Thermal effects in Ising Cosmology



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Understanding the Early Universe: interplay of theory and collider experiments

Universe & Collider

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INTRODUCTION/MOTIVATION

• OBSERVERS AND THERMAL PROPAGATORS

• COSMOLOGICAL OBSERVABLES FROM THERMAL EFFECTS

• COSMOLOGICAL OBSERVABLES FROM dS/CFT

• CONCLUSIONS

CONTENTS

• Inflation:

• The anisotropies leave their imprints on CMB

INTRO

1) An elegant explanation for the homogeneity and isotropy of the Universe

2) A causal mechanism to generate the inhomogeneities

• Precise measurements of CMB's anisotropies and spectral index provide a test-playground for inflation

Planck Collaboration, Y. Akrami et al., Astron. Astrophys. 641 (2020)



• Inflation works very well for a slowly rolling scalar field with

• Our proposal

Free massive scalar field and its thermal evolution under the dS/CFT correspondence

• The FLRW metric

$$ds^2 = a^2 \left(d\tau^2 - d\mathbf{x}^2 \right)$$

INTRO

 $\dot{\phi}^2 < V(\phi) \qquad \qquad n_{\rm s} \simeq (1 - 4\epsilon_{\rm H} + 2\delta_{\rm H})$

corresponds to de Sitter for $\alpha(\tau) = -\frac{1}{H\tau}$

• QFT in dS space:

Conformally flat metric with a time-like

$$ds^2 = a^2 \left(d\tau^2 - d\mathbf{x}^2 \right)$$

 $|in\rangle$ vacuum (observer) defined at τ

out vacuum (observer) defined at the

• The $\tau = 0$ surface is also called the Horizon of the expanding Poincare patch of dS space

A BIT OF TERMINOLOGY

ike coordinate
$$\tau \in (-\infty, 0]$$

and $\alpha(\tau) = -\frac{1}{H\tau}$

$$= -\infty \qquad \langle J | \Phi^{I} = \langle I | \Phi^{J} \qquad Bogolyubov$$

$$I, J = \text{in, out}$$

$$I, J = \text{in, out}$$

THERMAL PROPAGATORS

• The action to be quantized under thermal effects

$$\mathcal{S} = \int d^4x \,\sqrt{-g} \left[\frac{1}{2} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - \frac{1}{2} (m^2 + \xi \mathcal{R}) \phi^2 \right]$$

• Consider a d + 1 dimensional FLRW spacetime

$$ds^2 = a^2 \left(d\tau^2 - d\mathbf{x}^2 \right)$$

• Klein-Gordon equation for the mode $\phi_{\mathbf{k}} = \frac{\chi_{\mathbf{k}}}{1}$ α



THERMAL PROPAGATORS

• The solution is a combination of the Hankel functions $H^{1,2}_{\nu_{cl}}(\tau, |\mathbf{k}|)$ with weight

 $u_{\rm cl} = \frac{a}{2}$

• Quantization includes time-dependent vacua and a doubled Hilbert space

• Time-dependent vacua

in vacuum is empty for the "in" observer (Bunch-Davies vacuum)

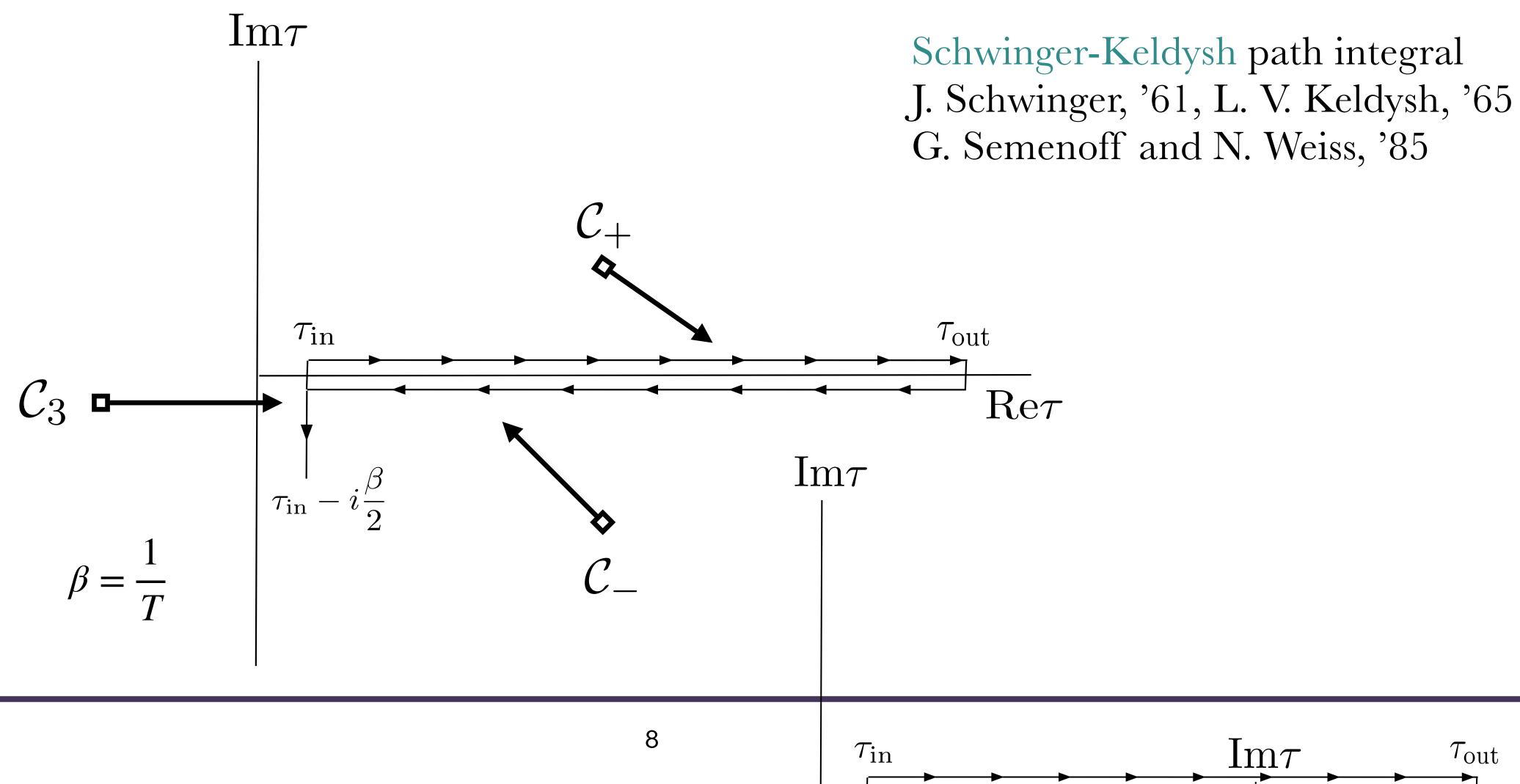
out vacuum is empty for the "out" observer

