

# Can kinetic Sunyaev-Zel'dovich effect be used to detect the interaction between DE and DM?

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# Outline:

- The interaction model between DE&DM
- The ISW effect as a probe of the interaction
- Probing the interaction with peculiar velocities
- The kinetic Sunyaev–Zel’dovich effect as a new

# *Known? Unknown!*

5%

95%

知之為知之，

5%

Present your understanding  
when you understand;

不知為不知，

95%

recognize your not understanding  
when you don't understand;

是知也。

that's the true meaning of  
understanding.

— 論語為政篇

— By Confucius

(Analects of Confucius)

# 95% Unknown: 25% DM+70% DE

## DE- $\Lambda$ ?

1. QFT value 123 orders larger than the observed
2. Coincidence problem:

Why the universe is accelerating just now?

In Einstein GR: Why are the densities of DM and DE of precisely the same order today?

$\Lambda$  is not the end story to account for the cosmic acceleration

Reason for proposing Quintessence, tachyon field, Chaplygin gas models etc.

No clear winner in sight

Suffer fine-tuning

• Why do we need the interaction between DE&DM?  
 A phenomenological generalization of the LCDM model is

$$\frac{\rho_M}{\rho_X} = r_0 \left( \frac{a_0}{a} \right)^\beta$$

LCDM

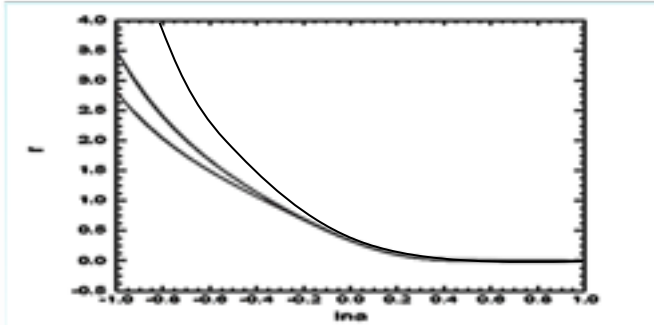
$$\begin{aligned} \beta &= 3 \\ \beta &= 0 \\ \beta &< 3 \end{aligned}$$

LCDM model,

Stationary ratio of energy densities

Coincidence problem less severe than

The period when energy densities of DE and DM are comparable is longer



The coincidence problem is less acute

$$\beta < 3$$

can be achieved by a suitable interaction between DE & DM

$$\dot{\rho}_M + 3H\rho_M = Q, \quad \dot{\rho}_X + 3H(1 + w_X)\rho_X = -Q.$$

# Do we need to live with Phantom?

- Degeneracy in the data.

SNe alone however are consistent with  $w$  in the range, roughly

$$-1.5 \leq w_{\text{eff}} \leq -0.7$$

WMAP:  $w = -1.06^{+0.13, -0.08}$

$w < -1$  from data is strong!

- One can try to model  $w < -1$  with scalar fields like quintessence. But that requires **GHOSTS**: fields with negative kinetic energy, and so with a Hamiltonian not bounded from below:

$$3 M_4^2 H^2 = - (\phi')^2 / 2 + V(\phi)$$

‘Phantom field’, Caldwell, 2002

- **Phantoms a** **Theoretical prejudice against  $w < -1$  is strong!**

# MAYBE NOT!!

- ***Conspiracies are more convincing if they DO NOT rely on supernatural elements!***

Ghostless explanations:

1) Modified gravity affects **EVERYTHING**, with the effect to make  $w < -1$ .

S. Yin, B. Wang, E. Abdalla, C.Y.Lin, arXiv:0708.0992, PRD (2007)

A. Sheykhi, B. Wang, N. Riazi, Phys. Rev. D 75 (2007) 123513

R.G. Cai, Y.G. Gong, B. Wang, JCAP 0603 (2006) 006

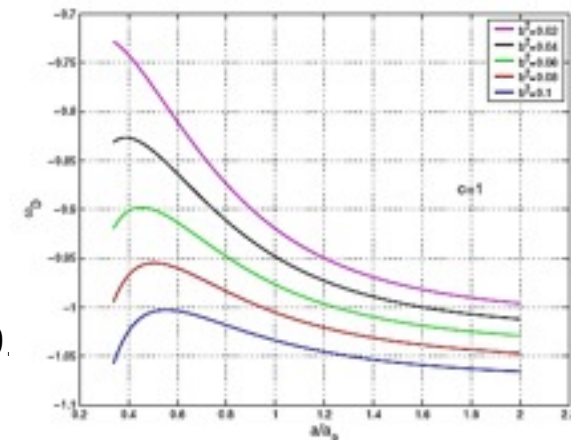
2) Another option: Interaction between DE and DM

**Super-acceleration ( $w < -1$ ) as signature of dark sector interaction**

B. Wang, Y.G.Gong and E. Abdalla, Phys.Lett.B624(2005)141

B. Wang, C.Y.Lin and E. Abdalla, Phys.Lett.B637(2006)357.

S. Das, P. S. Corasaniti and J. Khoury, Phys.Rev. D73 (2006) 083509.



# Interaction



70% DE



25% DM



# Interaction



70% DE



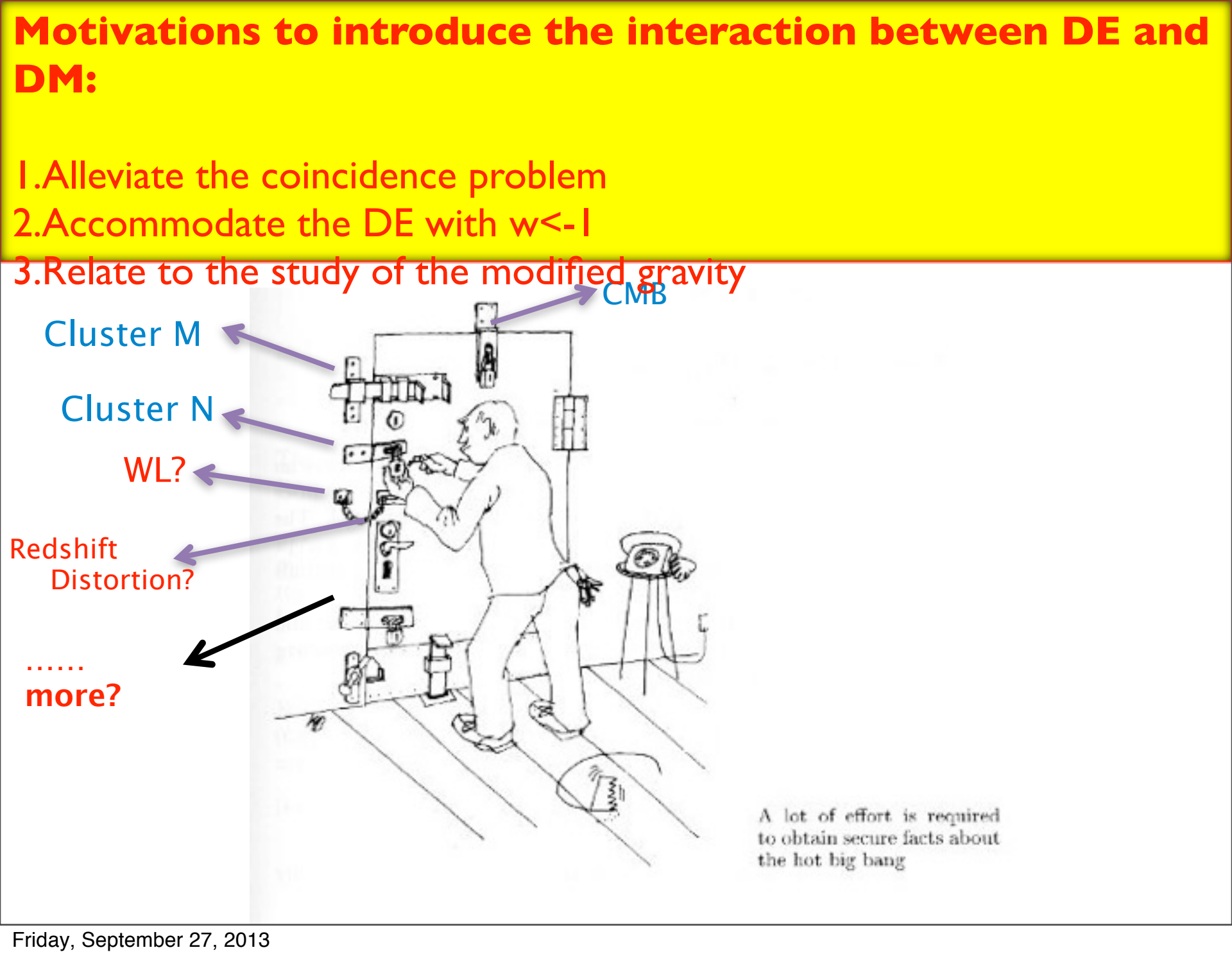
25% DM



# Motivations to introduce the interaction between DE and DM:

1. Alleviate the coincidence problem
2. Accommodate the DE with  $w < -1$
3. Relate to the study of the modified gravity





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Cluster M

Cluster N

WL?

Redshift Distortion?

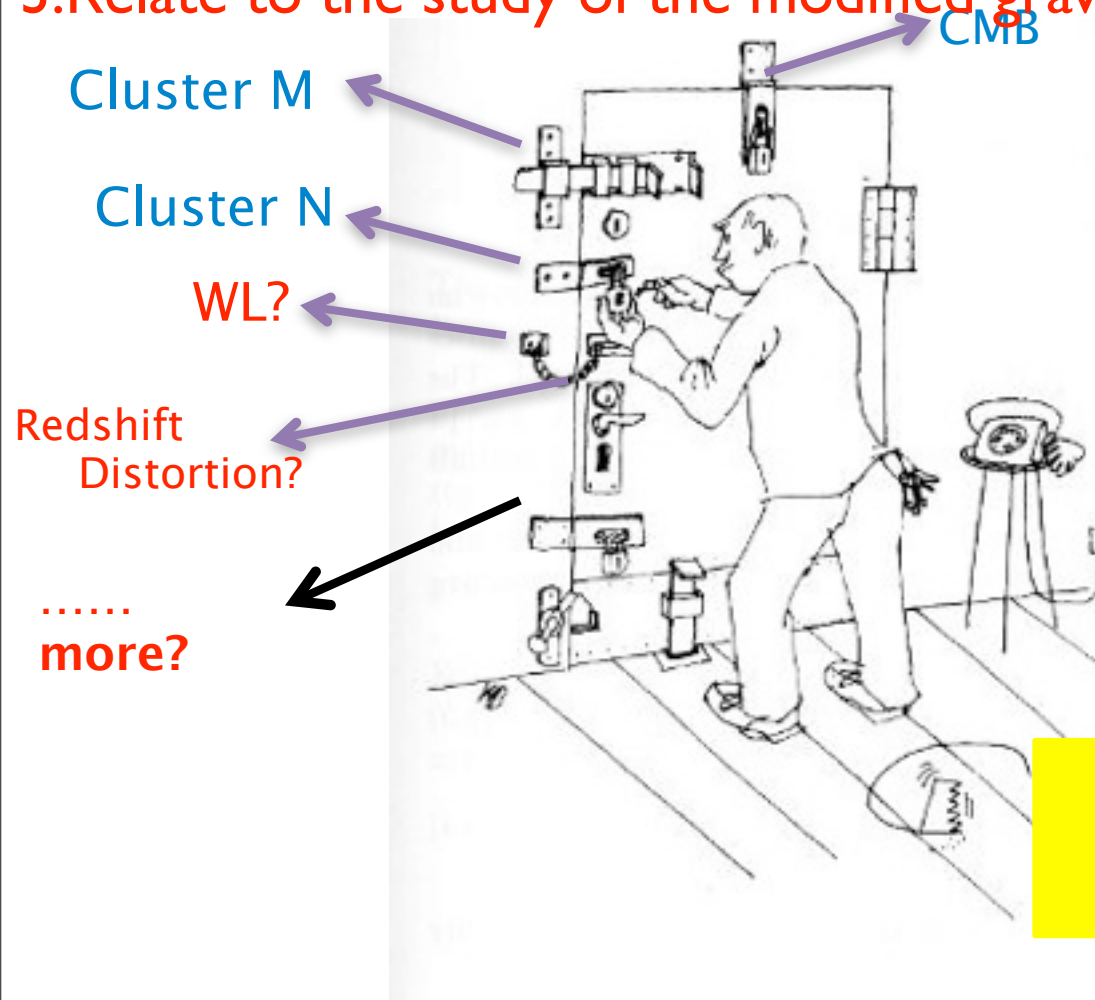
.....  
more?

CMB

A lot of effort is required to obtain secure facts about the hot big bang

# Motivations to introduce the interaction between DE and DM:

1. Alleviate the coincidence problem
2. Accommodate the DE with  $w < -1$
3. Relate to the study of the modified gravity



# The interaction model between DE & DM

## Phenomenological interaction forms:

$$\dot{\rho}_M + 3H\rho_M = Q, \quad \dot{\rho}_X + 3H(1 + w_X)\rho_X = -Q.$$

For  $Q > 0$  the energy proceeds from DE to DM

## Phenomenological forms of Q

$$(1) Q = \delta H(\rho_{DM} + \rho_{DE}), (2) Q = \delta H\rho_{DM} \text{ and } (3) Q = \delta H\rho_{DE}$$

# Perturbation theory when DE&DM are in interaction

Choose the perturbed spacetime

$$ds^2 = a^2 \left\{ - (1 + 2\phi) d\tau^2 + 2\partial_i B d\tau dx^i + \left[ (1 - 2\psi)\delta_{ij} + 2\partial_i \partial_j E \right] dx^i dx^j \right\}.$$

DE and DM, each with energy-momentum tensor  $T_{(\lambda)\mu}^{\mu\nu} = Q_{(\lambda)}^{\nu}$   
 $Q_{(\lambda)}^{\nu}$  denotes the interaction between different components.

The perturbed energy-momentum tensor reads

$$\delta T^{00} = \frac{1}{a^2} (\delta\rho - 2\psi\rho)$$

$$\delta T^{i0} = \frac{1}{a^2} [(p + \rho)V^i + p\partial^i B]$$

$$\delta T^{ij} = \frac{1}{a^2} [\delta p \delta^{ij} - p(2\phi\delta^{ij} + D^{ij} E)]$$

$$\delta T^{0i} = \delta T^{i0}$$

# Perturbation Theory

The perturbed Einstein equations

$$\delta g_{\mu}^{\nu} \longrightarrow \delta R_{\mu}^{\nu} \longrightarrow \delta G_{\mu}^{\nu}$$

$$\delta T_{\mu}^{\nu}$$

$$\nabla^2 \phi + 3\mathcal{H}(\mathcal{H}\psi - \phi') + \mathcal{H}\nabla^2 B - \frac{1}{6}[\nabla^2]^2 E = -4\pi G a^2 \delta\rho$$

$$\mathcal{H}\nabla^2 \psi - \nabla^2 \phi' + 2\mathcal{H}^2 \nabla^2 B - \frac{a''}{a} \nabla^2 B + \frac{1}{6}[\nabla^2]^2 E' = -4\pi G a^2 (\rho + p)\theta$$

$$-\partial^i \partial_j \psi - \partial^i \partial_j \phi + \frac{1}{2} \partial^i \partial_j E'' + \mathcal{H} \partial^i \partial_j E' + \frac{1}{6} \partial^i \partial_j \nabla^2 E - 2\mathcal{H} \partial^i \partial_j B - \partial^i \partial_j B' = 8\pi G a^2 \Pi_j^i$$

$$2\mathcal{H}\psi' + 4\frac{a''}{a}\psi - 2\mathcal{H}^2\psi + \frac{2}{3}\nabla^2\psi + \frac{2}{3}\nabla^2\phi - 4\mathcal{H}\phi' - 2\phi'' + \frac{4}{3}\mathcal{H}\nabla^2 B + \frac{2}{3}\nabla^2 B' - \frac{1}{9}[\nabla^2]^2 E = 8\pi G a^2 \delta p$$

The perturbed pressure of DE:

$$\delta p_d = C_e^2 \delta_d \rho_d + (C_e^2 - C_a^2) \left[ \frac{3\mathcal{H}(1+w)V_d \rho_d}{k} - a^2 Q_d^0 \frac{V_d}{k} \right]$$

$C_e^2$  is the sound speed in the rest frame,  $C_a^2$  is the adiabatic sound speed,



