How solid is the quantum gravity prediction for the Higgs boson mass?

Prediction of mass of Higgs boson

Asymptotic safety of gravity and the Higgs boson mass

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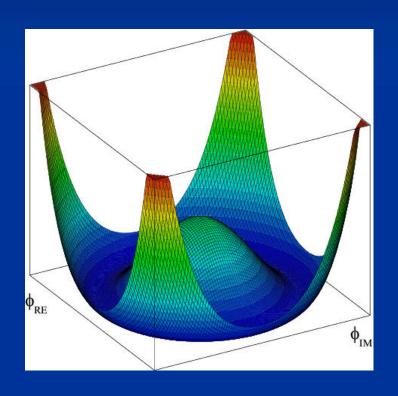
Abstract

There are indications that gravity is asymptotically safe. The Standard Model (SM) plus gravity could be valid up to arbitrarily high energies. Supposing that this is indeed the case and assuming that there are no intermediate energy scales between the Fermi and Planck scales we address the question of whether the mass of the Higgs boson m_H can be predicted. For a positive gravity induced anomalous dimension $A_{\lambda} > 0$ the running of the quartic scalar self interaction λ at scales beyond the Planck mass is determined by a fixed point at zero. This results in $m_H = m_{\min} = 126$ GeV, with only a few GeV uncertainty. This prediction is independent of the details of the short distance running and holds for a wide class of extensions of the SM as well.

s in
$$m_H = m_{\min} = 126$$
 GeV, with o

Why can quantum gravity make predictions for particle physics?

Effective potential for Higgs scalar



$$V(\varphi) = -\mu^2 \varphi^{\dagger} \varphi + \frac{1}{2} \lambda (\varphi^{\dagger} \varphi)^2$$

$$= \frac{1}{2}\lambda(\varphi^{\dagger}\varphi - \varphi_0^2)^2 + \text{const.})$$

Fermi scale

$$\varphi_0 = 175 \text{ GeV}$$

Quartic scalar coupling

prediction of mass of Higgs boson

=

prediction of value of quartic scalar coupling \(\lambda\)
at Fermi scale

$$m^2 = 2\lambda \varphi_0^2$$

Why can quantum gravity make predictions for quartic scalar coupling?

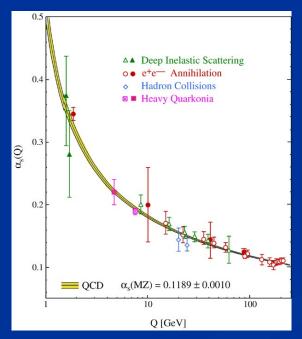
Mass scales

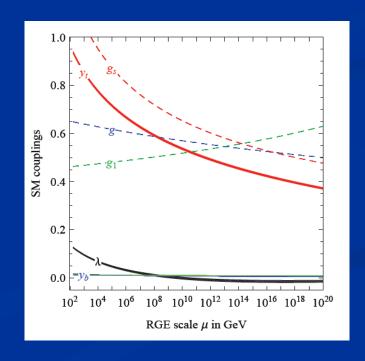
- Fermi scale $\varphi_0 \sim 100 \text{ GeV}$
- Planck mass M ~ 10¹⁸ GeV
- Gravity at Fermi scale is very weak: How can it influence the effective potential for the Higgs scalar and the mass of the Higgs boson?

$$\varepsilon = \frac{\varphi_0^2}{M^2} = 5 \cdot 10^{-33}$$

Quantum fluctuations induce running couplings

- possible violation of scale symmetry
- well known in QCD or standard model



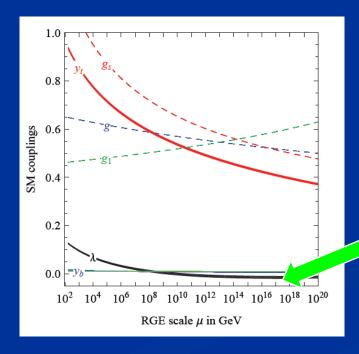


Bethke

Degrassi et al

Quantum fluctuations induce running couplings

- possible violation of scale symmetry
- well known in QCD or standard model



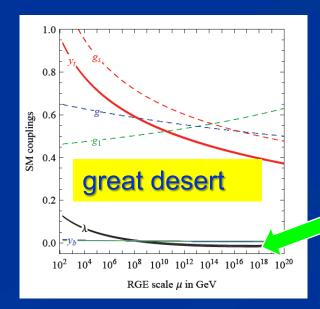
prediction of quantum gravity

The mass of the Higgs boson, the great desert, and asymptotic safety of gravity



key points

- great desert
- solution of hierarchy problem at high scale
- high scale fixed point
- vanishing scalar coupling at fixed point



fixed point



Planck scale, gravity

no multi-Higgs model

no technicolor

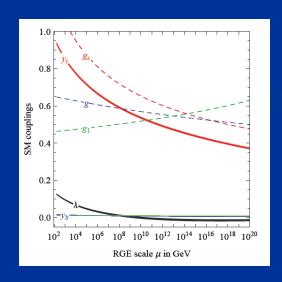
no low scale higher dimensions

no supersymmetry

Essential point for prediction of Higgs boson mass:

Initial value of quartic scalar coupling near Planck mass is predicted by quantum gravity

Extrapolate perturbatively to Fermi scale



Results in prediction for ratio Higgs boson mass over W- boson mass, or Higgs boson mass over top quark mass

Near Planck mass gravity is not weak!

