

Dark CP violation through the Z portal

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Based on [arXiv:1909.XXXX]

Corfu summer institute, 7 Sep 2019

- 1 Introduction and motivation
- 2 Scalar singlet extensions of the SM
- 3 Doublet extensions of the SM (2HDM)
- 4 Further doublet extensions of the SM (3HDM)
- 5 Summary

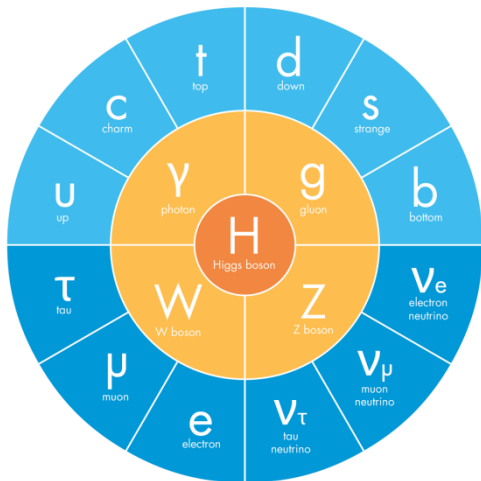
In praise of the Standard Model

Current formulation finalised
in the 70's predicted:

- the W & Z (1983)
- the top quark (1995)
- the tau neutrino (2000)
- “a” Higgs boson (2012)

FERMIONS (matter) | BOSONS (force carriers)

● Quarks ● Leptons | ● Gauge bosons ● Higgs boson



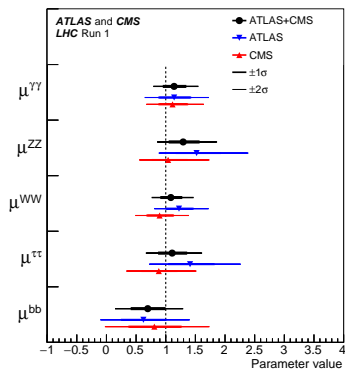
In criticism of the Standard Model

At the LHC:

- Higgs looks SM-like
- No signs of new physics

What is missing:

- Explanation for the fermion mass hierarchy
- EW vacuum stability
- Sufficient amount of CP violation
- Suitable candidate(s) for Dark Matter



[JHEP 08 (2016) 045]

Scalars to the rescue!

SM + singlet scalar extensions

 ϕ S

real singlet

complex singlet

extra singlets

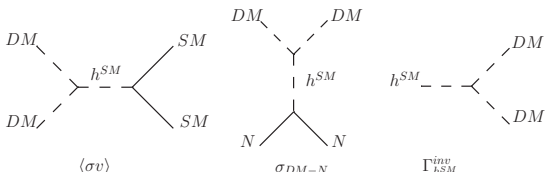
SM + real singlet (DM, CPV)

DM protected by a Z_2 symmetry (+, -): $SM \rightarrow SM, S \rightarrow -S$

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{2}(\partial S)^2 + \frac{1}{2}\mu_s^2 S^2 - \lambda_s S^4 - \lambda_{hs} \phi^2 S^2$$

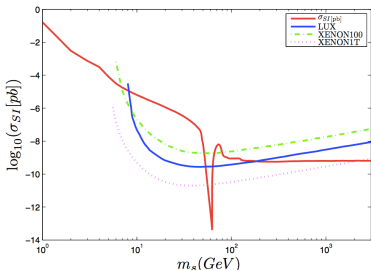
Z_2 symmetric Lagrangian, respected by the vacuum

$$\phi = \begin{pmatrix} G^+ \\ \frac{v_h + h + iG^0}{\sqrt{2}} \end{pmatrix}, \quad S = \begin{pmatrix} s \\ \sqrt{2} \end{pmatrix}$$



SM + real singlet (DM, CPV)