$$\frac{d}{d}\sqrt{1-\frac{4M^2}{d^2}}$$

N. A. Chernikov and E. A. Tagirov, '68 B. Allen, Phys. Rev. D32 (1985) 3136



Doubled Hilbert space



THERMAL PROPAGATORS

• The T = 0 ($C_3 = 0$) "in-in" field propagator

$$\mathcal{D} = \begin{bmatrix} \langle 0 | \mathcal{T}[\Phi^{+}(\tau_{1})\Phi^{+}(\tau_{2})] | 0 \rangle = \mathcal{D}_{++}(\tau_{1};\tau_{2}) & \langle 0 | \Phi^{-}(\tau_{1})\Phi^{+}(\tau_{2}) | 0 \rangle = \mathcal{D}_{+-}(\tau_{1};\tau_{2}) \\ \hline \langle 0 | \Phi^{+}(\tau_{2})\Phi^{-}(\tau_{1}) | 0 \rangle = \mathcal{D}_{-+}(\tau_{1};\tau_{2}) & \langle 0 | \mathcal{T}^{*}[\Phi^{-}(\tau_{1})\Phi^{-}(\tau_{2})] | 0 \rangle = \mathcal{D}_{--}(\tau_{1};\tau_{2}) \\ \hline \mathcal{D}_{-+}(\tau_{1};\tau_{2}) = \chi_{|\mathbf{k}|}(\tau_{1})\chi_{|\mathbf{k}|}^{*}(\tau_{2}) \\ \hline \mathcal{D}_{+-}(\tau_{1};\tau_{2}) = \mathcal{D}_{-+}^{*}(\tau_{1};\tau_{2}), \mathcal{D}_{--}(\tau_{1};\tau_{2}) = \mathcal{D}_{++}^{*}(\tau_{1};\tau_{2}) \\ \hline \mathcal{D}_{++}(\tau_{1};\tau_{2}) = \theta(\tau_{1}-\tau_{2})\mathcal{D}_{-+}(\tau_{1};\tau_{2}) + \theta(\tau_{2}-\tau_{1})\mathcal{D}_{+-}(\tau_{1};\tau_{2}) \\ \text{ie is hit} \text{ propagator} \\ \hline \mathcal{D}_{++} = \frac{i}{k^{2}-m^{2}+i\varepsilon} \end{bmatrix}$$

$$\begin{aligned}
\mathcal{T}[\Phi^{+}(\tau_{1})\Phi^{+}(\tau_{2})]|0\rangle &= \mathcal{D}_{++}(\tau_{1};\tau_{2}) &\langle 0| \Phi^{-}(\tau_{1})\Phi^{+}(\tau_{2})|0\rangle &= \mathcal{D}_{+-}(\tau_{1};\tau_{2}) \\
\Phi^{+}(\tau_{2})\Phi^{-}(\tau_{1})|0\rangle &= \mathcal{D}_{-+}(\tau_{1};\tau_{2}) &\langle 0| \mathcal{T}^{*}[\Phi^{-}(\tau_{1})\Phi^{-}(\tau_{2})]|0\rangle &= \mathcal{D}_{--}(\tau_{1};\tau_{2}) \\
\mathcal{D}_{-+}(\tau_{1};\tau_{2}) &= \chi_{|\mathbf{k}|}(\tau_{1})\chi_{|\mathbf{k}|}^{*}(\tau_{2}) \\
\mathcal{D}_{+-}(\tau_{1};\tau_{2}) &= \mathcal{D}_{-+}^{*}(\tau_{1};\tau_{2}), \mathcal{D}_{--}(\tau_{1};\tau_{2}) &= \mathcal{D}_{++}^{*}(\tau_{1};\tau_{2}) \\
\mathcal{D}_{++}(\tau_{1};\tau_{2}) &= \theta(\tau_{1}-\tau_{2})\mathcal{D}_{-+}(\tau_{1};\tau_{2}) + \theta(\tau_{2}-\tau_{1})\mathcal{D}_{+-}(\tau_{1};\tau_{2}) \\
\text{mit propagator} \\
\mathcal{D}_{++} &= \frac{i}{12}\frac{i}{\pi^{2}+i\pi^{2}}
\end{aligned}$$

• Th

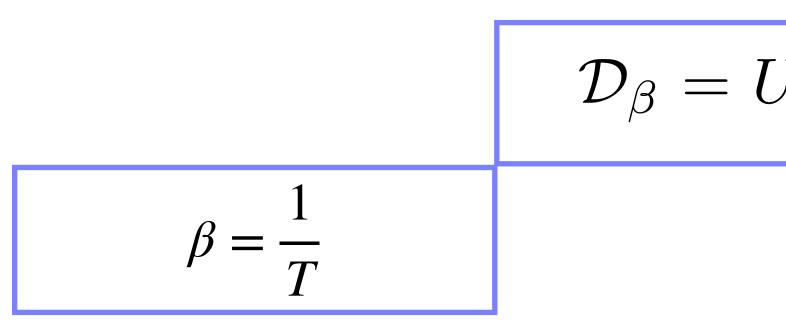
THERMAL PROPAGATORS

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• Concrete $T \neq 0$ ($C_3 \neq 0$) "out-out" field propagator should respect the KMS condition



$$\cosh \theta_{|\mathbf{k}|} = \frac{1}{\sqrt{1 - e^{-\beta \omega_{|\mathbf{k}|}}}} \quad and \quad \sinh \theta_{|\mathbf{k}|} = \sqrt{\cosh^2 \theta_{|\mathbf{k}|} - 1}$$

THERMAL PROPAGATORS

• Proof that Schwinger-Keldysh \equiv Thermofield dynamics for time-dependent Hamiltonian via "in-in"

$$U_{\beta} \mathcal{D} U_{\beta}^{T}$$
$$U_{\beta} = \begin{pmatrix} \cosh \theta_{|\mathbf{k}|} & \sinh \theta_{|\mathbf{k}|} \\ \sinh \theta_{|\mathbf{k}|} & \cosh \theta_{|\mathbf{k}|} \end{pmatrix}$$

