

Post-inflationary particle production: Sterile Neutrino with Secret Interactions

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Based on - A. Paul, A. Ghoshal, A. Chatterjee and S. Pal, arXiv:1808.09706 [astro-ph.CO] ¹

Outline of talk:

- Preheating
 - Analytic Understanding
 - Effect of Self Interaction term
 - Numerical Simulations (LATTICEASY)

- Scenario: Sterile Neutrinos
 - Neutrino Anomalies and introducing Sterile Neutrinos
 - Effects of neutrinos in cosmology
 - Secret Interaction with Pseudoscalar
 - Production from Preheating and constraints

- Conclusion

Pointer: A general problem for all cosmology models which predict light bosonic degrees of freedom with negligible initial abundance - Sterile ν , light DM, asymmetric DM, non-standard neutrino interaction, leptogenesis models, etc. Enhanced production from inflationary reheating.

What is Preheating?

- **Inflation:**

- Accelerated expansion of universe at the beginning to solve **Horizon problem**, **Flatness problem**, give **initial seed fluctuation** to explain structure formation
- Driven generally by energy density stored in a Scalar field, **Inflaton**

- **Dynamics of Inflaton after Inflation:**

- After slow-roll ends, inflaton field oscillates around the minima of potential
- Energy density of oscillating inflaton field evolves as matter $\sim 1/a^3$ for quadratic inflation
- Oscillating inflaton field is interpreted as collection of stationary inflaton particles which decay **perturbatively** - Reheating

- **Preheating:**

- **Non-perturbative** production of particles from the classical oscillating inflaton field
- Any field χ can be decomposed into fourier modes,

$$\chi(t, x) = \int \frac{d^3k}{(2\pi)^{3/2}} \left(a_k \chi_k e^{-ik \cdot x} + a_k^\dagger \chi_k^* e^{ik \cdot x} \right)$$

- Dynamics of the modes χ_k of a field χ are given by Mathieu equation -

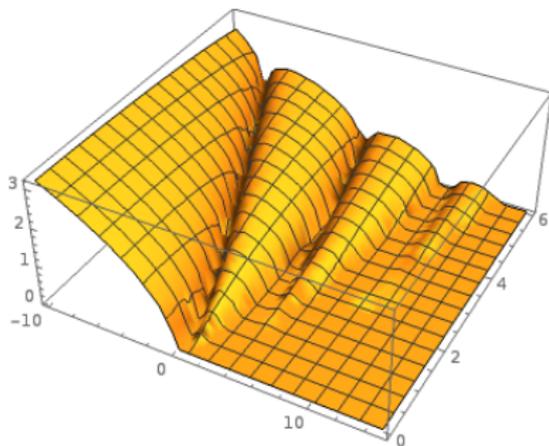
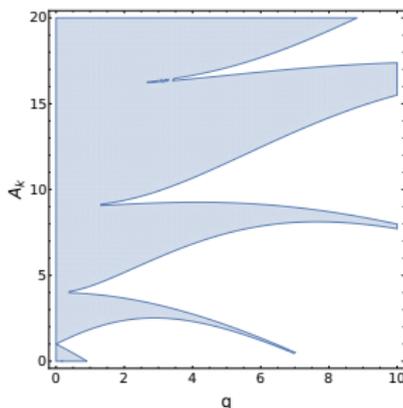
$$\frac{d^2 \chi_k}{dz^2} + (A_k - 2q \cos(2z)) \chi_k = 0$$

(where $z = m_\phi t$, $q = \frac{\lambda_\phi \chi \phi^2}{4m_\phi^2}$, $A_k = \frac{k^2}{m_\phi^2 a^2} + 2q$, a =Scale factor, t =time,

Φ =Amplitude of ϕ oscillation, the potential is $\frac{1}{2} m_\phi^2 \phi^2 + \frac{1}{2} \lambda_\phi \chi \phi^2 \chi^2$)

Mathieu instability bands

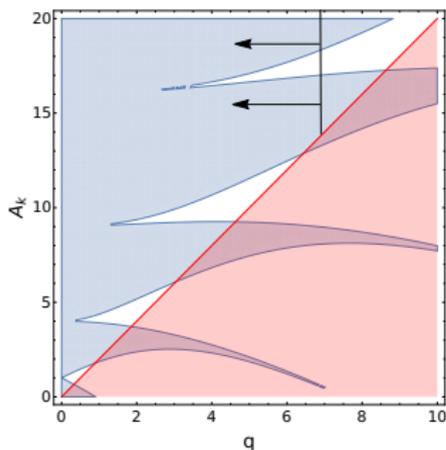
- Mathieu equation has oscillatory solution in certain regions (blue) of the $A_k - q$ parameter space, and exponentially growing solution at other regions (white) -



- Growing modes are interpreted as particle production
- For some q , lowest A_k has highest exponent of growing
- In terms of decay process of inflaton into bosons, this exponential growth in certain momentum modes can be understood as Bose enhancement, i.e. when a inflaton decays into two χ particles with momentum $m_\phi/2$, decayrate gets enhanced by a factor $(1 + 2n_k)$, resulting a exponential growth in those modes