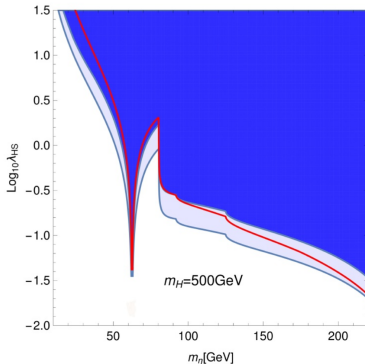
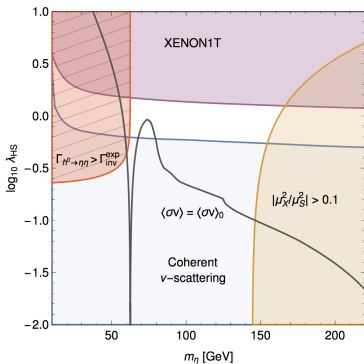
- Bounded from below potential: $h, s \rightarrow \infty \Rightarrow V > 0$
- Vacuum stability: $E_{VEW} < E_{v_i}$ or $\tau_{VEW} >$ age of the universe
- Perturbative unitarity: $|\lambda_i| \leq 4\pi$, $|\Lambda_i| \leq 8\pi$
- Higgs decays: $BR(h \rightarrow inv.) < 20\% \Rightarrow \lambda_{hs}$ small
- Relic density: λ_{hs} large
- Direct and indirect detection: λ_{hs} small



SM + complex singlet

(DM, CPV)

$$S = (v_s + s + i\chi)$$



[Phys.Rev. D99 (2019) no.7, 075028]

Further singlet extensions

(DM, ~~CPV~~)

SM+ 2 singlet scalars:

$S_1 \rightarrow -S_1$, $S_2 \rightarrow -S_2$, SM fields \rightarrow SM fields

- DM: the lightest particle from the dark sector S_1, S_2
- Introducing coannihilation channels: $S_1 S_2 \rightarrow h \rightarrow SM$
- Mixing in the dark sector $S_1, \chi_1, S_2, \chi_2 \rightarrow d_1, d_2, d_3, d_4$

does not result in CPV

[Phys.Rev.D. 83 (2011)]

Scalars to the rescue!

2 Higgs doublet model (2HDM)

$$\phi_1, \phi_2$$

CPC-2HDM

CPV-2HDM

IDM

The generic 2HDM

The general scalar potential:

$$\begin{aligned}
 V = & -\mu_1^2(\phi_1^\dagger\phi_1) - \mu_2^2(\phi_2^\dagger\phi_2) - \left[\mu_3^2(\phi_1^\dagger\phi_2) + h.c. \right] \\
 & + \frac{1}{2}\lambda_1(\phi_1^\dagger\phi_1)^2 + \frac{1}{2}\lambda_2(\phi_2^\dagger\phi_2)^2 + \lambda_3(\phi_1^\dagger\phi_1)(\phi_2^\dagger\phi_2) + \lambda_4(\phi_1^\dagger\phi_2)(\phi_2^\dagger\phi_1) \\
 & + \left[\frac{1}{2}\lambda_5(\phi_1^\dagger\phi_2)^2 + \lambda_6(\phi_1^\dagger\phi_1)(\phi_1^\dagger\phi_2) + \lambda_7(\phi_2^\dagger\phi_2)(\phi_1^\dagger\phi_2) + h.c. \right].
 \end{aligned}$$

Dangerous FCNCs appear

$$\mathcal{L}_Y = y_{ij}^1 \bar{\psi}_i \psi_j \phi_1 + y_{ij}^2 \bar{\psi}_i \psi_j \phi_2$$

$$Z_2 \text{ symmetry } (\phi_1 \rightarrow +\phi_1, \phi_2 \rightarrow -\phi_2) \Rightarrow \lambda_6 = \lambda_7 = 0$$

The CP-conserving 2HDM (DM, CPV)

The doublets compositions:

$$\phi_1 = \left(\begin{array}{c} \phi_1^+ \\ \frac{v_1 + h_1^0 + ia_1^0}{\sqrt{2}} \end{array} \right), \quad \phi_2 = \left(\begin{array}{c} \phi_2^+ \\ \frac{v_2 + h_2^0 + ia_2^0}{\sqrt{2}} \end{array} \right), \quad \tan \beta = \langle \phi_2 \rangle / \langle \phi_1 \rangle$$

