

# Gravitational Waves discovered !!!

## Collision of 2 BHs GW150914

Masses of BHs: 36 & 29 Solar Masses

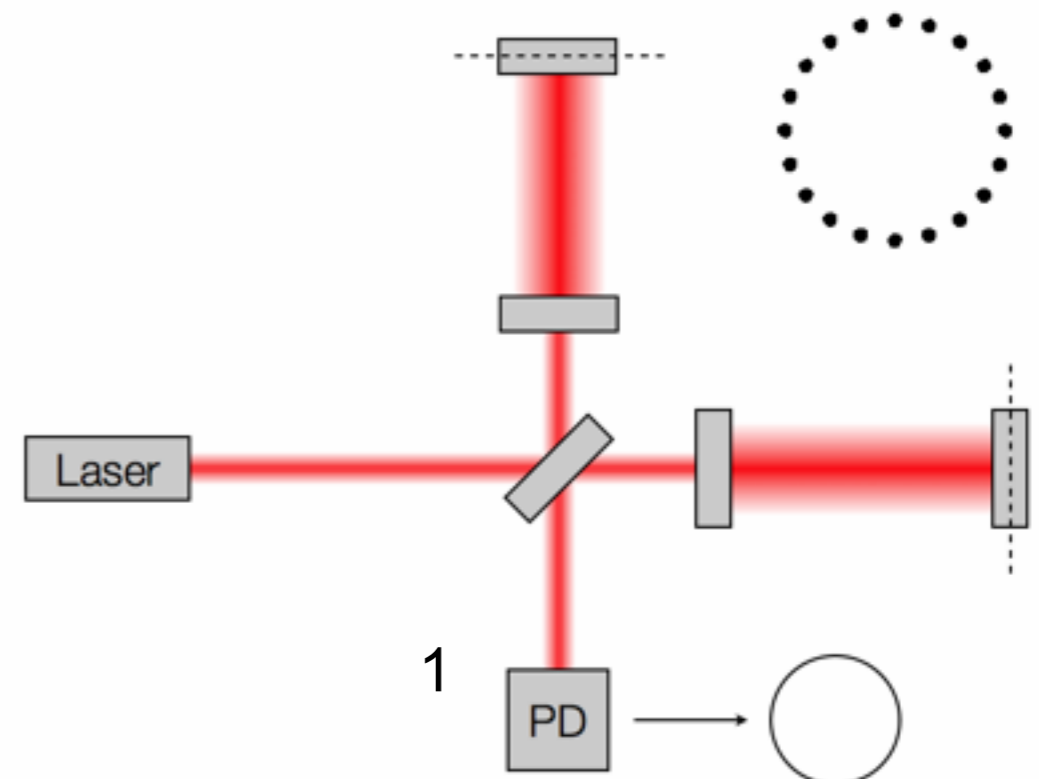
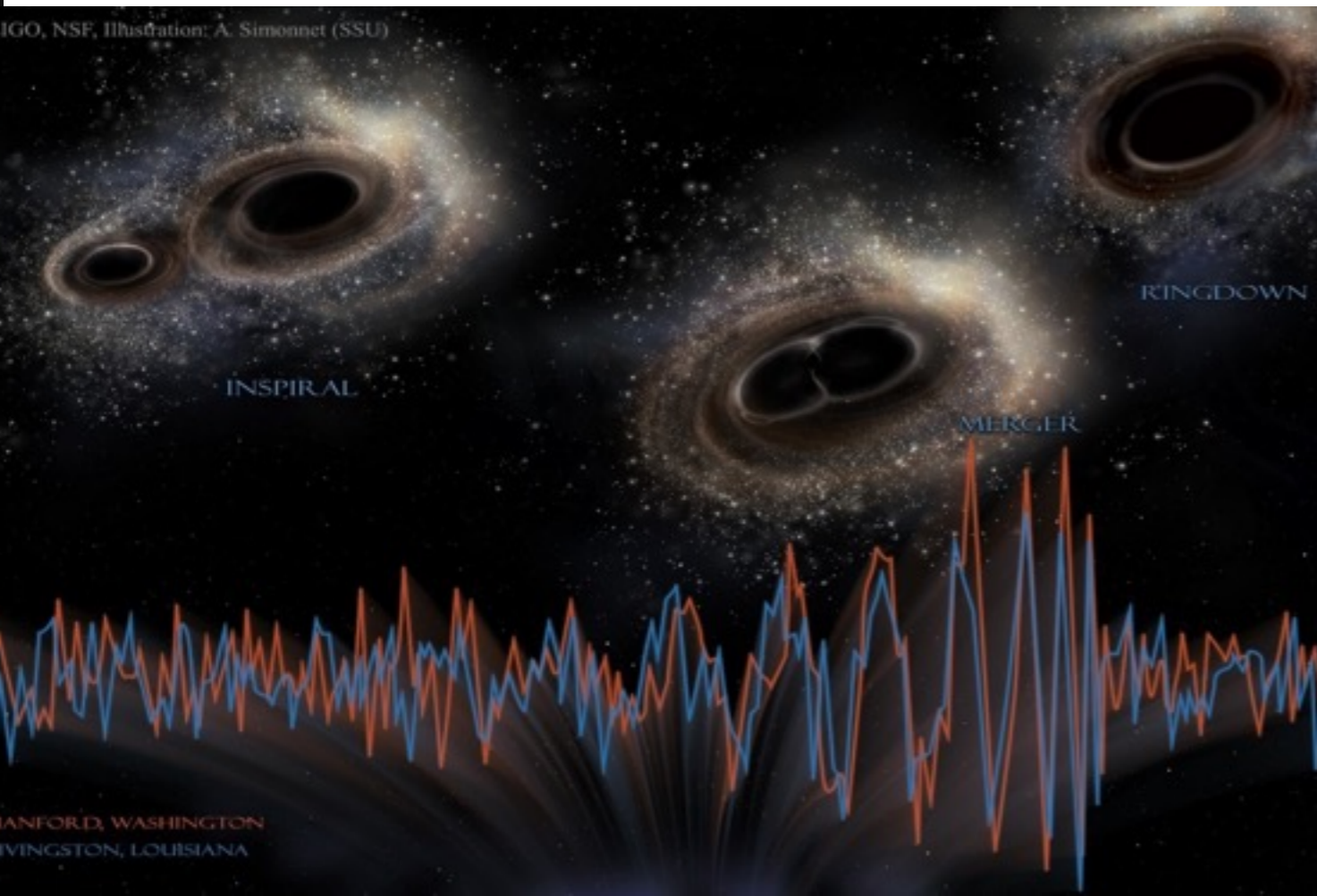
Distance to Earth 410 Mpc/1.340 GLy

Length Difference  $10^{-21}$  m in Ligo

## Binary NeutronStar Merger **GW170817**

Masses of the two NS  $\sim 1.4 M_{\odot}$  each

**GW sensitive to EoS and Phase transition !**



Credit: Les Wade from Kenyon College.

**MaGiC: Matter And Gravitation In Collisions  
of  
Relativistic Heavy Ions and GR Neutron Star Mergers**

**Probe the EoS of hot, dense matter by Flow + Gravitational Waves**

**Anton Motornenko, Stefan Schramm, Jan Steinheimer, Volodymyr Vovchenko,**

**Matthias Hanauske, Elias Most, Jens Papenfort, Luciano Rezzolla, Horst Stöcker \***

FIAS Frankfurt Institute for Advanced Studies, Giersch Science Campus and

Institut für Theoretische Physik, Johann Wolfgang Goethe Universität Frankfurt

GSI Helmholtzzentrum für Schwerionenforschung GmbH Darmstadt

**\*Walter Greiner Gesellschaft zur Förderung der physikalischen Grundlagenforschung e.V., Frankfurt**

# Matter, Gravity and Neutron Stars

1679 **I. Newton** published his theory of gravitation. According to Newton, gravity manifests itself as an instantaneous **force between masses** proportional to their masses and inversely proportional distance squared. With this theory he could explain all of the astronomical observations of this time.



