

ATOMKI NUCLEAR ANOMALIES AND (B-L)



Based on [JHEP 04 \(2024\) 003](#)

In collaboration with:

Pedro Ferreira (CFTC/ISEL) and
Bernardo Gonçalves (CFTP-IST/CFTC)

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CFTP-IST, Univ. of Lisbon



Workshop on the Standard Model and Beyond
Corfu, Greece
25 August – 4 September

The ATOMKI Anomaly(ies) : Brief overview

PRL 116, 042501 (2016)

PHYSICAL REVIEW LETTERS

week ending
29 JANUARY 2016

Observation of Anomalous Internal Pair Creation in ${}^8\text{Be}$: A Possible Indication of a Light, Neutral Boson

A. J. Krasznahorkay,^{*} M. Csatlós, L. Csige, Z. Gácsi, J. Gulyás, M. Hunyadi, I. Kuti, B. M. Nyakó, L. Stuhl, J. Timár, T. G. Tornyai, and Zs. Vajta

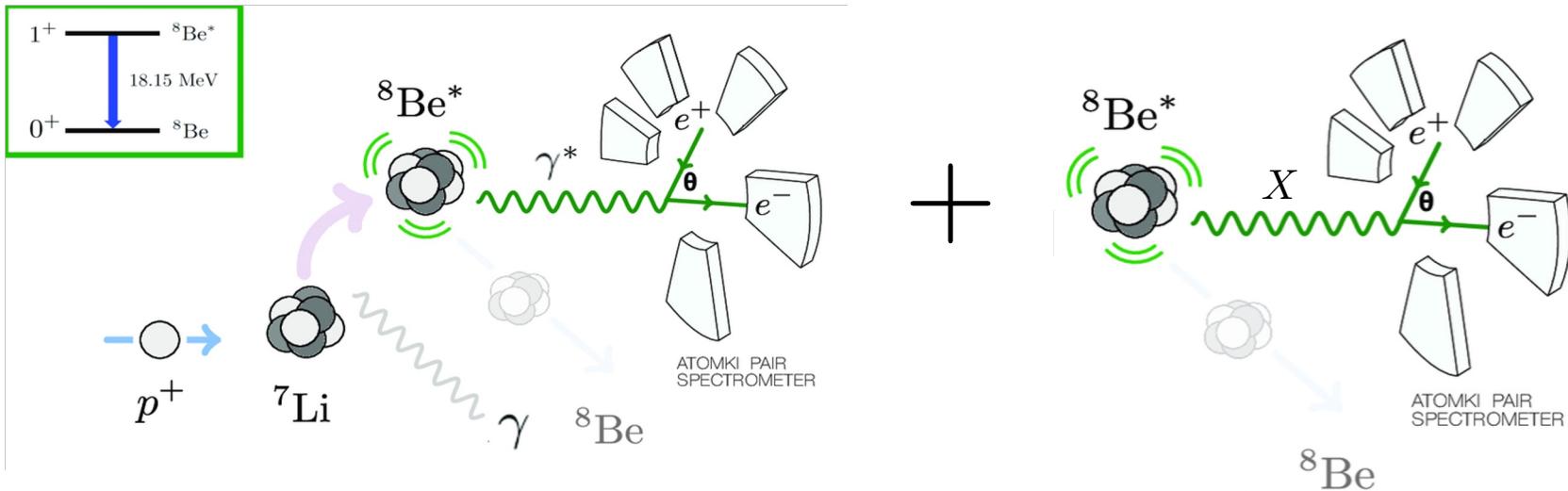
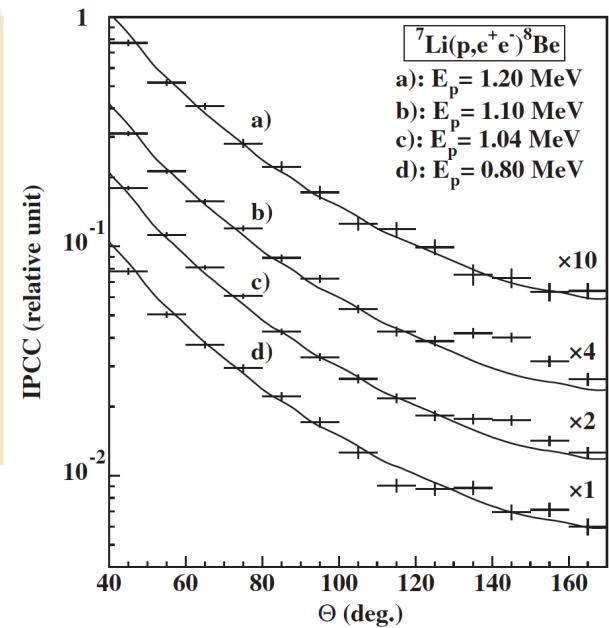
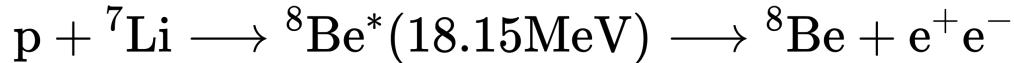
Institute for Nuclear Research, Hungarian Academy of Sciences (MTA Atomki), P.O. Box 51, H-4001 Debrecen, Hungary

T. J. Ketel

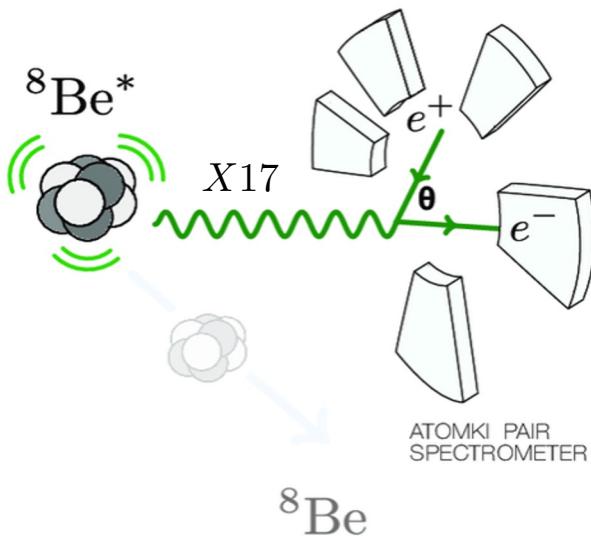
Nikhef National Institute for Subatomic Physics, Science Park 105, 1098 XG Amsterdam, Netherlands

A. Krasznahorkay

CERN, CH-1211 Geneva 23, Switzerland and Institute for Nuclear Research, Hungarian Academy of Sciences (MTA Atomki), P.O. Box 51, H-4001 Debrecen, Hungary



The ATOMKI Anomaly(ies) : Brief overview



our knowledge, no nuclear physics related description of such deviation can be made. The deviation between the experimental and theoretical angular correlations is significant and can be described by assuming the creation and subsequent decay of a $J^\pi = 1^+$ boson with mass $m_X c^2 = 16.70 \pm 0.35(\text{stat}) \pm 0.5(\text{syst}) \text{ MeV}$. The branching ratio of the e^+e^- decay of such a boson to the γ decay of the 18.15 MeV level of ${}^8\text{Be}$ is found to be 5.8×10^{-6} for the best fit.

$$m_X c^2 = 16.70 \pm 0.35(\text{stat}) \pm 0.5(\text{syst}) \text{ MeV}$$

PRL 117, 071803 (2016)

PHYSICAL REVIEW LETTERS

week ending
12 AUGUST 2016

Protophobic Fifth-Force Interpretation of the Observed Anomaly in ${}^8\text{Be}$ Nuclear Transitions

Jonathan L. Feng,¹ Bartosz Fornal,¹ Iftah Galon,¹ Susan Gardner,^{1,2} Jordan Smolinsky,¹ Tim M. P. Tait,¹ and Philip Tanedo¹

¹Department of Physics and Astronomy, University of California, Irvine, California 92697-4575, USA

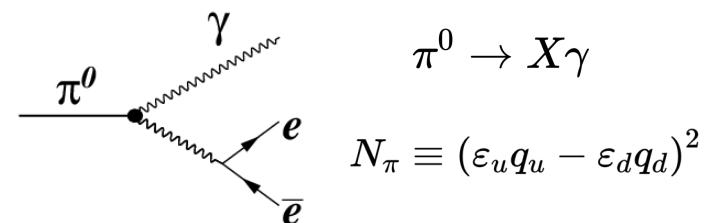
²Department of Physics and Astronomy, University of Kentucky, Lexington, Kentucky 40506-0055, USA

(Received 3 May 2016; published 11 August 2016)

Recently a 6.8σ anomaly has been reported in the opening angle and invariant mass distributions of e^+e^- pairs produced in ${}^8\text{Be}$ nuclear transitions. The data are explained by a 17 MeV vector gauge boson X that is produced in the decay of an excited state to the ground state, ${}^8\text{Be}^* \rightarrow {}^8\text{Be}X$, and then decays through $X \rightarrow e^+e^-$. The X boson mediates a fifth force with a characteristic range of 12 fm and has millicharged couplings to up and down quarks and electrons, and a proton coupling that is suppressed relative to neutrons. The protophobic X boson may also alleviate the current 3.6σ discrepancy between the predicted and measured values of the muon's anomalous magnetic moment.

DOI: 10.1103/PhysRevLett.117.071803

ATOMKI: $|\varepsilon_u + \varepsilon_d| \approx 3.7 \times 10^{-3}$



NA48/2: $|2\varepsilon_u + \varepsilon_d| < \varepsilon_{\max} = 8 \times 10^{-4}$

$$-0.067 < \frac{\varepsilon_p}{\varepsilon_n} < 0.078 \quad \text{"Protophobic" X17}$$

The ATOMKI Anomaly(ies) : Brief overview

PHYSICAL REVIEW C **104**, 044003 (2021)

New anomaly observed in ^4He supports the existence of the hypothetical X17 particle

A. J. Krasznahorkay , ^{1,*} M. Csatlós , L. Csige, ¹ J. Gulyás, ¹ A. Krasznahorkay , ^{1,†} B. M. Nyakó, ¹
I. Rajta, ¹ J. Timár , ¹ I. Vajda, ¹ and N. J. Sas²