Mass eigenstates:

$$\left(\begin{array}{c} h \\ H \end{array} \right) = \left(\begin{array}{cc} c_\alpha & s_\alpha \\ -s_\alpha & c_\alpha \end{array} \right) \left(\begin{array}{c} h_1^0 \\ h_2^0 \end{array} \right)$$

$$\left(\begin{array}{c} G^0 \\ A \end{array} \right) = \left(\begin{array}{cc} c_\beta & s_\beta \\ -s_\beta & c_\beta \end{array} \right) \left(\begin{array}{c} a_1^0 \\ a_2^0 \end{array} \right), \quad \left(\begin{array}{c} G^\pm \\ H^\pm \end{array} \right) = \left(\begin{array}{cc} c_\beta & s_\beta \\ -s_\beta & c_\beta \end{array} \right) \left(\begin{array}{c} \phi_1^\pm \\ \phi_2^\pm \end{array} \right)$$

More constraints

Electroweak precision observables:

S, T, U parameters

Flavour observables:

$$BR(B \rightarrow X_s \gamma), \quad B^0 - \bar{B}^0 \text{ mixing}$$

$$D_s \rightarrow \tau \nu_\tau, \quad D_s \rightarrow \mu \nu_\mu, \quad B \rightarrow D \tau \nu_\tau$$

LEP bounds:

$$m_{H^\pm} + m_{H,A} > m_{W^\pm}, \quad m_H + m_A > m_Z, \quad 2m_{H^\pm} > m_Z$$

$$m_{H^\pm} \gtrsim 70 - 90 \text{ GeV}$$

$$\text{if } M_H < 80 \text{ GeV and } M_A < 100 \text{ GeV} \Rightarrow M_A - M_H < 8 \text{ GeV}$$

LHC bound on the total decay signal strength:

$$\mu_{tot} = \frac{BR(h \rightarrow XX)}{BR(h_{SM} \rightarrow XX)} = 1.17 \pm 0.17$$

2HDM with CP-violation (CPV, $\mathbb{D}\mathbb{M}$)

The scalar potential with **softly broken** Z_2 symmetry:

$$\begin{aligned}
 V = & -\mu_1^2(\phi_1^\dagger\phi_1) - \mu_2^2(\phi_2^\dagger\phi_2) - \mu_3^2(\phi_1^\dagger\phi_2) + \frac{1}{2}\lambda_1(\phi_1^\dagger\phi_1)^2 + \frac{1}{2}\lambda_2(\phi_2^\dagger\phi_2)^2 \\
 & + \lambda_3(\phi_1^\dagger\phi_1)(\phi_2^\dagger\phi_2) + \lambda_4(\phi_1^\dagger\phi_2)(\phi_2^\dagger\phi_1) + \frac{1}{2}\lambda_5(\phi_1^\dagger\phi_2)^2 + h.c.
 \end{aligned}$$

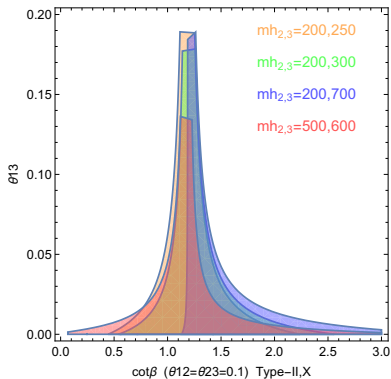
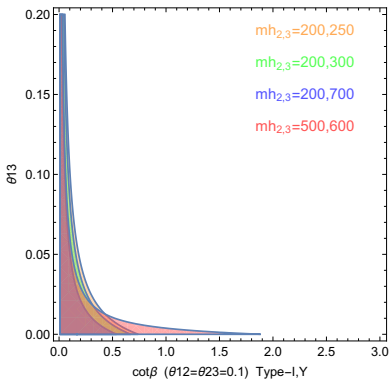
The only source of CPV-violation:

$$\text{Im}\mu_3^2 = \frac{v^2}{2} \text{Im}\lambda_5 \sin\beta \cos\beta$$

The CP mixed mass eigenstates in the *Higgs basis*:

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix} = \begin{pmatrix} 1 & \theta_{12} & \theta_{13} \\ -\theta_{12} & 1 & \theta_{23} \\ -\theta_{13} & -\theta_{23} & 1 \end{pmatrix} \begin{pmatrix} \phi_1^0 \\ \phi_2^0 \\ \phi_3^0 \end{pmatrix}$$

CPV angles constrained by EDM data



[JHEP 1809 (2018) 059]

The Inert Doublet Model (DM, CPV)