Predictive power!

Great desert

Big chance for understanding of quantum gravity!

Flowing couplings

Couplings change with momentum scale due to quantum fluctuations.

Renormalization scale k: Only fluctuations with momenta larger k are included. The scale k can be momenta, geometric quantities, or just be introduced "by hand".

Flow of k to zero: all fluctuations included, IR Flow of k to infinity: UV

Renormalization group

How do couplings or physical laws change with scale k?

Graviton fluctuations erase quartic scalar coupling

Renormalization scale k : Only fluctuations with momenta larger k are included

$$k \frac{\partial \lambda}{\partial k} = A \lambda$$

gravity induced anomalous dimension A > 0

Graviton fluctuations erase quartic scalar coupling

for k beyond Planck scale:

$$k \frac{\partial \lambda}{\partial k} = A \lambda$$

 $\lambda(k) = \lambda(\mu) \left(\frac{k}{\mu}\right)^A$

gravity induced anomalous dimension A: positive constant of order one

$$k \rightarrow 0 \Rightarrow \lambda \rightarrow 0$$

Fixed point

$$k \frac{\partial \lambda}{\partial k} = A \lambda$$

$$\lambda(k) = \lambda(\mu) \left(\frac{k}{\mu}\right)^A$$

The quartic scalar coupling λ has a fixed point at $\lambda=0$

It flows towards the fixed point as k is lowered: irrelevant coupling

For a UV – complete theory it is predicted to assume the fixed point value

Gravitational contribution to running quartic coupling

$$\partial_t \lambda = A_\lambda \lambda$$

$$\partial_t \lambda = A_{\lambda} \lambda$$

$$A = \frac{1}{48\pi^2 \tilde{M}_p^2} \left[\frac{20}{(1-v_0)^2} + \frac{1}{(1-v_0/4)^2} \right] \qquad \partial_t = k \partial_k$$

$$\partial_t = k \partial_k$$

running Planck mass: $M_{\rm p}^2(k) = M^2 + \tilde{M}_{\rm p*}^2 k^2$

$$M_{\rm p}^2(k) = M^2 + \tilde{M}_{\rm p*}^2 k^2$$

dimensionless squared Planck mass

$$\tilde{M}_{\rm p}^2 = \frac{M_{\rm p}^2}{k^2}$$

UV – fixed point for quartic coupling

Flow equation for λ : $\partial_t \lambda_H = A\lambda_H - C_H$

$$\partial_t \lambda_H = A\lambda_H - C_H$$

$$C_H^{(p)} = -\beta_\lambda^{(SM)}$$

$$C_H^{(p)} = -\beta_{\lambda}^{(SM)} \approx -\frac{1}{16\pi^2} \left\{ 12\lambda_H^2 + 12y_t^2 \lambda_H - 12y_t^4 + \frac{9}{4}g_2^2 + \frac{9}{10}g_2^2 g_1^2 + \frac{27}{100}g_1^4 - \left(9g_2^2 + \frac{9}{5}g_1^2\right)\lambda_H \right\}$$

Fixed point: $\lambda = C/A$

$$\lambda\left(k_{tr}\right)\approx0$$
 , $\beta_{\lambda}\left(k_{tr}\right)\approx0$

Strength of gravity

$$g_{grav} = 1 / w$$

running gravitational coupling

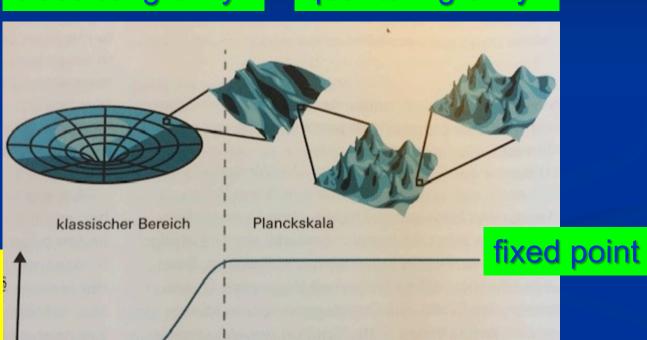
$$w = \frac{M^2}{2k^2}$$

M: Planck mass

Strength of gravity

classical gravity

quantum gravity



strength of gravity g_{grav}

inverse distance

energy

 Renormalization scale k : Only fluctuations with momenta larger k are included

Flowing Planck mass M²(k)