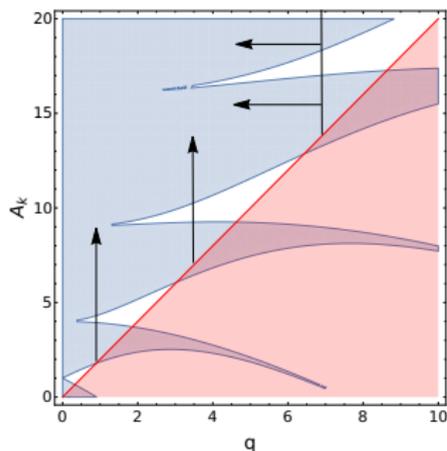
Identifying Growing modes with time

- We have, $q = \frac{\lambda_{\phi\chi}\phi^2}{4m_\phi^2}$, $A_k = \frac{k^2}{m_\phi^2 a^2} + 2q$
- For an interaction $\frac{1}{2}\lambda_{\phi\chi}\phi^2\chi^2$, an effective mass term of inflaton emerges
 $m_\phi^{eff} = \sqrt{m_\phi^2 + \lambda_{\phi\chi}\langle\chi^2\rangle}$
- So, with time Φ decreases and m_ϕ^{eff} increases, resulting a decrement in q
- The bands of growing modes gets narrower, but lower momentum modes become growing modes



Effect of Quartic self-interaction of χ

- $\lambda_\chi \chi^4$ gives rise to effective mass term of χ , $m_\chi^{eff} = \sqrt{\lambda_\chi \langle \chi^2 \rangle}$
- A_k gets modified into $A_k = \frac{k^2}{m_\phi^2 a^2} + \frac{m_\chi^2}{m_\phi^2} + 2q$



- Blocks lower momentum modes to come into play - **Quartic Blocking**

Numerical Simulation: LATTICEEASY

- As time goes on and the fluctuations grow, these effects begin to show up, Mathieu equation becomes insufficient to describe the preheating dynamics
- Numerical simulations become important to get accurate dynamics
- We use publicly available code LATTICEEASY for the simulation

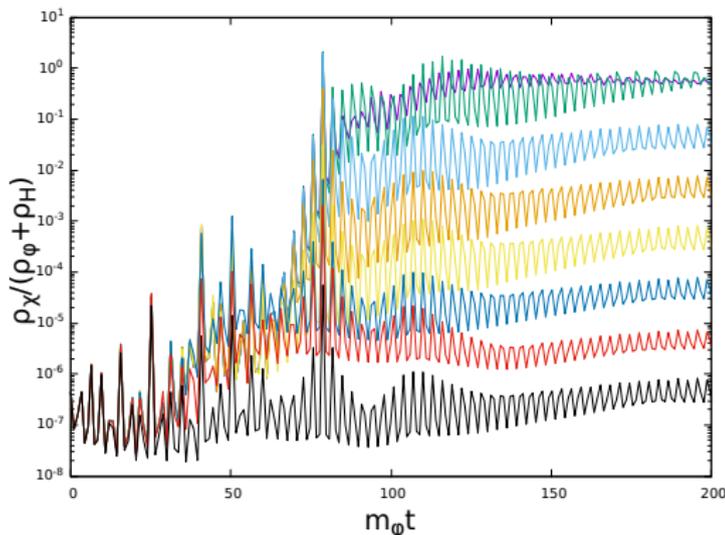


Figure: Quartic blocking - $\lambda_X = 10^i$ for $i = -7$ to 1 (from top to bottom)

Scenario 1: Sterile Neutrino Sector ¹

- Neutrino oscillation: Neutrinos can change flavour
- A flavour eigenstate is linear combination of mass eigenstates (which evolve in time as hamiltonian eigenstates)

$$|\nu_\alpha\rangle = \sum_{k=1}^3 U_{\alpha k}^* |\nu_k\rangle$$

$$|\nu_\alpha(t)\rangle = \sum_{k=1}^3 U_{\alpha k}^* e^{-iE_k t} |\nu_k\rangle$$

- Probability of detecting another flavour at time t,

$$P_{\nu_\alpha \rightarrow \nu_\beta} = |\langle \nu_\beta | \nu_\alpha(t) \rangle|^2 = \sum_{k,j=1}^3 U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^* e^{-i(E_k - E_j)t}$$

- For relativistic neutrinos,

$$E_i = \sqrt{|\vec{p}|^2 + m_i^2} \approx |\vec{p}| + \frac{m_i^2}{2|\vec{p}|}$$

$$P_{\nu_\alpha \rightarrow \nu_\beta} = \sum_{k,j=1}^3 U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^* \exp\left(-i \frac{\Delta m_{kj}^2}{2|\vec{p}|} t\right)$$

⇒ *Neutrino Oscillation* (depends on momentum and mass squared difference)