A Bogolyubov Transformation (BT) with coefficients

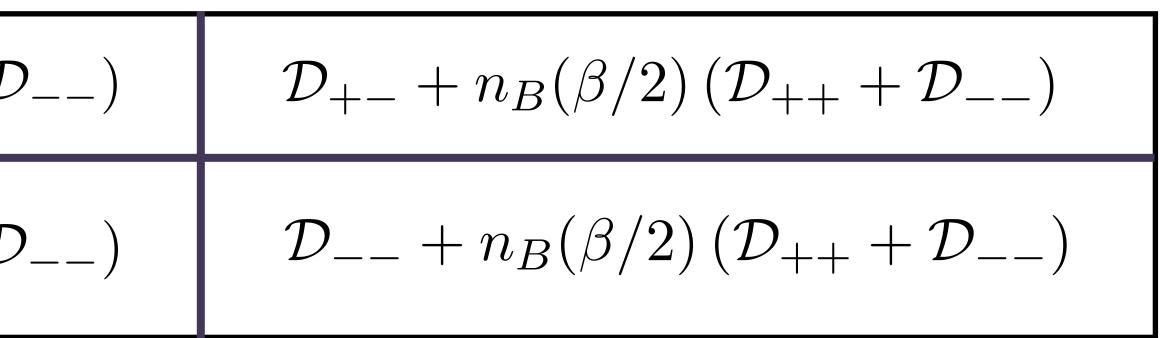
• The $T \neq 0$ ($C_3 \neq 0$) "out-out" field propagator

$$\mathcal{D}_{\beta/2} = \frac{\mathcal{D}_{++} + n_B(\beta/2) \left(\mathcal{D}_{++} + \mathcal{D}_{++}\right)}{\mathcal{D}_{-+} + n_B(\beta/2) \left(\mathcal{D}_{++} + \mathcal{D}_{++}\right)}$$

• the Bose-Einstein distribution parameter

 n_B

THERMAL PROPAGATORS



$$(\beta) = \frac{e^{-\beta\omega_{|\mathbf{k}|}}}{1 - e^{-\beta\omega_{|\mathbf{k}|}}}$$

- All the allowed thermal transformations of \mathcal{D} are correlators of the form $\mathcal{D}^{I}_{J,\alpha} = \langle J; \alpha |$
- In Thermofield dynamics language $(\Phi^I)^T = (\Phi^I)^T =$
- Exact dS space can only si $\frac{1}{\beta} = T = T_{A}$ • The thermal dS-scalar propagator admits a compact form

$$\mathcal{D}_{\beta} = \mathcal{D} + \left(\mathcal{D}_{++} + \mathcal{D}_{++}^*\right) \left(s^2 + sc\right)$$

THERMAL PROPAGATORS

$$|\mathcal{T}[\Phi^{I}(\Phi^{I})^{T}]|J;\alpha\rangle$$

$$(\Phi^{+,I}\Phi^{-,I}) \text{ with } I,J = \text{ in, out. } \alpha \text{ is a thermal index}$$

$$utain the G-H temperature$$

$$h_{S} = \frac{H}{2\pi} = \frac{1}{\delta}$$

$$\begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} \qquad \qquad s \equiv \sinh \theta_{|\mathbf{k}|} \\ c \equiv \cosh \theta_{|\mathbf{k}|}$$

• The thermal power spectrum for $\tau_1 = \tau_2$, $H|\tau| = 1$ and $|\mathbf{k}\tau| \leq 1$

$$\mathcal{P}_{S,\beta} \mathbf{1} = \mathcal{D}_{\beta} \mathbf{1}|_{\tau_1 = \tau_2} \qquad \kappa \equiv \omega_{|\mathbf{k}|} |\tau| \Big|_{|\mathbf{k}\tau|=1} = \sqrt{\frac{5 - d^2}{4} + M^2}$$
$$\mathcal{D}_{\beta} = \mathcal{D} + \left(\mathcal{D}_{++} + \mathcal{D}_{++}^*\right) \left(s^2 + sc\right) \begin{pmatrix} 1 & 1\\ 1 & 1 \end{pmatrix}$$

• Defines the observables n_S , n'_S , n''_S and f_{NL}

• The picture
$$\mathcal{D} \longrightarrow \mathcal{D}_{\beta} \longrightarrow |in >$$



• Time-independent BT $|in > \longrightarrow |out, \beta_{T_{dS}} > \longrightarrow Exact a$

P. R. Anderson, C. Molina-Paris and En Mottola, Phys. Rev. D 72 (2005) 0435 P. R. Anderson and E. Mottola, Phys. Rev 89 (2014) 104038

• Time-dependent BT $|in > \longrightarrow |out, \beta > \beta_{T_{dS}} > \longrightarrow Broken$

de Sitter
$$\longrightarrow d = 3, M^2 = 0 \rightarrow \kappa = i$$

mil
515
w. D
 $P_S(\tau) = \left(\frac{H}{2\pi}\right)^2 \left(1 + |\mathbf{k}\tau|\right) \Rightarrow P_S(0) = \left(\frac{H}{2\pi}\right)^2$
scale invariant spectrum

$$\kappa \to \Lambda = \kappa \left(1 + 2 \frac{e^{-2x\kappa}}{1 - e^{-2x\kappa}} \right) = \kappa \coth(x\kappa)$$



•
$$x = \frac{\pi H}{2\pi T}$$
, for $x \in [\pi, \infty)$. When $x = \pi$, admits its