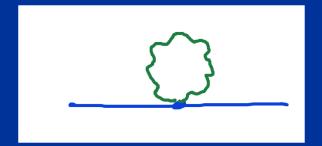
$$\partial_t M^2 = 4ck^2$$

$$\partial_t = k \partial_k$$

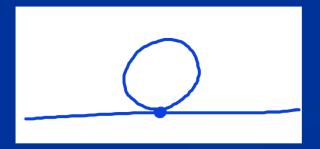
Universality of gravity



scalar loop, fermion loop



gauge boson loop

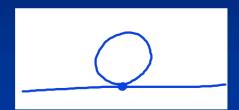


graviton loop

Universality of gravity







scalar loop, fermion loop

gauge boson loop

graviton loop

for massless particles: c is independent of coupling constants

$$\partial_t M^2 = 4ck^2$$

Renormalization scale k : Only fluctuations with momenta larger k are included

Flowing Planck mass M²(k)

$$\partial_t M^2 = 4ck^2$$

$$\partial_t = k \partial_k$$

matter contribution

$$c_M = \frac{\mathcal{N}_M}{192\pi^2}.$$

$$c_M = \frac{\mathcal{N}_M}{192\pi^2}$$
. $\mathcal{N}_M = 4 N_V - N_S - N_F$

with graviton contribution

$$c_M = \frac{1}{192\pi^2} \left(\mathcal{N}_M + \frac{43}{6} + \frac{75(1 - \eta_g/6)}{2(1 - v)} \right)$$

Flowing Planck mass M²(k)

$$\partial_t M^2 = 4ck^2$$

$$\partial_t = k \partial_k$$

solution:

$$M^2(k) = M^2 + 2c_M k^2$$

Flowing Planck mass M²(k)

$$\partial_t M^2 = 4ck^2$$

Dimensionless squared Planck mass

$$w = \frac{M^2}{2k^2}$$

$$w = \frac{M^2}{2k^2} \quad \partial_t w = -2w + 2c$$

solution:

$$w = c + \frac{\bar{M}^2}{2k^2}$$

$$M^2(k) = M^2 + 2c_M k^2$$

Fixed point and flow away from fixed point

UV - fixed point

$$w_* = c$$

$$\partial_t w = -2w + 2c$$

approached for k → ∞

$$w = c + \frac{\bar{M}^2}{2k^2}$$

$$M^2(k) = M^2 + 2c_M k^2$$

Near UV – fixed point : M ~ k

$$\tilde{M}_{p*}^2 = 2c$$

Transition to constant M for small k, gravity gets weak, w -1 decreases to zero

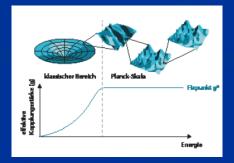
M is relevant parameter, cannot be predicted

Weak and constant gravity

$$M_{\mathbf{p}}^{2}(k) = \begin{cases} \tilde{M}_{\mathbf{p}*}^{2} k^{2} & \text{for } k > k_{t} \\ M^{2} & \text{for } k < k_{t} \end{cases}$$

$$k_t^2 = \frac{M^2}{\tilde{M}_{\mathbf{p}*}^2}$$

$$M_{\rm p}^2(k) = M^2 + \tilde{M}_{\rm p*}^2 k^2$$



Two regimes for the (inverse) strength of gravity

$$\tilde{M}_{\rm p}^2 = \frac{M_{\rm p}^2}{k^2} = \tilde{M}_{\rm p*}^2 \left[\left(\frac{k_t}{k} \right)^2 + 1 \right]$$

Gravitational contribution to running quartic coupling

$$\partial_t \lambda = A_\lambda \lambda$$

$$\partial_t \lambda = A_{\lambda} \lambda$$
 $A = \frac{1}{48\pi^2 \tilde{M}_{\rm p}^2} \left[\frac{20}{(1-v_0)^2} + \frac{1}{(1-v_0/4)^2} \right]$

$$\partial_t = k \partial_k$$

running Planck mass:

$$M_{\rm p}^2(k) = M^2 + \tilde{M}_{\rm p*}^2 k^2$$

dimensionless squared Planck mass

$$\tilde{M}_{\rm p}^2 = \frac{M_{\rm p}^2}{k^2} = \tilde{M}_{\rm p*}^2 \left[\left(\frac{k_t}{k} \right)^2 + 1 \right] \qquad k_t^2 = \frac{M^2}{\tilde{M}_{\rm p*}^2}$$

$$k_t^2 = \frac{M^2}{\tilde{M}_{\rm p*}^2}$$

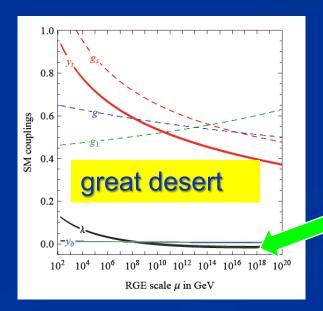
large k: constant A

small k: $A \sim k^2 / M^2$

transition at $k_t \sim 10^{19} \text{ GeV}$

Prediction for quartic Higgs coupling

- great desert
- high scale fixed point
- quartic scalar coupling predicted to be very small at transition scale where gravity decouples