¹Institute for Nuclear Research (ATOMKI), P.O. Box 51, H-4001 Debrecen, Hungary

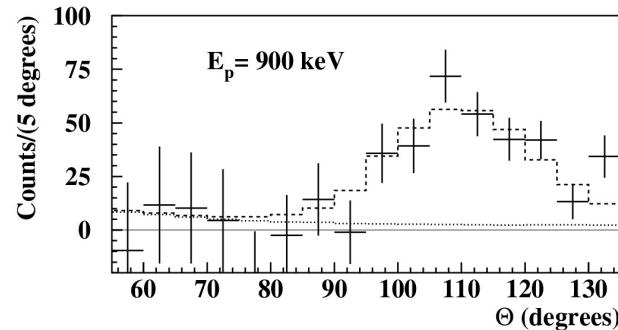
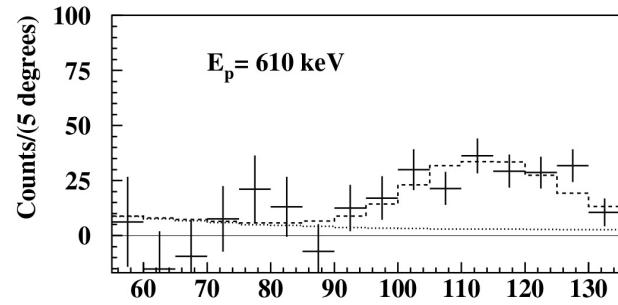
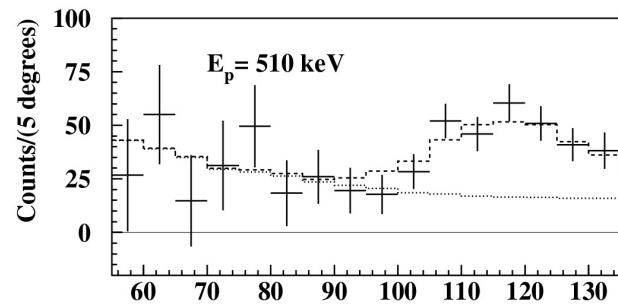
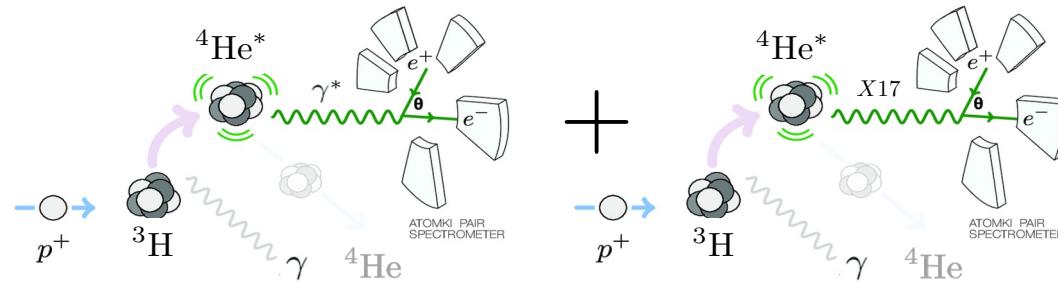
²University of Debrecen, 4010 Debrecen, PO Box 105, Hungary

(Received 27 October 2019; revised 30 June 2021; accepted 6 October 2021; published 18 October 2021)

Angular correlation spectra of e^+e^- pairs produced in the $^3\text{H}(p, e^+e^-)^4\text{He}$ nuclear reaction have been studied at $E_p = 510, 610$, and 900 keV proton energies. The main features of the spectra can be understood by taking into account the internal and external pair creations following the proton capture by ^3H . However, these processes cannot account for an observed peak around 115° in the angular correlation spectra. This anomalous excess of e^+e^- pairs can be described by the creation and subsequent decay of a light particle during the direct capture process. The derived mass of the particle is $m_Xc^2 = 16.94 \pm 0.12(\text{stat}) \pm 0.21(\text{syst})$ MeV. According to the mass this is likely the same X17 particle, which we recently suggested [Phys. Rev. Lett. **116**, 042501 (2016)] for describing the anomaly observed in the decay of ^8Be .

DOI: [10.1103/PhysRevC.104.044003](https://doi.org/10.1103/PhysRevC.104.044003)

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$$m_Xc^2 = 16.94 \pm 0.12_{\text{stat}} \pm 0.21_{\text{syst}} \text{ MeV}$$

Consistent with the ^8Be result !!

The ATOMKI Anomaly(ies) : Brief overview

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I. Rajta, ¹ J. Timár , ¹ I. Vajda, ¹ and N. J. Sas²

¹Institute for Nuclear Research (ATOMKI), P.O. Box 51, H-4001 Debrecen, Hungary

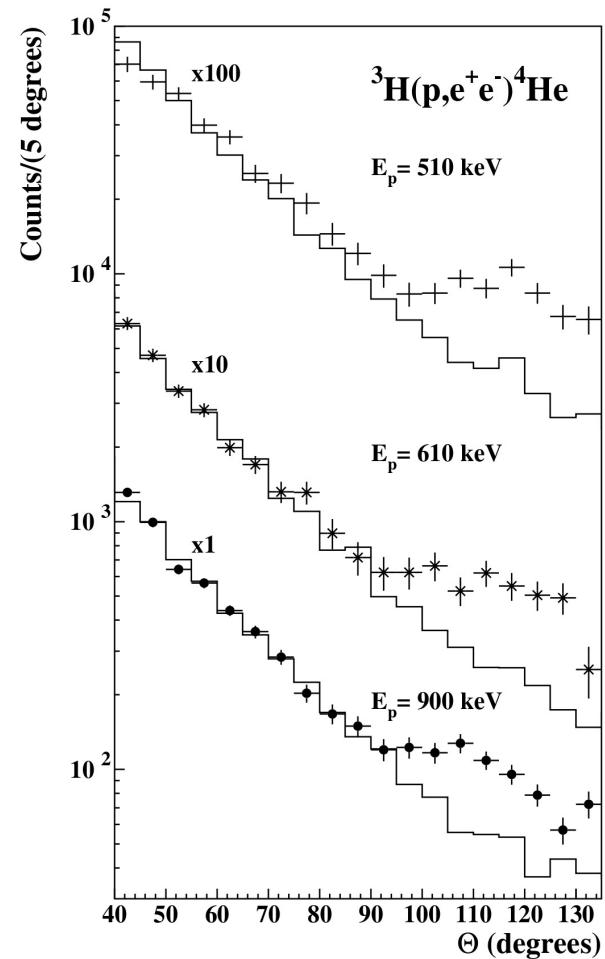
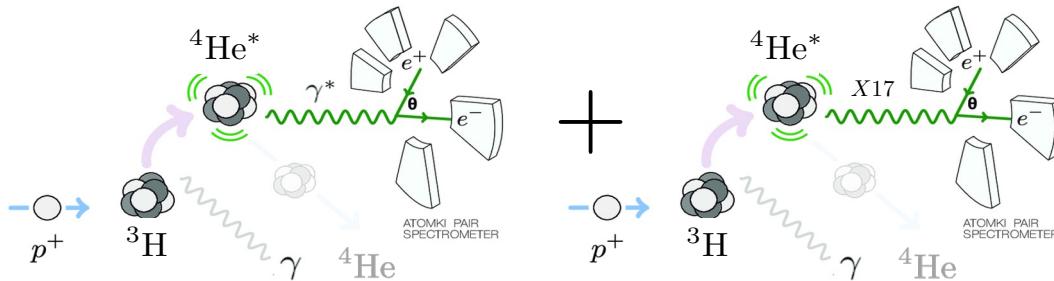
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Consistent with the ^8Be result !!

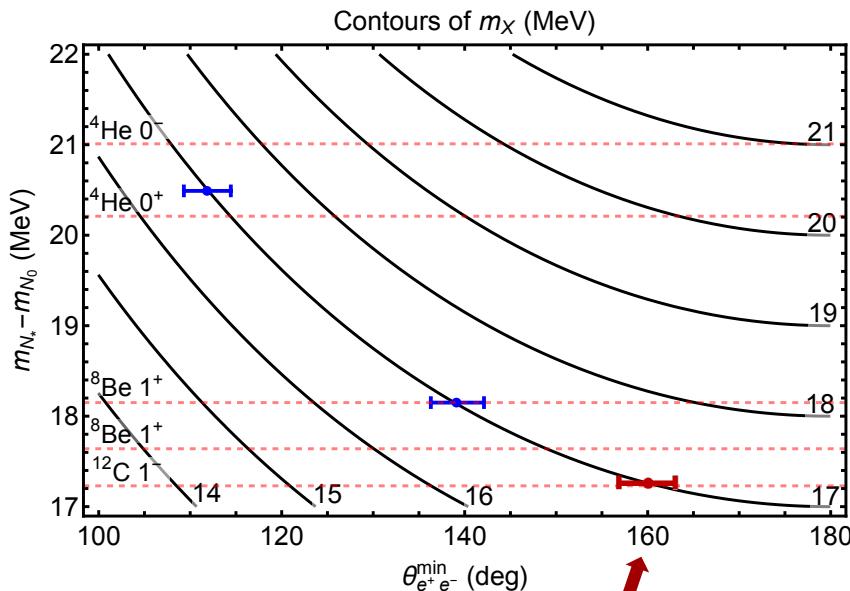
The ATOMKI Anomaly(ies) : Brief overview

PHYSICAL REVIEW D **102**, 036016 (2020)

Dynamical evidence for a fifth force explanation of the ATOMKI nuclear anomalies

Jonathan L. Feng^{●,*}, Tim M. P. Tait^{●,†}, and Christopher B. Verhaaren^{●,‡}

Department of Physics and Astronomy, University of California, Irvine, California 92697-4575, USA



$$\theta_{e^+e^-}^{\min} \simeq 2 \sin^{-1} \left(\frac{m_X}{m_{N_*} - m_{N_0}} \right)$$

$\theta_{e^+e^-}^{\min}(^{12}\text{C}) \simeq 160^\circ$

Feng et. al predict that for ^{12}C the should be seen at an angle **close to 160°** for X(17).

PHYSICAL REVIEW C **106**, L061601 (2022)

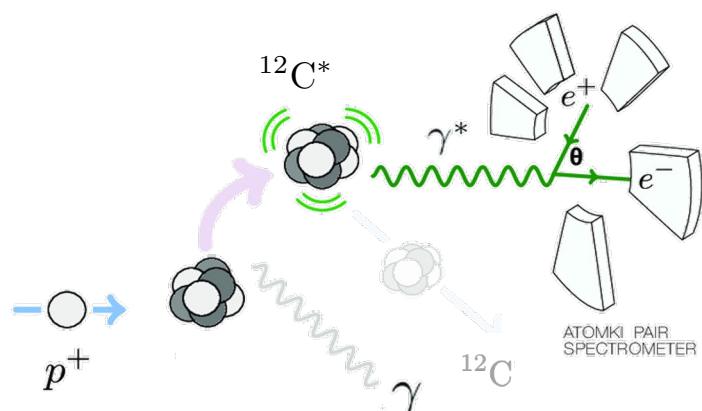
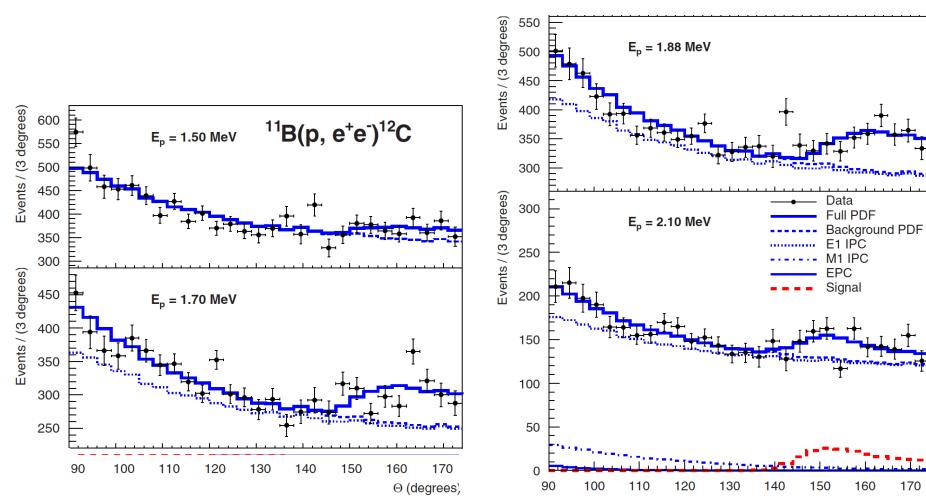
New anomaly observed in ^{12}C supports the existence and the vector character of the hypothetical X17 boson