• The transformed state has reduced isometry than Bunch-Davies

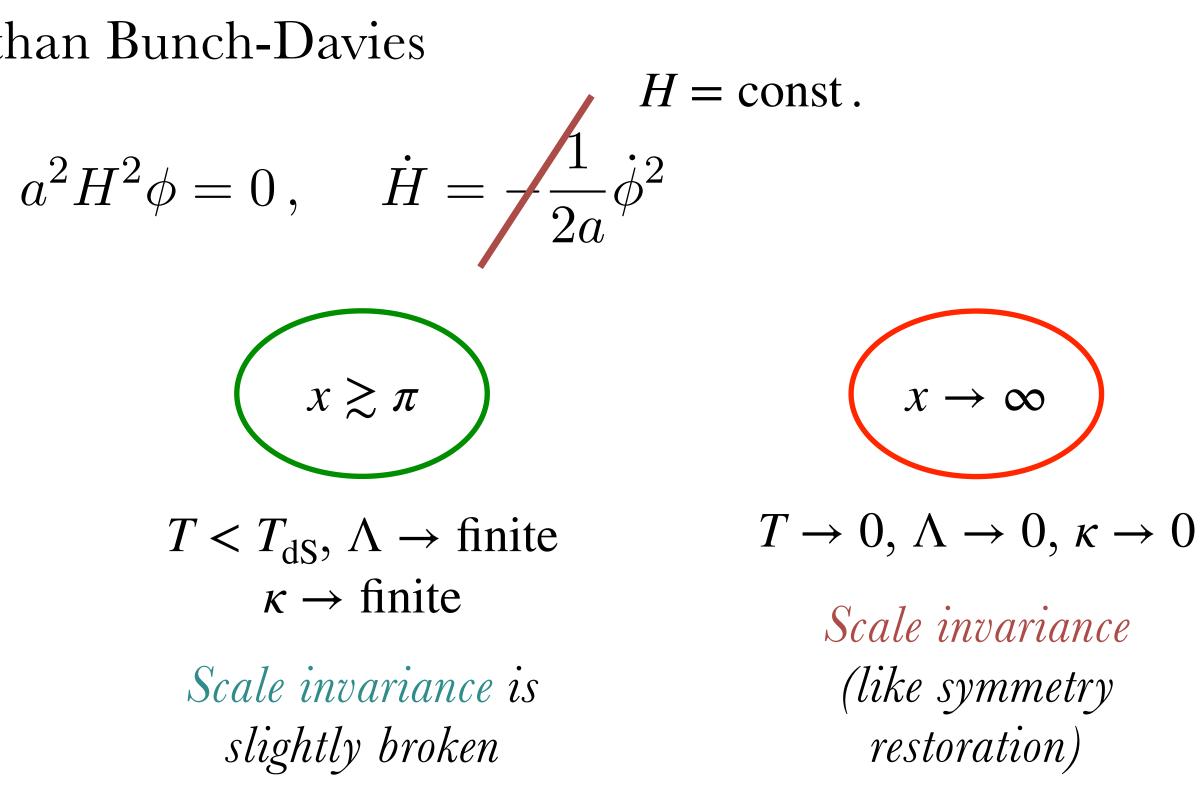
$$\ddot{\phi} + 2H\dot{\phi} + \left(\mu_H^2 + \xi \frac{\mathcal{R}}{H^2}\right) d\theta$$

• The limiting cases

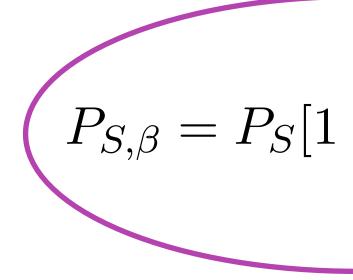
$$x = \pi$$

 $T = T_{\rm dS}, \Lambda \to \infty, \kappa \to i$

Scale invariance (like symmetry restoration) natural dS value where $T = T_{dS}$



• The spectral index of scalar curvature fluctuations, n_S , is shifted due to finite temperature effects



• All the freedom is included in Λ which admits its natural value when $x \approx \pi$

$$n_{S,\beta} = 1 + \frac{d \ln \left(|\mathbf{k}|^3 P_{S,\beta} \right)}{d \ln |\mathbf{k}|}$$

$$1 + 2(s^2 + sc)]$$

$$\delta n_S \equiv n_{S,\beta} - 1 = -\frac{2x}{\Lambda} \left[\frac{e^{-x\Lambda}}{1 - e^{-2x\Lambda}} \right]$$

• The shift is extended to other observables

$$n_{S,\beta}^{(1)} = \delta n_S \left[2 - \frac{1}{\Lambda^2} - \frac{x}{\Lambda} \left(1 + \frac{2e^{-2x\Lambda}}{1 - e^{-2x\Lambda}} \right) \right]$$

$$n_{S,\beta}^{(1)} = \frac{dn_{S,\beta}}{d\ln|\mathbf{k}|}, \quad n_{S,\beta}^{(2)} = \frac{dn_{S,\beta}^{(1)}}{d\ln|\mathbf{k}|} \qquad f_{NL} = \frac{5}{6} \frac{N_{\rho\rho}}{N_{\rho}^{2}}$$

$$n_{S,\beta}^{(2)} = \frac{\left(\frac{n_{S,\beta}}{N_{S,\beta}}\right)^{2}}{\delta n_{S}} + \delta n_{S} \left[-\frac{2}{\Lambda^{2}} + \frac{2}{\Lambda^{4}} - \frac{x}{\Lambda} \left(2 - \frac{1}{\Lambda^{2}}\right) \left(1 + \frac{2e^{-2x\Lambda}}{1 - e^{-2x\Lambda}}\right) + \frac{4x^{2}}{\Lambda^{2}} \frac{e^{-2x\Lambda}}{(1 - e^{-2x\Lambda})^{2}} \right]$$

$$N_{\rho} = \frac{\partial N}{\partial \rho}, \quad N_{\rho\rho} = \frac{\partial^{2}N}{\partial \rho^{2}} \text{ and } \rho \equiv P_{S,\beta}$$

$$f_{NL} = -\frac{5\left[x(-1+\Lambda^2)^2\left(1+x\Lambda\cot\left(\frac{x\Lambda}{A}\right)\right)+2\Lambda^3\sin\left(\frac{x\Lambda}{A}\right)\right]}{6\Lambda^2\left[x(-1+\Lambda^2)+\Lambda\sinh(x\Lambda)\right]}$$