# Perturbation Theory

$$\delta \nabla_{\mu} T_{\nu}^{\mu} = \delta Q_{\nu} \quad \rightarrow$$

DM:

$$D'_{gc} + \left\{ \left( \frac{a^2 Q_c^0}{\rho_c \mathcal{H}} \right)' + \frac{\rho'_c}{\rho_c \mathcal{H}} \frac{a^2 Q_c^0}{\rho_c} \right\} \Phi + \frac{a^2 Q_c^0}{\rho_c} D_{gc} + \frac{a^2 Q_c^0}{\rho_c \mathcal{H}} \Phi'$$

$$= -kV_c + 2\Psi \frac{a^2 Q_c^0}{\rho_c} + \frac{a^2 \delta Q_c^{0I}}{\rho_c} + \frac{a^2 Q_c^{0'}}{\rho_c \mathcal{H}} \Phi - \frac{a^2 Q_c^0}{\rho_c} \left( \frac{\Phi}{\mathcal{H}} \right)'$$

$$V'_c + \mathcal{H}V_c = k\Psi - \frac{a^2 Q_c^0}{\rho_c} V_c + \frac{a^2 \delta Q_{pc}^I}{\rho_c}$$

DE:

$$D'_{gd} + \left\{ \left( \frac{a^2 Q_d^0}{\rho_d \mathcal{H}} \right)' - 3w' + 3(C_e^2 - w) \frac{\rho'_d}{\rho_d} + \frac{\rho'_d}{\rho_d \mathcal{H}} \frac{a^2 Q_d^0}{\rho_d} \right\} \Phi + \left\{ 3\mathcal{H}(C_e^2 - w) + \frac{a^2 Q_d^0}{\rho_d} \right\} D_{gd} + \frac{a^2 Q_d^0}{\rho_d \mathcal{H}} \Phi'$$

$$= -(1+w)kV_d + 3\mathcal{H}(C_e^2 - C_a^2) \frac{\rho'_d}{\rho_d} \frac{V_d}{k} + 2\Psi \frac{a^2 Q_d^0}{\rho_d} + \frac{a^2 \delta Q_d^{0I}}{\rho_d} + \frac{a^2 Q_d^{0'}}{\rho_d \mathcal{H}} \Phi - \frac{a^2 Q_d^0}{\rho_d} \left( \frac{\Phi}{\mathcal{H}} \right)'$$

$$V'_d + \mathcal{H}(1-3w)V_d = \frac{kC_e^2}{1+w} D_{gd} + \frac{kC_e^2}{1+w} \frac{\rho'_d}{\rho_d \mathcal{H}} \Phi - (C_e^2 - C_a^2) \frac{V_d}{1+w} \frac{\rho'_d}{\rho_d} - \frac{w'}{1+w} V_d + k\Psi - \frac{a^2 Q_d^0}{\rho_d} V_d + \frac{a^2 \delta Q_{pd}^I}{\rho_d}$$

He, Wang, Jing, JCAP(09);  
He, Wang, Abdalla, PRD(II)

We have not specified the form of  
the interaction between dark  
sectors.

# Perturbation Equations

Phenomenological interaction forms:

$$(1) Q = \delta H(\rho_{DM} + \rho_{DE}), (2) Q = \delta H \rho_{DM} \text{ and } (3) Q = \delta H \rho_{DE}$$

$$a^2 Q_m^0 = 3\mathcal{H}(\lambda_1 \rho_m + \lambda_2 \rho_d)$$

$$a^2 Q_d^0 = -3\mathcal{H}(\lambda_1 \rho_m + \lambda_2 \rho_d)$$

**Perturbation equations:**

$$D'_m = -kU_m + 6\mathcal{H}\Psi(\lambda_1 + \lambda_2/r) - 3(\lambda_1 + \lambda_2/r)\Phi' + 3\mathcal{H}\lambda_2(D_d - D_m)/r \quad ,$$

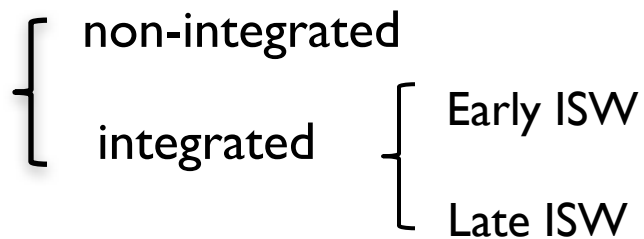
$$U'_m = -\mathcal{H}U_m + k\Psi - 3\mathcal{H}(\lambda_1 + \lambda_2/r)U_m \quad ,$$

$$D'_d = -3\mathcal{H}C_e^2 \{D_d - [3(\lambda_1 r + \lambda_2) + 3(1+w)]\Phi\} - 3\mathcal{H}(C_e^2 - C_a^2) \left[ \frac{3\mathcal{H}U_d}{k} - a^2 Q_d^0 \frac{U_d}{(1+w)\rho_d k} \right] \\ - 3\mathcal{H}w [3(\lambda_1 r + \lambda_2) + 3(1+w)]\Phi + 3\mathcal{H}wD_d + 3w'\Phi + 3(\lambda_1 r + \lambda_2)\Phi' - kU_d - 6\Psi\mathcal{H}(\lambda_1 r + \lambda_2) \\ + 3\mathcal{H}\lambda_1 r(D_d - D_m)$$

$$U'_d = -\mathcal{H}(1 - 3w)U_d + kC_e^2 \{D_d - 3[(\lambda_1 r + \lambda_2) + (1+w)]\Phi\} \\ - (C_e^2 - C_a^2)a^2 Q_d^0 \frac{U_d}{(1+w)\rho_d} + 3(C_e^2 - C_a^2)\mathcal{H}U_d + (1+w)k\Psi + 3\mathcal{H}(\lambda_1 r + \lambda_2)U_d.$$

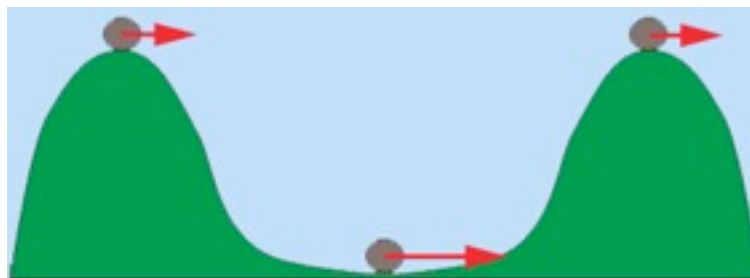
# Signature of the interaction in the CMB

## Sachs–Wolfe effects:



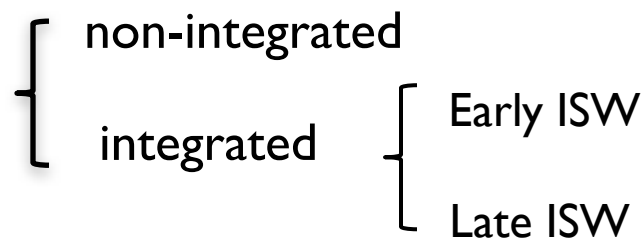
photons' initial conditions

has the unique ability to probe the  
“size” of DE: **EOS**, the speed of sound



# Signature of the interaction in the CMB

## Sachs–Wolfe effects:

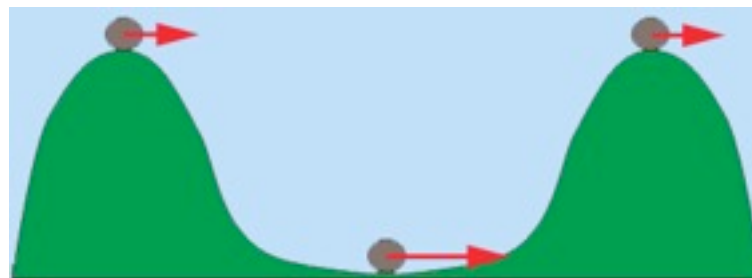


photons' initial conditions

has the unique ability to probe the  
“size” of DE: **EOS**, the speed of sound



*Signature of the interaction  
between DE and DM?*



# ISW imprint of the interaction

The analytical descriptions for such effect

$$C_l^{ISW} = 4\pi \int \frac{d^3k}{(2\pi)^3} P_\psi(k) \left| \int_{\tau_i}^{\tau_0} d\tau j_l(k[\tau_0 - \tau]) e^{\kappa(\tau_0) - \kappa(\tau)} [\Psi' - \Phi'] \right|^2$$

where  $P_\psi(k)$  is the power spectrum of the primordial curvature perturbation.  $j_l$  is the spherical Bessel functions.  $\kappa$  denotes the optical depth for Thompson scattering. From Einstein's equations, we obtain,

$$\Psi' - \Phi' = -2\Phi' - \mathcal{T}' = 2\mathcal{H} \left\{ \Phi + 4\pi G a^2 \sum V^i (p^i + \rho^i) / (\mathcal{H}k) + \mathcal{T} \right\} - \mathcal{T}'$$

$$\Phi' = -\mathcal{H}\Phi - \mathcal{H}\mathcal{T} - 4\pi G a^2 \sum V^i (p^i + \rho^i) / k$$

$$\Phi = \frac{4\pi G a^2 \sum \rho_i \{ D_g^i + 3\mathcal{H}U^i / k \}}{k^2 - 4\pi G a^2 \sum \rho'_i / \mathcal{H}}$$

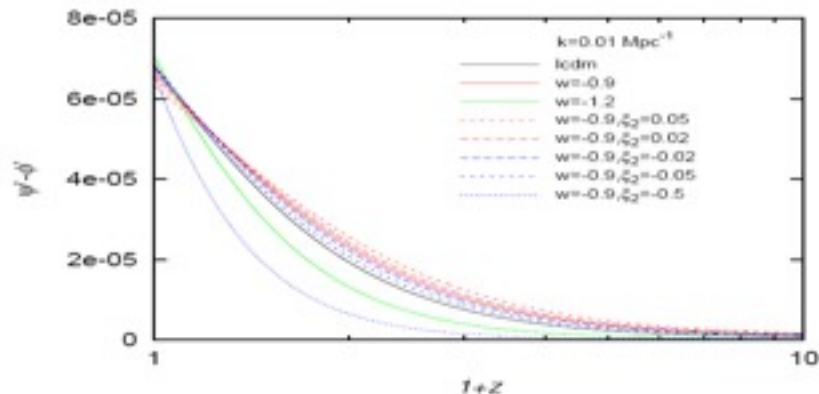
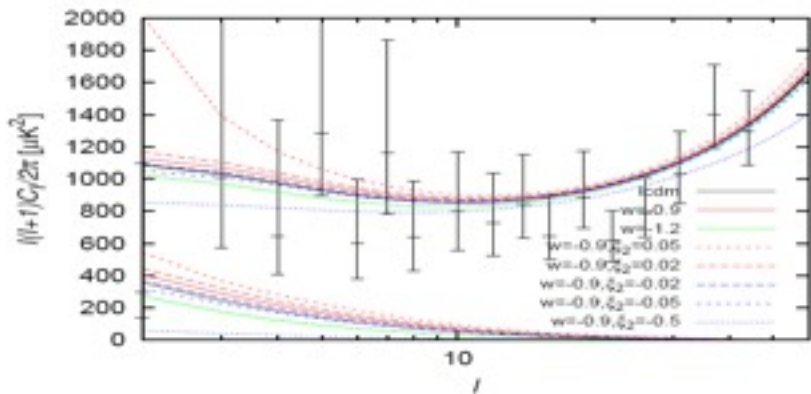
ISW effect is not simply due to the change of the CDM perturbation. The interaction enters each part of gravitational potential.

**J.H. He, B.Wang, P.J.Zhang, PRD(09)**

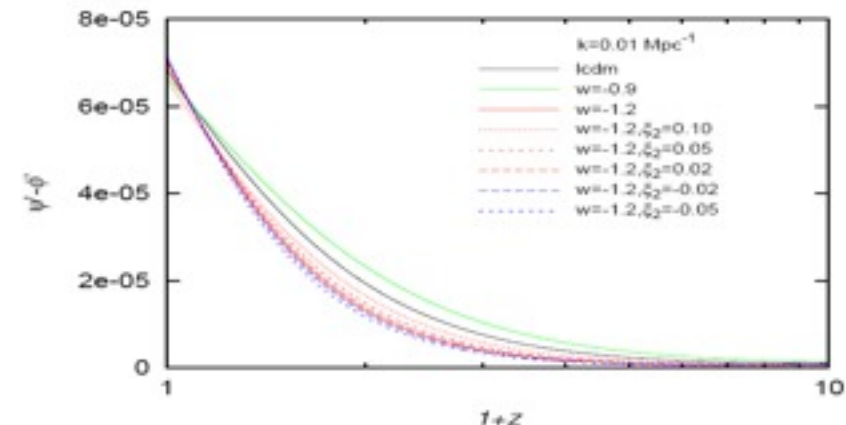
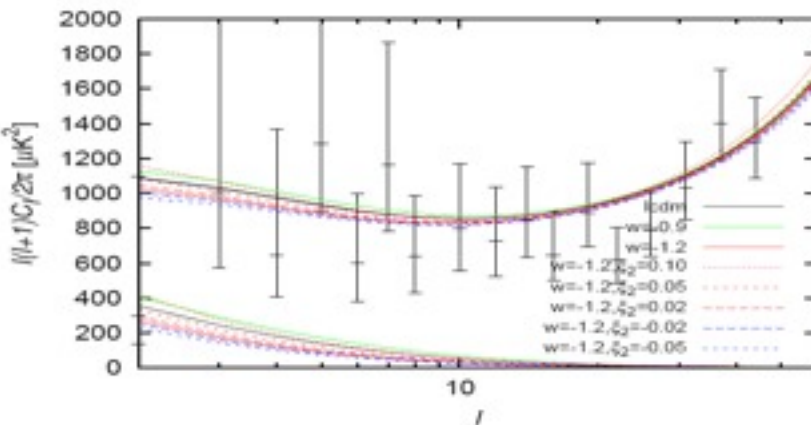
**J.H.He, B.Wang, E.Abdalla, PRD(11)**

# The ISW effect as a probe of the interaction

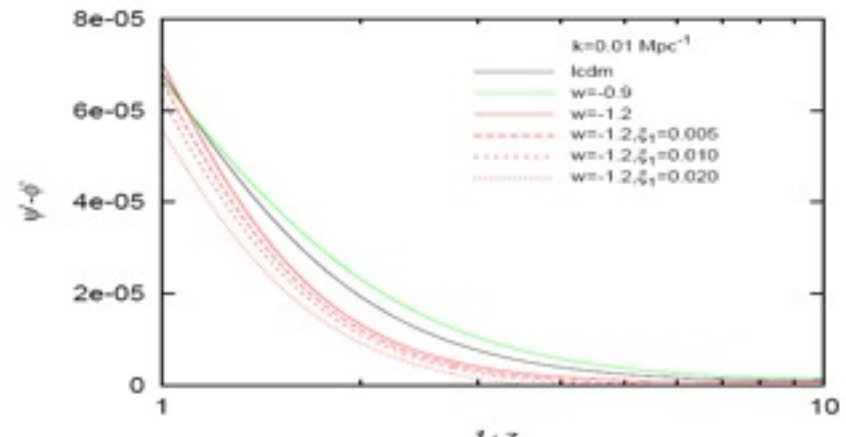
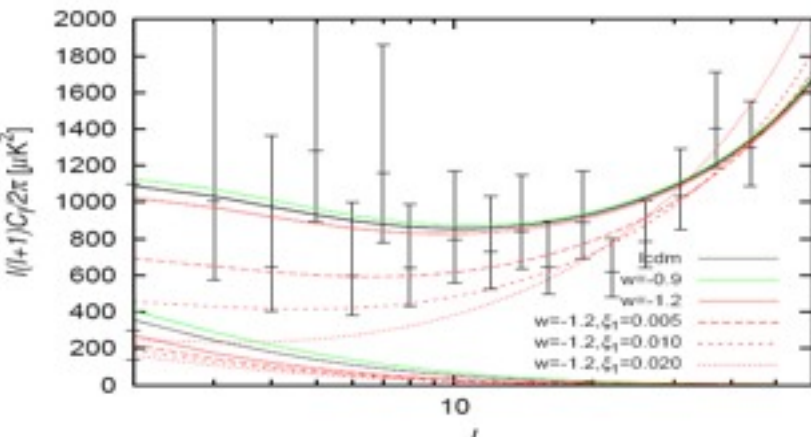
$\sim DE, w > -1$



