### Supersymmetrizing Massive Gravity

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### Outline

- Motivation
- Forming matter action
- Coupling to Supergravity
- Main results
- Summary

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- Forming massive gravity via Higgs mechanism (by Chamseddine and Mukhanov)
- Four scalar fields with global Lorentz symmetry coupled to gravity
- Scalar fields taking a vacuum expectation value breaking diffeomorphism invariance spontaneously
- Result massive graviton

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# FOUR CHIRAL SUPERFIELDS

• Consider four N = 1 chiral superfields with global Lorentz symmetry

 $\overline{D}_{\dot{\alpha}}\Phi^{A}\left(x,\theta,\overline{\theta}\right)=0$ 

• Given by

$$\Phi_{A} = \varphi_{A} + i(\theta\sigma^{\mu}\bar{\theta})\partial_{\mu}\varphi_{A} - \frac{1}{4}\theta\theta\bar{\theta}\bar{\theta}\partial_{\mu}\partial^{\mu}\varphi_{A} + \sqrt{2}\theta\psi_{A}$$
$$- \frac{i}{\sqrt{2}}\theta\theta\left(\partial_{\mu}\psi_{A}\sigma^{\mu}\bar{\theta}\right) + \theta\theta F_{A}$$

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### **BASIC FIELD**

- In bosonic case:  $H_{AB} = g^{\mu\nu} \partial_{\mu} \phi_A \partial_{\nu} \phi_B$
- Our case: Define *H*<sub>ABC</sub> as the basic field

$$H_{ABC} = D^{\alpha} \Phi_A(\sigma_B)_{\alpha \dot{\alpha}} \bar{D}^{\dot{\alpha}} \Phi_C^* = D \Phi_A \sigma_B \bar{D} \Phi_C^*$$
(1)

• Work instead with  $\overline{H}_{ABC} = H_{ABC} - Dx_A \sigma_B \overline{D} x_C^*$  to avoid including higher order terms

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## FORMING OUR ACTION

- Using this H<sub>ABC</sub> construct D-type terms to form the matter multiplets (H<sub>ABC</sub>H<sub>BCA</sub>,..)
- Couple to the Supergravity Lagrangian using the rules of tensor calculus.

$$L_{S.G} = -\frac{e}{2\kappa^2}R(e,w) - \frac{e}{3}|u|^2 + \frac{e}{3}A_{\mu}A^{\mu} - \frac{1}{2}\bar{\phi}_{\mu}R^{\mu}$$
(2)

- Lagrangian field content:
  - spin-2 field, *e*<sub>aµ</sub>
  - spin-3/2 field,  $\phi_{\mu}$
  - auxiliary fields *u*, *A*<sub>μ</sub>

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# COUPLING VETOR MULTIPLET TO SUPERGRAVITY

### Vector multiplet

$$V = (C, \xi, M, V_{\mu}, \lambda, D)$$
(3)

D-type multiplet action formula

$$e^{-1}L_{D} = D + \frac{i\kappa}{2}\bar{\phi}_{\mu}\gamma^{5}\gamma^{\mu}\lambda - \frac{\kappa}{3}(uM^{*} + u^{*}M) + \frac{i\kappa^{2}}{8}\epsilon^{\mu\nu\rho\sigma}\bar{\phi}_{\mu}\gamma_{\nu}\phi_{\rho}\bar{\xi}\phi_{\sigma}$$
$$+ \frac{2}{3}\kappa V_{\mu}\left(A^{\mu} + \frac{3}{8}ie^{-1}\epsilon^{\mu\rho\sigma\tau}\bar{\phi}_{\rho}\gamma_{\tau}\phi_{\sigma}\right) - i\frac{\kappa}{3}e^{-1}\bar{\xi}\gamma_{5}\gamma_{\mu}R^{\mu}$$
$$- \frac{2}{3}\kappa^{2}Ce^{-1}L_{S.G.} + e^{-1}L_{S.G.}$$
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 [P. Nath and R. Arnowitt and A. Chamseddine: Applied N=1 Supergravity, World Scientific Publishing, (1984)]

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### WHAT WE WANT?