Based on - A. Paul, A. Ghoshal, A. Chatterjee and S. Pal, arXiv:1808.09706 [astro-ph.CO] ¹

Neutrino Anomalies

- Small Baseline Experiments:
 - LSND and MiniBooNE observed excess in $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ channel
 - MiniBooNE have also indicated an excess of ν_e in the ν_μ beam
- Within a 3+1 framework, MiniBooNE result hints towards the existence of a sterile neutrino with eV mass at 4.8σ significance, which raises to 6.1σ when combined with the LSND data
- Daya Bay, NEOS, DANSS and other reactor experiments probed the ν_e disappearance in the $\bar{\nu}_e \rightarrow \bar{\nu}_e$ channel
- GALLEX ,SAGE have performed similar measurements in the $\nu_e \rightarrow \nu_e$ channel
- Caution: $\nu_\mu(\bar{\nu}_\mu) \rightarrow \nu_e(\bar{\nu}_e)$ appearance in LSND and MiniBooNE are in tension with strong constraints on ν_μ disappearance, mostly from MINOS and IceCUBE, while attempting to fit together using a 3+1 framework
- Although debatable in 3+1 framework, such a light additional sterile neutrino, with mixing $\sin \theta \lesssim \mathcal{O}(0.1)$ with the active neutrino species, can be consistent with constraints from various terrestrial neutrino experiments

From Particle Physics and Cosmology

- **Conclusions (from PP)-**

1. Neutrinos are massive (atleast (n-1) of n species) and oscillate between flavour eigenstates

2. Neutrino anomalies can possibly be solved if an extra sterile neutrino with eV mass and sizable mixing with active neutrinos is postulated

- **Cosmology** is affected mainly by 2 parameters related to neutrinos -

1. Total mass of neutrinos $\sum m_{\nu_i}$

2. Effective number of neutrinos N_{eff}

- $\sum m_{\nu_i}$ affects cosmology through -

$$\Omega_{\nu} = \frac{\sum m_{\nu_i} n_{\nu,0}}{\rho_{cr,0}} = \frac{\sum m_{\nu_i}}{eV} \frac{1}{94.1(93.1)h^2}$$

- N_{eff} affects cosmology through -

$$\rho_R = \rho_{\gamma} \left(1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} N_{\text{eff}} \right)$$

- These equations assume thermalization of neutrino species

Big Bang Nucleosynthesis (BBN)

- Before nucleosynthesis protons and neutrons were in equilibrium by weak interactions through active neutrinos
- As long as equilibrium holds, n:p ratio decreases exponentially with time -

$$\frac{n}{p} = \exp\left(\frac{-\Delta m}{T}\right)$$

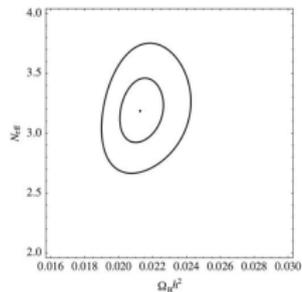
unless interaction rate becomes comparable to expansion rate H

→ reaction seizes

→ equilibrium breaks down

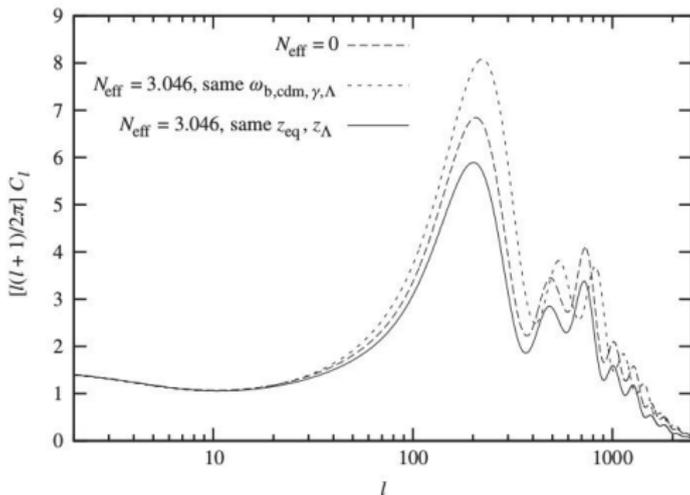
→ neutrinos decouple and n:p ratio stays frozen

- Nucleosynthesis (production of light nuclei ${}^2\text{H}$, ${}^3\text{He}$, ${}^4\text{He}$, ${}^7\text{Li}$ from neutron and proton) happens
 - Neutrons are unstable → only primordial n's present today are preserved in atoms mostly in ${}^4\text{He}$
- Larger N_{eff}
 - larger radiation density
 - larger Hubble parameter
 - earlier neutrino decoupling
 - larger n:p at freezeout
 - larger ${}^4\text{He}$ abundance
 - ${}^4\text{He}$ abundance data → N_{eff} is allowed upto 3.5 at 68% CL



Cosmic Microwave Background (CMB)