A. J. Krasznahorkay^{●,*}, A. Krasznahorkay[†], M. Begala, M. Csatlós[●], L. Csige[●], J. Gulyás, A. Krakó, J. Timár, I. Rajta, and I. Vajda[●]

Institute for Nuclear Research (ATOMKI), P.O. Box 51, H-4001 Debrecen, Hungary

N. J. Sas

University of Debrecen, Faculty of Science and Technology, Physics Institute, 4010 Debrecen, PO Box 105, Hungary



The ATOMKI Anomaly(ies) : Protophobic

Confirmation (?) with a similar experiment at VNU.

universe

MDPI

Article

Checking the ${}^8\text{Be}$ Anomaly with a Two-Arm Electron Positron Pair Spectrometer

Tran The Anh ¹, Tran Dinh Trong ^{2,*}, Attila J. Krasznahorkay ³, Attila Krasznahorkay ³, József Molnár ³, Zoltán Pintye ³, Nguyen Ai Viet ¹, Nguyen The Nghia ^{1,*}, Do Thi Khanh Linh ⁴, Bui Thi Hoa ¹, Le Xuan Chung ⁴ and Nguyen Tuan Anh ⁵

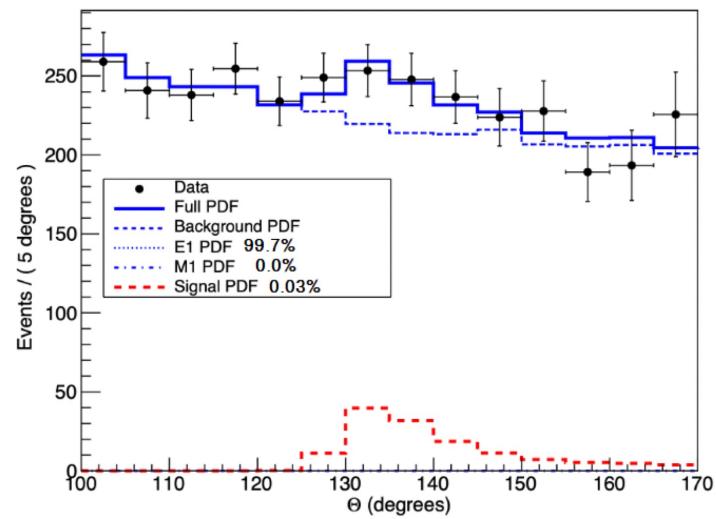
¹ Faculty of Physics, VNU-University of Science, 334 Nguyen Trai, Ha Noi 10000, Vietnam; ttanh@hus.edu.vn (T.T.A.); naviet@vnu.edu.vn (N.A.V.); buithihoa.k55@hus.edu.vn (B.T.H.)
² Institute of Physics, Vietnam Academy of Science and Technology, 18 Hoang Quoc Viet, Ha Noi 10000, Vietnam
³ Institute for Nuclear Research (HUN-REN ATOMKI), P.O. Box 51, H-4001 Debrecen, Hungary; kraszna@atomki.hu (A.J.K.); jmolan@atomki.hu (J.M.); pintye@atomki.hu (Z.P.)
⁴ Institute for Nuclear Science and Technology, VINATOM, 179 Hoang Quoc Viet, Ha Noi 10000, Vietnam; dtklinh@vinatom.gov.vn (D.T.K.L.); chungx@vinatom.gov.vn (L.X.C.)
⁵ Hanoi Irradiation Center, VINATOM, Cau Dien, Ha Noi 100000, Vietnam; nguyentuananh@chieuxa.vn

* Correspondence: tdtrong@iop.vast.vn (T.D.T.); nguyenthenghia@hus.edu.vn (N.T.N.)

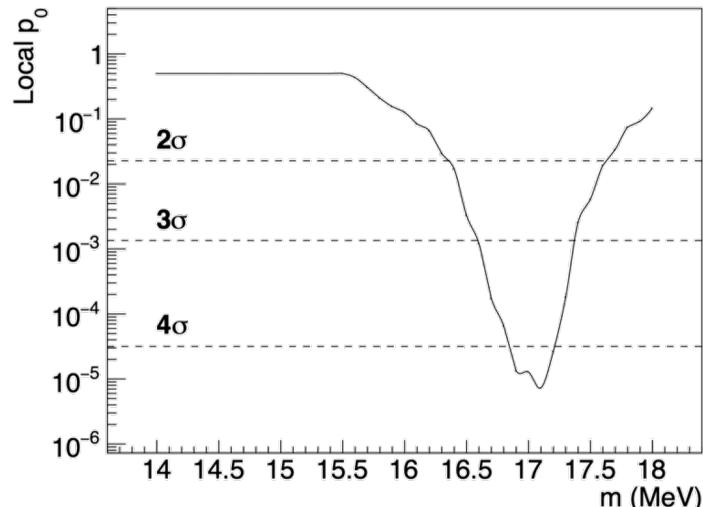
Received: 29 January 2024
Revised: 24 March 2024
Accepted: 29 March 2024
Published: 1 April 2024

4. Summary

We successfully built a two-arm e^+e^- spectrometer in Hanoi. The spectrometer was tested and calibrated using the 17.6 MeV M1 transition excited in the ${}^7\text{Li}(p,e^+e^-){}^8\text{Be}$ reaction. We have obtained a nice agreement between the experimentally determined acceptance of the spectrometer and the one coming from our simulation. The angular correlation of the e^+e^- pairs measured for the 17.6 MeV transition ($E_p = 441\text{keV}$) agrees well with the simulated one dominated by the M1 transition, and no anomaly was observed for this. However, a significant anomaly ($>4\sigma$) was observed for $E_p = 1225\text{ keV}$, which is the off-resonance region above the $E_p = 1040\text{ keV}$ resonance, at around 135° , in agreement with the ATOMKI results published in 2016 [1]. The mass of the hypothetical particle from this result was obtained to be 16.66 ± 0.47 (statistical) ± 0.35 (systematic) MeV. In the future, we plan to upgrade the spectrometer to obtain a wider angular acceptance.



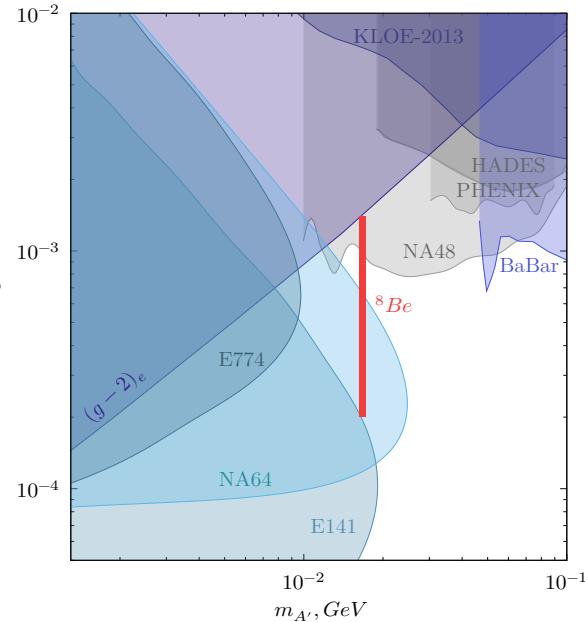
$$m_X = 16.7 \pm 0.47 \text{ (statistical)} \text{ (MeV)}$$



The ATOMKI Anomaly(ies) : Constraints

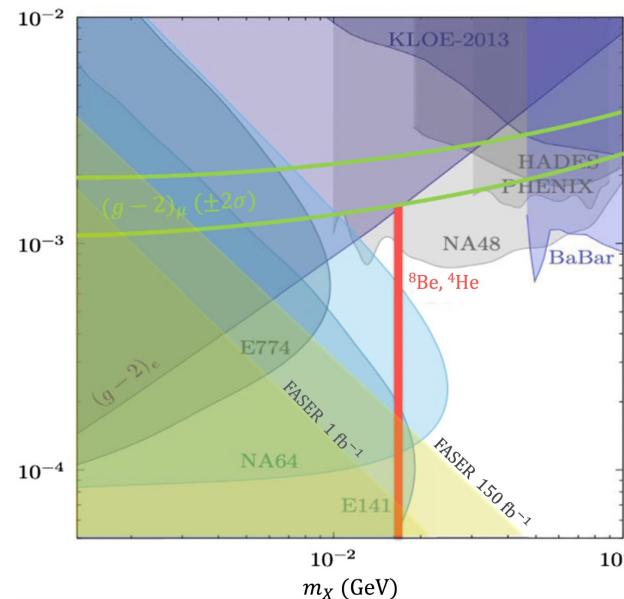
Protophobic vector boson X

[NA64 collab., PRD 101 \(2020\) 071101](#)



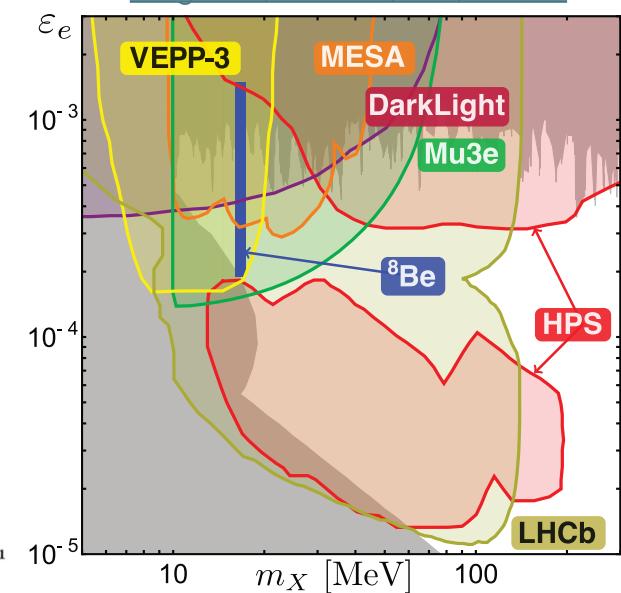
Protophobic vector boson X

[Alves et. al., Eur.Phys.J.C 83 \(2023\) 3](#)



Protophobic vector boson X

[Feng et al., PRL 117 \(2016\) 071803](#)



Very nice seminar at EPFL by M. Raggi. Available [here](#)

[Feng et all., PRD 102 \(2020\) 036016](#)

N_*	J_*^P	Scalar X	Pseudoscalar X	Vector X	Axial Vector X
$^8\text{Be}(18.15)$	1^+	...	$\mathcal{O}_{4P}^{(0)} (27)$	$\mathcal{O}_{5P}^{(1)} (37)$	$\mathcal{O}_{3S}^{(1)} (29), \mathcal{O}_{5D}^{(1)} (34)$
$^{12}\text{C}(17.23)$	1^-	$\mathcal{O}_{4P}^{(0)} (27)$...	$\mathcal{O}_{3S}^{(1)} (29), \mathcal{O}_{5D}^{(1)} (34)$	$\mathcal{O}_{5P}^{(1)} (37)$
$^4\text{He}(21.01)$	0^-	...	$\mathcal{O}_{3S}^{(0)} (39)$...	$\mathcal{O}_{4P}^{(1)} (40)$
$^4\text{He}(20.21)$	0^+	$\mathcal{O}_{3S}^{(0)} (39)$...	$\mathcal{O}_{4P}^{(1)} (40)$...