$\sim DE, w < -1$

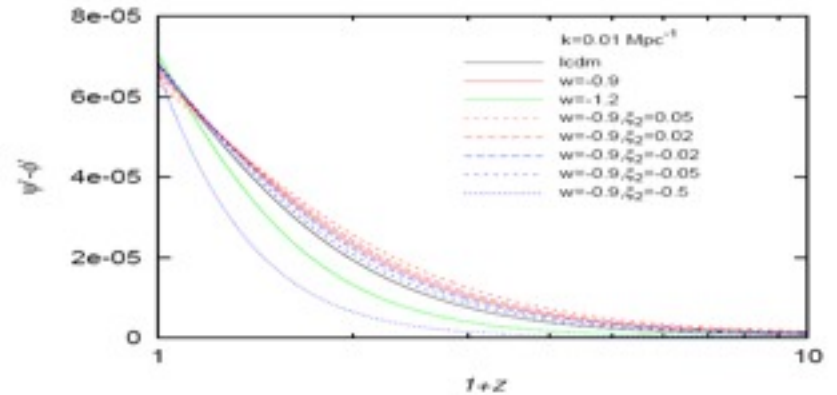
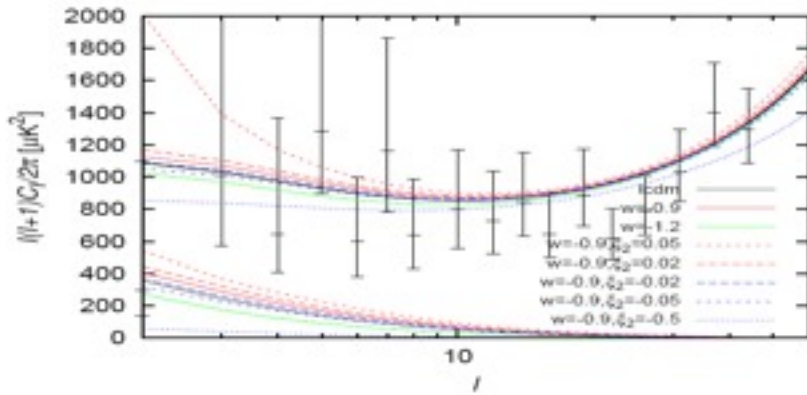


$\sim DM, w < -1$

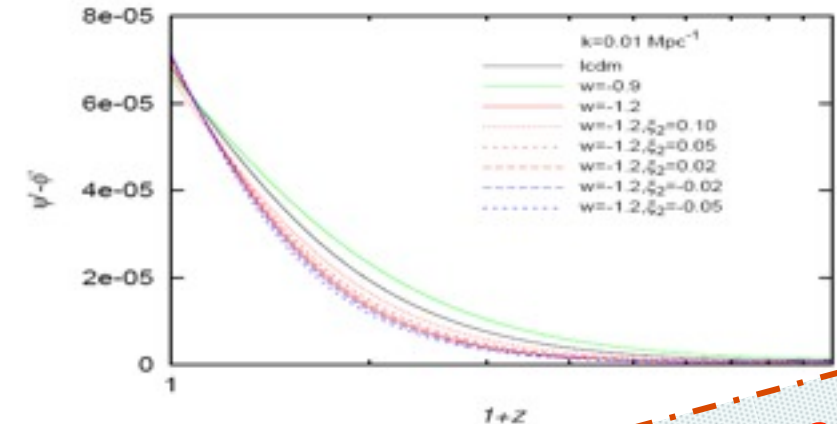
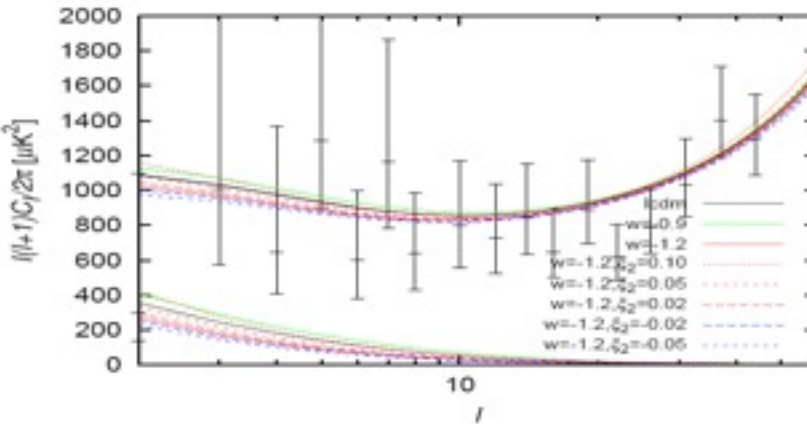


# The ISW effect as a probe of the interaction

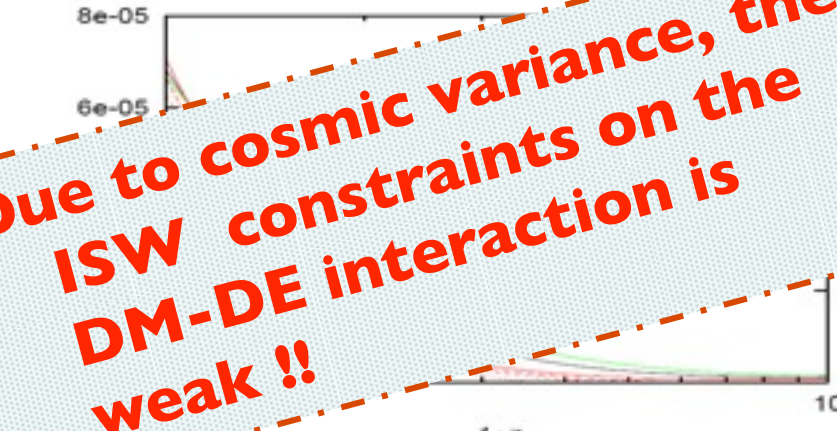
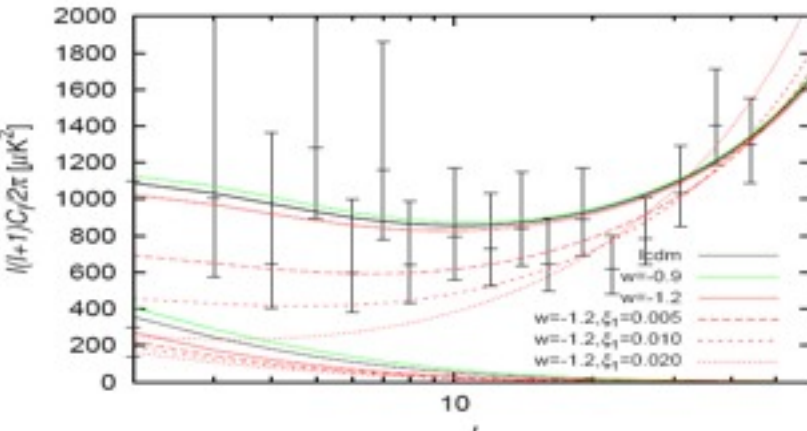
$\sim DE, w > -1$



$\sim DE, w < -1$



$\sim DM, w < -1$



**Due to cosmic variance, the ISW constraints on the DM-DE interaction is weak !!**

# The peculiar velocities

The evolution equation for the velocity of baryons

$$v'_b = -\mathcal{H}v_b + k\psi, \quad \Psi = -\Phi \quad \Phi = \frac{4\pi G a^2 \sum_i \rho_i (D_g^i - \rho'_i U_i / (1 + w_i) \rho_i k)}{k^2 - 4\pi G a^2 \sum_i \rho'_i / \mathcal{H}}$$

We compute the root mean square velocity dispersion of the baryon velocity field, smoothed on a sphere of radius  $r$ ,

$$\langle v_b^2 \rangle = \int d^3k W_r^2(k) P_v(k)$$

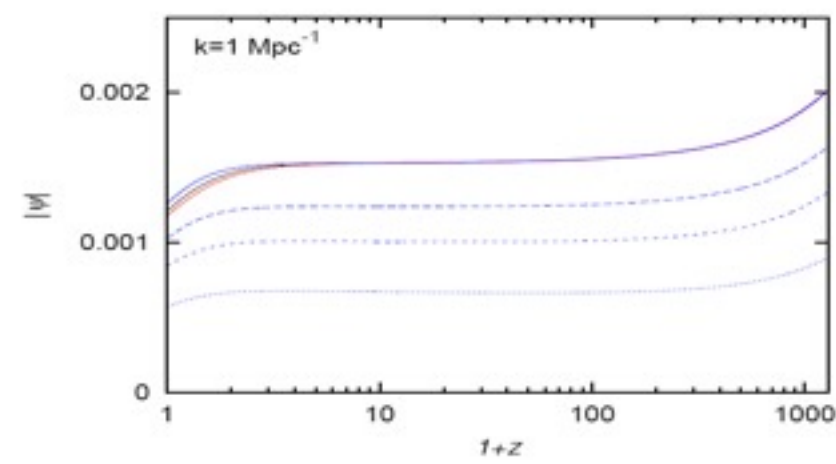
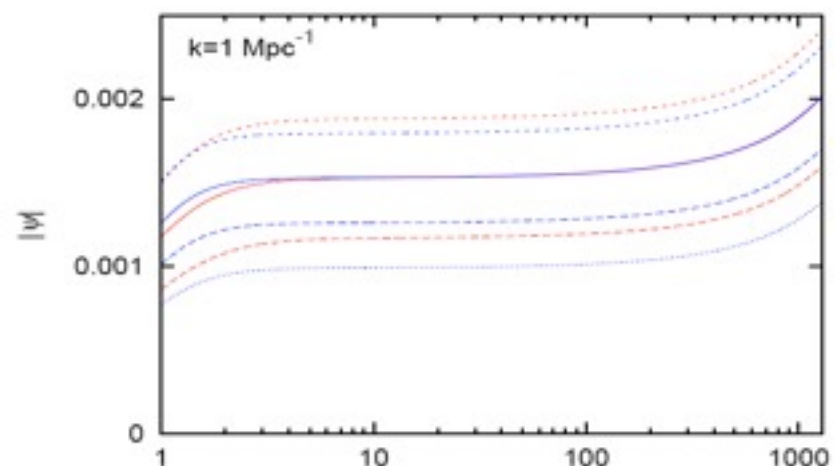
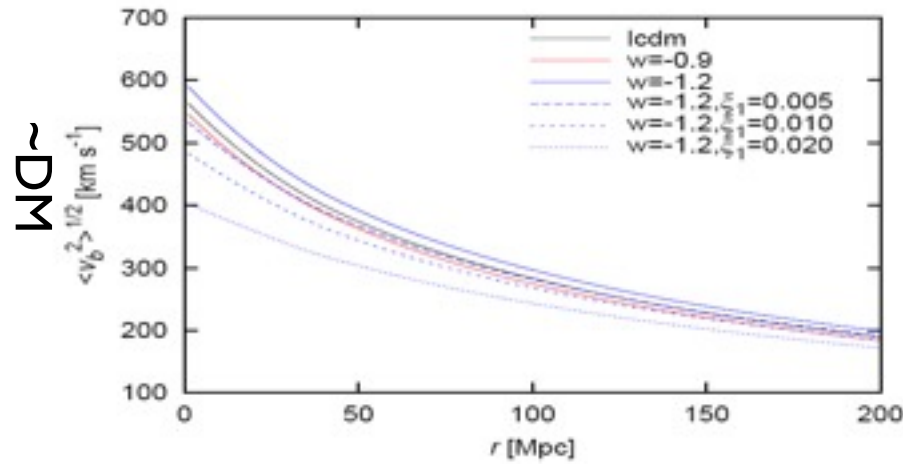
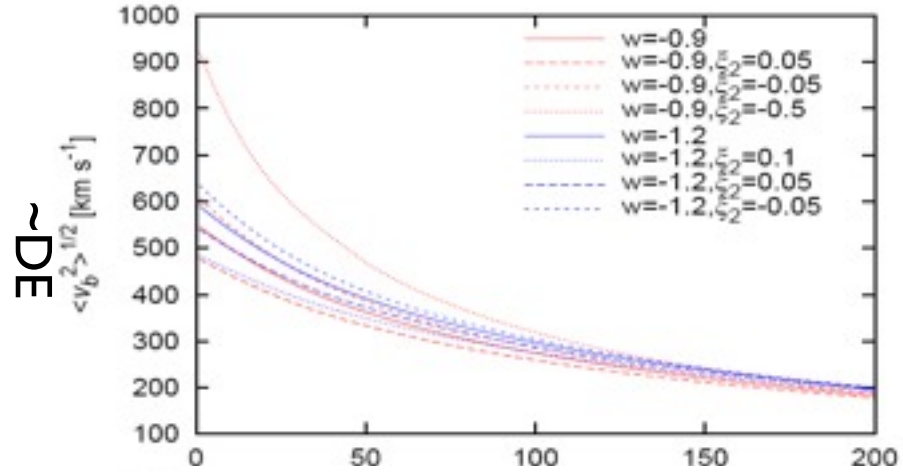
$W_r(k)$  is a top hat window function of radius  $r$   
 $P_v(k)$  is the power spectrum of the baryon velocity field

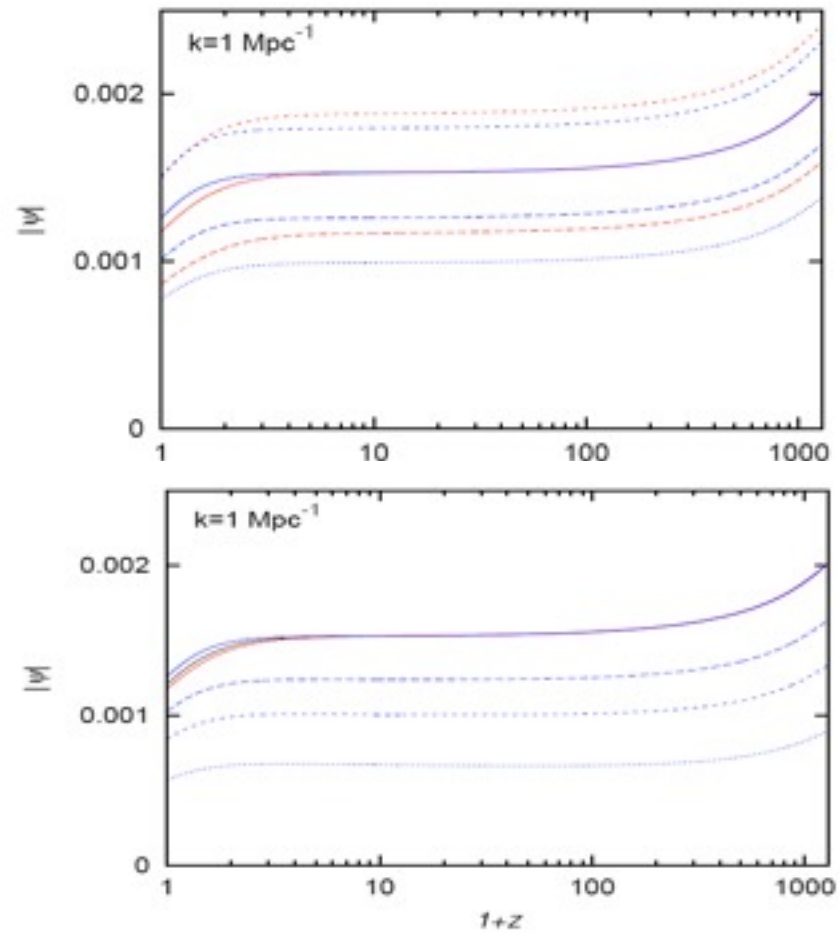
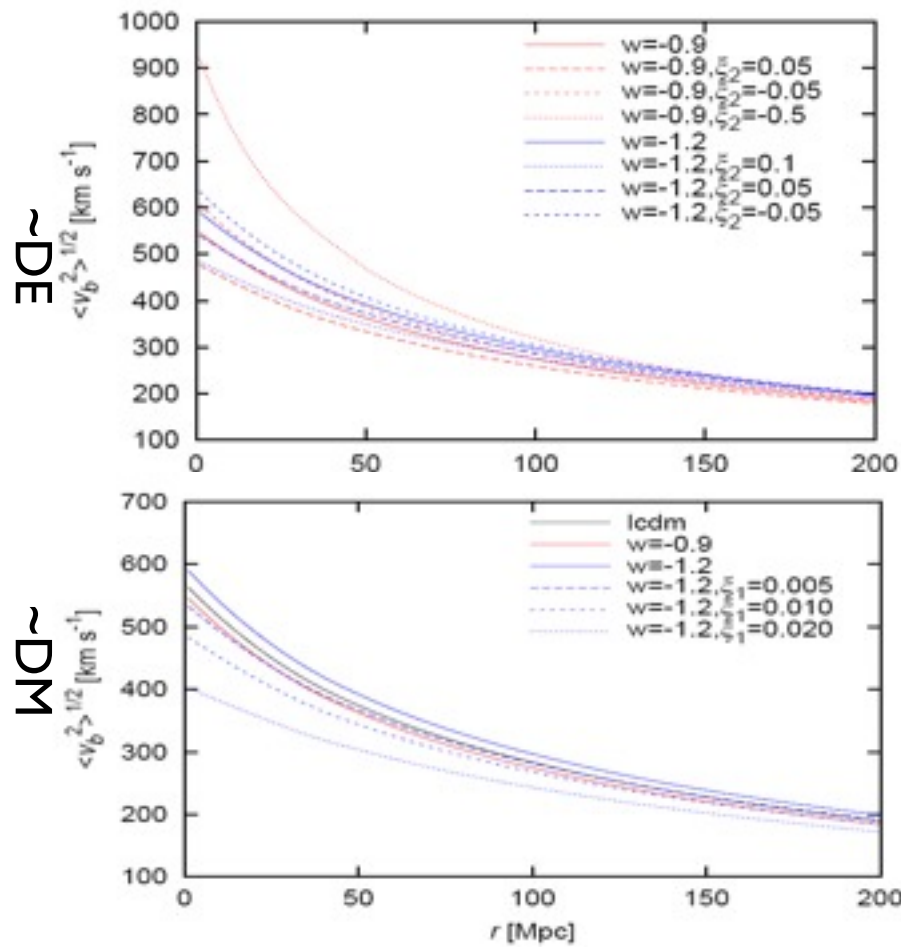
$$\text{Interaction} \longrightarrow \Phi = -\Psi \longrightarrow v_b$$