1915 **A. Einstein**, born in Ulm, published GR:

Gravity governs the motion of masses and light by curving spacetime.

1915 **Karl Schwarzschild**, born 1873 in Frankfurt am Main, found the static solution of GR - died in WW I just after publishing his article.

Consequences of Schwarzschild's vision: **black holes, neutron stars**

Add Einstein's Gravitational Waves + we see a **whole new Universe**

# Einstein equations - first solved by Karl Schwarzschild

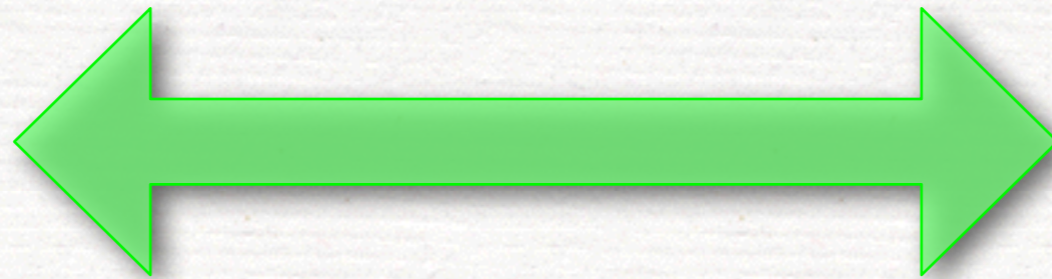
Einstein tensor

stress-energy tensor

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

spacetime  
curvature

mass and energy  
in the spacetime

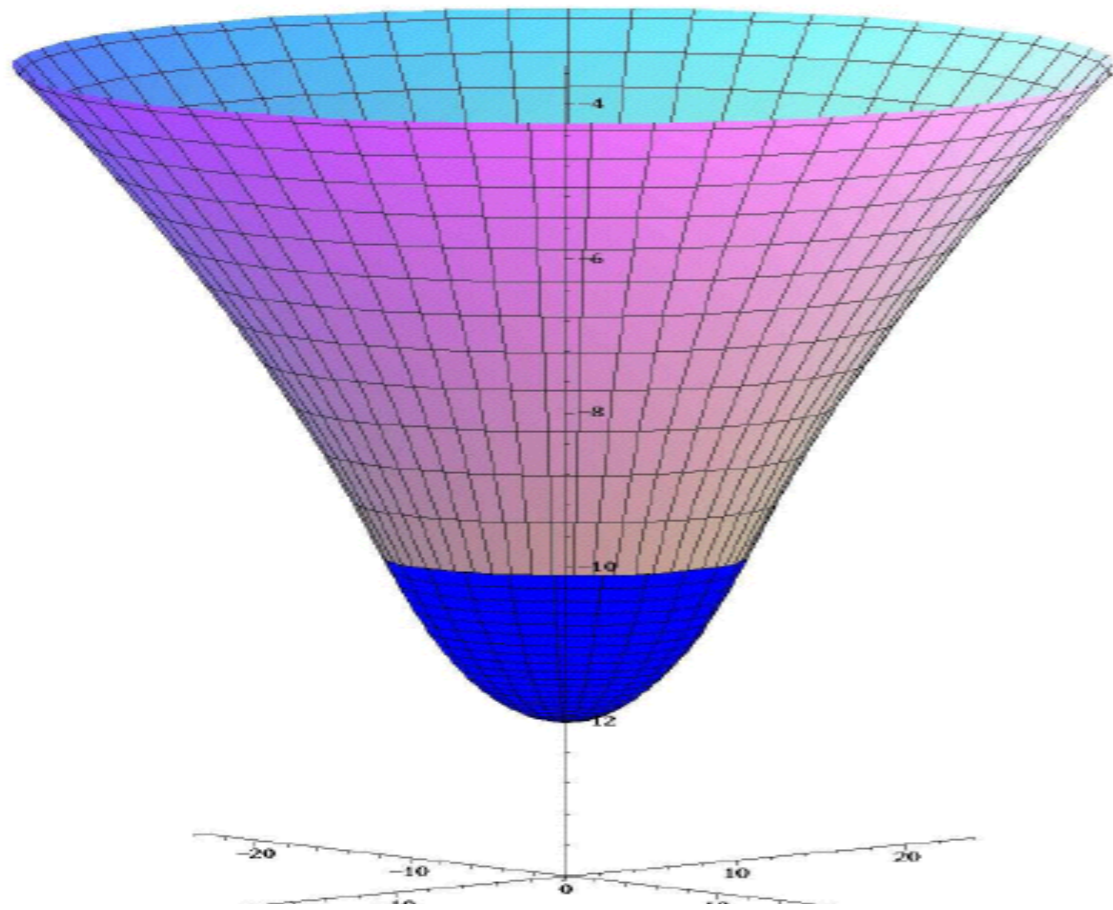


The importance of Einstein equations lies in setting a relation between the **curvature** and the **mass/energy**:

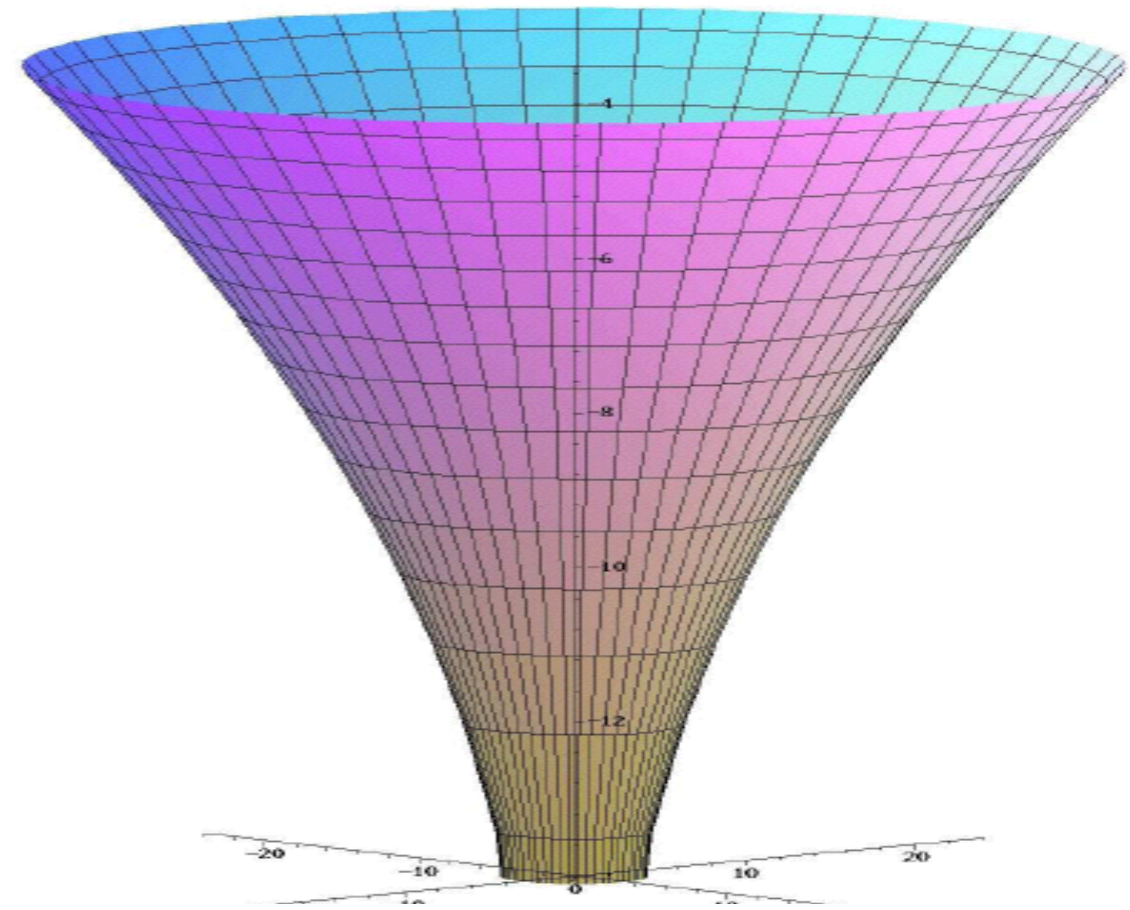
**gravity becomes the manifestation of spacetime curvature**