Scalar potential with an exact Z_2 symmetry:

$$Z_2 : \quad \phi_1 \rightarrow \phi_1, \quad \phi_2 \rightarrow -\phi_2, \quad \text{SM fields} \rightarrow \text{SM fields}$$

$$\begin{aligned} V = & -\mu_1^2(\phi_1^\dagger\phi_1) - \mu_2^2(\phi_2^\dagger\phi_2) + \frac{1}{2}\lambda_1(\phi_1^\dagger\phi_1)^2 + \frac{1}{2}\lambda_2(\phi_2^\dagger\phi_2)^2 \\ & + \lambda_3(\phi_1^\dagger\phi_1)(\phi_2^\dagger\phi_2) + \lambda_4(\phi_1^\dagger\phi_2)(\phi_2^\dagger\phi_1) + \frac{1}{2}\lambda_5(\phi_1^\dagger\phi_2)^2 \end{aligned}$$

The vacuum respects the Z_2 symmetry:

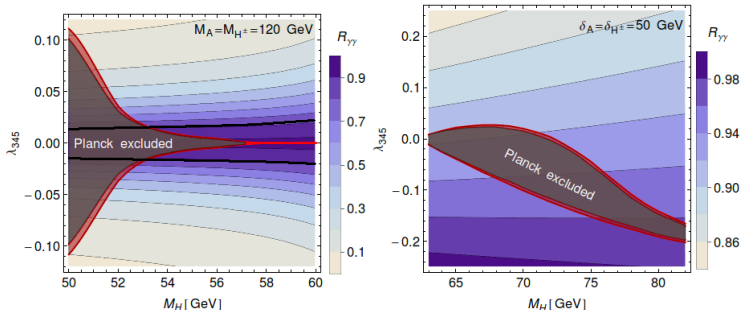
$$\langle \phi_1 \rangle = v, \quad \langle \phi_2 \rangle = 0$$

DM is the lightest neutral particle from the inert doublet: H, A

More constraints

Higgs invisible decays: $\text{BR}(h \rightarrow S_i S_j) < 0.23 - 0.36$

$h \rightarrow \gamma\gamma$ signal strength: $\mu_{\gamma\gamma} = 1.16^{+0.20}_{-0.18}$



[JHEP 09, 055 (2013)]

Scalars to the rescue!

3-Higgs doublet models

$$I(1+2)\text{HDM}$$
$$(0, \nu, \nu)$$

$$I(2+1)\text{HDM}$$
$$(0, 0, \nu)$$

The scalar potential with explicit CPV (DM, CPV)

$$V_{3HDM} = V_0 + V_{Z_2}$$

$$V_0 = \sum_i^3 \left[-\mu_i^2 (\phi_i^\dagger \phi_i) + \lambda_{ii} (\phi_i^\dagger \phi_i)^2 \right] \\ + \sum_{i,j}^3 \left[\lambda_{ij} (\phi_i^\dagger \phi_i) (\phi_j^\dagger \phi_j) + \lambda'_{ij} (\phi_i^\dagger \phi_j) (\phi_j^\dagger \phi_i) \right]$$

$$V_{Z_2} = -\mu_{12}^2 (\phi_1^\dagger \phi_2) + \lambda_1 (\phi_1^\dagger \phi_2)^2 + \lambda_2 (\phi_2^\dagger \phi_3)^2 + \lambda_3 (\phi_3^\dagger \phi_1)^2 + h.c.$$

The Z_2 symmetry

$$\phi_1 \rightarrow -\phi_1, \quad \phi_2 \rightarrow -\phi_2, \quad \phi_3 \rightarrow \phi_3, \quad \text{SM fields} \rightarrow \text{SM fields}$$

The CP-mixed mass eigenstates

The doublet compositions

$$\phi_1 = \begin{pmatrix} H_1^+ \\ \frac{H_1^0 + iA_1^0}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} H_2^+ \\ \frac{H_2^0 + iA_2^0}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{v + h + iG^0}{\sqrt{2}} \end{pmatrix}$$