M. Zaldarriaga, JCAP 10 (2004) 006 A. Riotto, Nucl. Phys. B868 (2013)577-595

• The physical case $\Lambda \rightarrow 1.5117$, $x \rightarrow \pi$

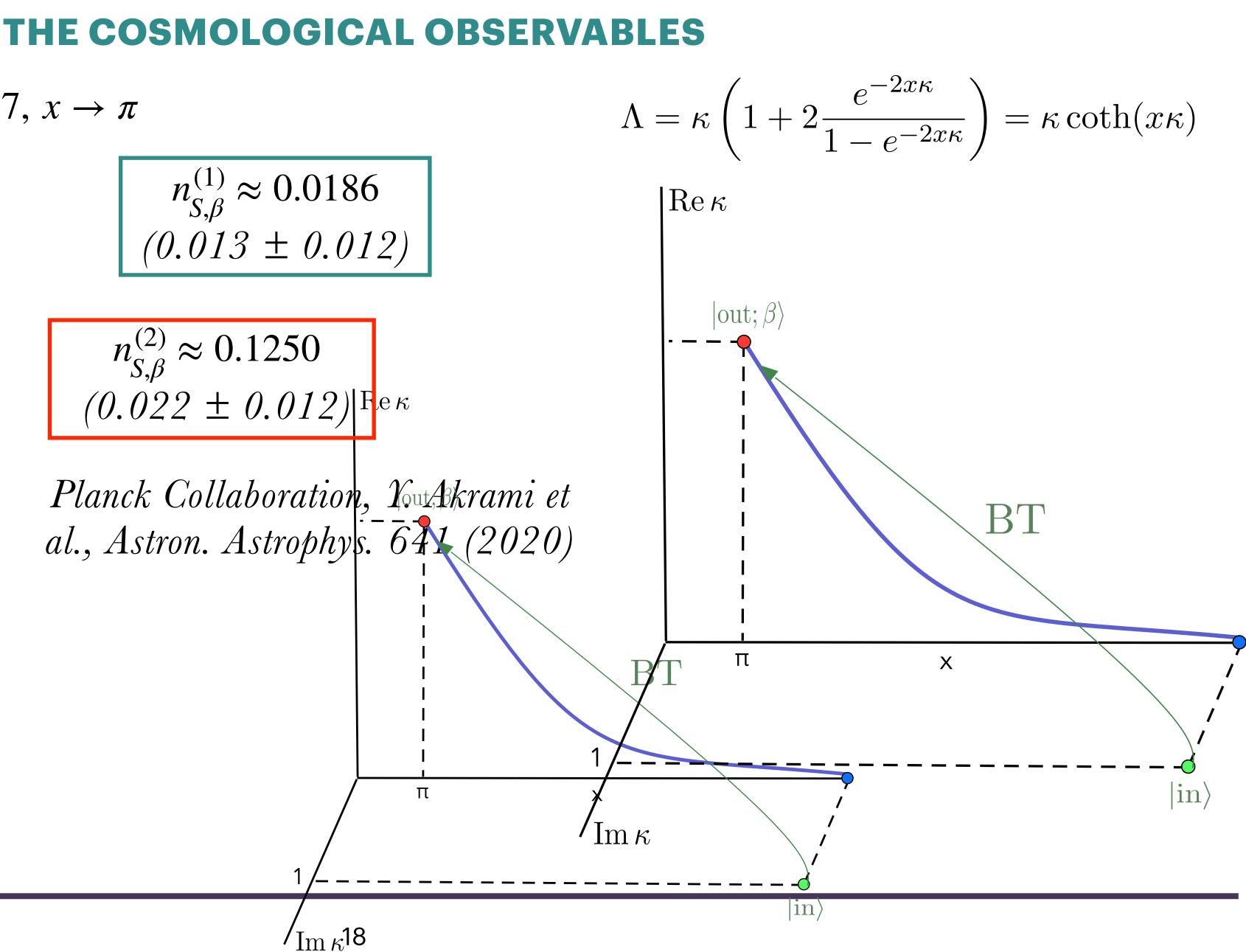
 $n_{S,\beta} \equiv n_S \approx 1 - 0.036 = 0.964$ (0.9649 ± 0.0042)

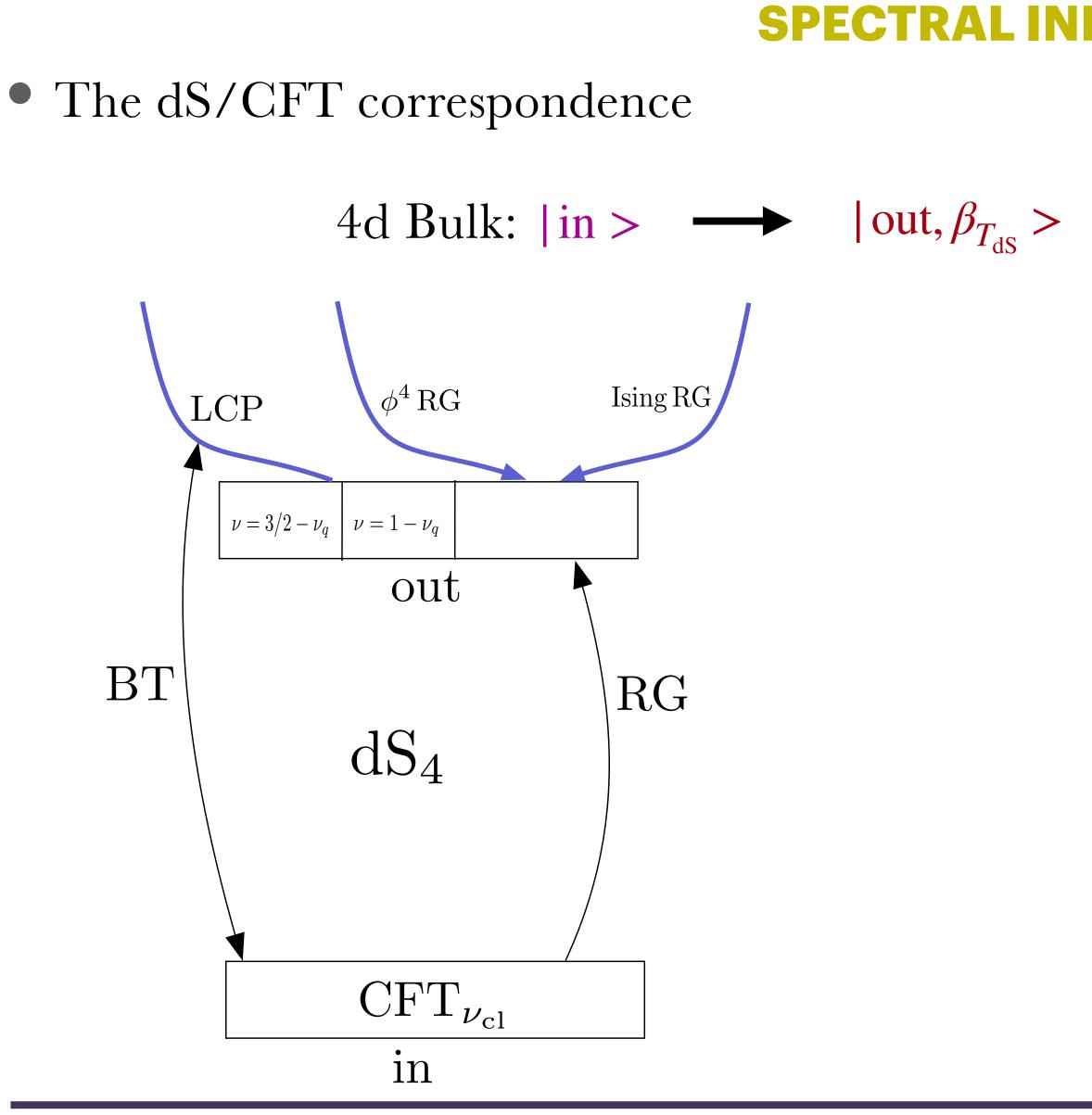
 $f_{NL} \approx -1.7138$? (-0.9 ± 5.1)