# Neutron Star - or Schwarzschild's Black Hole ?

Narrow transition from a very compact neutron star to a black hole - many of the spacetime properties are similar.



Neutron Star

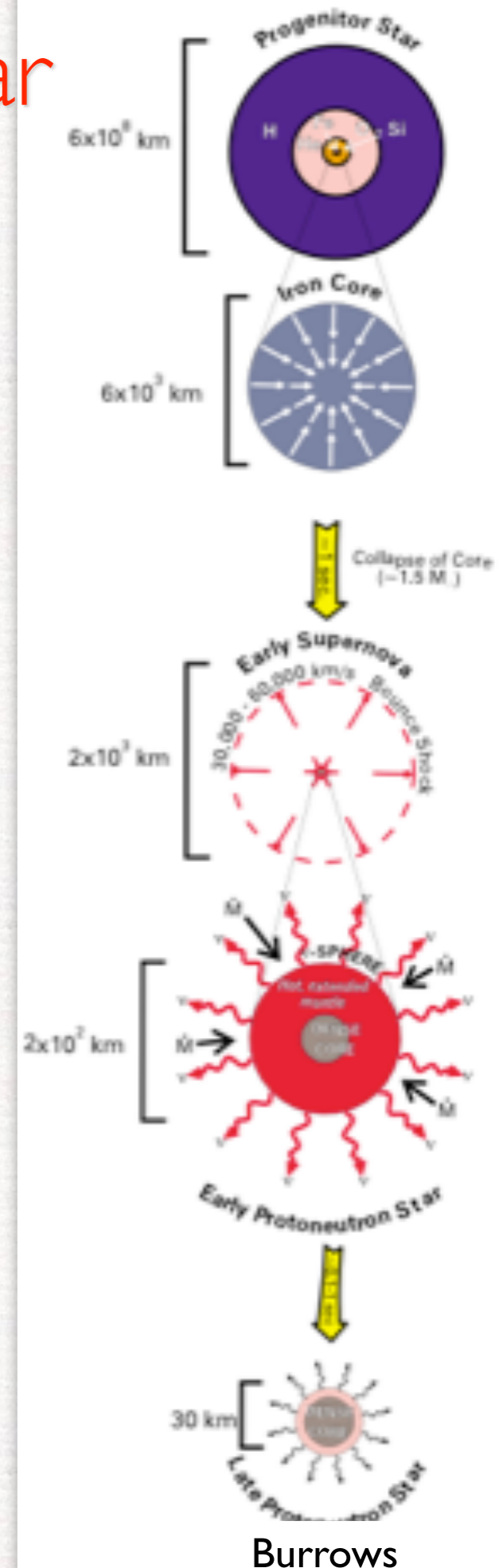
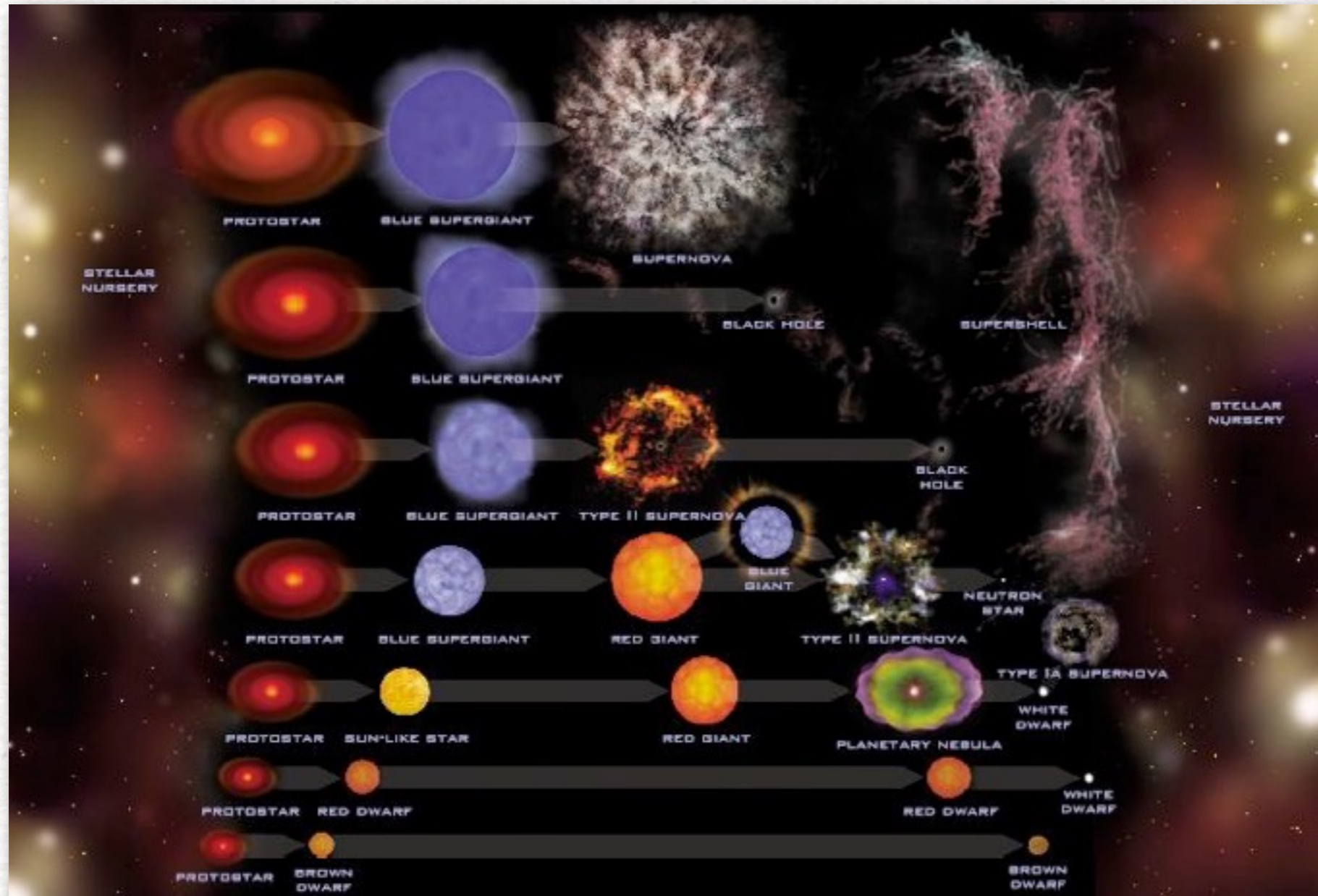


Black Hole

Two aspects differ: Neutron Stars have a **hard surface**, the curvature is large - but **finite** ;

Black Hole: **No Surface** - curvature is **infinite** at the centre - but there is a SINGULARITY : NEVER divide by zero !