- Larger N_{eff}
 - larger radiation density
 - later matter radiation equality
 - less time between equality and photon decoupling
 - smaller sound horizon
 - CMB TT peaks at higher l values with higher peak heights
- From CMB PS, adding the extra parameter N_{eff} with the other six, we can constrain N_{eff}



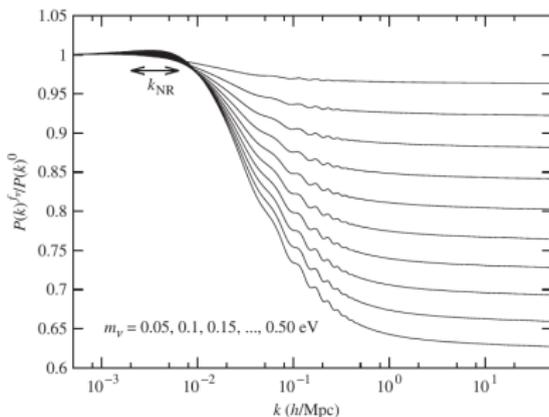
Large Scale Structure (LSS)

- In linear scalar perturbation theory, modes evolve as -

$$\delta_i'' + \frac{a'}{a} \delta_i' + \left(k^2 - \frac{3a^2 \mathcal{H}^2}{c_s^2} \right) c_s^2 \delta_i = 0$$

- Neutrino density enters the equation through \mathcal{H} and \mathcal{H}^2 term by Friedman equation
- A freestreaming length can be defined under which length scale the perturbation is suppressed -

$$\lambda_{fs}(\eta) = a(\eta) \frac{2\pi}{k_{fs}} = 2\pi \sqrt{\frac{2}{3}} \frac{c_\nu(\eta)}{\mathcal{H}(\eta)}$$



Constraints from Cosmology and Saving Sterile Neutrino: Pseudoscalar Interaction

$$\Delta N_{\text{eff}} \lesssim 0.5$$

$$\sum m_{\nu_i} < 0.16 \text{ eV (PLANCK TT + Low E + BAO)}$$

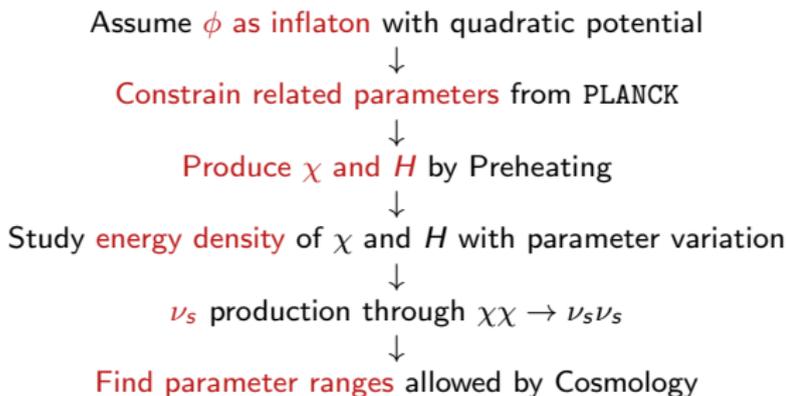
- **Conclusion from Standard Cosmology-**
Extra neutrino species needed by particle physics is **not allowed** in cosmology if thermalized
- **Saving Sterile Neutrino:** Hannestad et al. showed that adding a pseudoscalar interaction can solve the tension -

$$\mathcal{L} \sim g_s \chi \bar{\nu}_s \gamma_5 \nu_s$$

- MSW like potential induced by new interaction with $10^{-4} \gtrsim g_s \gtrsim 10^{-6}$ suppress sterile neutrino production by suppressing mixing angle until after neutrino decoupling, thus not letting it thermalise with plasma
- At late time, annihilation of ν_s to χ particles with chosen $m_\chi \lesssim 0.1\text{eV}$ can evade the mass bound of neutrinos
- From supernova energy loss argument $g_s \lesssim 10^{-4}$

Problem with this model

- We start at the inflationary epoch and see if the model fits in there
- Our workplan -



- A pseudoscalar χ coupled to the inflaton gets produced copiously during preheating
- Such an extra relativistic species is in direct conflict with N_{eff} bounds of BBN
- Need to suppress production of χ from preheating - **Quartic Blocking** or non-relativistic phase of inflaton

Potential and Parameter Choice

- The scalar potential is,

$$V = \frac{m_\phi^2}{2} \phi^2 + \frac{\lambda_\phi}{4} \phi^4 + \frac{\lambda_\chi}{4} \chi^4 + \frac{\lambda_H}{4} |H|^4 + \frac{\sigma_{\phi\chi}}{2} \phi \chi^2 + \frac{\sigma_{\phi H}}{2} \phi |H|^2 + \frac{\lambda_{\phi\chi}}{2} \phi^2 \chi^2 + \frac{\lambda_{\phi H}}{2} \phi^2 |H|^2 + \frac{\lambda_{\chi H}}{2} \chi^2 |H|^2$$