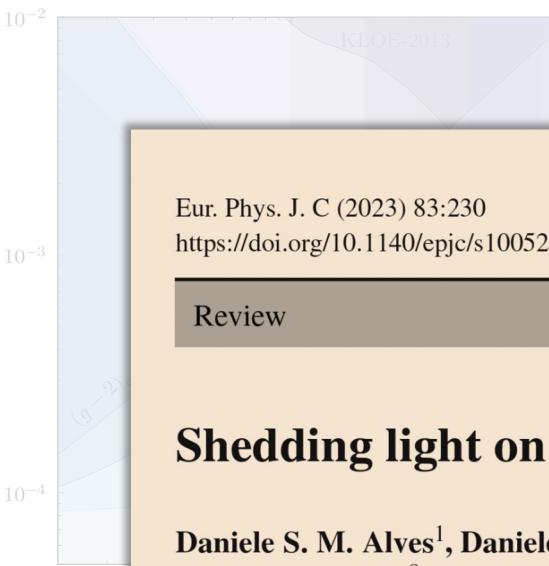
EFT for Nuclear
Transitions

$$\mathcal{L}_I = \sum_i c_i \mathcal{O}_i$$

The ATOMKI Anomaly(ies) : Constraints

Protophobic vector boson X

NA64 collab., PRD 101 (2020) 071101



Protophobic vector boson X

Alves et. al., Eur.Phys.J.C 83 (2023) 3



Protophobic vector boson X

Feng et al., PRL 117 (2016) 071803



Eur. Phys. J. C (2023) 83:230

<https://doi.org/10.1140/epjc/s10052-023-11271-x>

THE EUROPEAN
PHYSICAL JOURNAL C



Review

Shedding light on X17: community report

Daniele S. M. Alves¹, Daniele Barducci^{2,3}, Gianluca Cavoto^{2,3}, Luc Darmé⁴, Luigi Delle Rose^{5,6}, Luca Doria⁷, Jonathan L. Feng⁸, André Frankenthal⁹, Ashot Gasparian¹⁰, Evgeni Goudzovski¹¹, Carlo Gustavino³, Shaaban Khalil¹², Venelin Kozuharov¹³, Attila J. Krasznahorkay¹⁴, Tommaso Marchi¹⁵, Manuel Meucci^{2,3}, Gerald A. Miller¹⁶, Stefano Moretti¹⁷, Marco Nardecchia^{2,3}, Enrico Nardi¹⁸, Hugo Natal da Luz¹⁹, Giovanni Organtini^{2,3}, Angela Papa²⁰, Ann-Kathrin Perrevoort²¹, Vlasios Petousis¹⁹, Gabriele Piperno², Mauro Raggi^{2,3,a}, Francesco Renga³, Patrick Schwendimann²⁰, Rudolf Sýkora¹⁹, Claudio Toni^{2,3}, Paolo Valente³, Cecilia Voena³, Cheuk-Yin Wong²², Xilin Zhang²³

Feng et al.

N_*	$J_*^{P_*}$	Scalar X	Pseudoscalar X	Vector X	Axial Vector X
${}^8\text{Be}(18.15)$	1^+	...	$\mathcal{O}_{4P}^{(0)}$ (27)	$\mathcal{O}_{5P}^{(1)}$ (37)	$\mathcal{O}_{3S}^{(1)}$ (29), $\mathcal{O}_{5D}^{(1)}$ (34)
${}^{12}\text{C}(17.23)$	1^-	$\mathcal{O}_{4P}^{(0)}$ (27)	...	$\mathcal{O}_{3S}^{(1)}$ (29), $\mathcal{O}_{5D}^{(1)}$ (34)	$\mathcal{O}_{5P}^{(1)}$ (37)
${}^4\text{He}(21.01)$	0^-	...	$\mathcal{O}_{3S}^{(0)}$ (39)	...	$\mathcal{O}_{4P}^{(1)}$ (40)
${}^4\text{He}(20.21)$	0^+	$\mathcal{O}_{3S}^{(0)}$ (39)	...	$\mathcal{O}_{4P}^{(1)}$ (40)	...

EFT for Nuclear
Transitions

$$\mathcal{L}_I = \sum_i c_i \mathcal{O}_i$$

The ATOMKI Anomaly(ies) : Constraints

➤ VECTOR (V) AND AXIAL-VECTOR (A) Z' COUPLINGS TO FERMIONS:

General form: $\bar{f} \not{D} f \longrightarrow \mathcal{L} \supset e \bar{f}_a \gamma^\mu \left(\varepsilon_{ab}^V + \gamma^5 \varepsilon_{ab}^A \right) f_b Z'_\mu$

Couplings	Experimental range
ε_n^V	$2 \times 10^{-3} [4.1 \times 10^{-3}] \lesssim \varepsilon_n^V \lesssim 15 \times 10^{-3} [5.3 \times 10^{-3}]$
ε_p^V	$[0.7 \times 10^{-3}] \lesssim \varepsilon_p^V \lesssim 1.2 \times 10^{-3} [1.9 \times 10^{-3}]$
ε_{ee}^V	$0.4 \times 10^{-3} [0.63 \times 10^{-3}] \lesssim \varepsilon_{ee}^V \lesssim 2 \times 10^{-3} [1.2 \times 10^{-3}]$
ε_{ee}^A	$ \varepsilon_{ee}^A \lesssim 2.6 \times 10^{-9}$
$\varepsilon_{\nu_e \nu_e}^A$	$ \varepsilon_{\nu_e \nu_e}^A \lesssim 1.2 \times 10^{-5} [(3.5 - 4.5) \times 10^{-6}]$
$\varepsilon_{\nu_\mu \nu_\mu}^A$	$ \varepsilon_{\nu_\mu \nu_\mu}^A \lesssim 12.2 \times 10^{-5}$

[Hati, Kriewald, Orloff & Teixeira JHEP 07 \(2020\) 235](#)

[Denton and Gehrlein, PRD 108 \(2023\) 1, 015009](#)

What kind of **models** can accomodate these results?

The ATOMKI Anomaly(ies) : some (models)

PHYSICAL REVIEW D 96, 115024 (2017)

Explanation of the 17 MeV Atomki anomaly in a $U(1)'$ -extended two Higgs doublet model

Luigi Delle Rose,^{1,2} Shaaban Khalil,³ and Stefano Moretti^{1,2}



Available online at www.sciencedirect.com

ScienceDirect

NUCLEAR
PHYSICS B

Nuclear Physics B 919 (2017) 209–217

www.elsevier.com/locate/nuclphysb

Realistic model for a fifth force explaining anomaly
 ${}^8Be^* \rightarrow {}^8Be e^+ e^-$ decay

Pei-Hong Gu ^a, Xiao-Gang He ^{a,b,c,*}



PUBLISHED FOR SISSA BY SPRINGER

Atomki anomaly in gauged $U(1)_R$ symmetric model

Osamu Seto^{a,b} and Takashi Shimomura^c

Chinese Journal of Physics 71 (2021) 506–517

Contents lists available at ScienceDirect

Chinese Journal of Physics journal homepage: www.sciencedirect.com/journal/chinese-journal-of-physics

Check for updates

A Family-nonuniversal $U(1)'$ Model for Excited Beryllium Decays

Beyhan Puliç*

Department of Physics, Izmir Institute of Technology, Izmir, TR35430, Turkey



PUBLISHED FOR SISSA BY SPRINGER

Anomalies in 8Be nuclear transitions and $(g - 2)_{e,\mu}$: towards a minimal combined explanation

C. Hati,^a J. Kriewald,^b J. Orloff^b and A.M. Teixeira^b

[Feng et al., PRD 95 \(2017\) 035017](#)

PREPARED FOR SUBMISSION TO JHEP

HRI-RECAPP-2024-02

A 17 MeV pseudoscalar and the LSND, MiniBooNE and ATOMKI anomalies¹

Waleed Abdallah,^a Raj Gandhi,^b Tathgata Ghosh,^b Najimuddin Khan,^c Samiran Roy,^d and Subhojit Roy^e

PHYSICAL REVIEW D 95, 035017 (2017)

Particle physics models for the 17 MeV anomaly in beryllium nuclear decays

Jonathan L. Feng,^{1,*} Bartosz Fornal,¹ Iftah Galon,¹ Susan Gardner,^{1,2} Jordan Smolinsky,¹ Tim M. P. Tait,¹ and Philip Tanedo^{1,3}



PUBLISHED FOR SISSA BY SPRINGER



Explaining Atomki anomaly and muon $g - 2$ in $U(1)_X$ extended flavour violating two Higgs doublet model

Takaaki Nomura^a and Prasenjit Sanyal^{b,c}

The ATOMKI Anomaly(ies) : some (models)

PHYSICAL REVIEW D 96, 115024 (2017)

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Luigi Delle Rose,^{1,2} Shaaban Khalil,³ and Stefano Moretti^{1,2}

Available online at www.sciencedirect.com
ScienceDirect
Nuclear Physics B 919 (2017) 209–217
www.elsevier.com/locate/nuclphysb

NUCLEAR PHYSICS B

Realistic model for a fifth force explaining anomaly in ${}^8Be^* \rightarrow {}^8Be e^+ e^-$ decay

Pei-Hong Gu^a, Xiao-Gang He^{a,b,c,*}

JHEP

PUBLISHED FOR SISSA BY SPRINGER

Atomki anomaly in gauged $U(1)_R$ symmetric model

JHEP

PUBLISHED FOR SISSA BY SPRINGER

Anomalies in 8Be nuclear transitions and $(g - 2)_{e,\mu}$: towards a minimal combined explanation

Osamu Seto^{a,b} and Toshiaki Nomura^c

MOST OBVIOUS CHOICE: GAUGED $U(1)_{B-L}$...

Chinese Journal of Physics 71 (2021) 506–517

Contents lists available at ScienceDirect

Chinese Journal of Physics

journal homepage: www.sciencedirect.com/journal/chinese-journal-of-physics

A Family-nonuniversal $U(1)'$ Model for Excited Beryllium Decays

Beyhan Puliç*

Department of Physics, Izmir Institute of Technology, Izmir, TR35430, Turkey

Feng et all., PRD 95 (2017) 035017

PREPARED FOR SUBMISSION TO JHEP

HRI-RECAPP-2024-02

A 17 MeV pseudoscalar and the LSND, MiniBooNE and ATOMKI anomalies¹

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Particle physics models for the 17 MeV anomaly in beryllium nuclear decays

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JHEP

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Explaining Atomki anomaly and muon $g - 2$ in $U(1)_X$ extended flavour violating two Higgs doublet model

Takaaki Nomura^a and Prasenjit Sanyal^{b,c}

Vanilla (B-L) model : general structure

Vanilla B-L : SM + 3 RH N_R 's + 1 complex scalar S

Fields	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	Q_{B-L}
Vanilla $B - L$	$q_{iL} = (u_{iL}, d_{iL})^T$	3	2	1/6 1/3
	u_{iR}	3	1	2/3 1/3
	d_{iR}	3	1	-1/3 1/3
	$l_{iL} = (\nu_{iL}, e_{iL})^T$	1	2	-1/2 -1
	e_{iR}	1	1	-1 -1
	N_{iR}	1	1	0 -1
	Φ	1	2	1/2 0
	S	1	1	0 2

(Gauge) Lagrangian: $\mathcal{L} \supset -\frac{1}{4}\tilde{F}_{\mu\nu}\tilde{F}^{\mu\nu} - \frac{1}{4}\tilde{F}'_{\mu\nu}\tilde{F}'^{\mu\nu} + \frac{\epsilon_k}{2}\tilde{F}_{\mu\nu}\tilde{F}'^{\mu\nu}$