Λ	x
$\rightarrow 0$	$ ightarrow\infty$
10^{-6}	$3.5 \cdot 10^{7}$
0.01	1600
0.5	14.8
$\rightarrow 1.5117$	$\rightarrow \pi$

 $n_{S,\beta}^{(1)} pprox 0.0186$ (0.013 ± 0.012)

 $n_{S,\beta}^{(2)} \approx 0.1250$ (0.022 ± 0.012) |Fek

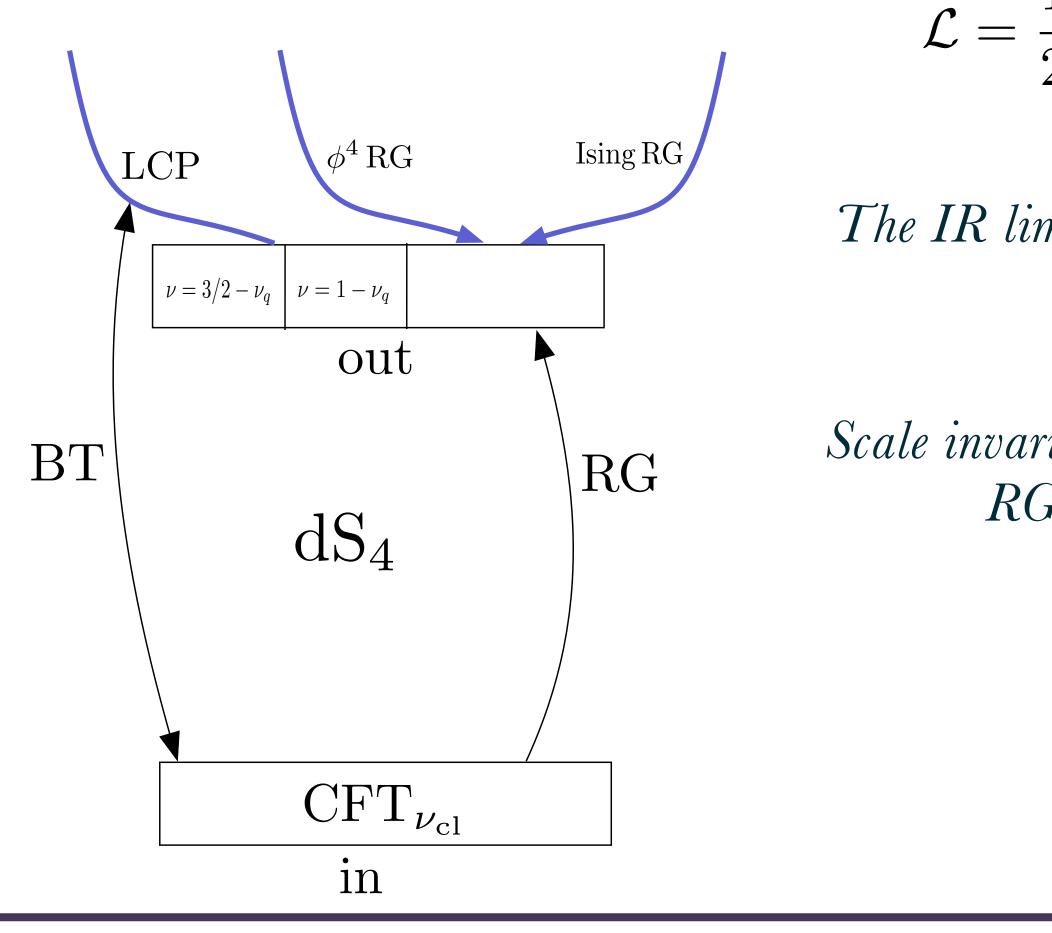




→ 3d Boundary: UV to IR RG flow

M. Bianchi, D.Z. Freedman and K. Skenderis Nucl. Phys. B 631 (2002) 159 I. Antoniadis, P. O. Mazur and E. Mottola, JCAP 09 (2012) 024

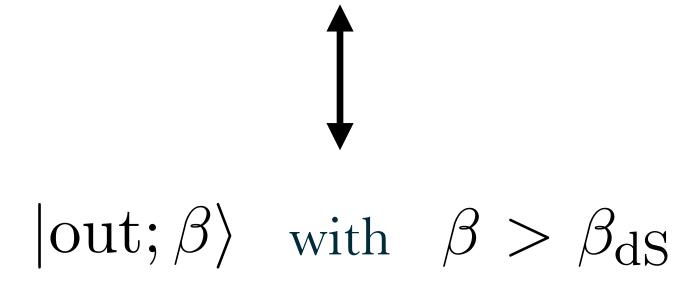
• The d = 3 scalar theory of the Ising field σ



 $\mathcal{L} = \frac{1}{2} \partial_i \sigma \partial_i \sigma - \lambda \sigma^4$

The IR limit is a exact 3d CFT as long as the BT preserves the SO(4) isometry.

