

$$g_{\mu\nu} = a^2(\eta) \text{diag}[-1, 1, 1, 1] + \delta a^2(\eta) g_{\mu\nu}^{(1)}$$