The mass eigenstates

$$m_{S_1^\pm}^2 = -\mu_2^2 - \mu_{12}^2 + \frac{1}{2}\lambda_{23}v^2, \quad m_{S_2^\pm}^2 = -\mu_2^2 + \mu_{12}^2 + \frac{1}{2}\lambda_{23}v^2$$

$$m_{S_{1,2}}^2 = -\mu_2^2 + \frac{v^2}{2}(\lambda'_{23} + \lambda_{23}) \mp \Lambda^\mp, \quad m_{S_{3,4}}^2 = -\mu_2^2 + \frac{v^2}{2}(\lambda'_{23} + \lambda_{23}) \mp \Lambda^\mp$$

$$\Lambda^\mp = \sqrt{(\mu_{12}^2)^2 + v^4|\lambda_2|^2 \mp 2v^2\mu_{12}^2|\lambda_2|\cos\theta_{CPV}}$$

S_1 is assumed to be the DM candidate

Setting Higgs portal couplings to zero

- **annihilation processes:**

$$S_1 S_1 \rightarrow VV, \quad S_1 S_1 \rightarrow VV^* \rightarrow Vff', \quad S_1 S_1 \rightarrow V^* V^* \rightarrow ff' ff'$$

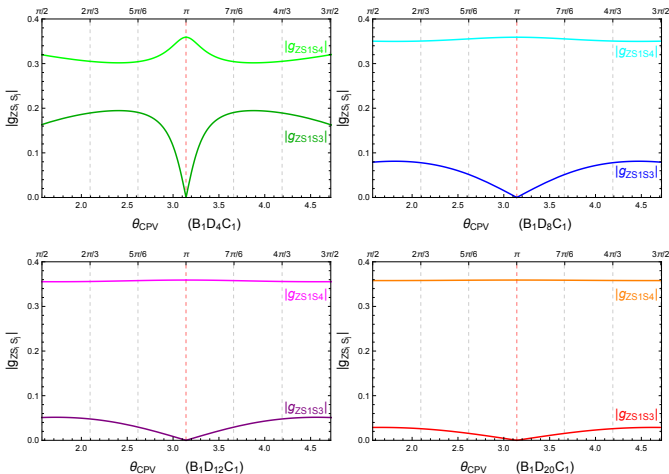
- **co-annihilation processes:**

$$S_1 S_{2,3,4} \rightarrow Z^* \rightarrow f\bar{f}, \quad S_1 S_{1,2}^{\pm} \rightarrow W^{\pm*} \rightarrow ff'$$

- **(co)annihilation of other dark states:**

$$S_i S_i \rightarrow VV, \quad S_i S_i \rightarrow VV^* \rightarrow Vff', \\ S_i S_i \rightarrow V^* V^* \rightarrow ff' ff', \quad S_i S_j \rightarrow V^* \rightarrow ff'$$

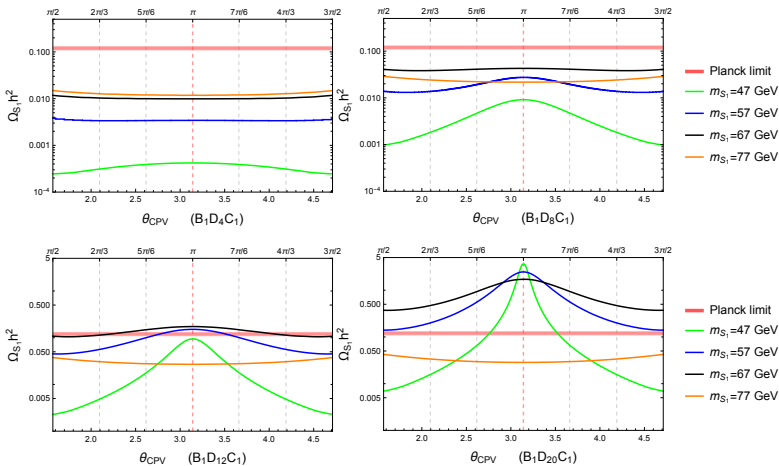
Type 1 benchmarks: $m_{S_1} \sim m_{S_3} \sim m_{S_2} \sim m_{S_4} \ll m_{S_1^\pm} \sim m_{S_2^\pm}$



$$\mathbf{B}_1 \mathbf{D}_4 \mathbf{C}_1 : \delta_{12} = 4 \text{ GeV}, \quad \delta_c = 1 \text{ GeV}, \quad \delta_{1c} = 50 \text{ GeV},$$

$$\mathbf{B}_1 \mathbf{D}_8 \mathbf{C}_1 : \delta_{12} = 8 \text{ GeV}, \quad \mathbf{B}_1 \mathbf{D}_{12} \mathbf{C}_1 : \delta_{12} = 12 \text{ GeV}, \quad \mathbf{B}_1 \mathbf{D}_{20} \mathbf{C}_1 : \delta_{12} = 20 \text{ GeV}$$

