

$$A_{-} = A_{-}^0 \cosh(\beta_k \eta) + \tilde{A}_{-}^0 \sinh(\beta_k \eta) + \Xi[H, \beta, \tilde{J}_{-}, \eta]$$