Scale invariance is broken via the Coleman-Weinberg mechanism. RG brings us in the vicinity of the IR fixed point



• In the dS/CFT correspondence: bulk field ϕ (Δ_{-}) dual to a boundary operator \mathcal{O} (Δ_{+})

$$\Delta_{-} = \frac{d}{2} - \nu$$

 (Δ_{-}, Δ)

Bulk and boundary propagators are related by

$$\langle \phi_{|\mathbf{k}|} \phi_{-|\mathbf{k}|} \rangle \sim \frac{1}{\langle \mathcal{O}_{|\mathbf{k}|} \mathcal{O}_{-|\mathbf{k}|} \rangle}$$

$$\Delta_+ = \frac{d}{2} + \nu$$

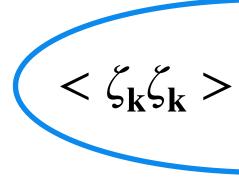
$$\Delta_+)_{\rm cl} = (0,3)$$

J. Maldacena, J. High Energy Phys. 05 (2003) 013 J. M. Maldacena and G. L. Pimentel, *JHEP 09 (2011) 045*

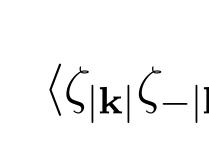




• There is a gauge of the metric where $\zeta_{\mathbf{k}} = z(\tau)\phi_{\mathbf{k}}$



• Then bulk and boundary propagator connection reforms to



SPECTRAL INDEX AND dS/CFT $<\zeta_{\bf k}\zeta_{\bf k}>\sim <\phi_{\bf k}\phi_{\bf k}>$

J. Maldacena, J. High Energy Phys. 05 (2003) 013 J. M. Maldacena and G. L. Pimentel, *JHEP 09 (2011) 045*

$$_{\mathbf{k}|}\rangle\sim\frac{1}{\langle\mathcal{O}_{|\mathbf{k}|}\mathcal{O}_{-|\mathbf{k}|}\rangle}$$



• The spectral index in holography

$$n_{S} - 1 = \frac{d}{d \ln |\mathbf{k}|} \left[\ln \left(|\mathbf{k}|^{3} P_{S,\beta} \right) \right] = \frac{d}{d \ln |\mathbf{k}|} \ln \left(|\mathbf{k}|^{3} \langle \zeta_{|\mathbf{k}|} \zeta_{-|\mathbf{k}|} \rangle \right)$$
$$= 3 - \frac{1}{\langle \mathcal{O}_{|\mathbf{k}|} \mathcal{O}_{-|\mathbf{k}|} \rangle} \left(\frac{d}{d \ln |\mathbf{k}|} \langle \mathcal{O}_{|\mathbf{k}|} \mathcal{O}_{-|\mathbf{k}|} \rangle \right)$$

• The Callan-Symanzik

$$\left(\frac{\partial}{\partial \ln |\mathbf{k}|} - \beta_{\lambda} \frac{\partial}{\partial \lambda} + (3 - 2\Delta_{\mathcal{O}})\right) \langle \mathcal{O}_{|\mathbf{k}|} \mathcal{O}_{-|\mathbf{k}|} \rangle = 0 \qquad \Delta_{\mathcal{O}}$$

$$n_{S} = 1 - 2\Gamma_{\mathcal{O}} - \beta_{\lambda} \frac{\partial}{\partial \lambda} \ln \langle \mathcal{O}_{|\mathbf{k}|} \mathcal{O}_{-|\mathbf{k}|} \rangle$$

$$\Delta_{\mathcal{O}} = \Delta_{+} = [\Delta_{\mathcal{O}}] + \Gamma_{\mathcal{O}} \text{ and } \beta_{\lambda} \equiv \mu \frac{\partial \lambda}{\partial \mu}$$

F. Larsen and R. McNees, JHEP 07 (2003) 051 J. P. van der Schaar, JHEP 01 (2004) 070

SPECTRAL INDEX AND dS/CFT $\gamma_{\sigma} \equiv \frac{1}{2} \mu \frac{\partial}{\partial \mu} \ln Z_{\sigma}$ 1 ZO $\Gamma_{\mathcal{O}} = -\gamma_{\mathcal{O}} + 2\gamma_{\sigma}$

• The anomalous dimension

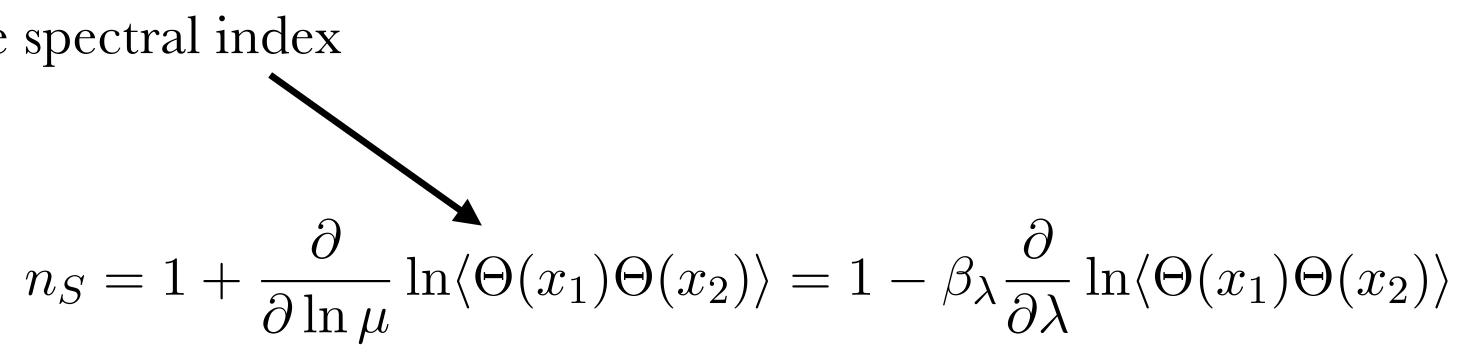
$$\gamma_{\mathcal{O}} \equiv \mu \frac{\partial}{\partial \mu} \ln$$

• For $\mathcal{O} = \sigma^4$ ($\Delta_{\sigma^4} = 3$) no shift to the spectral index

$$n_S = 1 - 2\Gamma_{\sigma^4} = 1 - 2\frac{\partial\beta_\lambda}{\partial\lambda}$$

• For us $\mathcal{O} = \Theta \equiv \delta^{ij} T_{ij}$ ($\Delta_{\Theta} = 3$) and the spectral index a conserved current $\Gamma_{\Theta} = 0$

F. Larsen and R. McNees, JHEP 07 (2003) 051 .7. P. van der Schaar, JHEP 01 (2004) 070



• Vanishing of the anomalous dimension of Θ

• Non-trivial vanishing for $\Gamma_{\Theta} = 0 \rightarrow \gamma_{\Theta} = 2\gamma_{\sigma}$