fixed point

Quantum Gravity

Quantum Gravity is a renormalisable quantum field theory

Asymptotic safety

Asymptotic safety of quantum gravity

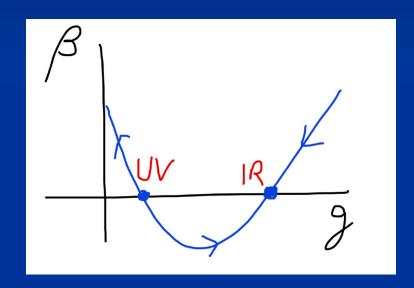
if UV fixed point exists:

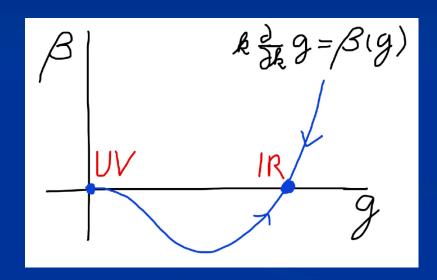
quantum gravity is non-perturbatively renormalizable!

S. Weinberg, M. Reuter

Asymptotic safety

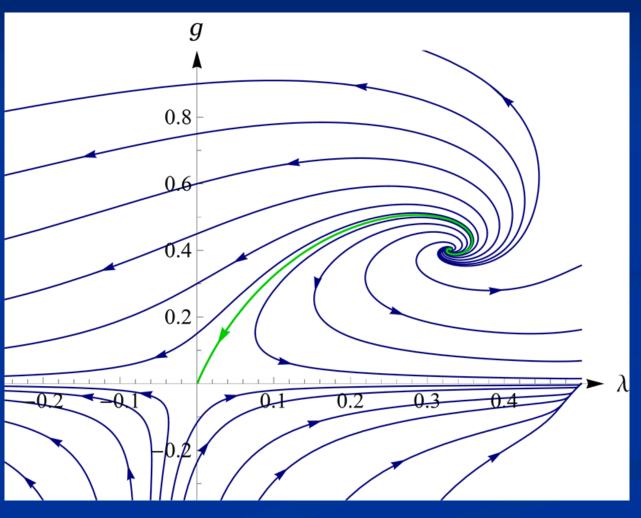
Asymptotic freedom





Relevant parameters yield undetermined couplings. Quartic scalar coupling is not relevant and can therefore be predicted.

UV- fixed point for quantum gravity



Wikipedia

Enhanced predictivity for UV – fixed point

- Free parameters of a theory correspond to relevant parameters for small deviations from fixed point.
- If the number of relevant parameters at the UV-fixed point is smaller than the number of free parameters (renormalizable couplings) in the standard model:
- Relations between standard model parameters become predictable!

Fixed points

$$g = \{g_1, ..., g_i, ...\}$$
 $\tilde{g}_i = g_i k^{-d_i}$

$$\tilde{g}_i = g_i k^{-d_i}$$

couplings

dimensionless

Flow equation

$$\partial_t \tilde{g}_i = \beta_i(\tilde{g})$$

Fixed points: zeros of beta-function No running No scale Quantum scale symmetry

Stability matrix

$$g = \{g_1, ..., g_i, ...\} \quad \tilde{g}_i = g_i k^{-d_i}$$

$$\tilde{g}_i = g_i k^{-d_i}$$

couplings

dimensionless

Flow equation

$$\partial_t \tilde{g}_i = \beta_i(\tilde{g}) = -d_i \tilde{g}_i + f_i(\tilde{g})$$

Expand in vicinity of fixed point

$$\partial_t \tilde{g}_i = \sum_j \frac{\partial \beta_i}{\partial \tilde{g}_j} \bigg|_{\tilde{g} = \tilde{g}_*} (\tilde{g}_j - \tilde{g}_{j*}) = -T_{ij} (\tilde{g}_j - \tilde{g}_{j*})$$

T: stability matrix

Critical exponents

$$\partial_t \tilde{g}_i = \sum_j \frac{\partial \beta_i}{\partial \tilde{g}_j} \bigg|_{\tilde{g} = \tilde{g}_*} (\tilde{g}_j - \tilde{g}_{j*}) = -T_{ij} (\tilde{g}_j - \tilde{g}_{j*})$$

 $\frac{\theta_l}{\theta_l}$: Eigenvalues of stability matrix T = Critical exponents

Linearized solution

$$\tilde{g}_i = \tilde{g}_{i*} + \sum_{l} C_l V_i^l \left(\frac{k}{\mu}\right)^{-\theta_l}$$

Irrelevant parameters: eigenvectors in coupling constant space with $\theta_l < 0$

flow towards fixed point values as k is lowered

Irrelevant parameters

- "Forget" information about initial values
- Central ingredient for predictivity of quantum field theories
- For UV complete theories: irrelevant parameters have to take precisely the fixed point values
- Relevant parameters flow away from fixed point as k is lowered – they are the only free parameters

Predictivity at fixed point

- Irrelevant parameters are predicted to take fixed point values
- Only relevant parameters are free
- Number of free parameters of a renormalizable quantum field theory = number of relevant parameters at the fixed point

a prediction...