- Parameter choices:** $m_\phi = 10^{-6} M_{\text{pl}}$ (successful inflation with small non-minimal coupling to gravity $\mathcal{O}(10^{-3})$)
 $\lambda_\phi = 10^{-14}$ (even if kept 0, will be generated through RGE)
 $\lambda_{\phi\chi} = \lambda_{\phi H} = 10^{-7}, 10^{-6}$ ($\gtrsim 10^{-8}$ for efficient preheating, higher value can ruin inflation)
 $\sigma_{\phi H} = 10^{-10}$ and $10^{-8} M_{\text{pl}}$ (to show two scenarios, one with a non-relativistic phase and one without)
 $\lambda_H = 10^{-7}$ and 10^{-4} (to keep minima of potential at 0,0,0 in field space, avoiding any additional mass term for χ or H)
 $\sigma_{\phi\chi}$ neglected (to avoid additional χ population during decay of ϕ)
 $\lambda_{\chi H}$ neglected (to avoid thermalisation between χ and H)
 λ_χ kept variable to suppress χ production variably
- Isocurvature bounds ($m_H, m_\chi > H$ during inflation) are trivially satisfied for parameter choice of $\lambda_{\phi\chi} = \lambda_{\phi H} = 10^{-7}$

ΔN_{eff} contribution from χ produced in (p)reheating

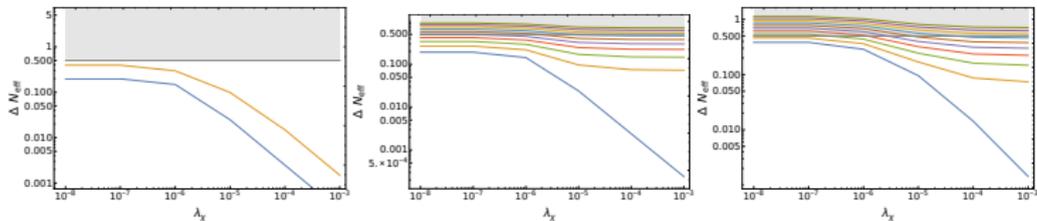


Figure: $\lambda_H = 10^{-7}$, $\sigma_{\phi H} = 10^{-10} M_{Pl}$, $\lambda_{\phi\chi} = \lambda_{\phi H} = 10^{-7}, 10^{-6}$ from bottom to top for the left panel. Plots in the centre and right panels correspond to the cases $\lambda_{\phi\chi} = \lambda_{\phi H} = 10^{-7}, 10^{-6}$, when a fraction of the inflaton (0 to 0.1 in steps of 0.01, from bottom to top) decays into χ respectively.

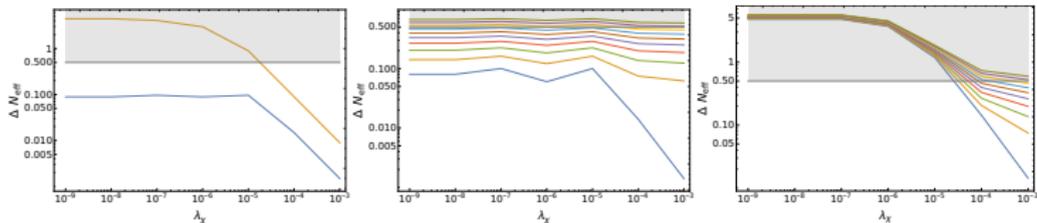


Figure: $\lambda_H = 10^{-4}$, $\sigma_{\phi H} = 10^{-8} M_{Pl}$, $\lambda_{\phi\chi} = \lambda_{\phi H} = 10^{-7}, 10^{-6}$ from bottom to top for the left panel. Plots in the centre and right panels correspond to the cases $\lambda_{\phi\chi} = \lambda_{\phi H} = 10^{-7}, 10^{-6}$, when a fraction of the inflaton (0 to 0.1 in steps of 0.01, from bottom to top) decays into χ respectively.

Additional bounds in $m_\chi - g_s$ plane

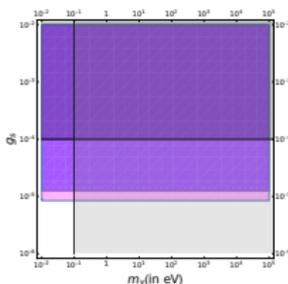


Figure: The blue and magenta regions correspond to the allowed regions in $m_\chi - g_s$ plane from N_{eff} constraints of BBN ($\Delta N_{\text{eff}} \lesssim 0.5$) for $\theta_0 = 0.1$ and 0.05

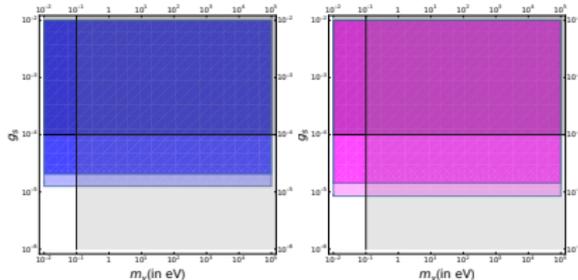


Figure: The region with lighter shade corresponds to the allowed region from N_{eff} constraints of BBN (for $\Delta N_{\text{eff}} \lesssim 0.5$). The region with darker shade is the new bound, if χ being produced during (p)reheating leads to a $\Delta N_{\text{eff}} = 0.4$. Left and right panels correspond to $\theta_0 = 0.1$ and 0.05 .