# Death of a Star - Birth of a Neutron Star



Neutron Stars are most commonly born in the violent death of massive Stars, i.e. Stars with

$$10M_{\odot} \lesssim M \lesssim 100M_{\odot}$$

ending their evolution as a **supernova collapse**

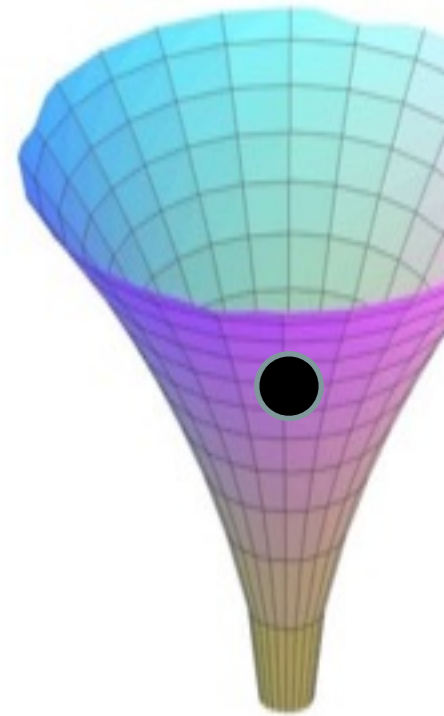
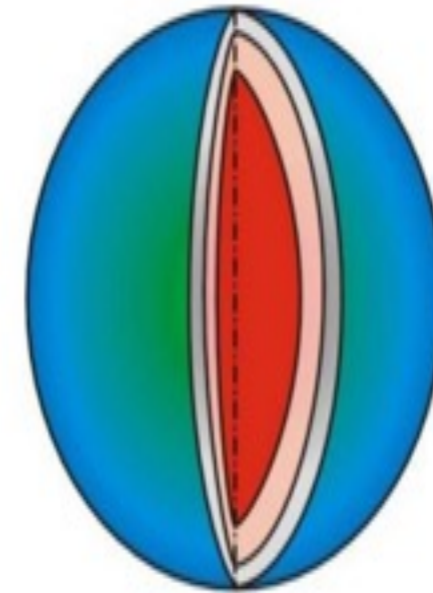
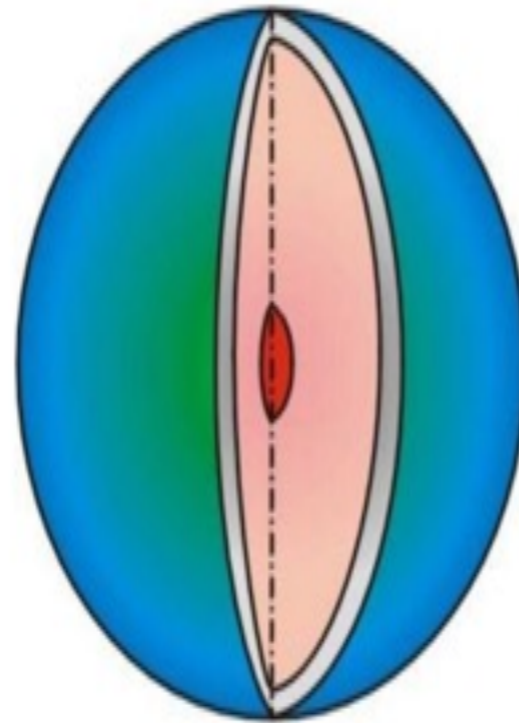
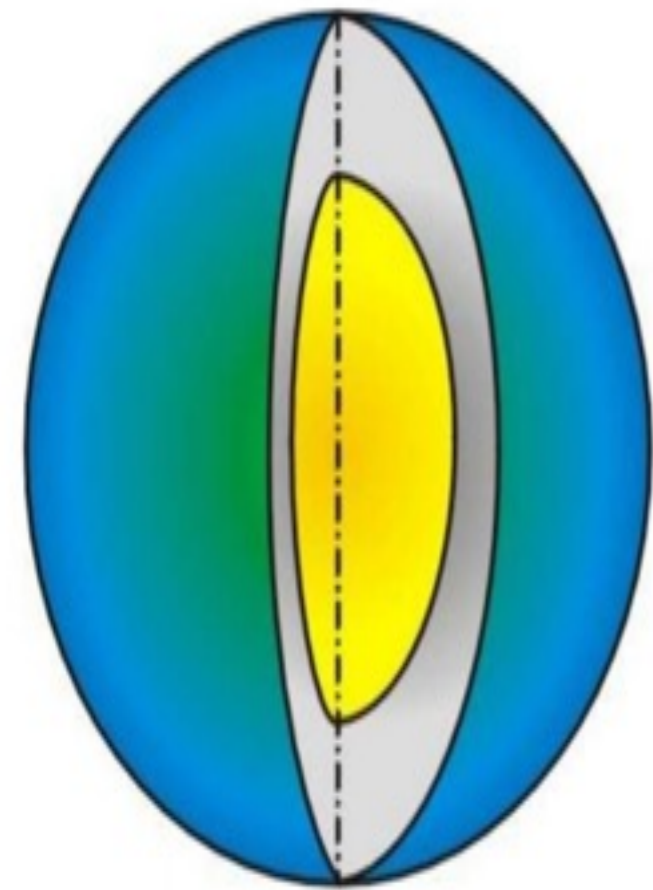
# Neutron Star, Quark Star, Black hole ?