Asymptotic safety of gravity and the Higgs'

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Institut für Theoretische Physik, Universität Heidelberg

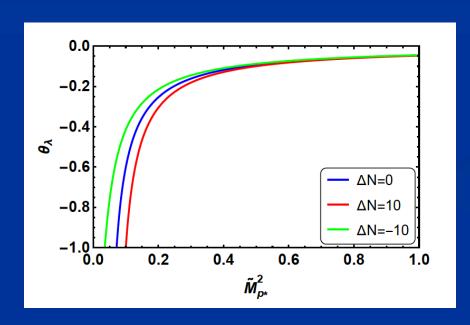
Abstract

coupling series in a low serie afe. The Standard Model (SM) plus gravity could be valid up to arbitrarily There are indications that gravity is a high energies. Supposing that the case and assuming that there are no intermediate energy scales between the stion of whether the mass of the Higgs boson m_H can be predicted. For a positive Fermi and Planck scales we $\lambda > 0$ the running of the quartic scalar self interaction λ at scales beyond the Planck gravity induced anomalor χ at zero. This results in $m_H = m_{\min} = 126$ GeV, with only a few GeV uncertainty. This mass is determined. prediction is inde details of the short distance running and holds for a wide class of extensions of the SM as well.

in $m_H = m_{\min} = 126$ GeV, with o

Quartic scalar coupling is irrelevant parameter

R. Perccacci et al



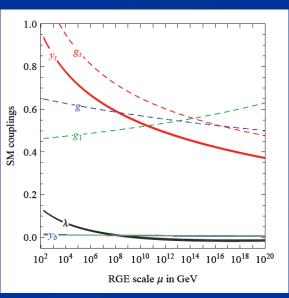
Pawlowski, Reichert, Yamada,...

Quartic couplings can be predicted!

Prediction of Higgs boson mass:

- Value of quartic scalar coupling near Planck mass is predicted by UV- fixed point
- Gravity decouples below Planck mass, resulting in perturbative flow

Extrapolate perturbatively to Fermi scale :



How to compute non-perturbative quantum gravity effects?

Quantum gravity computation by functional renormalization

Introduce infrared cutoff with scale k, such that only fluctuations with (covariant) momenta larger than k are included.

Then lower k towards zero

Exact renormalization group equation

Exact flow equation

for scale dependence of average action

$$\partial_k \Gamma_k[\varphi] = \frac{1}{2} \text{Tr} \left\{ \left(\Gamma_k^{(2)}[\varphi] + R_k \right)^{-1} \partial_k R_k \right\}$$

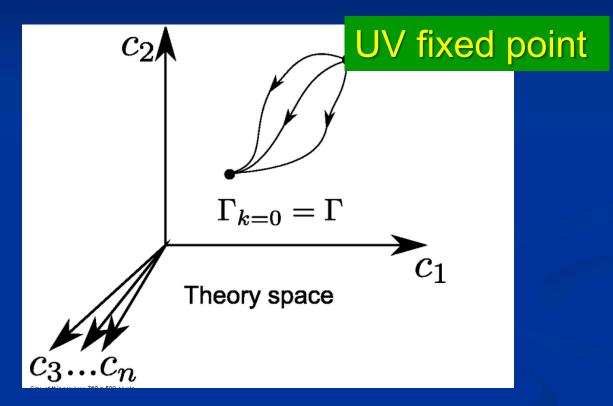
92

$$\left(\Gamma_k^{(2)}\right)_{ab}(q,q') = \frac{\delta^2 \Gamma_k}{\delta \varphi_a(-q)\delta \varphi_b(q')}$$

Tr:
$$\sum_{a} \int \frac{d^dq}{(2\pi)^d}$$

(fermions : STr)

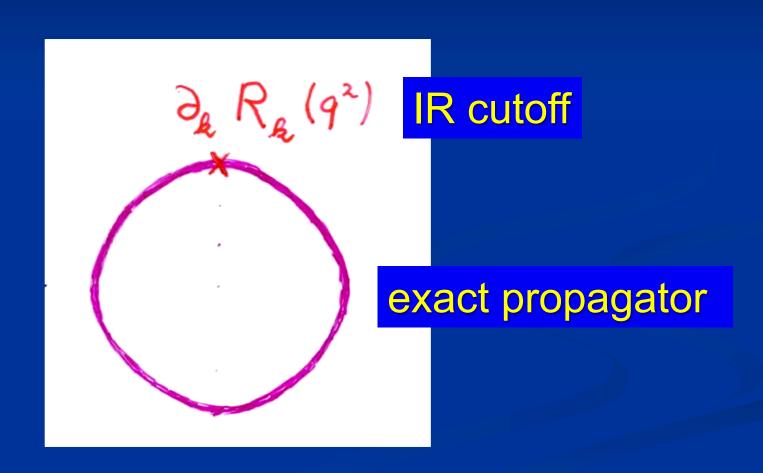
Ultraviolet fixed point



Extrapolation of microscopic law to infinitely short distances is possible.