Conclusion

- Production of a scalar during preheating can be suppressed with a quartic self interaction term

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- **Scenario:**
 - A sterile neutrino (with eV mass and sizable mixing with active neutrinos) is required to solve neutrino anomalies
 - This species, if thermalised with SM, is highly constrained by N_{eff} bounds from BBN
 - Secret interaction with χ is required to block ν_s production from ν_{active} upto BBN
 - New production channel opens through $\chi\chi \rightarrow \nu_s\nu_s$
 - To suppress this production channel, χ needs to be of sub-dominant energy-density after (p)reheating
 - This can be achieved through Quartic blocking and/or late inflaton decay into H giving rise to a non-relativistic phase

Thank You

Scenario 2: Dark Matter ²

- Presence of Dark Matter (DM) χ is motivationally well-established from observations at all scales - Astrophysical to Cosmological
- Production mechanism of DM is not so well-established
 - Standard mechanisms like freeze-out require SM-DM interactions
 - No such hint till now from direct or in-direct searches
- Interesting to explore DM production mechanisms without SM-DM interaction - Production of two uncoupled sectors (DM and SM) from (p)reheating ?
- To keep in mind:
 - Right DM relic, i.e. $\rho_\chi/\rho_{SM} = 5.3$ now
 - BBN bounds on extra relativistic species, i.e. $\rho_\chi/\rho_{SM} \lesssim 0.051$ during BBN
 - Isocurvature bounds

Based on - N. Bernal, A. Chatterjee and A. Paul, arXiv:1809.02338 [hep-ph] ²

Initial ρ_χ/ρ_{SM} required

- $\rho_\chi/\rho_{SM} = 5.3$ now, ρ_χ if present from beginning, needs to start much low on density (as depending on their mass m_χ , they become non-relativistic, giving boost to their density)

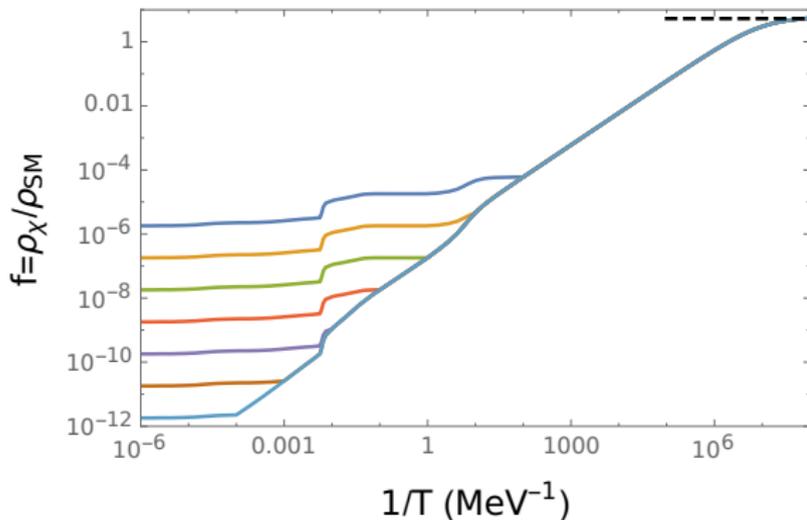


Figure: $m_\chi = 0.01, 0.05, 0.3, 2, 10, 50$ and 300 MeV (from top to bottom)

- BBN bounds are trivially satisfied for $m_\chi \gtrsim 0.01$ MeV as clear from figure

Potential and Parameter Choice

- The scalar potential is,

$$V = \frac{m_\phi^2}{2}\phi^2 + \frac{\lambda_\phi}{4}\phi^4 + \frac{\lambda_\chi}{4}\chi^4 + \frac{\lambda_H}{4}|H|^4 + \frac{\sigma_{\phi\chi}}{2}\phi\chi^2 + \frac{\sigma_{\phi H}}{2}\phi|H|^2 \\ + \frac{\lambda_{\phi\chi}}{2}\phi^2\chi^2 + \frac{\lambda_{\phi H}}{2}\phi^2|H|^2 + \frac{\lambda_{\chi H}}{2}\chi^2|H|^2$$

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 $\lambda_H = 10^{-7}$ (to prevent quartic blocking of Higgs)
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Production from Preheating with Quartic Blocking