## Planck intermediate results. XIII. Constraints on peculiar velocities

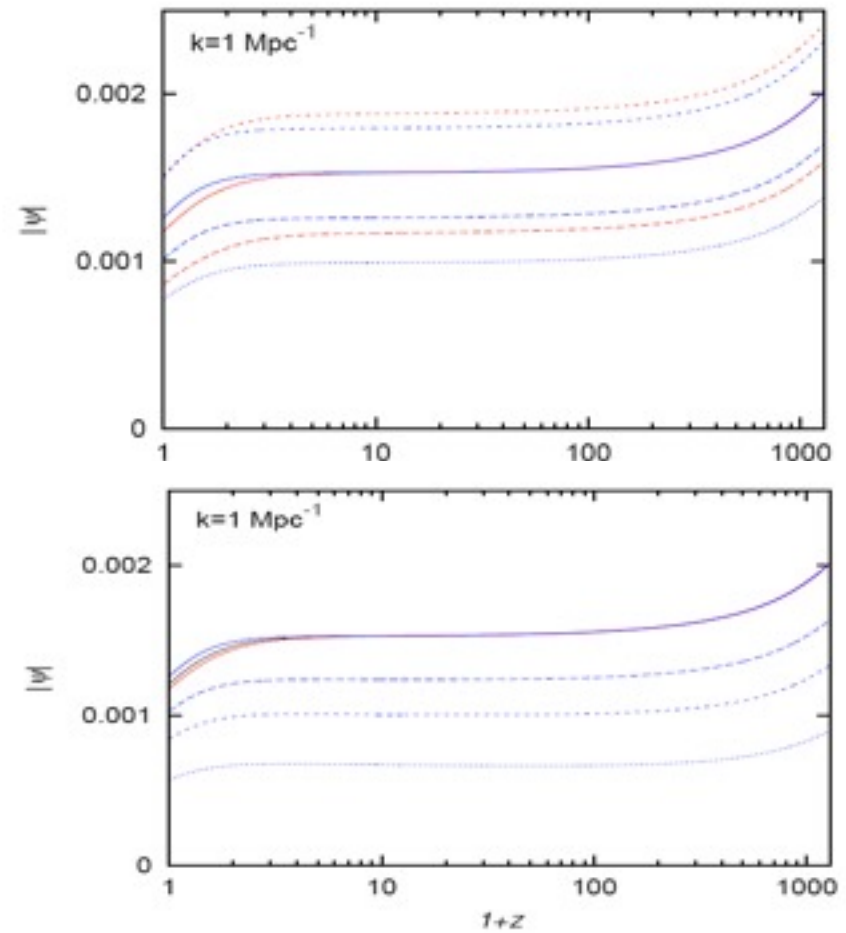
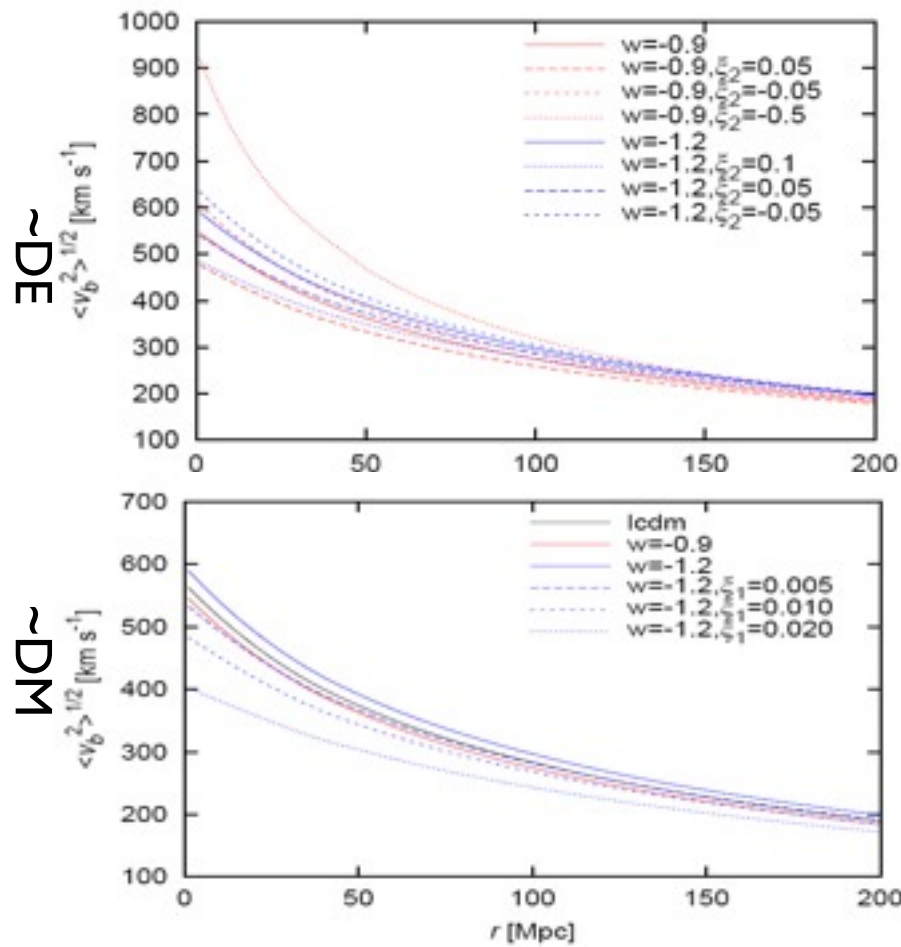
**1303.5090:** radial velocity at  $z=0.15$  to be below 800km/s at 95%C.L., 3 times of LCDM prediction



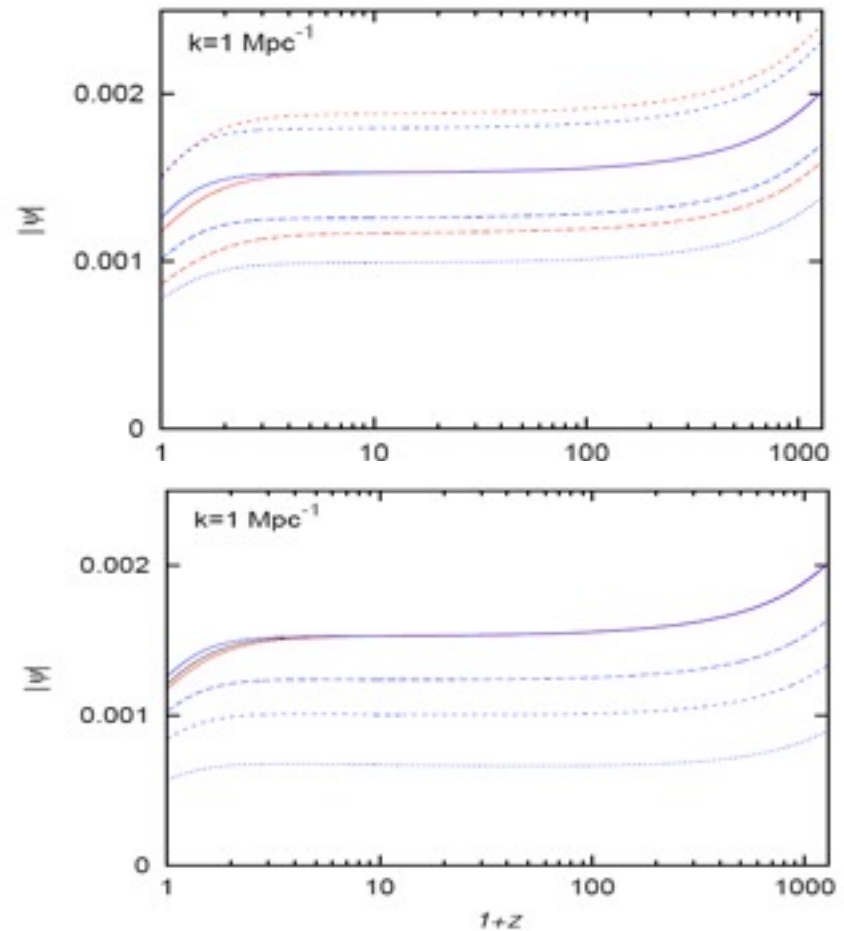
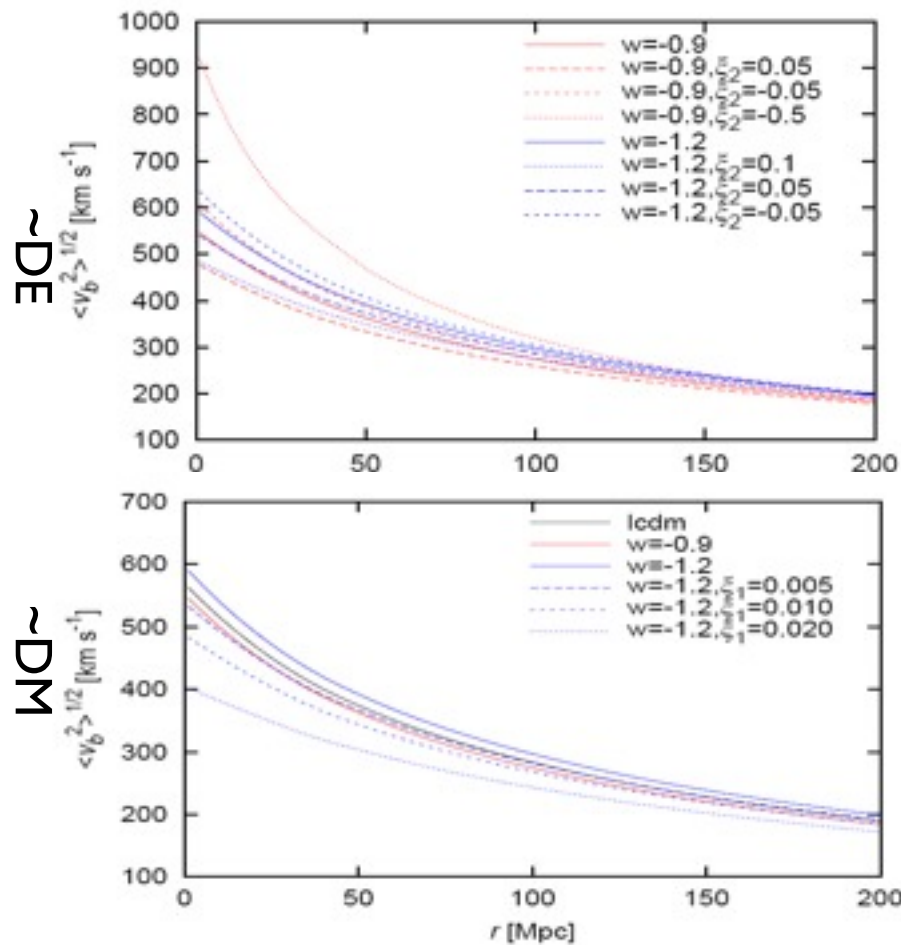




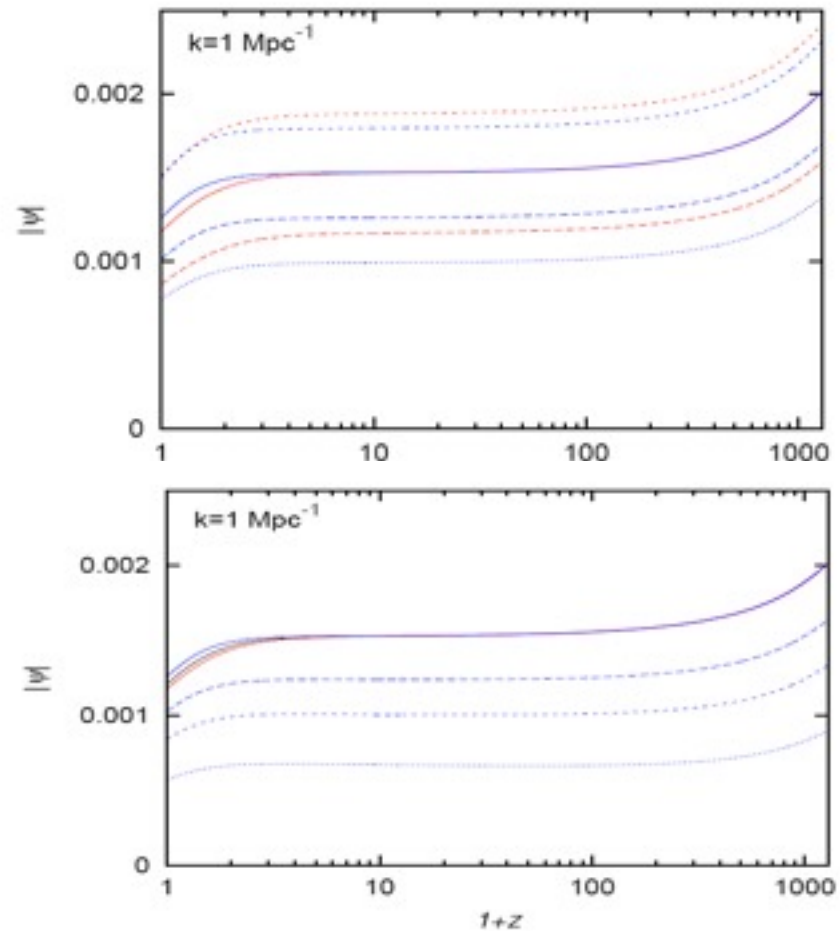
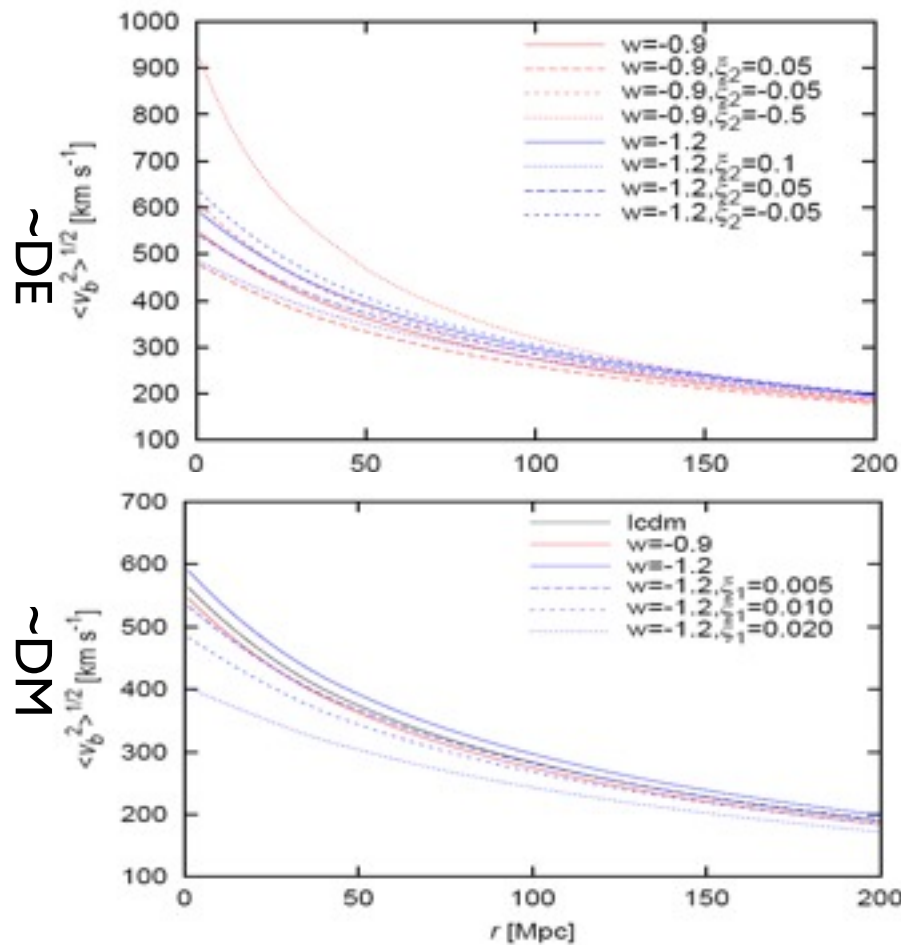
- No interaction,  $w$  influence  $\varphi$  at small  $z$ , suppression of the velocity for  $w > -1$ , enhancement for  $w < -1$ , compared with  $w = -1$