Complete theory

Functional flow equation for scale dependent effective action



Gauge invariant flow equation involves projection on physical fluctuations

$$k\partial_k \bar{\Gamma} = \zeta_k = \pi_k + \delta_k - \epsilon_k$$

$$\pi_k = \frac{1}{2} Str(k\partial_k \bar{R}_P G_P)$$

G_P: propagator for physical fluctuations

$$PG_P = G_P P^T = G_P$$

$$\delta_{\xi}\bar{g} = (1 - P)\delta_{\xi}\bar{g}$$

measure contributions $\delta_k - \epsilon_k$ do not depend on effective action

$$\delta_k - \epsilon_k$$

Closed flow equation

projection on physical fluctuations makes second functional derivative invertible

$$\bar{\Gamma}_P^{(2)} = P^T \bar{\Gamma}^{(2)} P$$

$$\bar{\Gamma}_P^{(2)} = P^T \bar{\Gamma}^{(2)} P \qquad \bar{\Gamma}^{(2)ij} = \frac{\partial^2 \bar{\Gamma}}{\partial \bar{g}_i \partial \bar{g}_j}$$

$$\left(\bar{\Gamma}_P^{(2)} + \bar{R}_P\right) G_P = P^T$$

Gauge invariant flow equation

- similar to background field method with physical gauge
- for gravity: block diagonal form for physical modes and gauge modes
- gauge mode contribution together with regularization of Faddeev – Popov determinant (or equivalently ghosts) takes simple universal form

Prediction of mass of Higgs boson?

Quartic scalar coupling irrelevant?

needs $\theta_l < 0$ or A>0

Flow equation for dimensioless effective potential and field dependent Planck mass

M. Yamada, ...

truncation: (K=1)

$$\bar{\Gamma}_k = \int_x \sqrt{g} \left\{ -\frac{F}{2}R + U + \sum_{i=1}^{N_S} \frac{K_i}{2} \partial^{\mu} \varphi_i \partial_{\mu} \varphi_i \right\}$$

dimensionless fields and functions

$$\tilde{\rho} = \rho/k^2$$

$$\tilde{\rho} = \rho/k^2 \frac{u(\tilde{\rho}) = U/k^4}{w(\tilde{\rho}) = F/2k^2}$$

effective potential

$$k\partial_{k}u = 2\tilde{\rho}\,\partial_{\tilde{\rho}}u - 4u + \frac{1}{32\pi^{2}}\left(N_{S} - 2N_{F} + 2N_{V} - \frac{8}{3}\right) + \frac{5}{24\pi^{2}}\left(1 - \frac{u}{w}\right)^{-1},\tag{5}$$

gravitational coupling

$$k\partial_k w = 2\tilde{\rho}\,\partial_{\tilde{\rho}} w - 2w + \frac{1}{96\pi^2} \left(-N_S - N_F + 4N_V + \frac{43}{6} \right) + \frac{25}{64\pi^2} \left(1 - \frac{u}{w} \right)^{-1}. \tag{6}$$

scaling solution for massless particles

$$\partial_t u(\tilde{\rho}) = 2\tilde{\rho} \,\partial_{\tilde{\rho}} u - 4 \left[u - \frac{1}{128\pi^2} \left(\tilde{\mathcal{N}}_U + \frac{20}{3(1-v)} \right) \right] ,$$

$$\partial_t w(\tilde{\rho}) = 2\tilde{\rho} \, \partial_{\tilde{\rho}} w - 2 \left[w - \frac{1}{192\pi^2} \left(\tilde{\mathcal{N}}_M + \frac{75}{2(1-v)} \right) \right]$$

$$\tilde{\mathcal{N}}_U = \mathcal{N}_U - \frac{8}{3} = N_S + 2N_V - 2N_F - \frac{8}{3}$$

$$\tilde{\mathcal{N}}_M = \mathcal{N}_M + \frac{43}{6} = -N_S + 4N_V - N_F + \frac{43}{6}$$