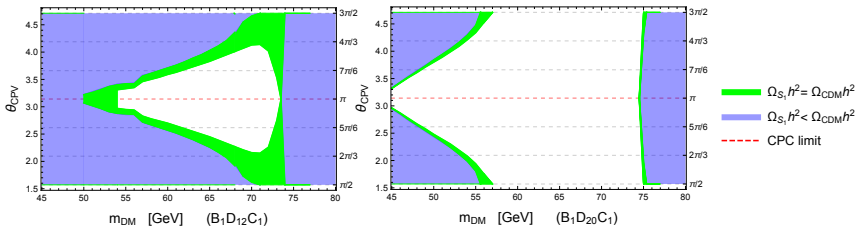
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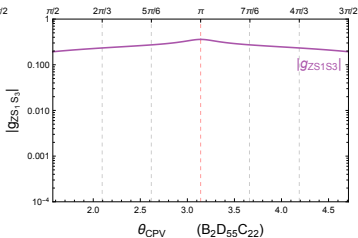
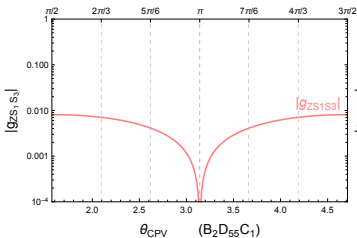
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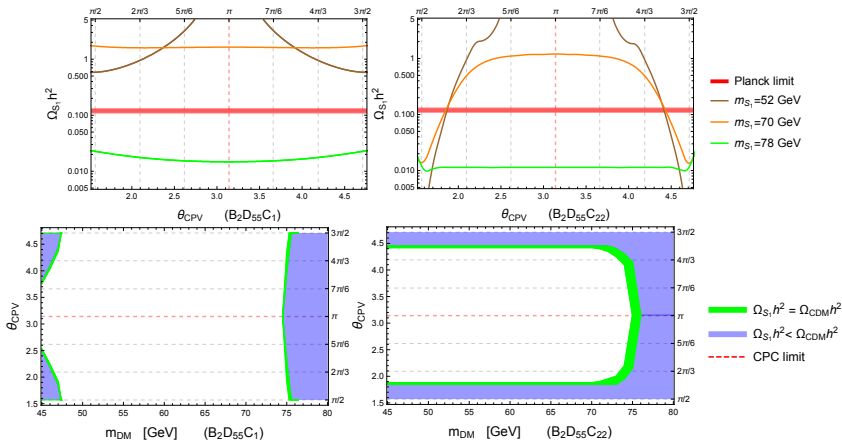
Type 2 benchmarks: $m_{S_1} \sim m_{S_3} \ll m_{S_2} \sim m_{S_4} \sim m_{S_1^\pm} \sim m_{S_2^\pm}$



$$B_2D_{55}C_1 : \delta_{12} = 55 \text{ GeV}, \quad \delta_c = 1 \text{ GeV}, \quad \delta_{1c} = 50 \text{ GeV},$$

$$B_2D_{55}C_{22} : \delta_{12} = 55 \text{ GeV}, \quad \delta_c = 22 \text{ GeV}, \quad \delta_{1c} = 50 \text{ GeV}$$