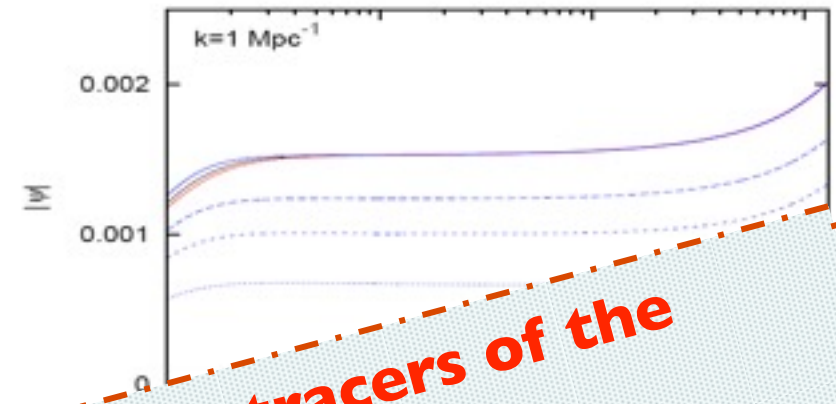
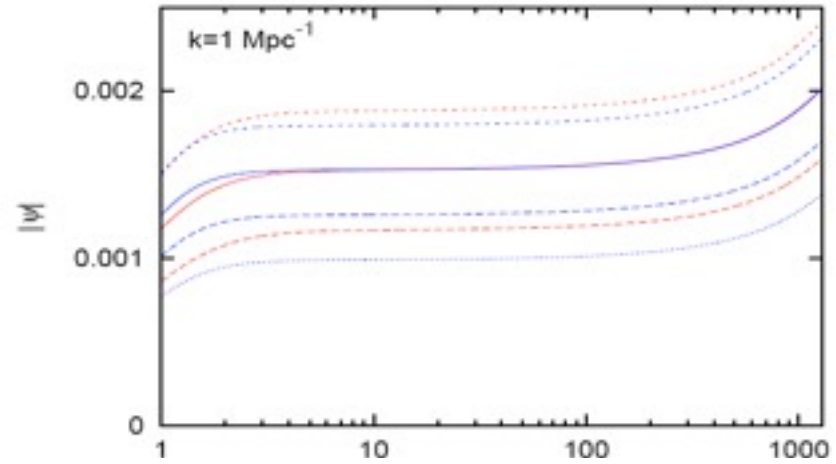
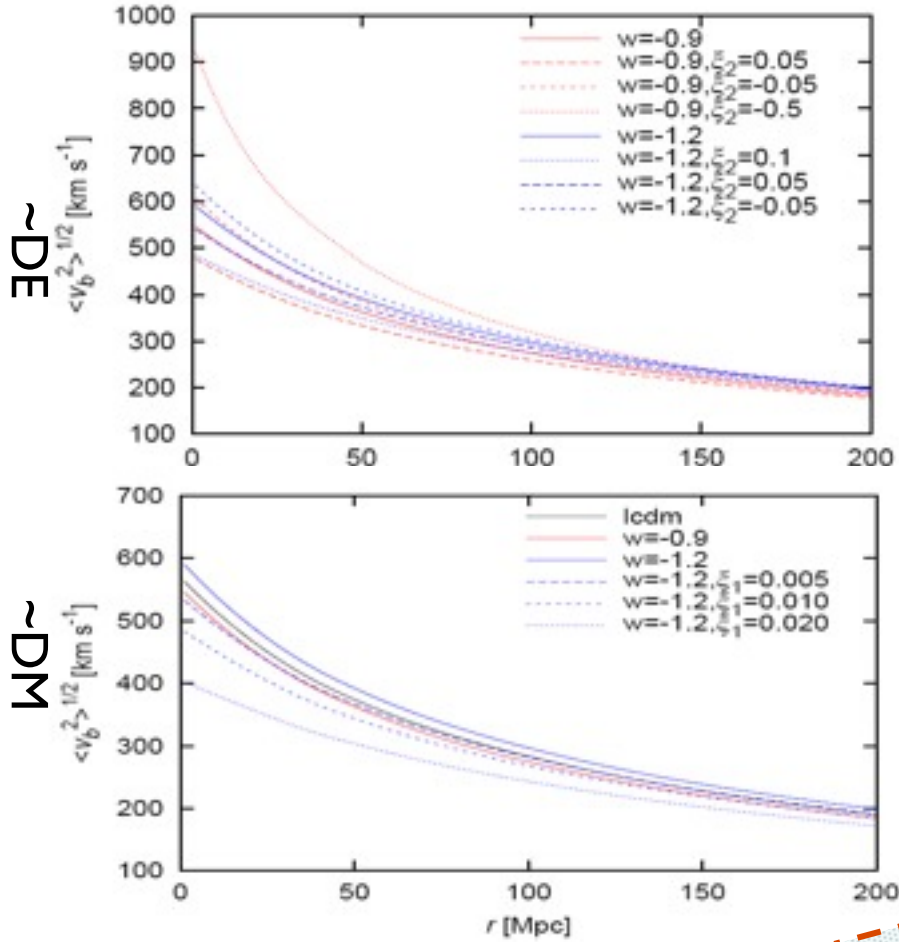
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- With interaction,  $\varphi$  evolves during a longer period than in non-interacting models. Larger couplings give smaller peculiar velocities. The peculiar velocities changes larger when the coupling is proportional to the DM than to the DE.



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- For negative coupling and with  $w < -1$ , the peculiar velocity could be larger than in the



- No interaction,  $w$  influence  $\varphi$  at small  $z$ , suppression of the velocity for  $w > -1$ , enhancement for  $w < -1$ , compared with  $w=-1$
- With interaction,  $\varphi$  evolves during a longer period than in non-interacting models. Larger couplings give smaller peculiar velocities. The peculiar velocities changes larger when the coupling is proportional to the DM than to the DE.
- For negative coupling and with  $w < -1$ , the peculiar velocity could be larger than in the  $\Lambda\text{CDM}$  model by a factor of two.



**Use clusters as tracers of the velocity field.**  
**The velocity can be directly measured by the Kinematic Sunyaev-Zel'dovich effect**

- No interaction,  $w$  influence  $\varphi$  at small  $r$  for  $w < -1$ , compared with  $w = -1$
- With interaction,  $\varphi$  evolves during growth. Couplings give smaller peculiar velocities. Coupling is proportional to the DM thermal velocity.
- For negative coupling and with  $w < -1$ , peculiar velocity is larger than in the LCDM model by a factor of two.

# Change in CMB spectrum

Photon

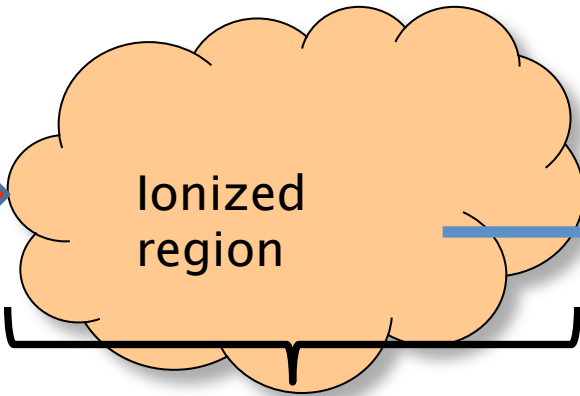
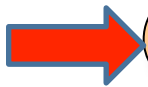


Temperature:  $T(1+\Theta)$ ,  $T$  background,  $\Theta$  is the perturbation

Mean temperature ↑

Anisotropy, primordial set up at  $z=1100$

Photon



Ionized region

Optical depth  $\tau$



Only a fraction of photon,  $\exp(-\tau)$ , escapes, contribution to temperature  $T(1+\Theta) \exp(-\tau)$ .

Ionized region contribution to the temperature  $T(1-\exp(-\tau))$

Equilibrated temperature  $T$

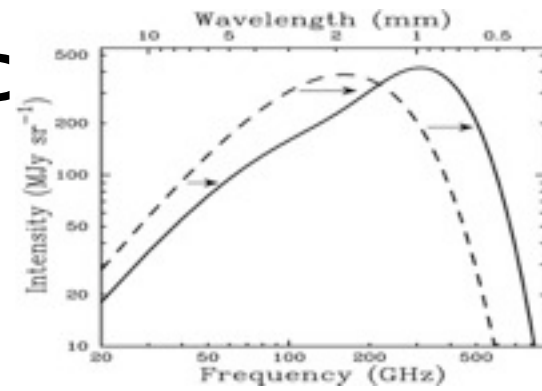
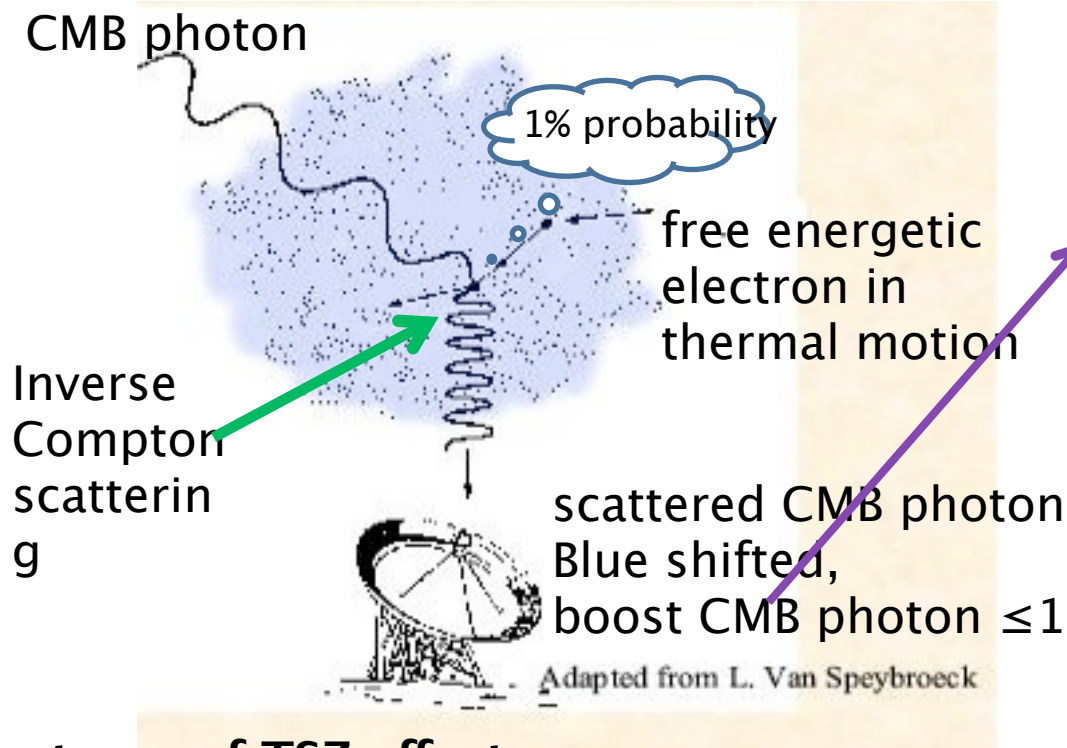
Temperature we see today:

$$T(1+\Theta) \exp(-\tau) + T(1-\exp(-\tau)) = T[1 + \Theta \exp(-\tau)]$$

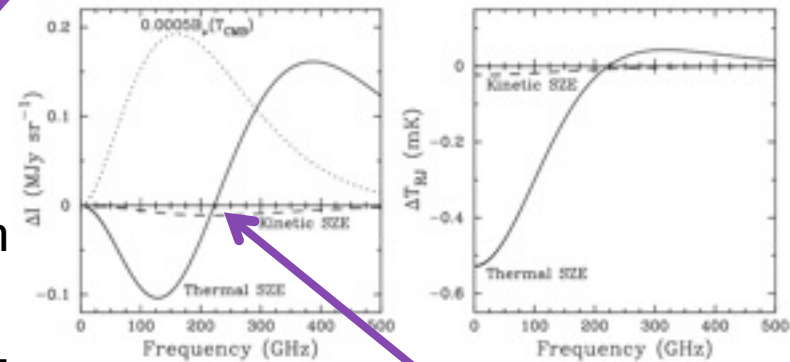
Only those scale within the horizon at the time of reionization get suppressed by  $\exp(-\tau)$ ,  $l > \eta_0 / \eta_{\text{reion}}$ , small  $l$  will not be affected

# Sunyaev Zel'dovich effect

## The thermal SZ effect



distortion in the CMB spectrum



218GHz

### Features of TSZ effect:

1. CMB ↓ at frequency <218GHz, ↑ CMB at frequency >218GHz
2. TSZ depends on the depth of the cluster gas, distortion strong at the center, weak at the edge
  - Independent of the redshift
  - Intensity of TSZ depends on the cluster mass



## The kinetic SZ effect

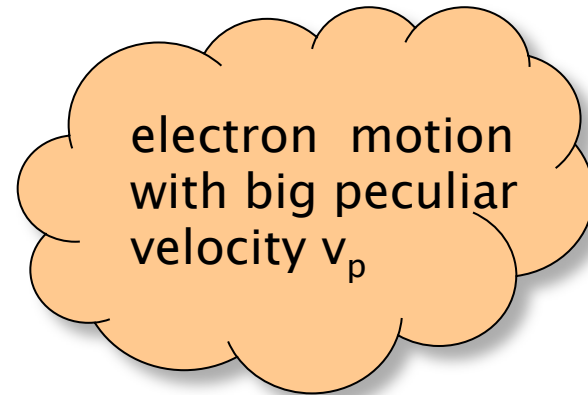
$$\frac{\Delta T}{T}|_{CMB} = \int v_p n_e \sigma_T dl$$

$v_p$ : peculiar velocity

scattering probability

Interesting to study KSZ effect

$$T_{CMB} = 2.73K$$



$$T_{CMB} = 2.73 + \Delta T$$

**PLANCK result: the upper limit of the peculiar velocity can be three times of the LCDM prediction**

# The KSZ effect

- $n_e$ : the electron density,
- $\sigma_T$ : the Thomson cross section
- $k$ : the Thomson optical depth
- $v$ : the peculiar velocity of the electrons
- $\hat{n}$ : the unit vector along the l.o.s.

$$\frac{\Delta T(\hat{n})}{T_{CMB}} = \int_{t_{re}}^{t_0} n_e \sigma_T e^{-\kappa} (\mathbf{v} \cdot \hat{\mathbf{n}}) dt,$$

Using the comoving distance  $x$  and neglecting any interaction of electrons with other particles,

$$n_e(x, z) = \chi_e \bar{n}_e(0) a^{-3} [1 + \delta_e(x, z)]$$

$\bar{n}_e(0)$  the mean electron number density at present

$$\frac{\Delta T(\hat{n})}{T_{CMB}} = \bar{n}_e(0) \sigma_T \int a^{-2} \chi_e e^{-\kappa} (\mathbf{p} \cdot \hat{\mathbf{n}}) dx, \quad \chi_e \text{ is the ionization fraction}$$

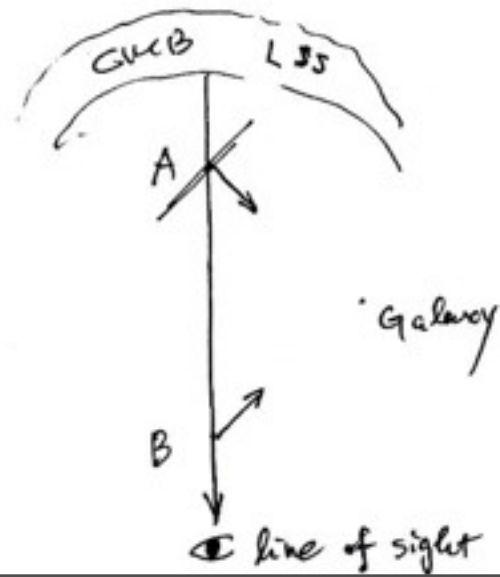
peculiar momentum  $\mathbf{p} \equiv (1 + \delta_e) \mathbf{v}$

$p_E$ : gradient component

$p_B$ : curl component

$p_E$ : no contribution to KSZ,  
cancels out when integrating along the l.o.s.