• Expanding the fields around the vacuum solution

$$\varphi^{\mathcal{A}} = \mathbf{x}^{\mathcal{A}} + \chi^{\mathcal{A}}, \qquad \mathbf{e}^{\mu}_{\mathcal{A}} = \delta^{\mu}_{\mathcal{A}} + \bar{\mathbf{e}}^{\mu}_{\mathcal{A}},$$

An action with the following required conditions

- A Fierz-Pauli term for the vierbeins ( $\bar{e}^{\mu}_{A}\bar{e}^{A}_{u}-\bar{e}^{2}$
- No linear vierbein term

$$\left(\partial_{\mu}\chi_{A}\partial^{\mu}\chi^{A*} - \partial_{A}\chi^{A}\partial_{B}\chi^{B*}\right) \tag{6}$$

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where *I* is a constant

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### MATTER ACTION

### • First four conditions well satisfied with three D-type terms:

- НаввНсса
- $\bar{H}_{AB}\bar{H}^*_{AB}$  where  $H_{AB}=D\Phi_A D\Phi_B$
- Gravitino massive by adding two F-type terms and coupling them to supergravity:
  - $\bar{D}^2 \left( D \Phi_A \sigma^{AB} D \Phi_B \right)$
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# COUPLING CHIRAL MULTIPLET TO SUPERGRAVITY

• Chiral multiplet (F-type)

$$F = (z, X_L, h) \tag{8}$$

- Complex scalar field z
- Left-handed Weyl spinors X<sub>L</sub>
- Complex auxiliary field h
- Action formula

$$e^{-1}L_F = h + \kappa uz + \kappa \bar{\phi}_{\mu} \gamma^{\mu} \chi + i\kappa^2 \bar{\phi}_{\mu} \gamma^{\mu\nu} \phi_{\nu R} z + h.c.$$
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#### Main Results

# MAIN RESULTS

### Global supersymmetry promoted to a local one using the rules of tensor calculus

- Scalar components of the chiral multiplets φ<sub>A</sub> acquired a vacuum expectation value
- $\bullet \rightarrow$  Diffeomorphism invariance and local supersymmetry broken spontaneously

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  - Scalar fields  $\chi_A \rightarrow$  vectors
  - Chiral spinors  $\psi_A \rightarrow \text{spin-3/2}$  Rarita-Schwinger fields
- Spectrum of the model in the broken phase:
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# • Counting degrees of freedom: supergravity coupled to a N = 1 supersymmetry model similar to the Wess-Zumino model

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- one massless spin-2 graviton (two bosonic dof)
- one massless spin-3/2 gravitino (two fermionic dof)

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- *N* = 1 supersymmetry model:
  - Four spin-0 particles, φ<sup>A</sup>, with only six degrees of freedom (3 times 2) since φ<sup>0</sup> decouples due to Fierz-Pauli choice
  - Six fermionic degrees of freedom forming a multiplet
- Overall eight fermionic degrees of freedom and eight bosonic degrees of freedom

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# DEGREES OF FREEDOM: AFTER COUPLING

### • After coupling to supergravity: *N* = 1 massive representation

### Bosonic degrees of freedom

- A massive spin-2 particle, with five degrees of freedom
- A massive vector field (spin-1 particle), three degrees of freedom

### Overall eight bosonic degrees of freedom

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## DEGREES OF FREEDOM: AFTER COUPLING

### • Fermionic degrees of freedom

- Two massive spin-3/2 particles,  $\phi_{\mu}$  and  $\psi_{\rm A}$  with four degrees of freedom each
- Overall eight fermionic degrees of freedom
- Same number of degrees of freedom as before coupling

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### • Constructed a supersymmetric theory of massive gravity

- Coupled a pure Supergravity multiplet to a matter multiplet
- Left with two massive spin-3/2 particles,  $\phi_{\mu}$  and  $\psi_{A}$  with completely different masses
- Similar to the N = 2 supersymmetry in which we have two gravitinos, but there they have the same mass.

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