Neutron Stars

Hybrid Stars

Quark Stars

Black Holes



$$\rho_c = \rho_0$$

$$\approx 2 \rho_0$$

$$\approx 5 \rho_0$$

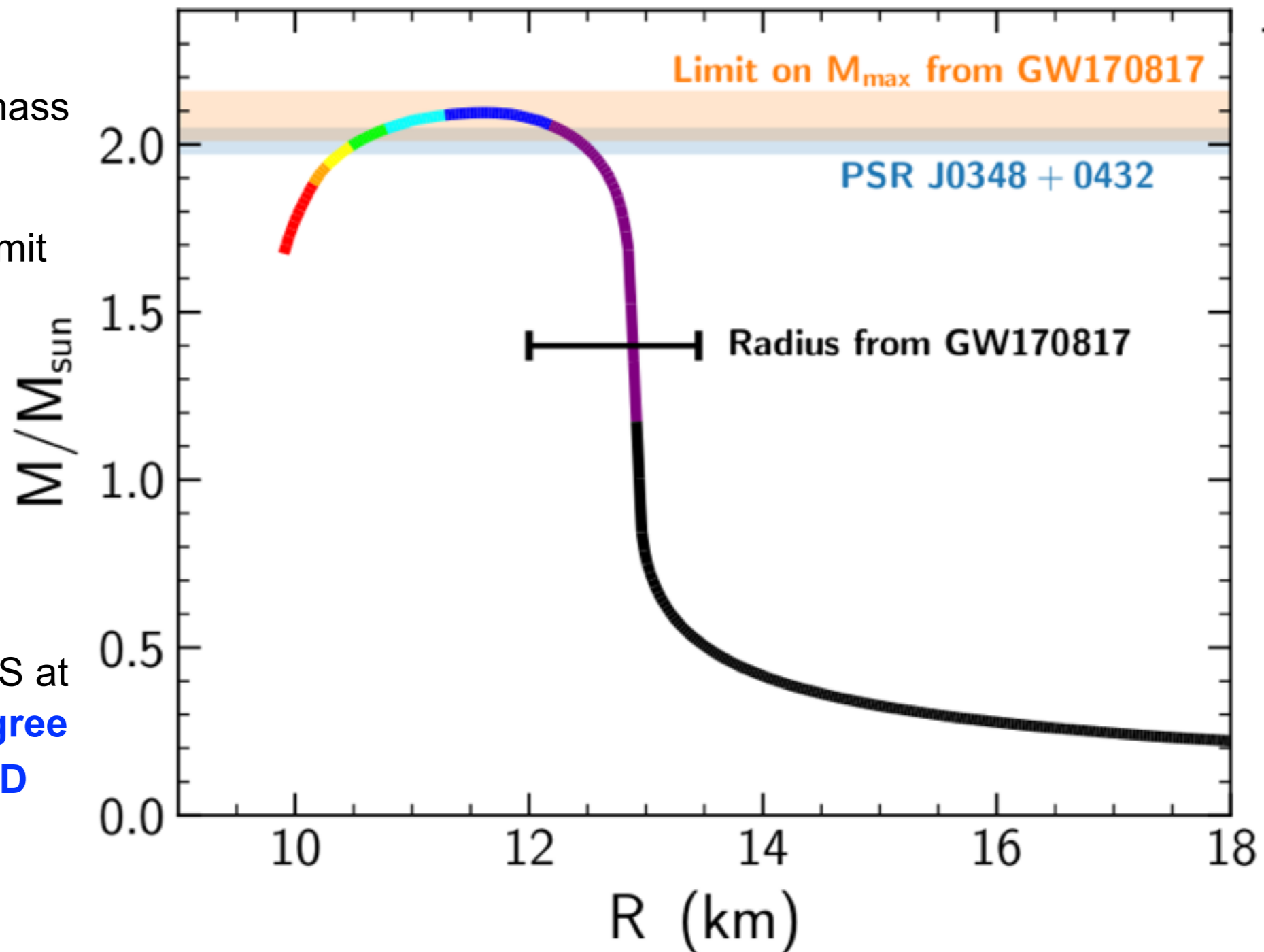
...  $\infty$

central density  $\rho_c$  in the star

$$(\rho_0 := 0.15/\text{fm}^3)$$

## Features:

- Maximum NS-mass observed
- $=2.0xM_{\text{solar}}$  &  $<2.1xM_{\text{solar}}$ - limit of GW170817
- Radii  $\sim 13\text{km}$  according to various observational findings
- hybrid star's EoS at high  $\mu_B$  must **agree with lattice QCD data** at low  $\mu_B$



A. **Motornenko**, Vovchenko, Steinheimer, Schramm, Stoecker 1809.02000



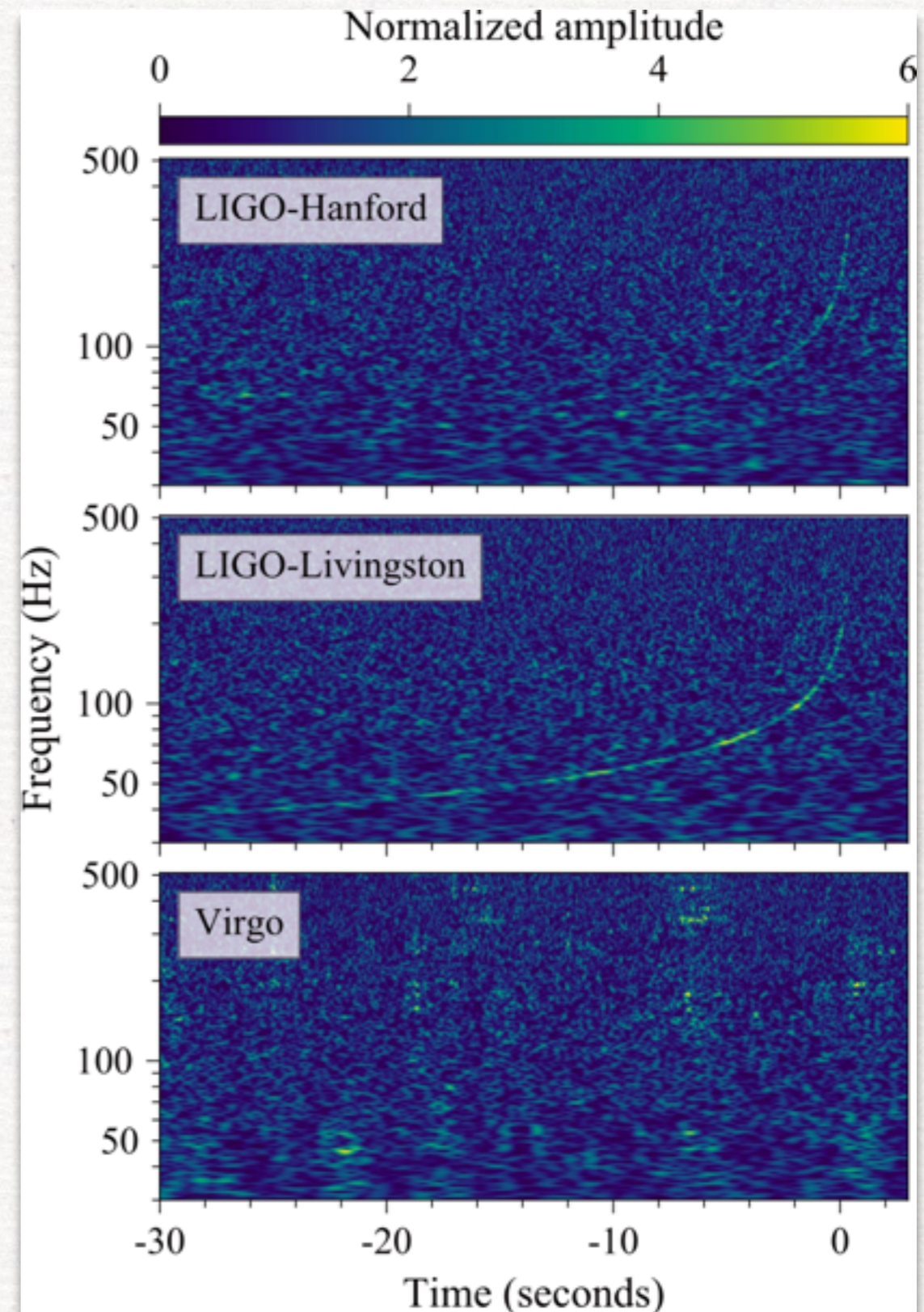
# The riddle of the maximum mass

- As mentioned already, the EOS of nuclear matter is **unknown**.
- Hence, unknown is the **maximum mass**, i.e., mass above which it will collapse to a BH.
- The observation of GW170817 can help solve this riddle