Kinetic mixing parameter ϵ_k constrained to be small by Z-pole measurements

Covariant derivative: $\tilde{D}_\mu = \partial_\mu + \dots + ig'Y_f\tilde{B}_\mu + ig_{B-L}Q_f^{B-L}\tilde{B}'_\mu$

Which can be brought to its final convenient form in terms of gauge boson mass eigenstates
 (see e.g. [Hati, Kriewald, Orloff & Teixeira JHEP 07 \(2020\) 235](#))

Vanilla (B-L) model : general structure

Bring to the canonical form

Redefinition of the gauge fields:

$$\tilde{B}_\mu = B_\mu + \frac{\epsilon_k}{\sqrt{1 - \epsilon_k^2}} B'_\mu , \quad \tilde{B}'_\mu = \frac{1}{\sqrt{1 - \epsilon_k^2}} B'_\mu$$

Redefinition of coupling constants:

$$\varepsilon' = \frac{\epsilon_k}{\sqrt{1 - \epsilon_k^2}}, \quad \varepsilon'_{B-L} = \frac{g_{B-L}}{\sqrt{1 - \epsilon_k^2}}$$

$$D_\mu = \partial_\mu + \cdots + igT_{3f}W_{3\mu} + ig'Y_fB_\mu + i\left(\varepsilon'g'Y_f + \varepsilon'_{B-L}Q_f^{B-L}\right)B'_\mu$$

➤ **GAUGE BOSON MASSES:** $\mathcal{L}_{\text{mass}}^{\text{gauge}} \supseteq (D_\mu\langle\Phi\rangle)^\dagger(D^\mu\langle\Phi\rangle) + (D_\mu\langle S\rangle)^\dagger(D^\mu\langle S\rangle)$

 $\langle\Phi\rangle = \begin{pmatrix} 0 \\ v/\sqrt{2} \end{pmatrix}, \quad \langle S\rangle = w/\sqrt{2}$  B' mass term: $m_{B'}^2 = 4\varepsilon'_{B-L}w^2$

 $\langle\Phi\rangle = \begin{pmatrix} 0 \\ v/\sqrt{2} \end{pmatrix}, \quad \langle S\rangle = w/\sqrt{2}$  B' mass term: $m_{B'}^2 = 4\varepsilon'_{B-L}w^2$

Physical gauge boson masses

$$M_A = 0, \quad M_{Z,Z'} = \frac{g}{\cos\theta_w} \frac{v}{2} \left[\frac{1}{2} \left(\frac{\varepsilon'^2 + 4m_{B'}^2/v^2}{g^2 + g'^2} + 1 \right) \mp \frac{g' \cos\theta_w \varepsilon'}{g \sin 2\theta'} \right]^{\frac{1}{2}}$$

Vanilla (B-L) model : general structure

Small kinetic mixing  $(\epsilon_k \ll 1)$

$$M_Z^2 \simeq \frac{g^2 + g'^2}{4} v^2, \quad M_{Z'}^2 \simeq m_{B'}^2, \quad \tan 2\theta' \simeq -2\varepsilon' \sin \theta_w$$

Covariant derivative in terms of physical gauge bosons

$$D_\mu \supset \partial_\mu + i \frac{g}{\cos \theta_w} (T_{3f} - \sin^2 \theta_W Q_f) Z_\mu + ieQ_f A_\mu + ie(\varepsilon Q_f + \varepsilon_{B-L} Q_f^{B-L}) Z'_\mu$$

$$\varepsilon = \varepsilon' \cos \theta_w, \quad e \varepsilon_{B-L} = \varepsilon'_{B-L}$$

➤ **SCALAR SECTOR:** $V_{\text{Higgs}} = \mu^2 |\Phi|^2 + m^2 |S|^2 + \frac{\lambda_1}{2} |\Phi|^4 + \frac{\lambda_2}{2} |S|^4 + \lambda_3 |\Phi|^2 |S|^2$

- In the limit of **small kinetic mixing**: $\langle S \rangle = w/\sqrt{2} \rightarrow m_{Z'} \simeq 2e|\varepsilon_{B-L}|w = 17 \text{ MeV}$

Two **CP-even** scalars h and χ with masses $m_{h,\chi}$ with $m_h = 125 \text{ GeV}$

- In terms of **scalar masses and mixing**:

$$\lambda_1 = \frac{1}{v^2} (c_\alpha^2 m_h^2 + s_\alpha^2 m_\chi^2), \quad \lambda_2 = \frac{1}{w^2} (s_\alpha^2 m_h^2 + c_\alpha^2 m_\chi^2), \quad \lambda_3 = \frac{1}{vw} (m_h^2 - m_\chi^2) s_\alpha c_\alpha$$

Vanilla (B-L) model : general structure

- Boundness from below and perturbative unitarity constraints :

[Coimbra, Sampaio & Santos, Eur.Phys.J.C 73 \(2013\) 2428](#)

$$0 < \lambda_{1,2} \leq 8\pi , \quad -\sqrt{\lambda_1 \lambda_2} < \lambda_3 \leq 8\pi , \quad |a_{\pm}| = \left| \frac{3}{2}\lambda_1 + \lambda_2 \pm \sqrt{\left(\frac{3}{2}\lambda_1 + \lambda_2\right)^2 + \lambda_2^2} \right| \leq 8\pi$$

$$\xrightarrow[c_\alpha = 1]{\lambda_1 \simeq m_h^2/v^2, \lambda_2 \simeq m_\chi^2/w^2} \frac{3}{2} \frac{m_h^2}{v^2} + \frac{m_\chi^2}{w^2} + \sqrt{\left(\frac{3}{2} \frac{m_h^2}{v^2} + \frac{m_\chi^2}{w^2}\right)^2 + \left(\frac{m_\chi^2}{w^2}\right)^2} \leq 8\pi, \quad w^{-2} = \frac{4e^2 \varepsilon_{B-L}^2}{m_{Z'}^2}$$

Lowest allowed value:
 $\varepsilon_{B-L} = 2 \times 10^{-3}$ \longrightarrow $m_\chi \lesssim \begin{cases} 45 \text{GeV}, c_\alpha = 1.0 \\ 34 \text{GeV}, c_\alpha = 0.97 \end{cases} < m_h/2 \longrightarrow h \rightarrow \chi\chi, Z'Z'$ are allowed

➤ VECTOR (V) AND AXIAL-VECTOR (A) Z' COUPLINGS TO FERMIONS:

General form: $\bar{f} \not{D} f \longrightarrow \mathcal{L} \supset e \bar{f}_a \gamma^\mu \left(\varepsilon_{ab}^V + \gamma^5 \varepsilon_{ab}^A \right) f_b Z'_\mu$

Vanilla (B-L) model vs ATOMKI

Couplings	Vanilla $B - L$	Experimental range
ε_n^V	ε_{B-L}	$2 \times 10^{-3} [4.1 \times 10^{-3}] \lesssim \varepsilon_n^V \lesssim 15 \times 10^{-3} [5.3 \times 10^{-3}]$
ε_p^V	$\varepsilon + \varepsilon_{B-L}$	$[0.7 \times 10^{-3}] \lesssim \varepsilon_p^V \lesssim 1.2 \times 10^{-3} [1.9 \times 10^{-3}]$
ε_{ee}^V	$-(\varepsilon + \varepsilon_{B-L})$	$0.4 \times 10^{-3} [0.63 \times 10^{-3}] \lesssim \varepsilon_{ee}^V \lesssim 2 \times 10^{-3} [1.2 \times 10^{-3}]$
ε_{ee}^A	0	$ \varepsilon_{ee}^A \lesssim 2.6 \times 10^{-9}$
$\varepsilon_{\nu_e \nu_e}^A$	ε_{B-L}	$ \varepsilon_{\nu_e \nu_e}^A \lesssim 1.2 \times 10^{-5} [(3.5 - 4.5) \times 10^{-6}]$
$\varepsilon_{\nu_\mu \nu_\mu}^A$	ε_{B-L}	$ \varepsilon_{\nu_\mu \nu_\mu}^A \lesssim 12.2 \times 10^{-5}$



[Hati, Kriewald, Orloff & Teixeira JHEP 07 \(2020\) 235](#)

[Denton and Gehrlein, PRD 108 \(2023\) 1, 015009](#)

HOW DO WE SUPPRESS THE Z' COUPLINGS TO NEUTRINOS?

SOLUTION: ADD VECTOR-LIKE LEPTONS!

[Feng et. all, PRD 95 \(2017\) 3, 035017](#)

[Hati, Kriewald, Orloff & Teixeira JHEP 07 \(2020\) 235](#)

(B-L) + VLLs model : general structure

(B-L) + VLLs: Vanilla (B-L) + 3 Doublet VLL pairs + 3 charged singlet VLL pairs

Fields	SU(3) _c	SU(2) _L	U(1) _Y	Q_{B-L}
$q_{iL} = (u_{iL}, d_{iL})^T$	3	2	1/6	1/3
u_{iR}	3	1	2/3	1/3
d_{iR}	3	1	-1/3	1/3
$l_{iL} = (\nu_{iL}, e_{iL})^T$	1	2	-1/2	-1
e_{iR}	1	1	-1	-1
N_{iR}	1	1	0	-1
Φ	1	2	1/2	0
S	1	1	0	2
$L_{iL,R} = (\mathcal{N}_{iL,R}, \mathcal{E}_{iL,R})^T$	1	2	-1/2	1
$E_{iL,R}$	1	1	-1	1

$i = 1, 2, 3$ ←

Lepton Yukawa and mass terms

$$\begin{aligned} \mathcal{L}_{\text{lepton}} = & -y_l^{ij} \overline{l_i L} \Phi e_{jR} - y_\nu^{ij} \overline{l_i L} \tilde{\Phi} N_{jR} - \frac{1}{2} y_M^{ij} S \bar{N}_{iR}^c N_{jR} - \lambda_L^{ij} S^* \overline{l_i L} L_{jR} - \lambda_E^{ij} S \overline{E_{iL}} e_{jR} \\ & - M_L^{ij} \overline{L_i L} L_{jR} - M_E^{ij} \overline{E_{iL}} E_{jR} - h^{ij} \overline{L_i} \Phi E_{jR} - k^{ij} \overline{E_{iL}} \Phi^\dagger L_{jR} + \text{H.c.}, i, j = 1, 2, 3 \end{aligned}$$

For simplicity, all Yukawa and mass matrices are considered **real and diagonal**.

(B-L) + VLLs model : general structure

- Charged- and neutral-lepton mass matrix (after SSB):

$$\mathcal{L}_{\text{c.l.}} = \overline{\psi_L^\ell} \mathcal{M}_\ell \psi_R^\ell + \text{H.c.}, \quad \psi_{\text{L,R}}^\ell = (e_{\text{L,R}}, \quad \mathcal{E}_{\text{L,R}}, \quad E_{\text{L,R}})^T$$

$$\mathcal{L}_{\text{n.l.}} = \overline{\psi_L^\nu} \mathcal{M}_\nu \psi_L^\nu + \text{H.c.}, \quad \psi_L^\nu = (\nu, \quad N^c, \quad \mathcal{N}, \quad \mathcal{N}^c)^T$$

Mass matrices

$$\mathcal{M}_\ell = \begin{pmatrix} y_l \frac{v}{\sqrt{2}} & \lambda_L \frac{w}{\sqrt{2}} & 0 \\ 0 & M_L & h \frac{v}{\sqrt{2}} \\ \lambda_E \frac{w}{\sqrt{2}} & k \frac{v}{\sqrt{2}} & M_E \end{pmatrix}, \quad \mathcal{M}_\nu = \begin{pmatrix} 0 & y_\nu \frac{v}{\sqrt{2}} & 0 & \lambda_L \frac{w}{\sqrt{2}} \\ y_\nu \frac{v}{\sqrt{2}} & y_M \frac{w}{\sqrt{2}} & 0 & 0 \\ 0 & 0 & 0 & M_L \\ \lambda_L \frac{w}{\sqrt{2}} & 0 & M_L & 0 \end{pmatrix}$$

Each entry is a 3×3 diagonal matrix with distinct $y_{l,\nu,M}^i, \lambda_{L,E}^i, M_{L,E}^i, k_i$ and h_i elements.