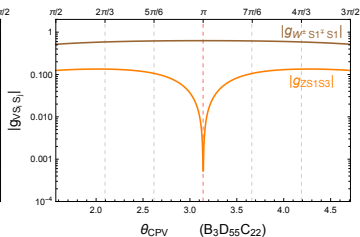
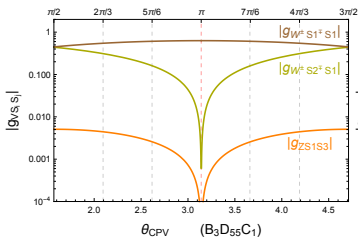
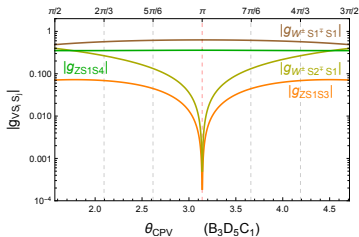
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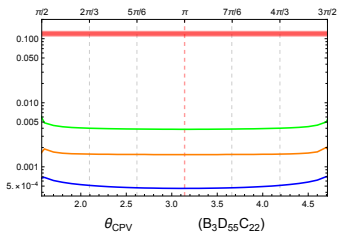
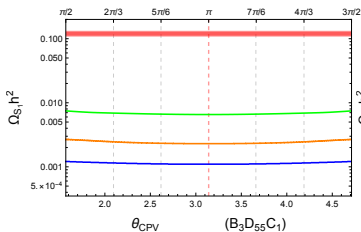
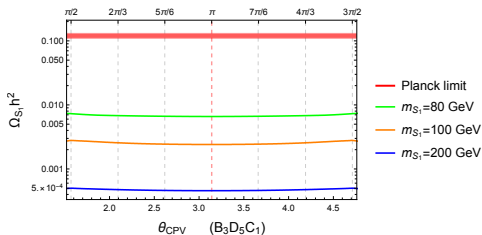
Type 3 benchmarks: $m_{S_1} \sim m_{S_3} \sim m_{S_2} \sim m_{S_4} \sim m_{S_1^\pm} \sim m_{S_2^\pm}$



$$B_3D_5C_1: \delta_{12} = 5 \text{ GeV}, \quad \delta_c = 1 \text{ GeV}, \quad \delta_{1c} = 1 \text{ GeV},$$

$$B_3D_{55}C_1: \delta_{12} = 55 \text{ GeV}, \quad \delta_c = 1 \text{ GeV}, \quad B_3D_{55}C_{22}: \delta_{12} = 55 \text{ GeV}, \quad \delta_c = 22 \text{ GeV}$$

Type 3 benchmarks: $m_{S_1} \sim m_{S_3} \sim m_{S_2} \sim m_{S_4} \sim m_{S_1^\pm} \sim m_{S_2^\pm}$

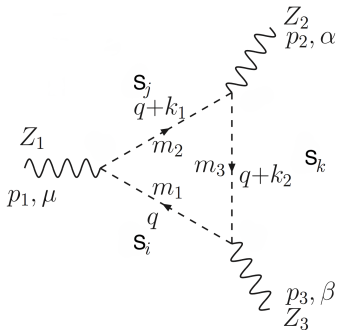


$$B_3 D_5 C_1 : \delta_{12} = 5 \text{ GeV}, \quad \delta_c = 1 \text{ GeV}, \quad \delta_{1c} = 1 \text{ GeV},$$

$$B_3 D_{55} C_1 : \delta_{12} = 55 \text{ GeV}, \quad \delta_c = 1 \text{ GeV}, \quad B_3 D_{55} C_{22} : \delta_{12} = 55 \text{ GeV}, \quad \delta_c = 22 \text{ GeV}$$

Dark CPV observables: the ZZZ vertex

$$e\Gamma_{ZZZ}^{\alpha\beta\mu} = ie \frac{q^2 - M_Z^2}{M_Z^2} [f_4(q^\alpha g^{\mu\beta} + q^\beta g^{\mu\alpha}) + f_5 \epsilon^{\mu\alpha\beta\rho} (p_1 - p_2)_\rho]$$



$$f_4 = \frac{M_Z^2 |g_{ZS_2S_3}| |g_{ZS_1S_3}| |g_{ZS_1S_2}|}{2\pi^2 e (q^2 - M_Z^2)} \sum_{i,j,k}^4 \epsilon_{ijk} C_{002}(M_Z^2, M_Z^2, q^2, m_i^2, m_j^2, m_k^2)$$

Summary

Scalar extensions with or without a Z_2 symmetry:

- SM + scalar singlet(s)

- $\phi_{SM}, S \Rightarrow DM, CPV$
- $\phi_{SM}, S_1, S_2 \Rightarrow DM, CPV$

- 2HDM: SM + scalar doublet

- Type-I, Type-II, ...: $\phi_1, \phi_2 \Rightarrow CPV, DM$
- IDM - I(1+1)HDM: $\phi_1, \phi_2 \Rightarrow DM, CPV$