$$M_1 + M_2 = 2.74^{+0.04}_{-0.01} M_{\odot}$$

$$M_1 = 1.36 - 1.60 M_{\odot}$$

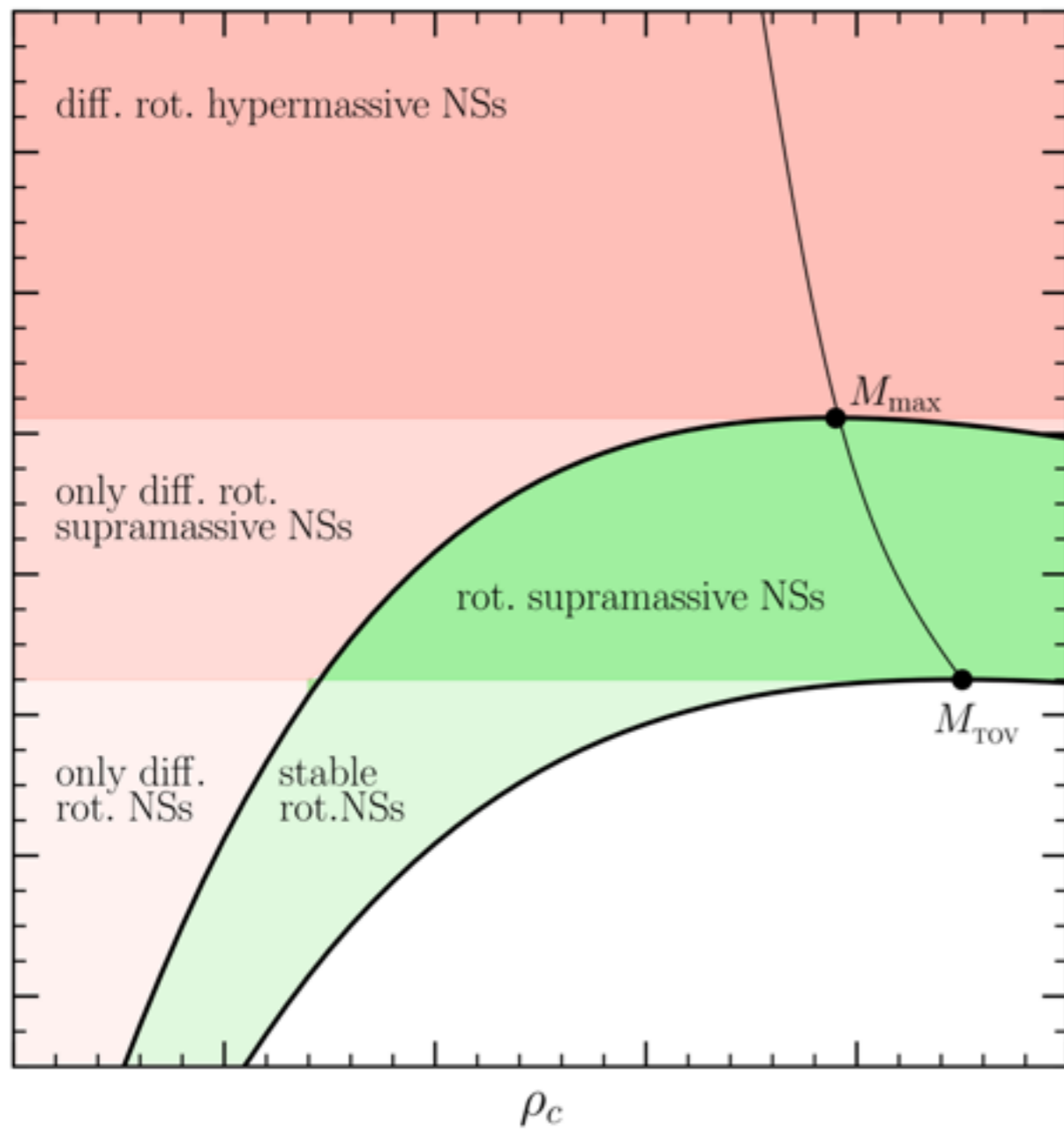
$$M_2 = 1.17 - 1.36 M_{\odot}$$



# The outcome of GW170817

- The product of GW170817 was likely a hypermassive star, i.e. a differentially rotating object with initial **gravitational** mass

$$M_1 + M_2 = 2.74_{-0.01}^{+0.04} M_{\odot}$$



- Green** region is for **uniformly** rotating equilibrium models.
- Salmon** region is for **differentially** rotating equilibrium models.

- Supramassive** stars have

$$M > M_{\text{TOV}}$$

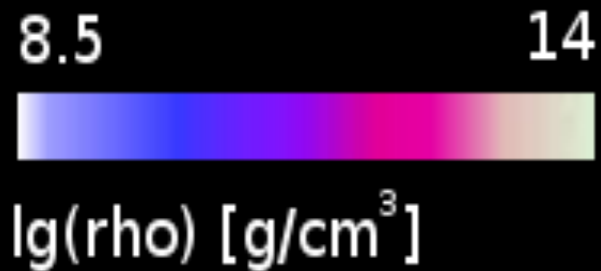
- Hypermassive** stars have

$$M > M_{\max}$$

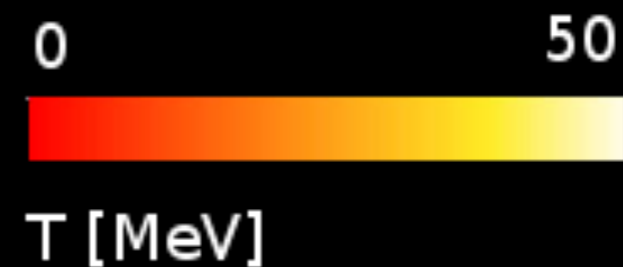
The Death Star will be revived only once she is attracted to her Partner !

Credits: Cosima Breu, David Radice und Luciano Rezzolla

**Density of  
NeutronStar Matter**



**Temperature of  
NeutronStar Matter**



# Numerical Relativity: probing the extreme with relativistic EoS and relativistic Hydro

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = 8\pi T_{\mu\nu} \quad (\text{field eqs : } 6 + 6 + 3 + 1)$$

$$\nabla_{\mu}T^{\mu\nu} = 0, \quad (\text{cons. en./mom. : } 3 + 1)$$

$$\nabla_{\mu}(\rho u^{\mu}) = 0, \quad (\text{cons. of baryon no : } 1)$$

$$p = p(\rho, \epsilon, \dots). \quad (\text{EoS : } 1 + \dots)$$

$$\nabla_{\nu}^*F^{\mu\nu} = 0, \quad (\text{Maxwell eqs. : induction, zero div.})$$