- Mass-eigenstate basis: $\mathcal{M}_\ell^{\text{diag}} = U_L^\dagger \mathcal{M}_\ell U_R$, $\mathcal{M}_\nu^{\text{diag}} = U_\nu^T \mathcal{M}_\nu U_\nu$

Three (four) charged (neutral) leptons ℓ_a (ν_a) for each family.

(B-L) + VLLs model : general structure

➤ **Z' couplings to (physical) fermions:** $\mathcal{L} \supset e \bar{f}_a \gamma^\mu \left(\varepsilon_{ab}^V + \gamma^5 \varepsilon_{ab}^A \right) f_b Z'_\mu$

Couplings	Vanila (B - L) + VLLs
ε_n^V	ε_{B-L}
ε_p^V	$\varepsilon + \varepsilon_{B-L}$
$\varepsilon_{\ell_a \ell_b}^{V(A)}$	$\frac{1}{2} \sum_{i=1}^3 (\varepsilon Q_i + \varepsilon_{B-L} Q_i^{B-L}) \left[(U_R^\dagger)_{ai} (U_R)_{ib} \pm (U_L^\dagger)_{ai} (U_L)_{ib} \right]$
$\varepsilon_{\nu_a \nu_b}^{V(A)}$	$\pm \frac{1}{2} \sum_{i=1}^{12} \varepsilon_{B-L} Q_i^{B-L} [(U_\nu^*)_{ia} (U_\nu)_{ib} \mp (U_\nu)_{ia} (U_\nu^*)_{ib}]$

$$Q_i^{B-L} = \{-1, +1, +1\}$$

$$Q_i = \{-1, -1, -1\}$$

$$Q_i^{B-L} = \{-1, -1, +1, +1\}$$

Comparing with what we have seen before:

Couplings	Experimental range
ε_n^V	$2 \times 10^{-3} [4.1 \times 10^{-3}] \lesssim \varepsilon_n^V \lesssim 15 \times 10^{-3} [5.3 \times 10^{-3}]$
ε_p^V	$[0.7 \times 10^{-3}] \lesssim \varepsilon_p^V \lesssim 1.2 \times 10^{-3} [1.9 \times 10^{-3}]$
ε_{ee}^V	$0.4 \times 10^{-3} [0.63 \times 10^{-3}] \lesssim \varepsilon_{ee}^V \lesssim 2 \times 10^{-3} [1.2 \times 10^{-3}]$
ε_{ee}^A	$ \varepsilon_{ee}^A \lesssim 2.6 \times 10^{-9}$
$\varepsilon_{\nu_e \nu_e}^A$	$ \varepsilon_{\nu_e \nu_e}^A \lesssim 1.2 \times 10^{-5} [(3.5 - 4.5) \times 10^{-6}]$
$\varepsilon_{\nu_\mu \nu_\mu}^A$	$ \varepsilon_{\nu_\mu \nu_\mu}^A \lesssim 12.2 \times 10^{-5}$

CAN $\varepsilon_{\nu\nu}$ BE
 NATURALLY
 SUPPRESSED?

(B-L) + VLLs model : $\varepsilon_{\nu_1 \nu_1}^A$ suppression (?)

➤ Z' couplings to neutrinos:

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & y_\nu \frac{v}{\sqrt{2}} & 0 & \lambda_L \frac{w}{\sqrt{2}} \\ y_\nu \frac{v}{\sqrt{2}} & y_M \frac{w}{\sqrt{2}} & 0 & 0 \\ 0 & 0 & 0 & M_L \\ \lambda_L \frac{w}{\sqrt{2}} & 0 & M_L & 0 \end{pmatrix} \xrightarrow{\frac{y_\nu v}{y_M w}, \frac{y_\nu v}{\lambda_L w}, \frac{y_\nu v}{M_L} \ll 1} U_\nu \simeq \begin{pmatrix} -\frac{1}{\sqrt{1+\Lambda_L^2}} & 0 & -\frac{1}{\sqrt{2}} \frac{\Lambda_L}{\sqrt{1+\Lambda_L^2}} & \frac{1}{\sqrt{2}} \frac{\Lambda_L}{\sqrt{1+\Lambda_L^2}} \\ 0 & 1 & 0 & 0 \\ \frac{\Lambda_L}{\sqrt{1+\Lambda_L^2}} & 0 & -\frac{1}{\sqrt{2}} \frac{1}{\sqrt{1+\Lambda_L^2}} & \frac{1}{\sqrt{2}} \frac{1}{\sqrt{1+\Lambda_L^2}} \\ 0 & 0 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

$\Lambda_L \equiv \frac{\lambda_L w}{\sqrt{2} M_L}$

THE A-V COUPLING TO NEUTRINOS IS NOW: $\varepsilon_{\nu_1 \nu_1}^A \simeq \varepsilon_{B-L} \left(\frac{1 - \Lambda_L^2}{1 + \Lambda_L^2} \right)$

Couplings	Vanilla $B - L +$ VLLs	Experimental range
ε_n^V	ε_{B-L}	$2 \times 10^{-3} [4.1 \times 10^{-3}] \lesssim \varepsilon_n^V \lesssim 15 \times 10^{-3} [5.3 \times 10^{-3}]$
$\varepsilon_{\nu_1 \nu_1}^A$	$\varepsilon_{B-L} \left(\frac{1 - \Lambda_L^2}{1 + \Lambda_L^2} \right)$	$ \varepsilon_{\nu_e \nu_e}^A \lesssim 1.2 \times 10^{-5} [3.5 - 4.5] \times 10^{-6}$

CONCLUSION: To suppress $\varepsilon_{\nu \nu}^A$ we must have: $\Lambda_L \equiv \frac{\lambda_L w}{\sqrt{2} M_L} \simeq 1$

$$\xrightarrow{\delta_L \ll 1} \frac{\varepsilon_{\nu_1 \nu_1}^A}{\varepsilon_n^V} \simeq \delta_L \lesssim 10^{-3}$$

There is no reason for this “tunning”...
(still, let us turn a blind eye on this detail)

(B-L) + VLLs model : $\varepsilon_{\nu_1 \nu_1}^A$ suppression (?)

➤ Z' couplings to charged leptons:

$$\mathcal{M}_\ell = \begin{pmatrix} y_l \frac{v}{\sqrt{2}} & \lambda_L \frac{w}{\sqrt{2}} & 0 \\ 0 & M_L & h \frac{v}{\sqrt{2}} \\ \lambda_E \frac{w}{\sqrt{2}} & k \frac{v}{\sqrt{2}} & M_E \end{pmatrix} \xrightarrow[h=k=0]{y_l v, y_l w \ll 1}$$

Coupling	Experimental range
ε_{ee}^A	$ \varepsilon_{ee}^A \lesssim 2.6 \times 10^{-9}$

With respect to the coupling with the neutron:

$$\delta_E = \Lambda_E - 1 \ll 1 \longrightarrow \left| \frac{\varepsilon_{\ell_1^\pm \ell_1^\mp}^A}{\varepsilon_n^V} \right| \simeq \delta_E / 2 \lesssim 10^{-6} \quad \text{!!!!}$$

BOTTOM-LINE CONCLUSION: $\Lambda_{L,E} \equiv \frac{\lambda_{L,E} w}{\sqrt{2} M_{L,E}} \simeq 1$

Let's just accept this and move on...

Ferreira, Gonçalves & FRJ, JHEP 04 (2024) 003

$$U_L \simeq \begin{pmatrix} \frac{1}{\sqrt{1+\Lambda_L^2}} & \frac{\Lambda_L}{\sqrt{1+\Lambda_L^2}} \\ -\frac{\Lambda_L}{\sqrt{1+\Lambda_L^2}} & \frac{1}{\sqrt{1+\Lambda_L^2}} \\ 0 & 0 & 1 \end{pmatrix}$$

$$U_R \simeq \begin{pmatrix} \frac{1}{\sqrt{1+\Lambda_E^2}} & 0 & \frac{\Lambda_E}{\sqrt{1+\Lambda_E^2}} \\ 0 & 1 & 0 \\ -\frac{\Lambda_E}{\sqrt{1+\Lambda_E^2}} & 0 & \frac{1}{\sqrt{1+\Lambda_E^2}} \end{pmatrix}$$

$$\Lambda_{L,E} \equiv \frac{\lambda_{L,E} w}{\sqrt{2} M_{L,E}} \quad \downarrow \quad \delta_L = \Lambda_L - 1 \ll 1$$

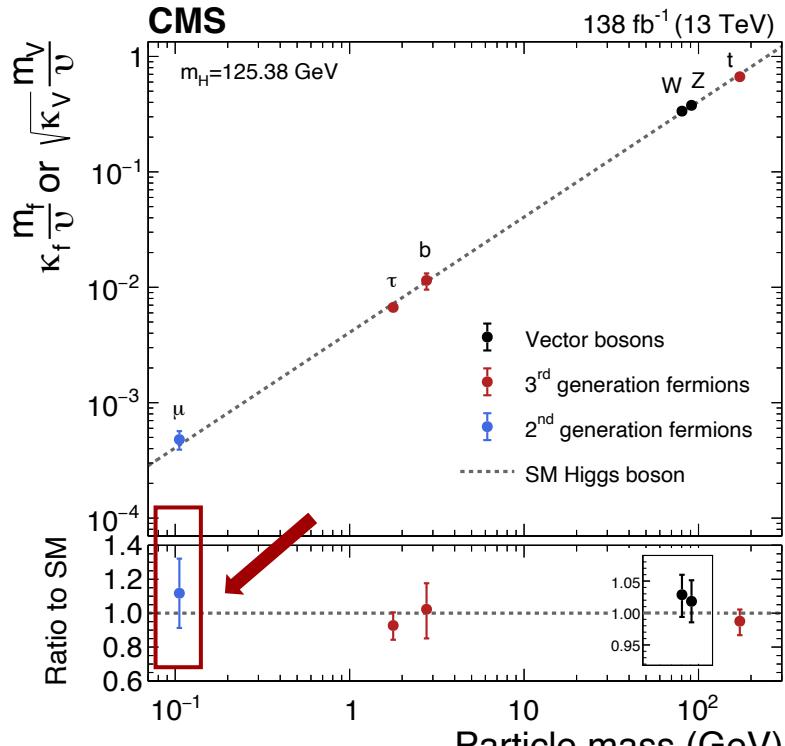
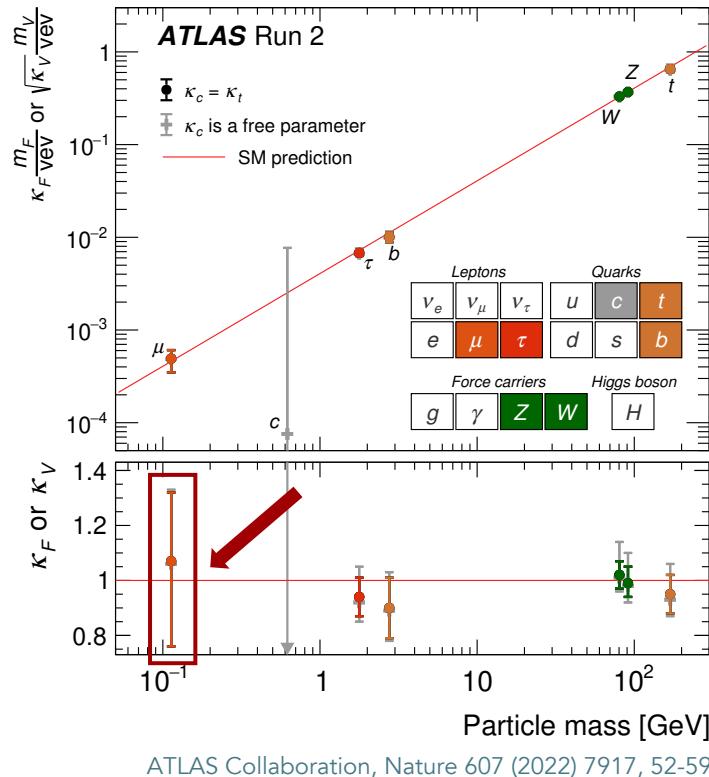
The A-V Z' couplings to charged leptons are:

$$\varepsilon_{\ell_1^\pm \ell_1^\mp}^A \simeq \frac{1}{2} \varepsilon_{B-L} \left(\frac{\Lambda_E^2 - 1}{1 + \Lambda_E^2} \right)$$

