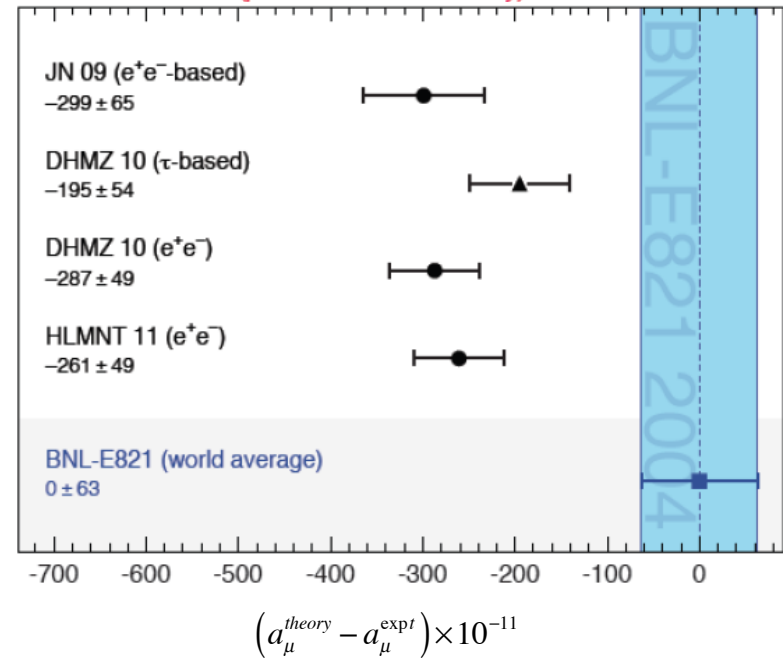
# Muon g-2

$$a_{\mu}^{theory} - a_{\mu}^{expt} = -(28.7 \pm 8.0) \times 10^{-10}$$

Theory error from hadronic contribution:

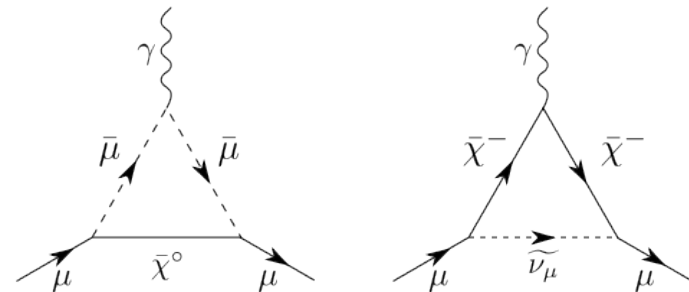
$$\delta a_{\mu}^{e^+e^-} = 3.6 \sigma$$

$$\delta a_{\mu}^{\tau} = 2.4 \sigma$$



## SUSY

$$\delta a_{\mu}^{SUSY} = -13 \times 10^{-10} \left( \frac{100 \text{ GeV}}{M_{SUSY}} \right)^2 \tan \beta$$



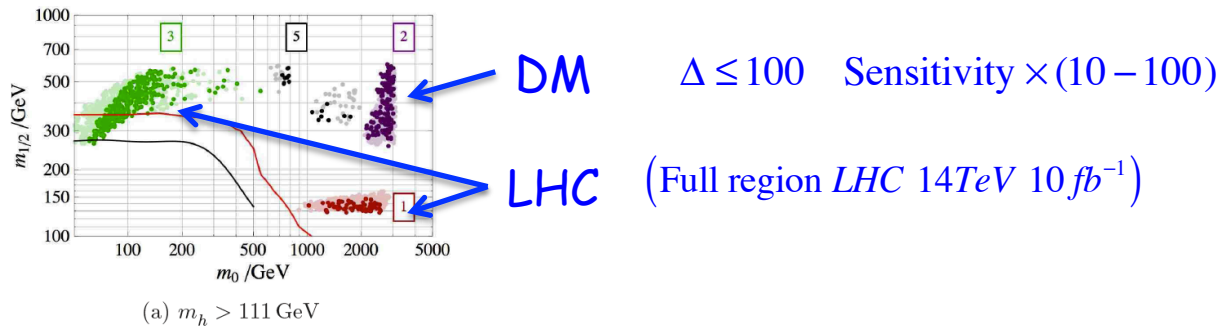
Needs light sleptons - anomaly/mirage spectrum?

# Summary (before Higgs discovery)

- Hierarchy problem  $\Rightarrow$  SUSY breaking structure and/or further states

- CMSSM  $m_i = M_0$   $Max[\Delta_{EW}, \Delta_{\Omega}] = 15(29)$ ,  $m_h = 114(116) \pm 2 GeV$

## Complementary DM & LHC searches



(Gauge mediation  $\Delta \gg 100$ )

- NMSSM Reduced  $\Delta \Rightarrow$  GNMSSM  $\Rightarrow Z_{4R}, Z_{8R}$

SUSY states can be (slightly) heavier  
 $m_h \rightarrow 130 GeV$

- Gaugino focus point  $M_i = \eta_i M_{1/2}$

Characteristic  $\eta_i$

Light  $\chi^{0,\pm}$

$\delta(b \rightarrow s\gamma)$  significant

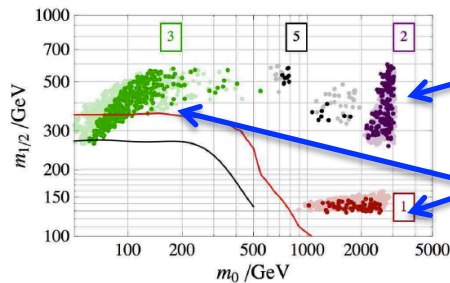
$\delta(g-2)$  Small(?)

# Summary (after Higgs discovery)

- Hierarchy problem  $\Rightarrow$  SUSY breaking structure and/or further states

- CMSSM  $m_i = M_0$   $Max[\Delta_{EW}, \Delta_{\Omega}] = 15(29)$ ,  $m_h = 114(116) \pm 2 GeV$

## Complementary DM & LHC searches



(a)  $m_h > 111 GeV$

DM  $\Delta \leq 100$  Sensitivity  $\times (10 - 100)$  (Now achieved!)

LHC (Full region  $LHC 14TeV 10 fb^{-1}$ )

$$\Delta_{MSSM} > 300 \text{ for } m_H = 126 GeV$$

- NMSSM Reduced  $\Delta \Rightarrow$  GNMSSM  $\Rightarrow Z_{4R}, Z_{8R}$

Further light/invisible Higgs a possibility



- Gaugino focus point

Mixed anomaly mediation, mirage mediation ...

Light sleptons...g-2!



- Natural SUSY, SPLIT SUSY...