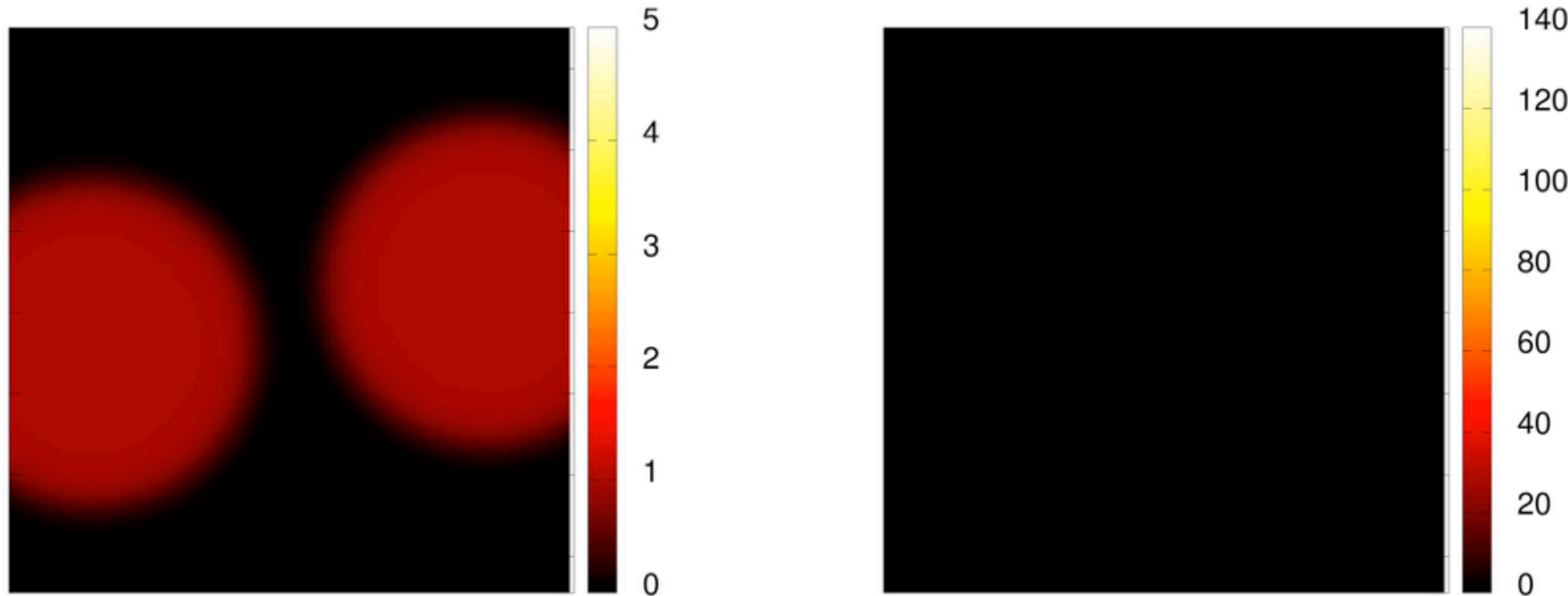
$$T_{\mu\nu} = T_{\mu\nu}^{\text{fluid}} + T_{\mu\nu}^{\text{em}} + \dots$$

These are the equations we normally solve: Einstein equations and those of relativistic hydrodynamics and MHD

The codes built are “**theoretical laboratories**”, representing our approximation to “*reality*”... they must and can be continuously improved: microphysics, magnetic fields, viscosity, radiation transport ,...

# Relativistic 3+1 Dim Hydrodynamics for Heavy Ion Collisions@FAIR

Gold+Gold collisions at GSI: Helmholtz Zentrum für Schwerionenforschung.  
At the FAIR facility: with high intensity beam



Density in units of nuclear ground state density

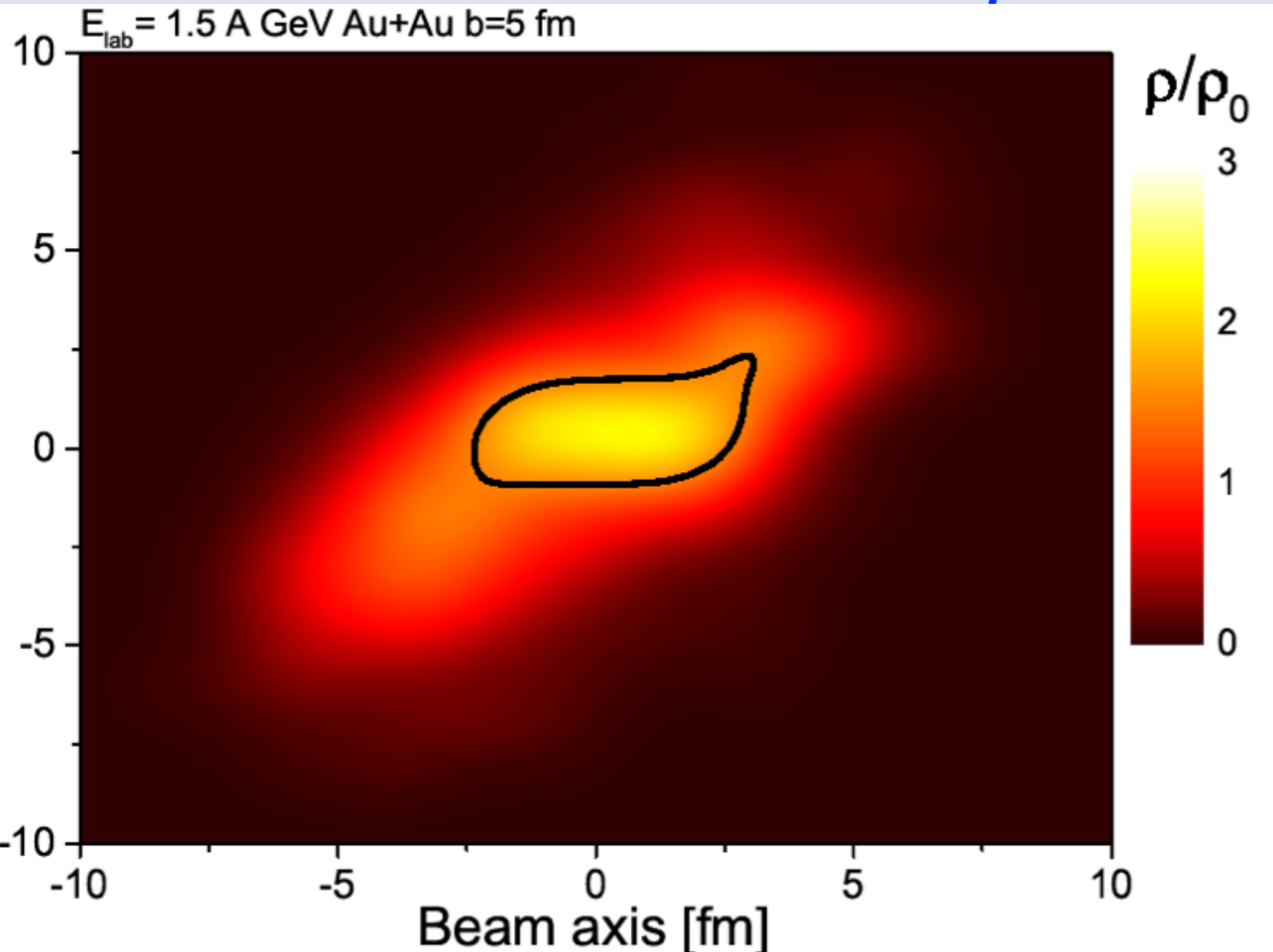
Temperature in MeV

time= 0.08 fm/c

Jan Steinheimer , FIAS, Flux-corrected Transport Code Frankfurt  
Special Relativistic 3+1 Dim Hydrodynamics for HIC since '80-/'90-ies  
G.Graebner, D.Rischke et al., Goethe University