(B-L) + VLLs model : a real problem

➤ Charged-lepton couplings with the Higgs

Ferreira, Gonçalves & FRJ, JHEP 04 (2024) 003



Coupling modifiers : $-\mathcal{L} \supset \frac{m_\ell}{v} \kappa_\ell h \bar{\ell}_L^\pm \ell_R^\pm + \text{H.c.}$

$$\kappa_\ell = |(U_L)_{11}|^2 |(U_R)_{11}|^2 = \frac{1}{1 + \Lambda_L^2} \frac{1}{1 + \Lambda_E^2}$$

$$\xrightarrow{\Lambda_{L,E} = 1 + \delta_{L,E}} \kappa_\ell = \frac{1}{4} + \mathcal{O}(\delta_L, \delta_E)$$

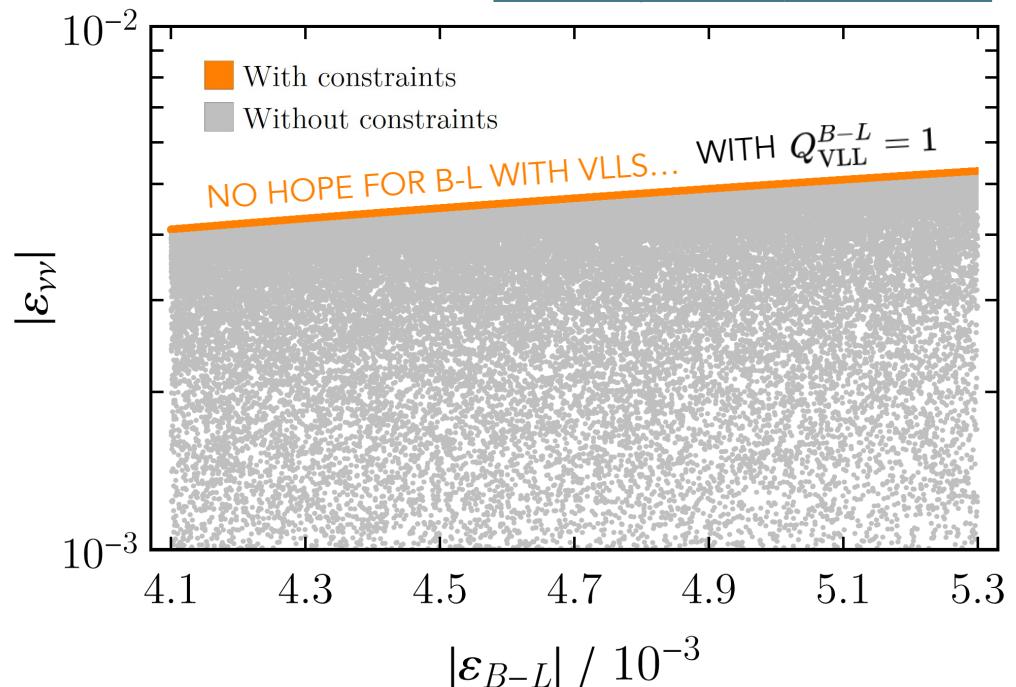


(B-L) + VLLs model : The full picture

Ferreira, Gonçalves & FRJ, JHEP 04 (2024) 003

➤ Full numerical analysis:

- $M_{L,E} \in [100 \text{ GeV}, 1 \text{ TeV}]$
- $m_\chi \in [10, 62.5] \text{ GeV}$ with c_α free
- Lepton mixing angles $\in [0, \pi/2]$
- Vary $4.1 \times 10^{-3} \lesssim \varepsilon_{B-L} \lesssim 5.3 \times 10^{-3}$
- All Yukawa couplings $< \sqrt{4\pi}$
- Boundness from below and a_\pm



Compute the couplings

$$\begin{aligned}\varepsilon_{\nu_a \nu_b}^{V(A)} &= \pm \frac{1}{2} \sum_{i=1}^{12} \varepsilon_{B-L} Q_i^{B-L} [(U_\nu^*)_{ia} (U_\nu)_{ib} \mp (U_\nu)_{ia} (U_\nu^*)_{ib}] \\ \varepsilon_{\ell_a \ell_b}^{V(A)} &= \frac{1}{2} \sum_{i=1}^3 (\varepsilon Q_i + \varepsilon_{B-L} Q_i^{B-L}) \left[\left(U_R^\dagger \right)_{ai} (U_R)_{ib} \pm \left(U_L^\dagger \right)_{ai} (U_L)_{ib} \right]\end{aligned}$$

**Numerical results
confirm the analytical
findings.**

APPLY CONSTRAINTS: (S,T,U), invisible Higgs decays, coupling modifiers, neutrino non-unitarity constraints.

(B-L) + VLLs model : possible wayout (?)

WHAT IF $Q_{\text{VLL}}^{B-L} \neq 1$?

[Denton and Gehrlein, PRD 108 \(2023\) 1, 015009](#)

$$\rightarrow \varepsilon_{\nu_1 \nu_1}^A = \varepsilon_{B-L} \left(\frac{1 - Q_{\text{VLL}}^{B-L} \Lambda_L^2}{1 + \Lambda_L^2} \right)$$

Neutrino coupling suppression for
 $Q_{\text{VLL}}^{B-L} \Lambda_L^2 \simeq 1$

This implies: $Q_{\text{VLL}}^{B-L} \gtrsim \frac{1}{\Lambda_L^2} \simeq (57 - 95) \left(\frac{M_L}{130 \text{GeV}} \right)^2 \left(\frac{\sqrt{4\pi}}{\lambda_L} \right)^2 \rightarrow Q_{\text{VLL}}^{B-L} \gtrsim 57$



[Ferreira, Gonçalves & FRJ, JHEP 04 \(2024\) 003](#)

(once more, let us turn a blind eye on this ugly requirement)

With $Q_{\text{VLL}}^{B-L} \Lambda_L^2 \simeq 1$: $\varepsilon_{\ell'_1 \ell_1^\mp}^A \simeq \frac{1}{2} \varepsilon_{B-L} \left(\frac{Q_{\text{VLL}}^{B-L} \Lambda_E^2 - 1}{1 + \Lambda_E^2} \right)$, $\varepsilon_{\ell_1^\pm \ell_1^\mp}^V \simeq -\varepsilon$

Couplings	Experimental range
ε_n^V	$2 \times 10^{-3} [4.1 \times 10^{-3}] \lesssim \varepsilon_n^V \lesssim 15 \times 10^{-3} [5.3 \times 10^{-3}]$
ε_p^V	$[0.7 \times 10^{-3}] \lesssim \varepsilon_p^V \lesssim 1.2 \times 10^{-3} [1.9 \times 10^{-3}]$
ε_{ee}^V	$0.4 \times 10^{-3} [0.63 \times 10^{-3}] \lesssim \varepsilon_{ee}^V \lesssim 2 \times 10^{-3} [1.2 \times 10^{-3}]$
ε_{ee}^A	$ \varepsilon_{ee}^A \lesssim 2.6 \times 10^{-9}$
$\varepsilon_{\nu_e \nu_e}^A$	$ \varepsilon_{\nu_e \nu_e}^A \lesssim 1.2 \times 10^{-5} [(3.5 - 4.5) \times 10^{-6}]$
$\varepsilon_{\nu_\mu \nu_\mu}^A$	$ \varepsilon_{\nu_\mu \nu_\mu}^A \lesssim 12.2 \times 10^{-5}$

ε_{B-L}

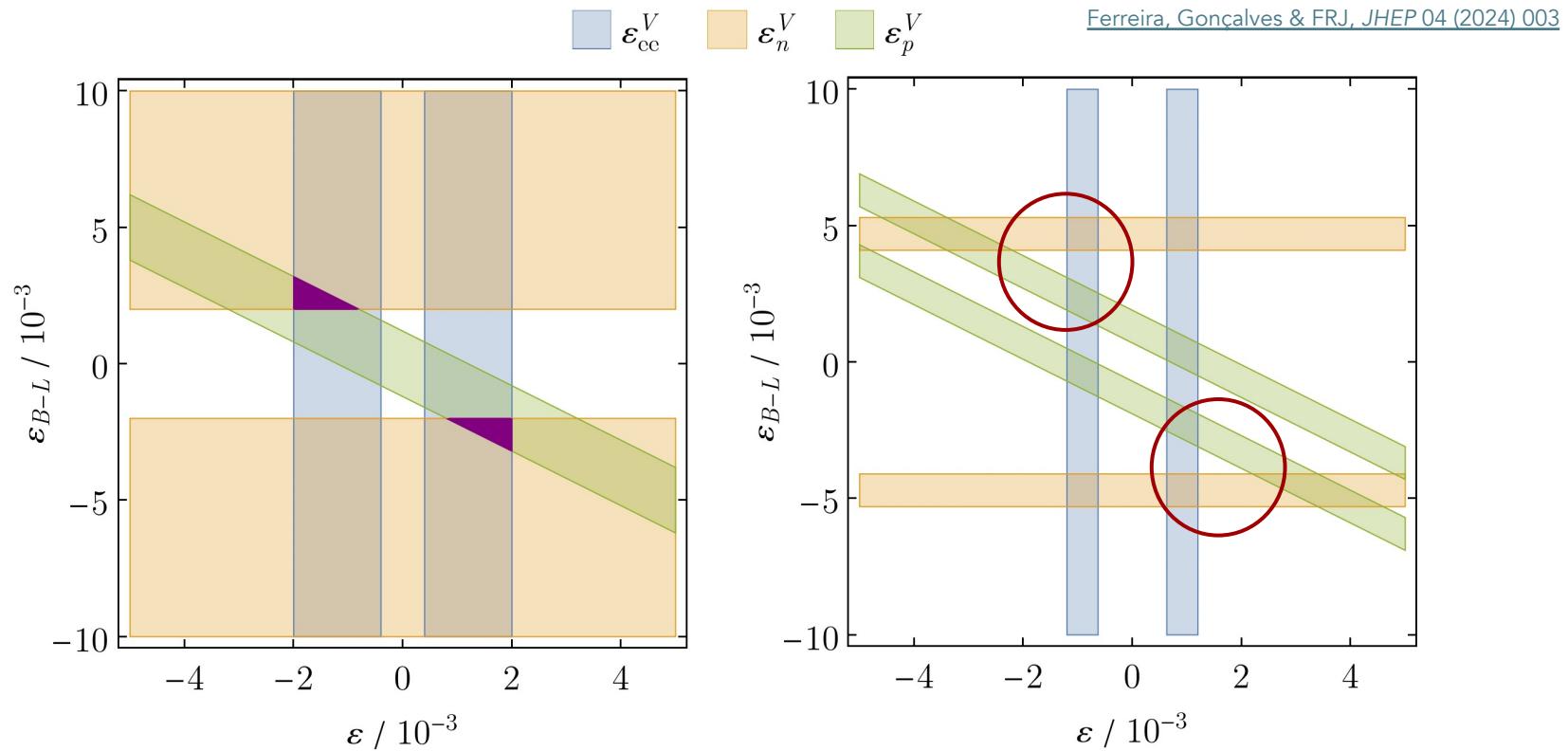
$\varepsilon + \varepsilon_{B-L}$

$-\varepsilon$

$\rightarrow Q_{\text{VLL}}^{B-L} \Lambda_E^2 \simeq 1$

$Q_{\text{VLL}}^{B-L} \Lambda_L^2 \simeq 1$

(B-L) + VLLs model : some tension & a real problem



There appears to be some tension, but...