$p_B$ : contributes to KSZ



$$\nabla \times \mathbf{p} = (1 + \delta_e) \nabla \times \mathbf{v} + \nabla \delta_e \times \mathbf{v},$$

the rotational mode of  $\mathbf{v}$

the cross-talk between the density and the velocity

In the linear regime, only the irrotational component of the velocity fields couples to gravity,

**The KSZ effect is due to the cross-talk between the density gradient and the velocity.**

$$C_l^{KSZ} = \frac{16\pi^2}{(2l+1)^3} (\bar{n}_e(0)\sigma_T)^2 \int_0^{z_{re}} (1+z)^4 \chi_e^2 \frac{1}{2} \Delta_B^2(k, z)|_{k=l/x} e^{-\kappa x(z)} \frac{dx(z)}{dz} dz$$

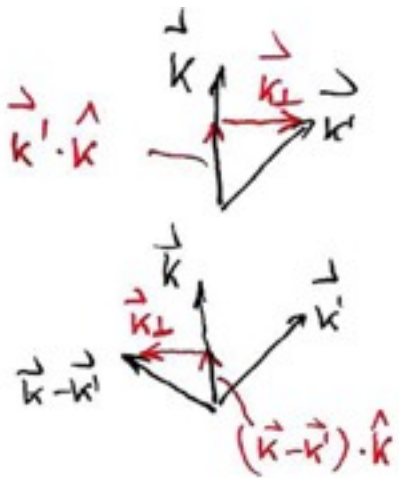
This formula is in the same form as the KSZ effect of the LCDM model

$$\Delta_B^2(k, z) = \frac{k^3}{2\pi^2} P_B(k, z) \quad \text{Where,}$$

$$P_B(k) = \langle p_B^*(\mathbf{k}) p_B(\tilde{\mathbf{k}}) \rangle = \int \frac{d^3 \mathbf{k}'}{(2\pi)^3} \int \frac{d^3 \tilde{\mathbf{k}}'}{(2\pi)^3} \langle \delta_e^*(\mathbf{k} - \mathbf{k}') \delta_e(\tilde{\mathbf{k}} - \tilde{\mathbf{k}}') v^*(\mathbf{k}') v(\tilde{\mathbf{k}}') \rangle \\ \times |\mathbf{k}'| |\tilde{\mathbf{k}}'| \beta(\mathbf{k}, \mathbf{k}') \beta(\tilde{\mathbf{k}}, \tilde{\mathbf{k}}'),$$

$$\beta_2(\vec{k}, \vec{k}') = \frac{1}{|\vec{k}'|^2} [\vec{k}' - \hat{k} \hat{k}] = \frac{1}{|\vec{k}'|} [\hat{k}_\perp]$$

$$\beta_1(\vec{k}, \vec{k} - \vec{k}') = \frac{1}{|\vec{k} - \vec{k}'|^2} [(\vec{k} - \vec{k}') - (\vec{k} - \vec{k}') \cdot \hat{k} \hat{k}] = \frac{1}{|\vec{k} - \vec{k}'|} [\hat{k}_\perp]$$



In the linear perturbation theory and for subhorizon perturbations,

$$v = -\delta'_e/k = -aHf_e(a)\delta_e/k,$$

$$aHf_e = a\dot{D}_e/D_e \quad D_e(z) \equiv \delta_e(z)/\delta_e(0)$$

Thus:

$$P_B(k, z) = \frac{a^2}{2} \int \frac{d\mathbf{k}'^3}{(2\pi)^3} \left( \frac{\dot{D}_e}{D_e} \right)^2 P(k', z) P(k - k', z) \\ \times [W_g(k - k')\beta(\mathbf{k}, \mathbf{k}') + W_g(k')\beta(\mathbf{k}, \mathbf{k} - \mathbf{k}')]^2$$

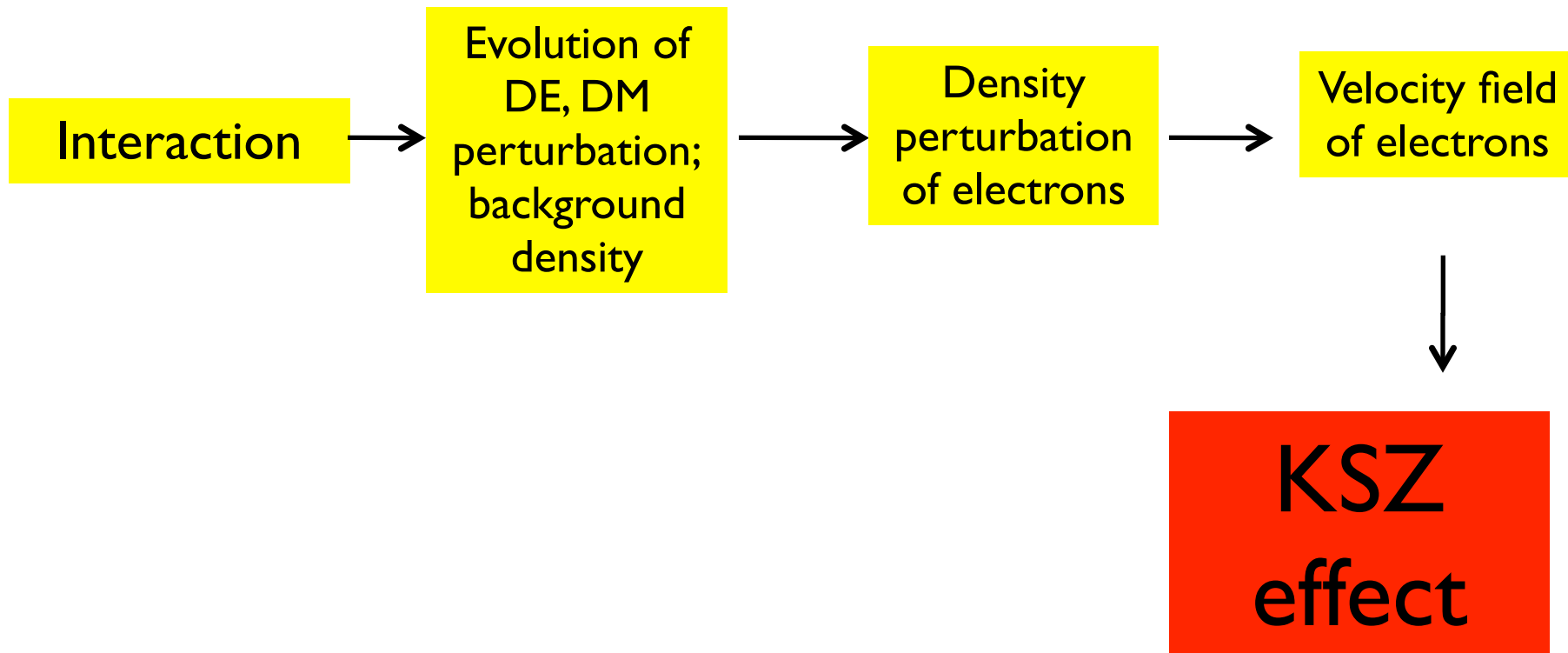
$W_g(k)$  is the transfer function

These equations are formally identical to the KSZ contribution in the concordance  $\Lambda$ CDM model, **BUT...**

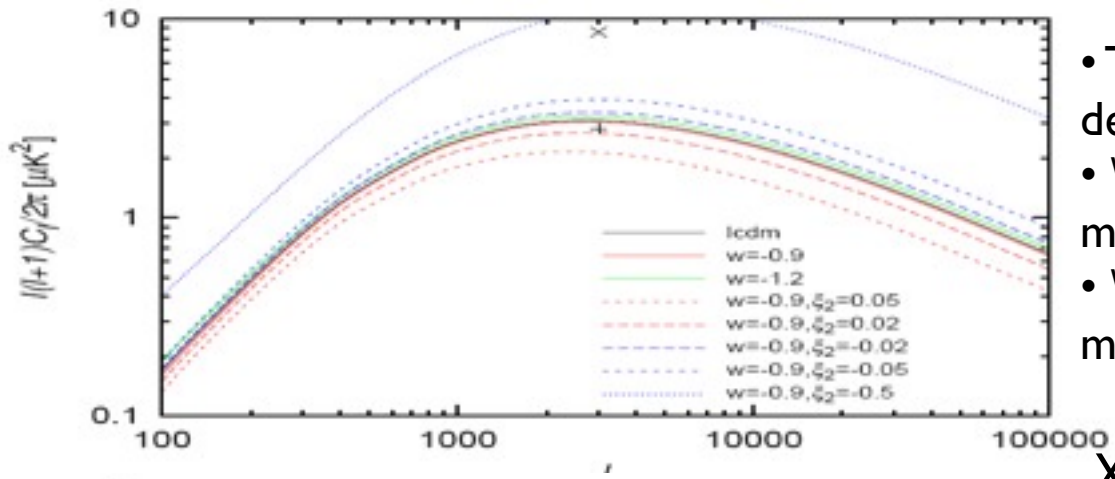
$$\delta_e'' + \frac{a'}{a}\delta_e' + 3\phi'' + 3H\phi' + k^2\psi = 0$$

In the small scale approximation  $k \gg aH$ , neglect the time variation of the potential

$$\delta_e'' + \frac{a'}{a}\delta_e' - 4\pi G a^2 (\rho_b \delta_b + \rho_c \delta_c + \rho_d \delta_d) = 0,$$

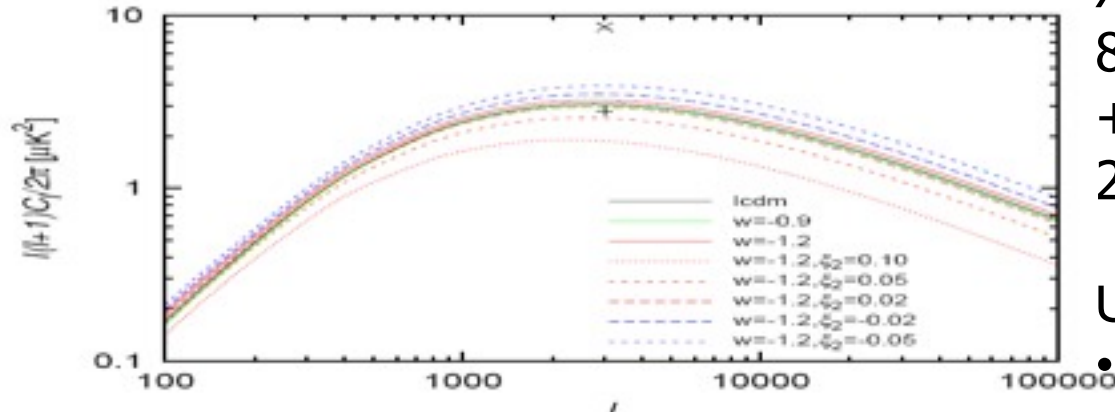


$\sim DE, w > -1$



- The amplitude increases with decreasing of coupling
- $\xi > 0$ , smaller than the LCDM model
- $\xi < 0$ , larger than the LCDM model

$\sim DE, w < -1$

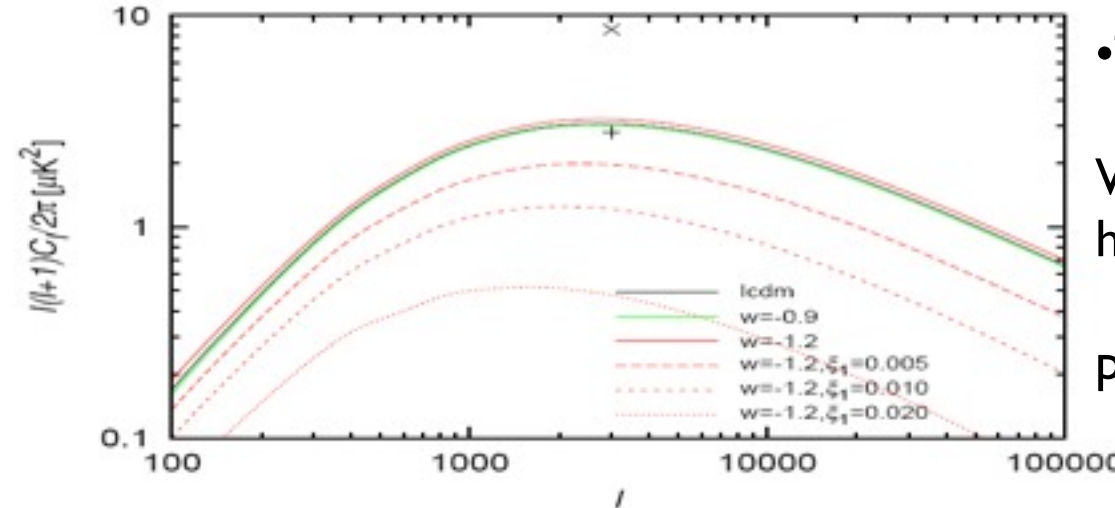


X: upper limit from ACT  
 $8.6 \mu K^2$  at  $l=3000$   
 +: upper limit from SPT  
 $2.8 \mu K^2$  at  $l=3000$

Upper limits depend on:

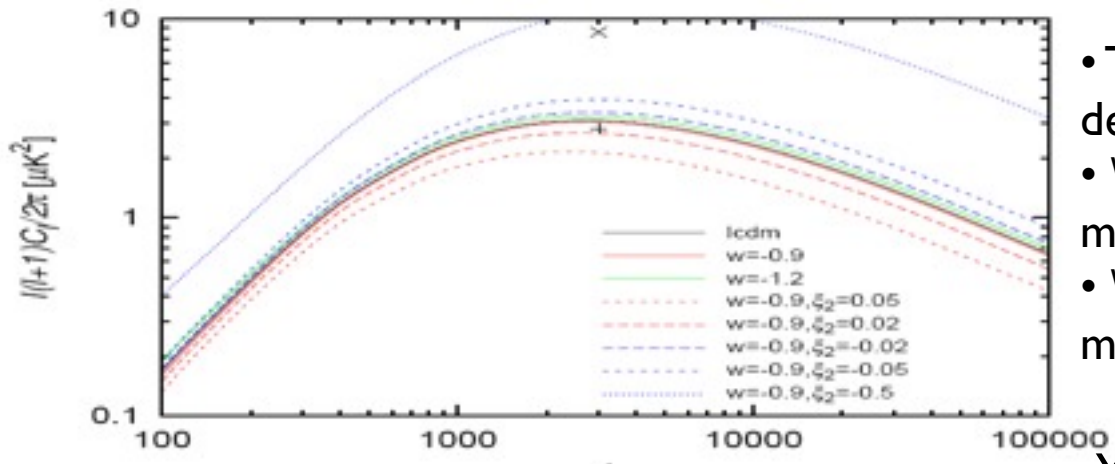
- reionization history
- the modeling of CIB
- TSZ contribution