• Near the IR Wilson-Fisher fixed point $2\gamma_{\sigma} = \eta$ the Ising field critical exponent

K. G. Wilson, Phys. Rev. 179, 1499 S. E. Derkachov, J.A. Gracey, A.N. Manashov, Eur. Phys. J. C2 569-579 C. Coriano, L. Delle Rose and K. Skenderis, Eur. Phys. J. C 81 2, 174 *J. Henriksson, ArXiv: 2201.09520*

A sunset-like diagram with $\sigma \Box \sigma$ insertion cancels the usual sunset

• Rewrite the Callan- Symanzik equation for Θ

$$\left[\left(\frac{\partial}{\partial \ln \mu} + \eta\right) + \left(\beta_{\lambda}\frac{\partial}{\partial \lambda} - \eta\right)\right] \langle \Theta(x_1)\Theta(x_2)\rangle \simeq 0$$

• Very close to the IR Wilson-Fisher fixed point

$$\left(\beta_{\lambda}\frac{\partial}{\partial\lambda}-\eta\right)\langle\Theta(x_1)\Theta(x_2)\rangle\simeq 0$$

• The c_{Θ} -coupling satisfies the scaling equation

$$\equiv -\beta_{\lambda}\mu^{\varepsilon}\sigma^{4} \text{ and } \Gamma_{\Theta} = \eta - \eta$$

t
$$\beta_{\lambda}^2 < < \frac{\partial \beta_{\lambda}}{\partial \lambda}$$

$$\beta_{\lambda}\partial_{\lambda}c_{\Theta} = \eta c_{\Theta}$$

Meaningful only outside the IR fixed point

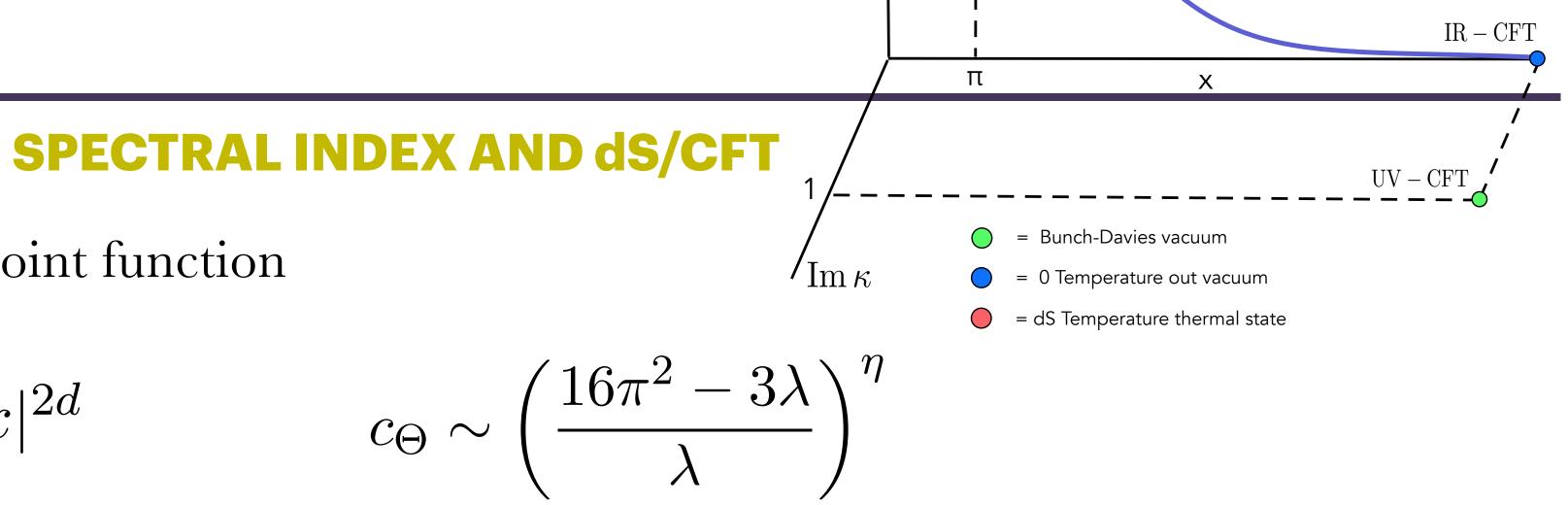
• The approximate conformal 2-point function

$$\langle \Theta \Theta \rangle = c_{\Theta} / |x|^{2d}$$

• The critical exponent η non-perturbative admits the numerical value $\eta \approx 0.036$ (MC simulation)

$$n_S \simeq 1 - \eta$$

• So $\Lambda \approx 1.5117$ is indeed fixed independently (without connection to the inflationary characteristics)



<
$$n_S \simeq 1 - 0.036 = 0.964$$

• Z_{σ} cannot be decoupled justifying the existence of the eigenvalue equation

- The justification from boundary arguments Renormalized Θ comes from $\Theta \equiv -\beta_{\lambda}\mu^{\varepsilon}\sigma^{4}$ $Z_{\Theta} = 1$
- From bulk arguments

Connect bulk and boundary $\longrightarrow \mu = aH$ and $\lambda = \phi$ w/o forgetting Z_{σ}





CONCLUSIONS

- on the nearly zero temperature |out > vacuum, which is connected to an interacting IR CFT, in the universality class of the 3d Ising model.
- parameter of the breaking of the scale invariant spectrum of curvature fluctuations
- η fixes the parametric freedom in the dS scalar theory, yielding the prediction $n_{S,\beta} \approx 0.964$, up to errors associated with its lattice Monte Carlo measurements.
- Heating up the system $T = T_{dS}$ numerically in a controlled way we evaluated additional cosmological current experimental bounds while $n_{S,\beta}^{(2)}$ exceeds them

• We considered a thermal scalar in de Sitter background. Starting from the Bunch-Davies |in > vacuum, a Bogolyubov Transformation placed us somewhere in the interior of the finite temperature phase diagram.

• The low temperature limit is considered in such a way that instead of returning to the BD vacuum, we landed

• This interacting CFT is rather special, in the sense that the boundary operator that couples to the scalar curvature perturbations in the bulk has a classical scaling dimension. The critical exponent η is the order

observables $n_{S,\beta}^{(1)}$, f_{NL} and $n_{S,\beta}^{(2)}$. We finally note that our predicted values of $n_{S,\beta}$, $n_{S,\beta}^{(1)}$ and f_{NL} are well within



THANK YOU