There is a more serious problem than that.

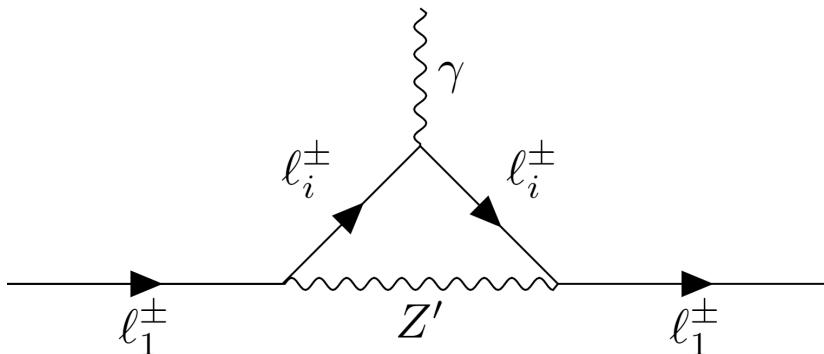
$$(g - 2)_\mu$$

(B-L) + VLLs model : the real problem

➤ Two new contributions to the $(g-2)_\mu$: $\Delta a_\mu = \Delta a_\mu^{Z'} + \Delta a_\mu^\chi$

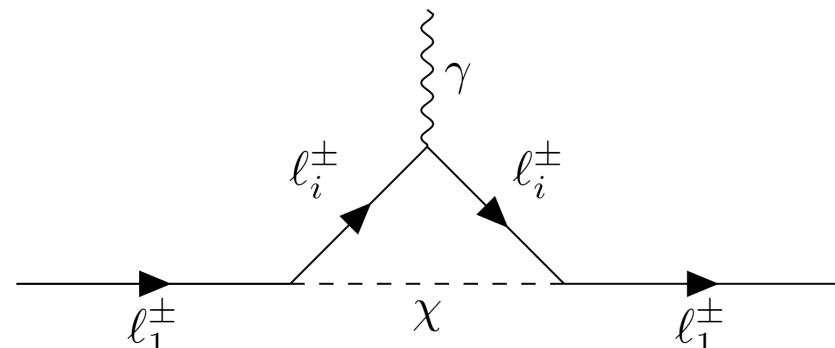
Ferreira, Gonçalves & FRJ,
JHEP 04 (2024) 003

$$\Delta a_\mu^{Z'} \simeq \mathcal{A}_\mu + \mathcal{A}_{\text{VLL}}$$



$$-\frac{m_\mu^2 e^2}{8\pi^2 m_{Z'}^2} (\mathcal{C}_\mu \varepsilon^2 + \mathcal{C}_{\text{VLL}} \varepsilon_{B-L}^2 Q_{\text{VLL}}^{B-L})$$

$$\Delta a_\mu^\chi \simeq \mathcal{A}_L + \mathcal{A}_E$$



$$\frac{m_\mu^2 e^2}{4\pi^2 m_{Z'}^2} \varepsilon_{B-L}^2 (\mathcal{C}_L \Lambda_L^2 + \mathcal{C}_E \Lambda_E^2)$$

$$m_{Z'} = 17 \text{ MeV} \quad \downarrow \quad M_{E,L} \gg m_{Z'}$$

$$\mathcal{C}_\mu = 2F_{Z'}\left(\frac{m_\mu^2}{m_{Z'}^2}\right) - G_{Z'}\left(\frac{m_\mu^2}{m_{Z'}^2}\right) \simeq 0.321$$

$$\mathcal{C}_{\text{VLL}} = F_{Z'}\left(\frac{M_L^2}{m_{Z'}^2}\right) + F_{Z'}\left(\frac{M_E^2}{m_{Z'}^2}\right) \simeq 2 \lim_{x \rightarrow \infty} F_{Z'}(x) = \frac{5}{6}$$

$$m_\chi \lesssim 22 \text{ GeV} \quad \downarrow \quad M_{E,L} \gg m_\chi$$

$$\mathcal{C}_{L,E} = \frac{M_{L,E}^2}{m_\chi^2} F_\chi\left(\frac{M_{L,E}^2}{m_\chi^2}\right)$$

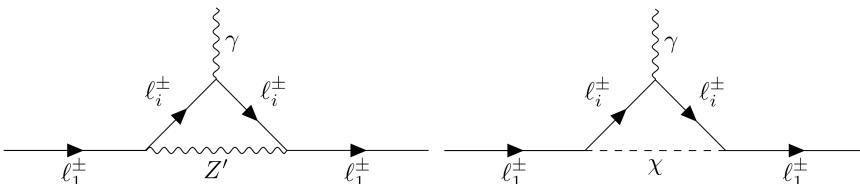
$$\mathcal{C}_{L,E} \simeq \lim_{x \rightarrow \infty} x F_\chi(x) = \frac{1}{6}$$

(B-L) + VLLs model : final verdict

➤ BENCHMARK:

$$Q_{\text{VLL}}^{B-L} = 24, \quad \Lambda_L = \Lambda_E = \frac{1}{\sqrt{24}}$$

$$\varepsilon = -1.5 \times 10^{-3}, \quad \varepsilon_{B-L} = 2 \times 10^{-3}$$



$$\mathcal{A}_\mu \simeq -3.26 \times 10^{-8}$$

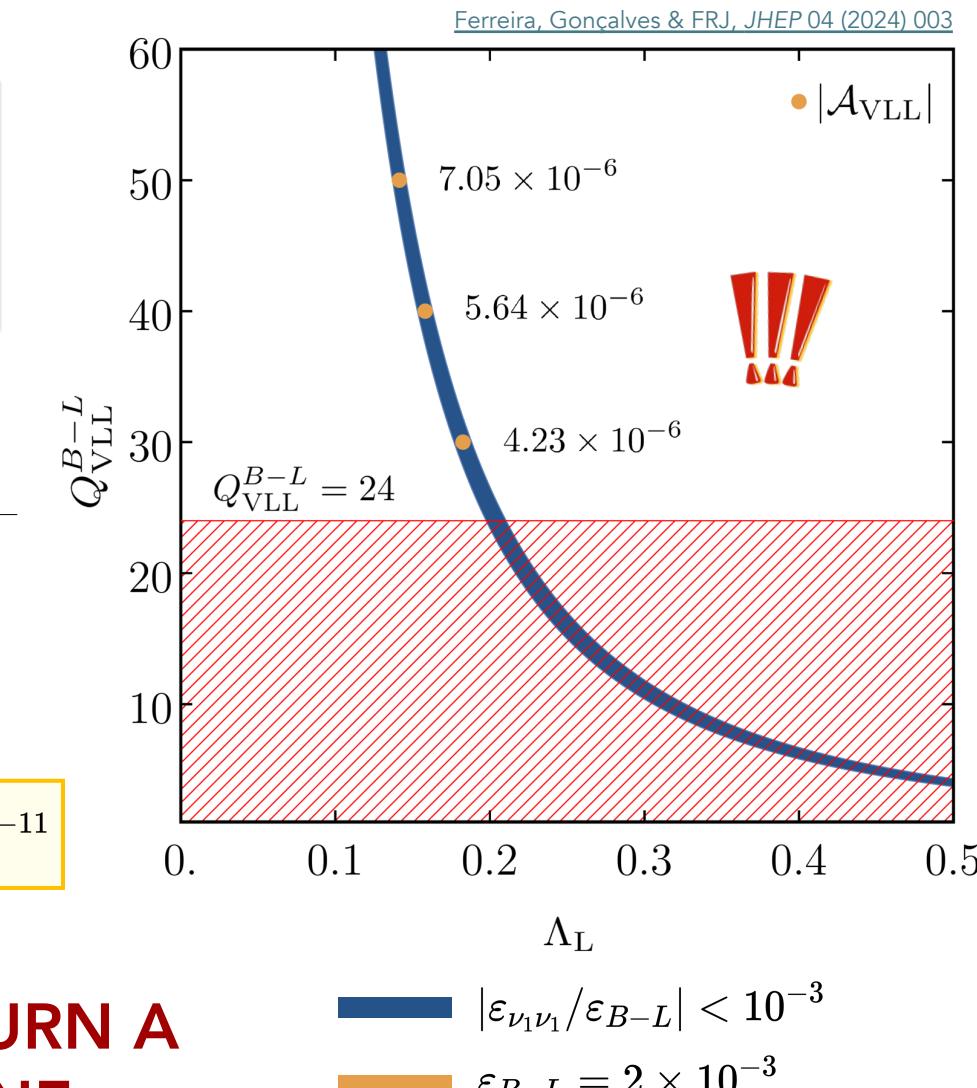
$$\mathcal{A}_{L,E} \simeq 2.51 \times 10^{-9}$$

$$\mathcal{A}_{\text{VLL}} \simeq -3.61 \times 10^{-6}$$

$$\Delta a_\mu = a_\mu(\text{Exp}) - a_\mu(\text{SM}) = (251 \pm 59) \times 10^{-11}$$

[B. Abi et al. \(Muon \$g-2\$ Collaboration\), PRL 126, 141801](#)

**THERE IS NO WAY TO TURN A
BLIND EYE ON THIS ONE...**



CONCLUSIONS

- ATOMKI anomalies: evidence of **new physics** (?)
 - **High** statistical significance $\gtrsim 6 \sigma$
 - **Different** detector configurations were used
 - **New X17 particle** imply remarkable fits
 - Different nuclei ${}^8\text{Be}$ - ${}^4\text{He}$ - ${}^{12}\text{C}$ anomalies
 - ${}^{12}\text{C}$ anomaly **predicted and confirmed**
 - Independent **confirmation** from VNU (?)
- VANILLA B-L: doesn't work!
- B-L + VLLs leads to problems (Higgs couplings, muon g-2, neutrino constraints)
- If **confirmed** we will have to bring up the right model...



Ευχαριστώ!