$\sim DM, w < -1$



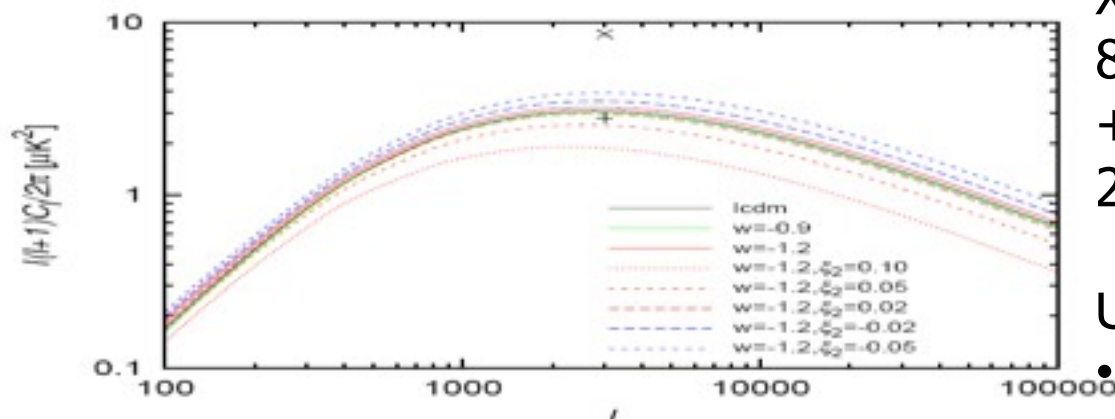
We just consider:  
 homogeneous, linear  
 patchy reionization, nonlinear

$\sim DE, w > -1$



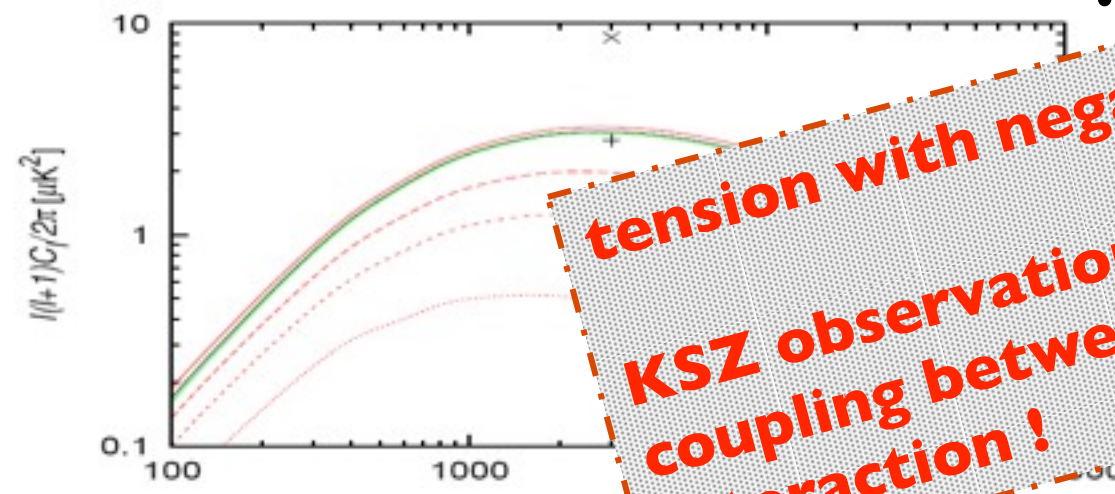
- The amplitude increases with decreasing of coupling
- $\xi > 0$ , smaller than the  $\Lambda$ CDM model
- $\xi < 0$ , larger than the  $\Lambda$ CDM model

$\sim DE, w < -1$



X: upper limit from ACT  $8.6 \mu K^2$  at  $l = 3000$   
 +: upper limit from SPT  $2.8 \mu K^2$  at  $l = 3000$

$\sim DM, w < -1$



Upper limits depend on:  
 • reionization history  
 • the model

**tension with negative coupling**  
**KSZ observations favor a positive coupling between DM-DE interaction!**

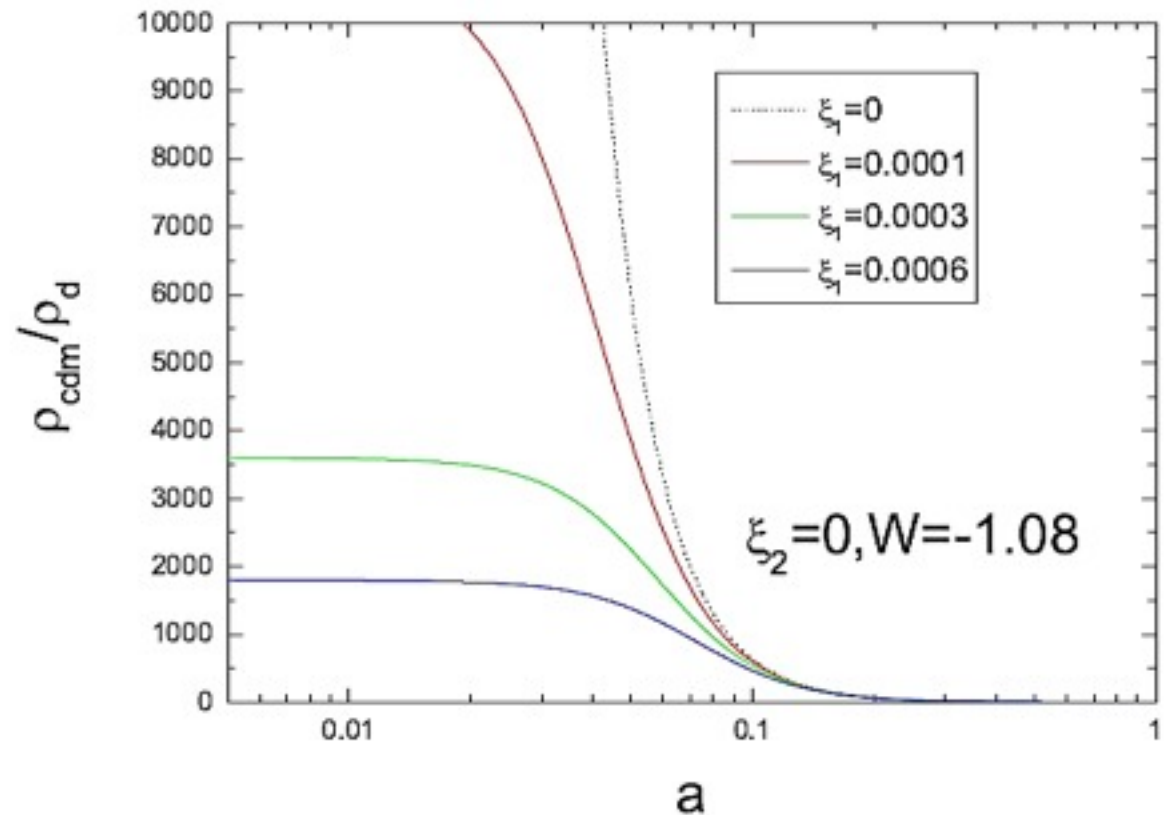
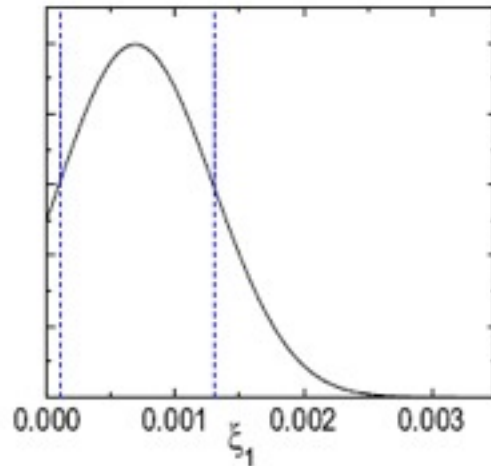
...non, nonlinear

**KSZ observations favor a positive coupling between DM-DE interaction**

**Encouraging !! Consistent with CMB and galaxy cluster test**

## Alleviate the coincidence problem

Interaction proportional to the energy density of DM



J.H. He, B.Wang, P.J.Zhang, PRD(09); J.H.He, B.Wang, E.Abdalla, PRD

(11)



# Summary:

## KSZ effect:

- potential,
- peculiar velocity,
- Large at big  $l$ ,
- from the moment of reionization  $z \sim 10$ .

## ISW effect:

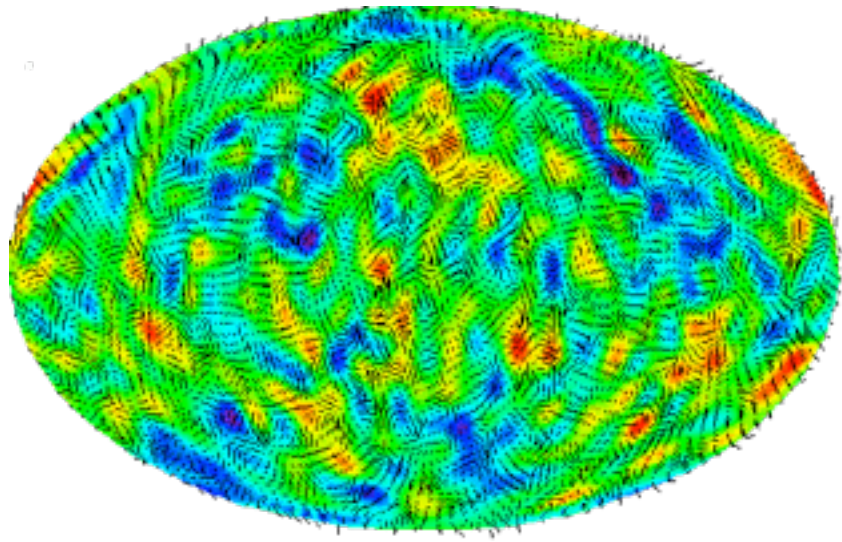
- time evolution of the potential,
- at large angular scales,
- during the period of acceleration

complementary

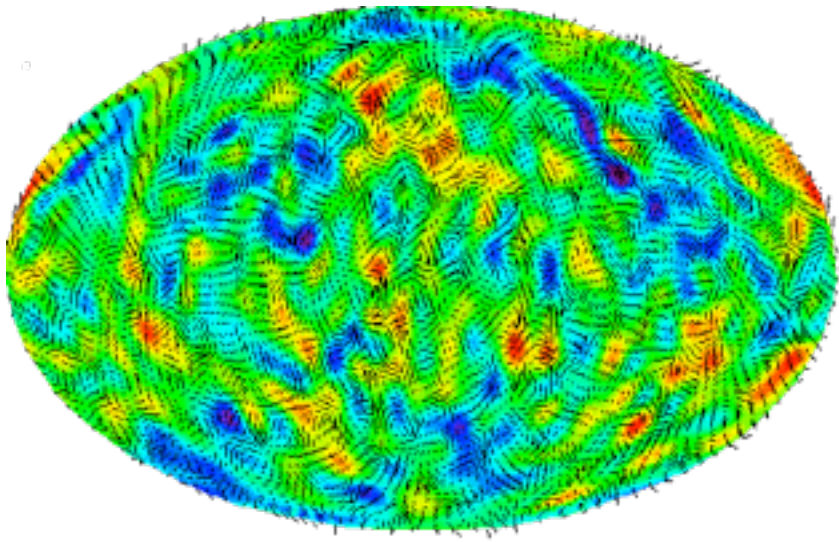
Alternatively:

The peculiar velocity - use clusters as tracers  
(DE&DM interaction)

***Thanks!!!***

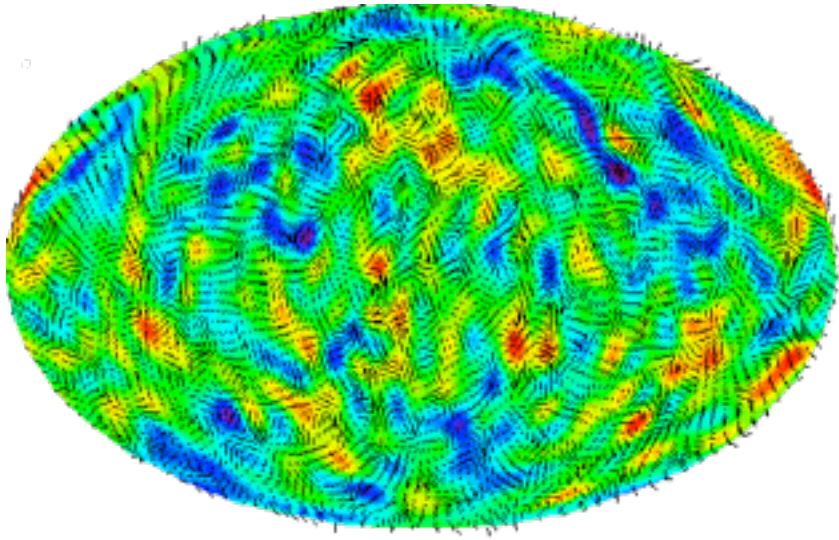


1992 COBE satellite result **2006  
Nobel Prize**



1992 COBE satellite result **2006 Nobel Prize**

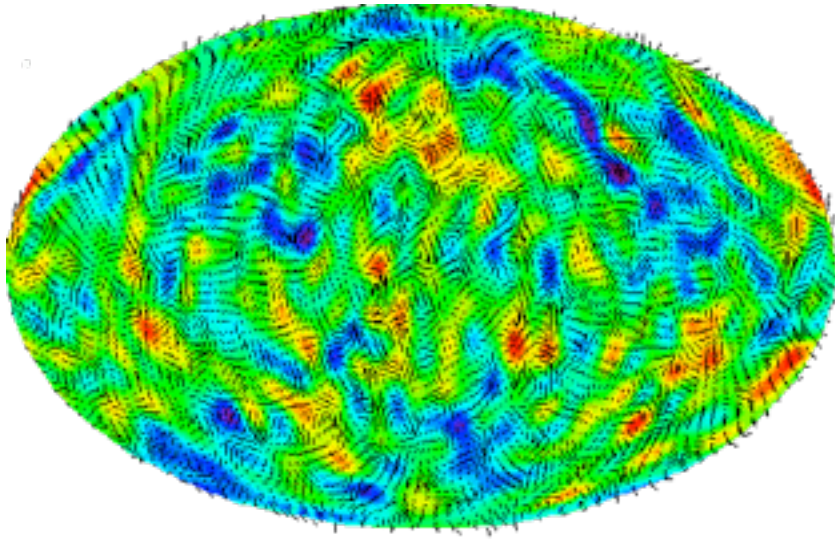
1998 SNIa result **2011 Nobel Prize**

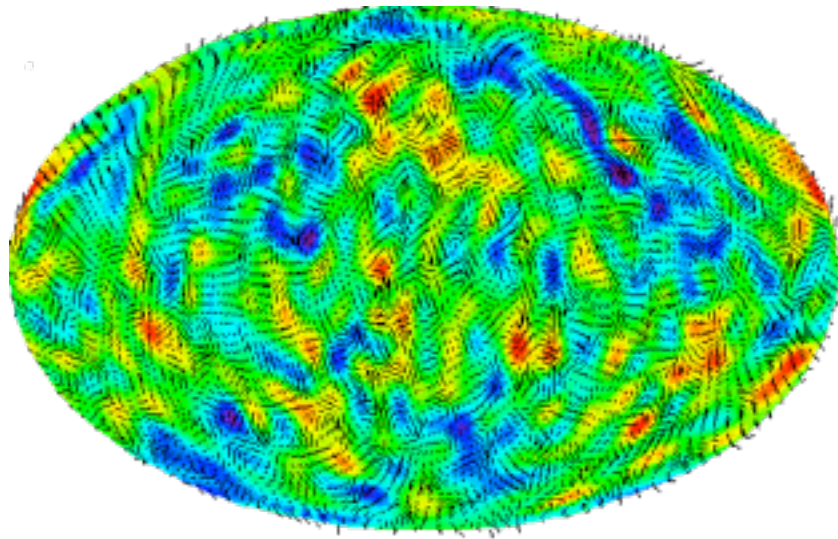


1992 COBE satellite result **2006 Nobel Prize**

1998 SNIa result **2011 Nobel Prize**

2001 launched WMAP Satellite



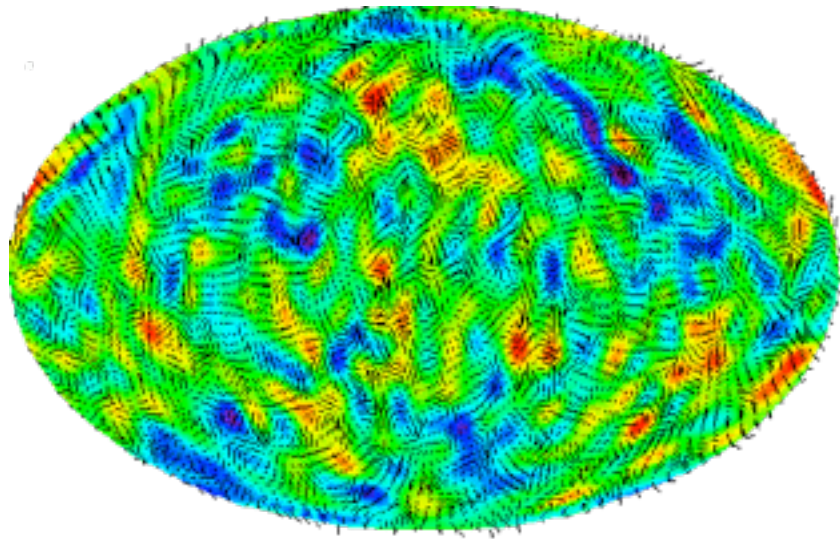


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WMAP Precision in measuring cosmological parameters has been improved to 10% even higher