$$v = \frac{u}{w}$$

scaling solution: r.h.s. vanishes

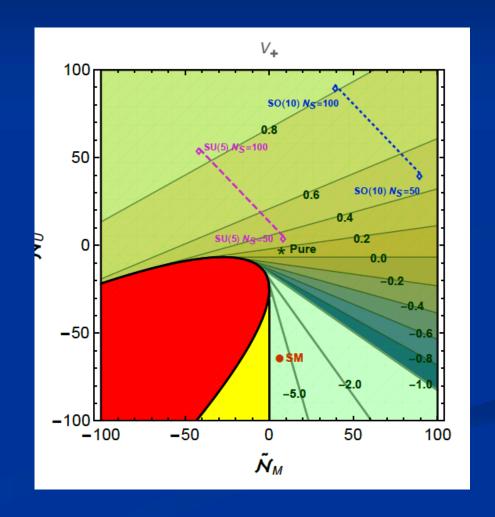
constant scaling solution

$$u_* = \frac{1}{128\pi^2} \left(\tilde{\mathcal{N}}_U + \frac{20}{3(1 - v_*)} \right),$$

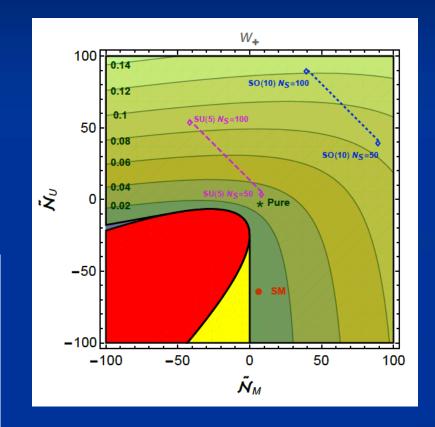
$$w_* = \frac{1}{192\pi^2} \left(\tilde{\mathcal{N}}_M + \frac{75}{2(1 - v_*)} \right)$$

$$v_* = \frac{u_*}{w_*} = \frac{3\tilde{\mathcal{N}}_U(1 - v_*) + 20}{2\tilde{\mathcal{N}}_M(1 - v_*) + 75}$$

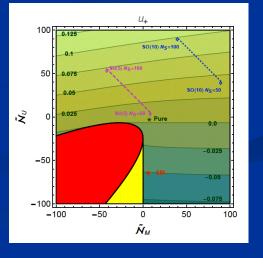
$$\begin{split} \partial_t u(\tilde{\rho}) &= 2\tilde{\rho} \, \partial_{\tilde{\rho}} u - 4 \left[u - \frac{1}{128\pi^2} \left(\tilde{\mathcal{N}}_U + \frac{20}{3(1-v)} \right) \right] \,, \\ \partial_t w(\tilde{\rho}) &= 2\tilde{\rho} \, \partial_{\tilde{\rho}} w - 2 \left[w - \frac{1}{192\pi^2} \left(\tilde{\mathcal{N}}_M + \frac{75}{2(1-v)} \right) \right] \end{split}$$



stable gravity: w > 0







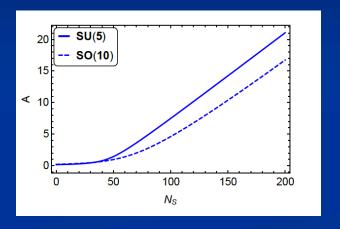
Critical exponents

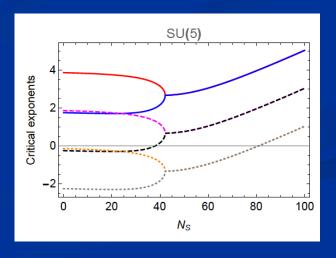
$$\partial_t \tilde{g}_i = -T_{ij}(\tilde{g}_j - \tilde{g}_{j*})$$

$$\tilde{g}_i = (u_0, w_0, \tilde{m}_H^2, \xi_H, \tilde{\lambda}_H, w_2)$$

$$T_{ij} = -\frac{\partial \beta_i}{\partial g_j} \bigg|_{g_j = g_{j*}}$$

$$T^{(56)} = \begin{pmatrix} -A & Av \\ -\frac{15A}{8} & -2 + \frac{15Av}{8} \end{pmatrix}$$





Quartic scalar couplings are
irrelevant couplings
for all models

(within range of validity of truncation)

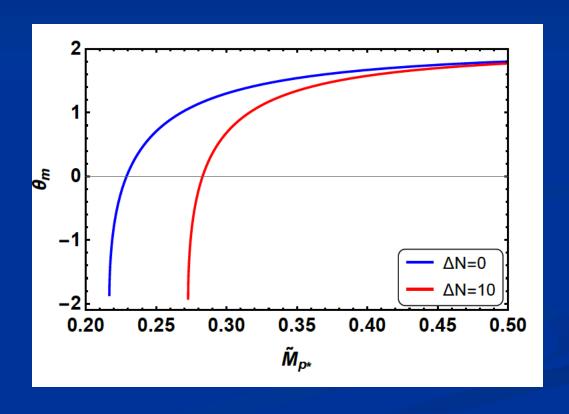
Quartic scalar couplings are predicted for given quantum field theories with gravity

Predictivity for Fermi scale?

Scalar mass term irrelevant?