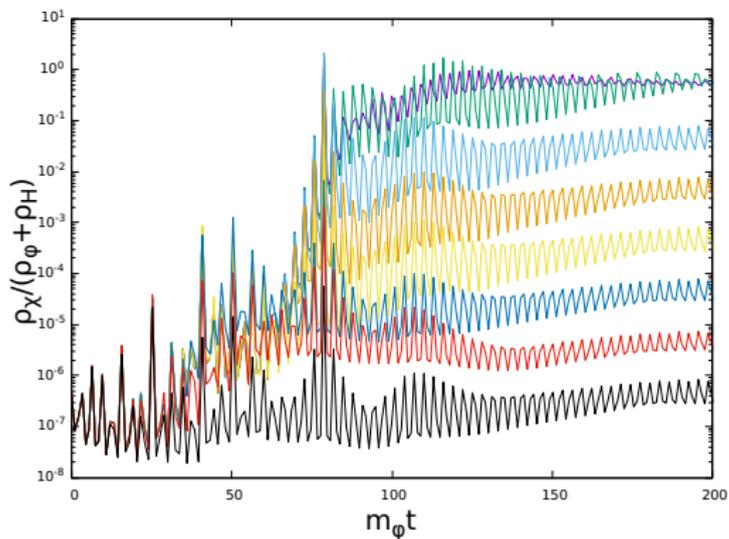
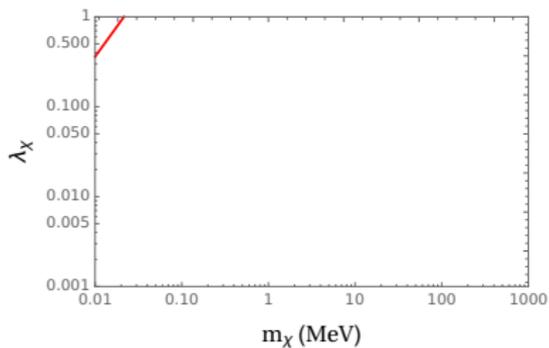
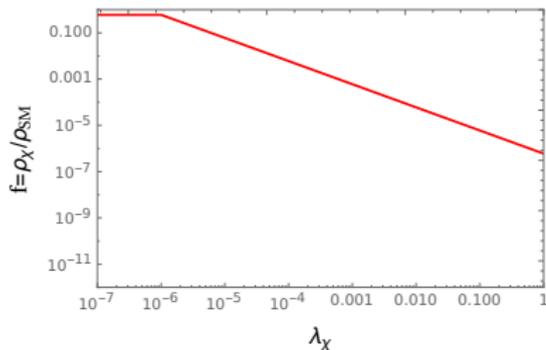


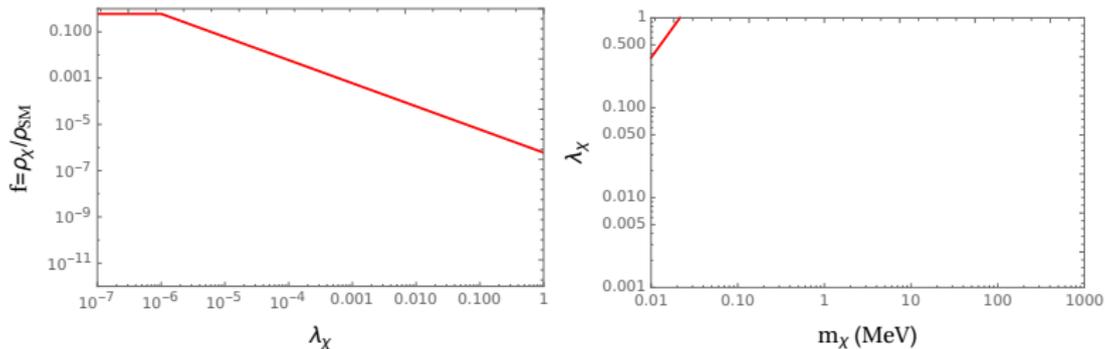
Figure: Result from LATTICEASY with $\lambda_X = 10^i$ for $i = -7$ to 1 (from top to bottom)

Is Quartic Blocking enough for right DM relic ?



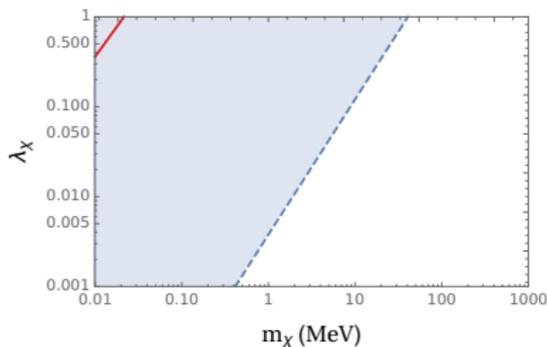
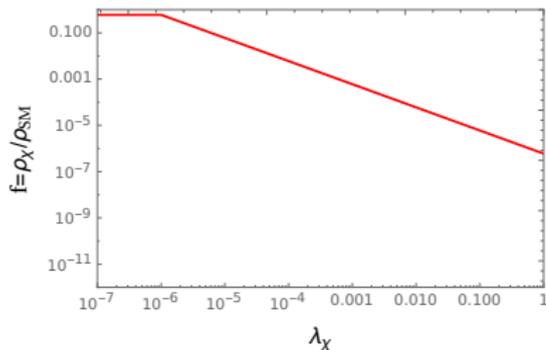
- Yes, for a very small range of m_χ