**1992 COBE satellite result 2006 Nobel Prize**

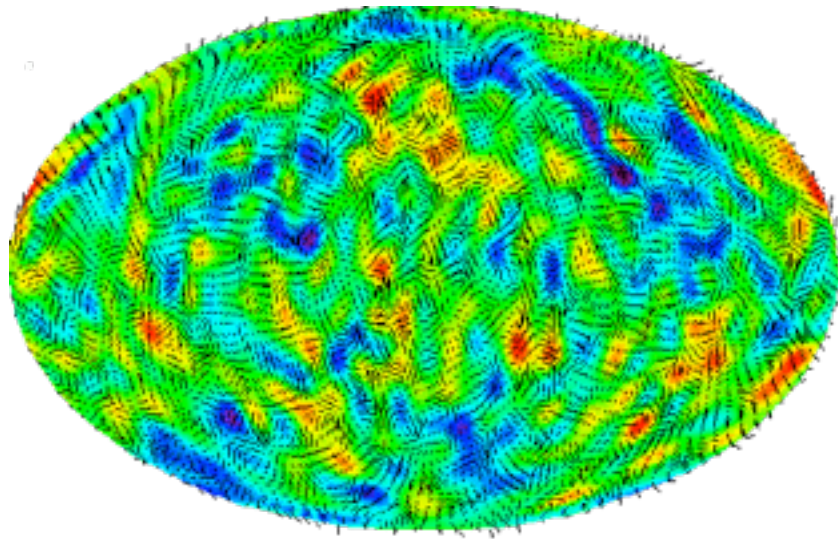
**1998 SNIa result 2011 Nobel Prize**

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**WMAP Precision in measuring cosmological parameters has been improved to 10% even higher**

**HST result on Hubble constant, Weak lensing measurement etc.**





**1992 COBE satellite result 2006 Nobel Prize**

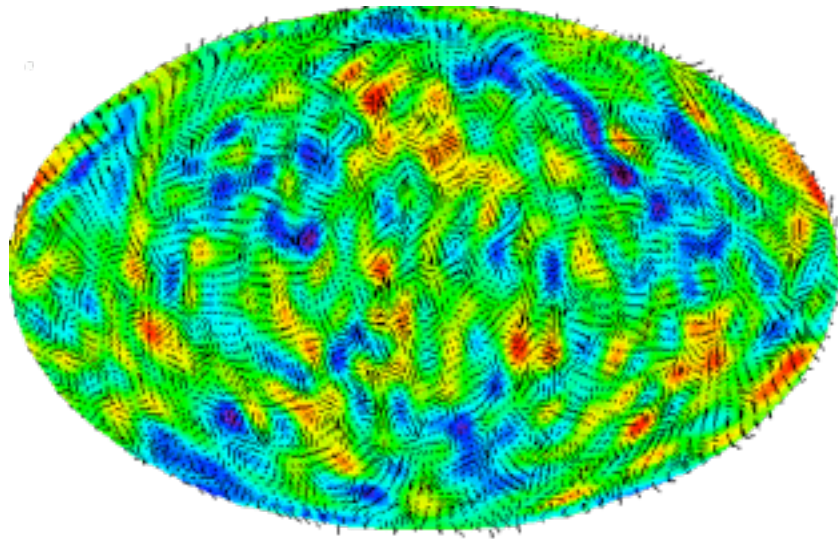
**1998 SNIa result 2011 Nobel Prize**

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**WMAP Precision in measuring cosmological parameters has been improved to 10% even higher**

**HST result on Hubble constant, Weak lensing measurement etc.**

**2009 launched PLANCK Satellite**



1992 COBE satellite result **2006 Nobel Prize**

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WMAP Precision in measuring cosmological parameters has been improved to 10% even higher

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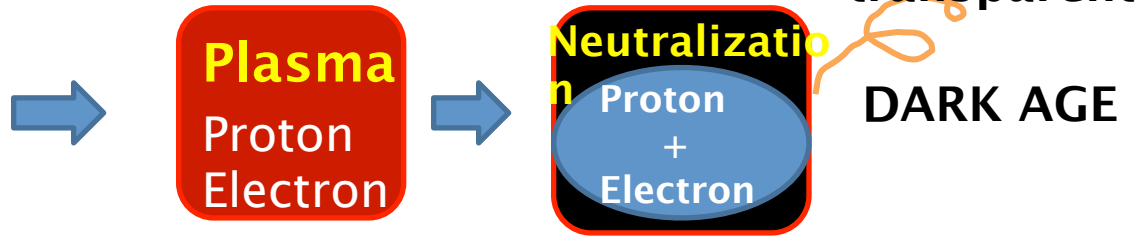
2009 launched PLANCK Satellite

# Precision Cosmology

# Problems in Cosmology

## 1. Reionization time

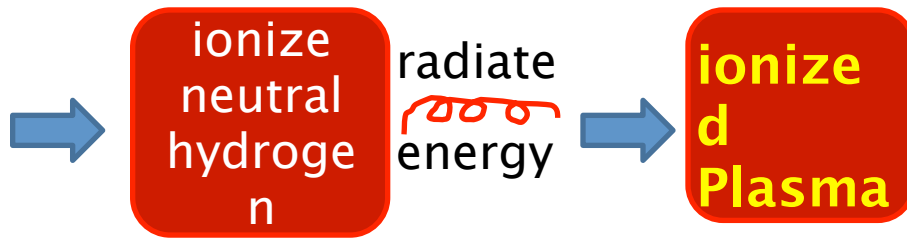
The first phase change of hydrogen in the universe



CMB  
↑  
Photons

The second phase change of hydrogen in the universe

objects started to form in the early universe



Reionization

$6 < z < 20$ , exactly what

Important to the formation of stars, galaxies etc.

## Observing the Reionization

**CMB:** ionized free electrons scatter photons, secondary anisotropies. WMAP:

$z \sim 11$   
**Quasars:** brightest objects, energy absorbed by neutral hydrogen, Lyman transition

**Gunn-Peterson trough**

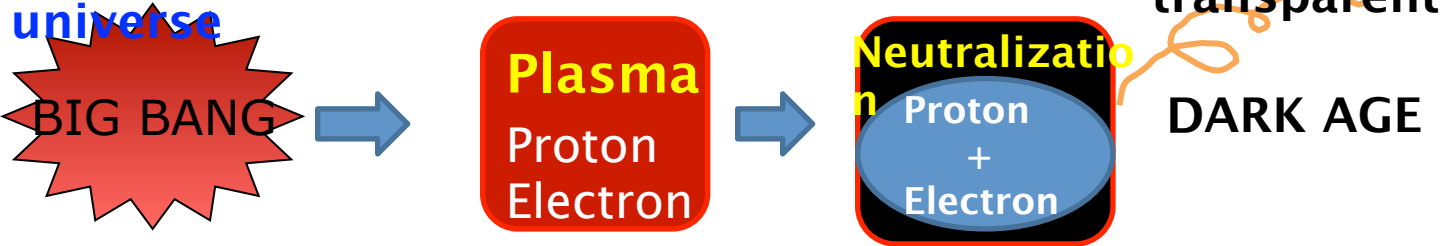
SDSS:  $z \sim 6$



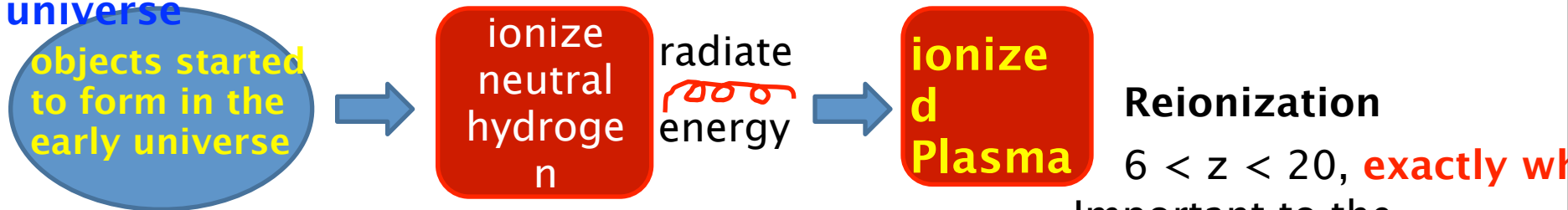
# Problems in Cosmology

## 1. Reionization time

The first phase change of hydrogen in the universe



The second phase change of hydrogen in the universe



### Observing the Reionization

**CMB:** ionized free electrons scatter photons, secondary anisotropies. WMAP:

**Quasars:**  $z \sim 11$  brightest objects, energy absorbed by neutral hydrogen, Lyman transition

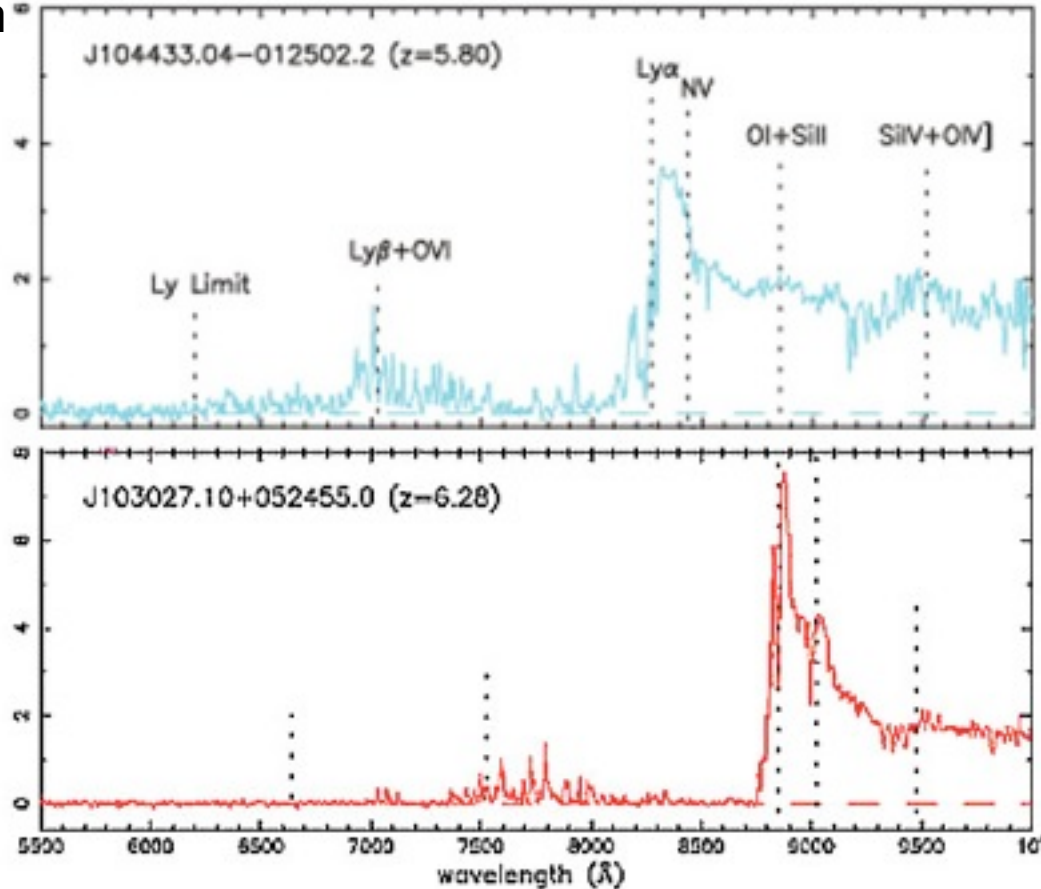
**Gunn-Peterson trough**

SDSS:  $z \sim 6$



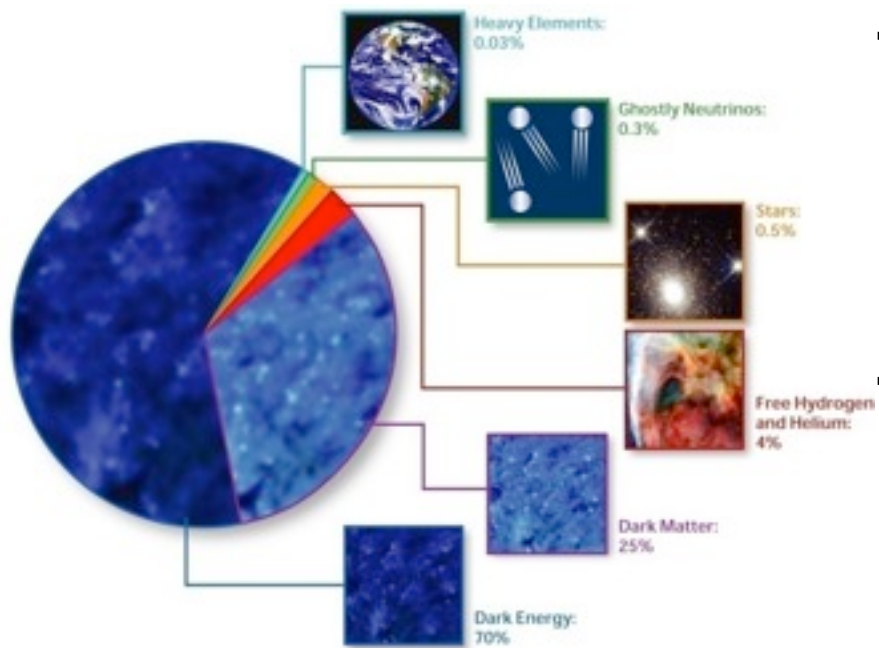
# Gunn–Peterson trough in the quasar's spectrum

Quasars below a certain redshift will not show the Gunn–Peterson trough



quasars above  $z = 6$  showed a Gunn–Peterson trough, indicating that the IGM was still at least partly neutral. The end of reionization around  $z=6$ .

## 2. Missing baryons



4-5% Baryons of total contents of the universe

**50% baryons missing. WHY???**

Direct measurement in local universe:

Stars  
Interstellar medium  
Intercluster medium

Structure formation model: Majority of baryons in IGM,

- hot ( $10^5\text{k} \sim 10^7\text{k}$ ), ionized, transparent to Lyman-alpha radiation, hard to trace by Lyman-alpha forest

- Not too hot, x-ray weak

# Is TSZ effective to answer the above two problems?

The intensity of TSZ  $\sim n_e$  of free electrons,  $T$ ,

1. **Missing baryons:** likely in less dense region with lower  $T$   
**TSZ effect is limited in answering the missing baryon problem.**
2. **Reionization:** must know information about the fraction and dynamics of free electrons at high redshift  $z \sim 10$   
Lyman-alpha forest — effective to detect the last reionization

At high redshift  $T$  is high, small change of  $n_e$  can result in the TSZ

if we compare with usual CMB  
**TSZ has the possibility to disclose the onset of the Reionization**

# Is KSZ effective to answer the above two problems?

The intensity of TSZ  $\sim n_e$  of free electrons,  $v_p$

1. **Missing baryons:** likely in less dense region with lower T, but with  $n_e$  of free electrons,  $v_p$   
**KSZ effect is possible in answering the missing baryon problem.**
2. **Reionization:** since the peculiar velocity three times the LCDM prediction in IGM from Planck, if the onset of Reionization happens at small redshift with low T,

**KSZ has the possibility to disclose the onset of the Reionization**