Higgs mass term is irrelevant for strong enough gravity?

Neglecting mixing with other couplings:



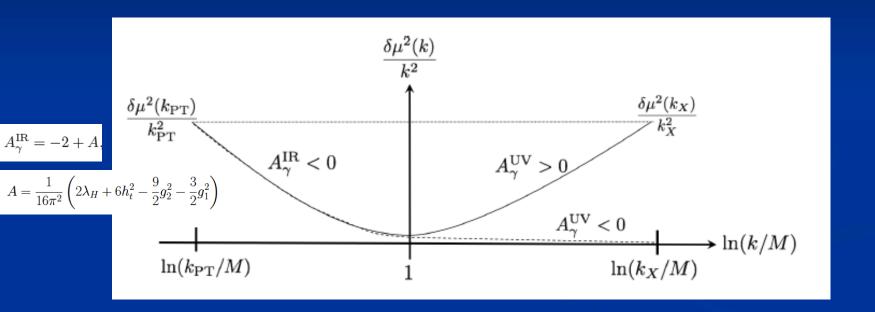
Gauge hierarchy

Possible explanation of small parameter: distance from second order vacuum electroweak phase transition is

irrelevant parameter

at UV – fixed point

Possible explanation of gauge hierarchy



Gauge hierarchy problem in asymptotically safe gravity –the resurgence mechanism

Christof Wetterich¹ and Masatoshi Yamada¹

Phys.Lett. B770 (2017) 268-271

Prediction of Fermi scale

- If scalar mass term is irrelevant and vacuum electroweak phase transition would be precisely second order:
- The Fermi scale would be predicted to be zero!
- Running gauge and Yukawa couplings in standard model imply that vacuum electroweak phase transition is not precisely second order. Small effect.
- Small Fermi scale and huge gauge hierarchy expected.
- May be a couple of orders too small as compared to observation? Not known definitely.

Predictions of quantum gravity?

Simple approximation for graviton contribution to scalar potential:

- Predicts mass of Higgs scalar
- Solves Gauge Hierarchy problem?
- Solves cosmological constant problem

Conclusions

 Quantum gravity is a renormalizable quantum field theory, realized by UV - fixed point of running couplings or flowing effective action

Quantum gravity is predictive :

Mass of the Higgs boson (and more ...?)

Properties of inflation

Properties of dark energy

Quantum gravity prediction for the cosmological "constant"?

Variable Gravity

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} \left(B(\chi/\mu) - 6 \right) \partial^\mu \chi \partial_\mu \chi \right\}$$

quantum effective action, variation yields field equations

Asymptotically vanishing cosmological "constant"

What matters: Ratio of potential divided by fourth power of Planck mass

$$\frac{V}{\chi^4} = \frac{\mu^2 \chi^2}{\chi^4} = \frac{\mu^2}{\chi^2}$$

■ vanishes for $\chi \rightarrow \infty$!

small dimensionless number?

- needs two intrinsic mass scales
- standard approach :V and M (cosmological constant and Planck mass)
- variable gravity : Planck mass moving to infinity , with fixed V → ratio vanishes asymptotically!

Variable Gravity in scaling frame

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} \left(B(\chi/\mu) - 6 \right) \partial^\mu \chi \partial_\mu \chi \right\}$$

Variable gravity in Einstein frame

Weyl scaling:

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu} , \ \varphi = \frac{2M}{\alpha} \ln\left(\frac{\chi}{\mu}\right)$$

effective action in Einstein frame:

$$\Gamma = \int_{x} \sqrt{g'} \left\{ -\frac{1}{2} M^{2} R' + V'(\varphi) + \frac{1}{2} k^{2}(\varphi) \partial^{\mu} \varphi \partial_{\mu} \varphi \right\}$$

$$V'(\varphi) = M^4 \exp\left(-\frac{\alpha\varphi}{M}\right)$$
 $k^2 = \frac{\alpha^2 B}{4}$

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Quintessence

Dynamical dark energy, generated by scalar field (cosmon)

Prediction:

homogeneous dark energy influences recent cosmology

- of same order as dark matter -

Original models do not fit the present observations modifications

(different growth of neutrino mass)

Quantum gravity restricts the increase of scalar potential for large fields

In quantum gravity,
the graviton fluctuations can
play an important role on
distances as large as the
size of the Universe

- for long range scalar fields and dynamical dark energy
- not for all quantities

Graviton barrier

Quantum gravity computation:

For
$$\chi \to \infty$$

V cannot increase stronger than M²!

Instability of graviton propagator is avoided

Graviton barrier and solution of the cosmological constant problem

V cannot increase stronger than M²!

If M increases with χ , and for cosmological solutions where χ asymptotically diverges for time going to infinity:

Effective cosmological constant vanishes in infinite future

$$\mathbf{M} = \chi : \mathbf{V} = \mu^2 \chi^2$$

Asymptotically vanishing cosmological "constant"

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