- 3HDM: SM + 2 scalar doublets

- Weinberg model: $\phi_1, \phi_2, \phi_3 \Rightarrow CPV, DM$
- I(1+2)HDM: $\phi_1, \phi_2, \phi_3 \Rightarrow DM, CPV$
- I(2+1)HDM: $\phi_1, \phi_2, \phi_3 \Rightarrow CPV, DM$

BACKUP SLIDES

The CP-mixed mass eigenstates

The doublet compositions

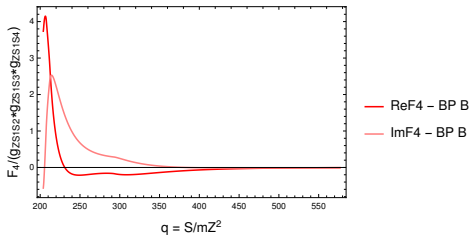
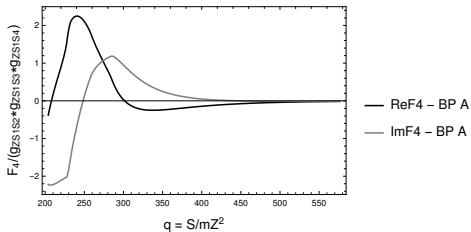
$$\phi_1 = \begin{pmatrix} H_1^+ \\ \frac{H_1^0 + iA_1^0}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} H_2^+ \\ \frac{H_2^0 + iA_2^0}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{\nu + h + iG^0}{\sqrt{2}} \end{pmatrix}$$

The mass eigenstates

$$S_1 = \frac{\alpha H_1^0 + \alpha H_2^0 - A_1^0 + A_2^0}{\sqrt{2\alpha^2 + 2}}, \quad S_2 = \frac{-H_1^0 - H_2^0 - \alpha A_1^0 + \alpha A_2^0}{\sqrt{2\alpha^2 + 2}}$$
$$S_3 = \frac{\beta H_1^0 - \beta H_2^0 + A_1^0 + A_2^0}{\sqrt{2\beta^2 + 2}}, \quad S_4 = \frac{-H_1^0 + H_2^0 + \beta A_1^0 + \beta A_2^0}{\sqrt{2\beta^2 + 2}}$$
$$S_1^\pm = \frac{H_2^\pm + H_1^\pm}{\sqrt{2}}, \quad S_2^\pm = \frac{H_2^\pm - H_1^\pm}{\sqrt{2}}$$

S_1 is assumed to be the DM candidate

f_4 values for exemplary benchmark points

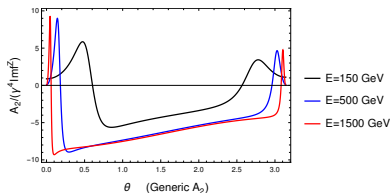
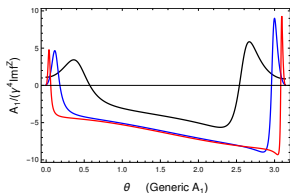


A_1 and A_2 asymmetries in $f\bar{f} \rightarrow ZZ$

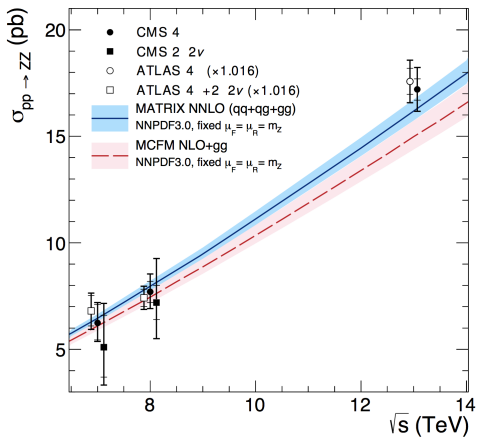
Assuming the momenta and helicities of ZZ are known:

$$A_1^{ZZ} \equiv \frac{\sigma_{+,0} - \sigma_{0,-}}{\sigma_{+,0} + \sigma_{0,-}}, \quad A_2^{ZZ} \equiv \frac{\sigma_{0,+} - \sigma_{-,0}}{\sigma_{0,+} + \sigma_{-,0}},$$

$\sigma_{\lambda,\bar{\lambda}}$: unpolarized-beam cross sections for ZZ production with helicities λ and $\bar{\lambda}$



$pp \rightarrow ZZ$ at CMS



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Typical cross sections for DD and ID experiments

