The Higgs portal and an inflaton

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Focus points:

- direct renormalizable inflaton couplings
- preheating , reheating
- non-thermal dark matter production
- collective effects (resonances, rescattering,...)
- inflaton = dark matter ?

Based on

2105.05860 (Lebedev, Yoon) 2107.06292 (Lebedev, Smirnov, Solomko, Yoon) + **review** 2104.03342

Framework

General statement :

The only renormalizable coupling of the inflaton to the SM is

$$V_{\phi h} = \frac{1}{2} \lambda_{\phi h} \phi^2 H^{\dagger} H + \sigma_{\phi h} \phi H^{\dagger} H$$

On general grounds, expected to drive reheating

Scalar dark matter s :

$$V_{\phi s} = \frac{1}{4} \lambda_{\phi s} \phi^2 s^2 + \frac{1}{2} \sigma_{\phi s} \phi s^2$$

Simplified cases:

(a)
$$V_{\phi s} = \frac{\lambda_{\phi s}}{4} \phi^2 s^2$$
, $V_{\phi h} = \frac{\sigma_{\phi h}}{2} \phi h^2$,
(b) $V_{\phi s} = \frac{\sigma_{\phi s}}{2} \phi s^2$, $V_{\phi h} = \frac{\sigma_{\phi h}}{2} \phi h^2$,
(c) $V_{\phi s} = \frac{\sigma_{\phi s}}{2} \phi s^2$, $V_{\phi h} = \frac{\lambda_{\phi h}}{4} \phi^2 h^2$.

Inflaton potential <u>after</u> inflation :

$$V_{\phi} = rac{m_{\phi}^2}{2} \phi^2$$
 or $V_{\phi} = rac{1}{4} \lambda_{\phi} \phi^4$

Main challenge:

complicated collective effects

(often invalidate perturbative description)

Reheating + DM production in ϕ^2



Equation of motion for the s-Fourier modes X_k (Mathieu eq.) :

$$X_k'' + \left(A_k + 2q\cos 4z\right)X_k = 0$$

$$q \equiv \frac{\lambda_{\phi s} \Phi^2}{2m_{\phi}^2} \qquad \qquad A_k \equiv \frac{4k^2}{m_{\phi}^2 a^2} + 2q$$





- the inflaton background gets destroyed by DM rescattering
- the system becomes relativistic (w \sim 1/3)
- it reaches quasi—equilibrium during preheating



$$H_R \simeq \Gamma_{\phi \to hh} , \quad \Gamma_{\phi \to hh} = \frac{\sigma_{\phi h}^2}{8\pi m_{\phi}}$$

no initial condition dependence)

Correct relic DM abundance:



"Strong coupling" (still very weak):

Schematically:



Reheating + DM production in ϕ^4

Inflaton EOM :

$$\ddot{\phi} + 3H\dot{\phi} + \lambda_{\phi}\phi^3 = 0 \qquad \implies \qquad \phi(t) = \frac{\Phi_0}{a(t)}\operatorname{cn}\left(x, \frac{1}{\sqrt{2}}\right), \quad x \equiv (48\lambda_{\phi})^{1/4}\sqrt{t}$$

DM momentum mode EOM (Lame eq.) :

$$X_k'' + \left(\kappa^2 + \frac{\lambda_{\phi s}}{2\lambda_{\phi}} \operatorname{cn}\left(x, \frac{1}{\sqrt{2}}\right)\right) X_k = 0, \quad \kappa^2 \equiv \frac{k^2}{\lambda_{\phi} \Phi_0^2}$$

Inflaton fluctuation EOM (Lame eq. with q=3):

$$\varphi_k'' + \left[\kappa^2 + 3 \operatorname{cn}^2\left(x, \frac{1}{\sqrt{2}}\right)\right] \varphi_k = 0$$
 New feature !

Stability chart:



Resonant DM production at tiny couplings

as long as

$$\lambda_{\phi h}\gtrsim\lambda_{\phi}$$

Correct relic DM abundance:



Quasi—equilibrium sets in at

$$\lambda_{\phi h} \gtrsim \lambda_{\phi}$$

$$Y \simeq 0.4 \, \frac{\Gamma_{\phi \to hh}^{1/2}}{m_{\phi}}$$

(no coupling dependence, no initial condition dependence)

Inflaton = DM ?

Minimal model :

$$\mathcal{L}_{J} = \sqrt{-\hat{g}} \left(-\frac{1}{2} \Omega \hat{R} + \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi + (D_{\mu} H)^{\dagger} D^{\mu} H - V(\phi, H) \right)$$
$$\Omega = 1 + \xi_{h} h^{2} + \xi_{\phi} \phi^{2}$$
$$V(\phi, h) = \frac{1}{4} \lambda_{h} h^{4} + \frac{1}{4} \lambda_{\phi h} h^{2} \phi^{2} + \frac{1}{4} \lambda_{\phi} \phi^{4} + \frac{1}{2} m_{h}^{2} h^{2} + \frac{1}{2} m_{\phi}^{2} \phi^{2}$$

canonically normalized inflaton

Inflation :





Preheating :

$$V_E = \frac{1}{4} \lambda_{\phi h} h^2 \phi^2 + \frac{1}{4} \lambda_{\phi} \phi^4$$

Excellent fit!

Results:

(1) non—thermal: too much DM

ed efficient SM production
$$\rightarrow$$

$$\lambda_{\phi h} \gtrsim \lambda_{\phi}$$

no resonant Higgs production I
inflaton fluctuation production

 $\varphi_k'' + \left[\kappa^2 + 3\operatorname{cn}^2\left(x, \frac{1}{\sqrt{2}}\right)\right] \varphi_k = 0$

resonant Higgs production

quasi--equilibrium

 $X_k'' + \left(\kappa^2 + \frac{\lambda_{\phi s}}{2\lambda_{\phi}} \operatorname{cn}\left(x, \frac{1}{\sqrt{2}}\right)\right) X_k = 0$



suppressed SM matter production









(2) thermal: **possible**

"singlet scalar DM" freeze--out $\lambda_{\phi h}(1\,{
m TeV})\gtrsim 0.25$



large loop correction to inflaton potential (loss of unitarity)

Exception:

Higgs resonance

 $m_{\phi} \simeq m_{h_0}/2$ $\lambda_{\phi h} \gtrsim 10^{-4}$



thermal inflaton DM

(in a very narrow mass range)

CONCLUSION

- collective effects are essential
- quasi-equilibrium in the inflaton-DM system
- breakdown of perturbative approach
- minimal inflaton DM model: thermal DM, tuned inflaton mass