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Suppression due to non-relativistic phase of inflaton

- After preheating, a similar amount of energy density (like H) is still stored in inflaton
- Reheating ends when this left over energy density decays into other visible or dark sectors
- $\sigma_{\phi H}$ and $\sigma_{\phi\chi}$ helps to decay inflaton into H and χ
- $\sigma_{\phi\chi}$ is kept negligible *w.r.t* other parameters in order to avoid population of already overpopulated χ sector
- Decay energy scale of inflaton depends solely on $\sigma_{\phi H}$
- If inflaton decays (only to H) after it becomes non-relativistic, ρ_{χ}/ρ_{SM} gets additional depletion by a factor a_d/a_t (where a_d is scale factor during decay of inflaton and a_t is scale factor when inflaton becomes non-relativistic) as matter scales as $1/a^3$ and radiation scales as $1/a^4$
- So, by changing $\sigma_{\phi H}$ we can vary a_d/a_t , resulting additional suppression as required to get right DM relic evading Bullet cluster bounds

Suppression by a_d/a_t

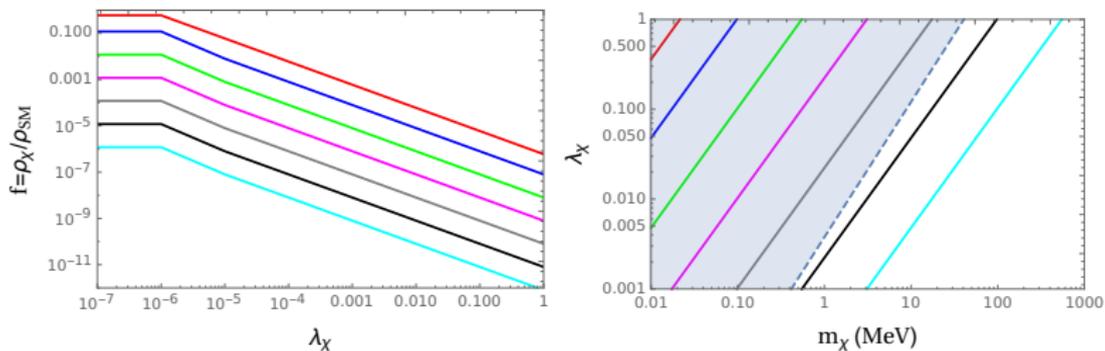


Figure: Lines from top to bottom corresponds to $a_d/a_t = 10^i$ for $i = 0$ to 6

Additional Depletion via Cannibalization

- Having a quartic self coupling $\lambda_\chi \chi^4$ gives rise to additional suppression of DM energy density through **cannibalization** mechanism
- This energy density suppression happens due to number depleting 4-2 scattering processes, described by Boltzman equation

$$\frac{dn}{dt} + 3H(T)n = -\langle\sigma v^3\rangle_{4\rightarrow 2} [n^4 - n^2 n_{\text{eq}}^2], \quad (1)$$

$$\text{with } \langle\sigma v^3\rangle_{4\rightarrow 2} \sim \frac{27\sqrt{3}}{8\pi} \frac{\lambda_\chi^4}{m_\chi^8}$$

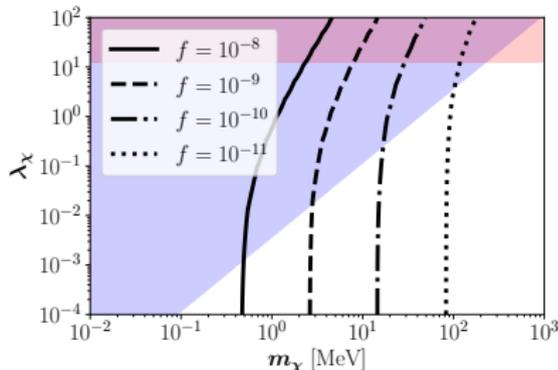


Figure: Values of f that yield the observed DM relic density, in the (m_χ, λ_χ) plane

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- **Scenario 2:**
 - Standard DM production mechanisms like freeze-out require SM-DM interaction
 - Non-observation of any such hint in the direct and indirect searches lead us to explore non-thermal production processes without need of SM-DM interaction
 - We explore production of DM from preheating, and find that it generally overproduces
 - Quartic blocking can suppress production of DM during preheating, but that parameter region is excluded by Bullet cluster observations
 - Additional depletion of DM/SM ratio by a non-relativistic phase of inflaton before it decays to SM and Cannibalization mechanism can give right DM relic avoiding Bullet cluster bounds