## Neutronstar merger vs. heavy ion collisions

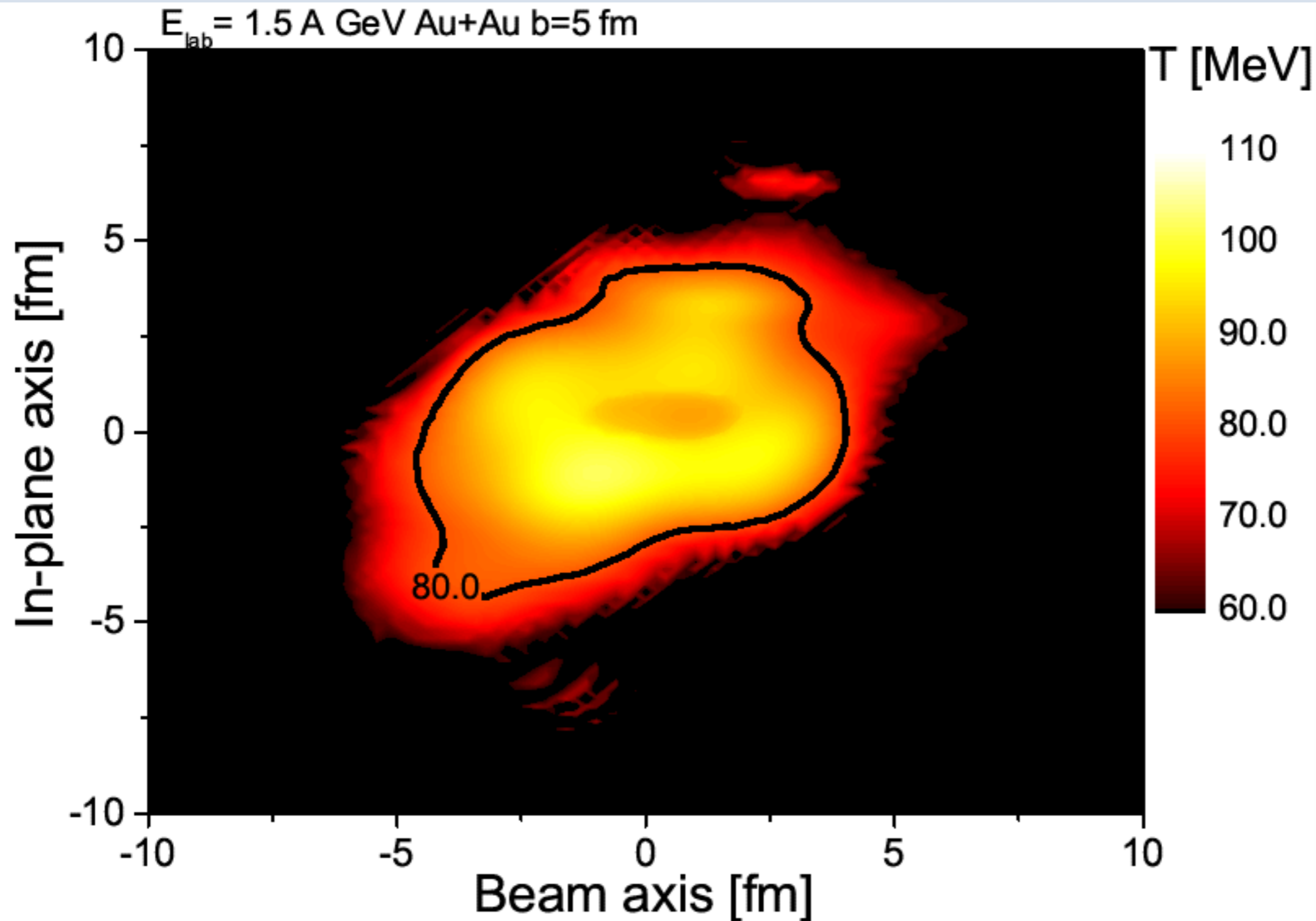
### Which densities are expected ?



- Beam energy corresponds to GSI-SIS18.
- 3-5 times nuclear ground state density reached.
- Large inhomogeneity.
- Short lifetime  $\sim 20 \text{ fm}/c$
- Small system size  $\sim 10 \text{ fm}$

# Neutronstar merger vs. heavy ion collisions

## Which *temperatures* are expected?



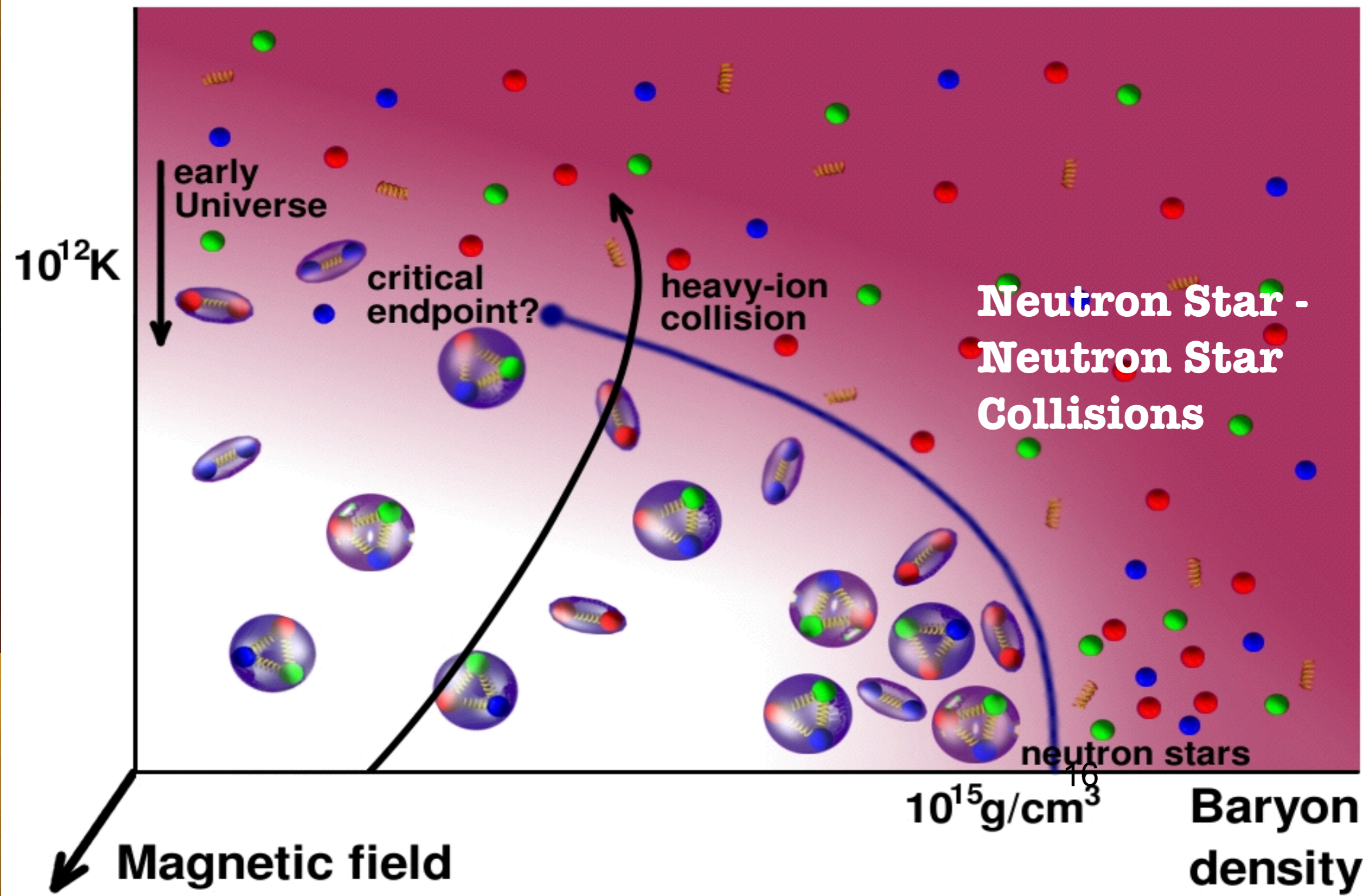
JanSteinheimer  
et.al: Coarse -  
grained  
UrQMD-  
simulation input  
for hydrodyn.  
evolution

- Beam energy corresponds to GSI-SIS18.
- Temperatures** up to  $T=90 \text{ MeV}$  reached.
- Large inhomogeneity.
- Short lifetime  $\sim 20 \text{ fm/c}$
- Small system size  $\sim 10 \text{ fm}$

# FAIR: Dense Matter, Strange Matter, Quark Matter, Quark Stars?

## Relativistic collisions of NS-NS vs. Heavy Ions

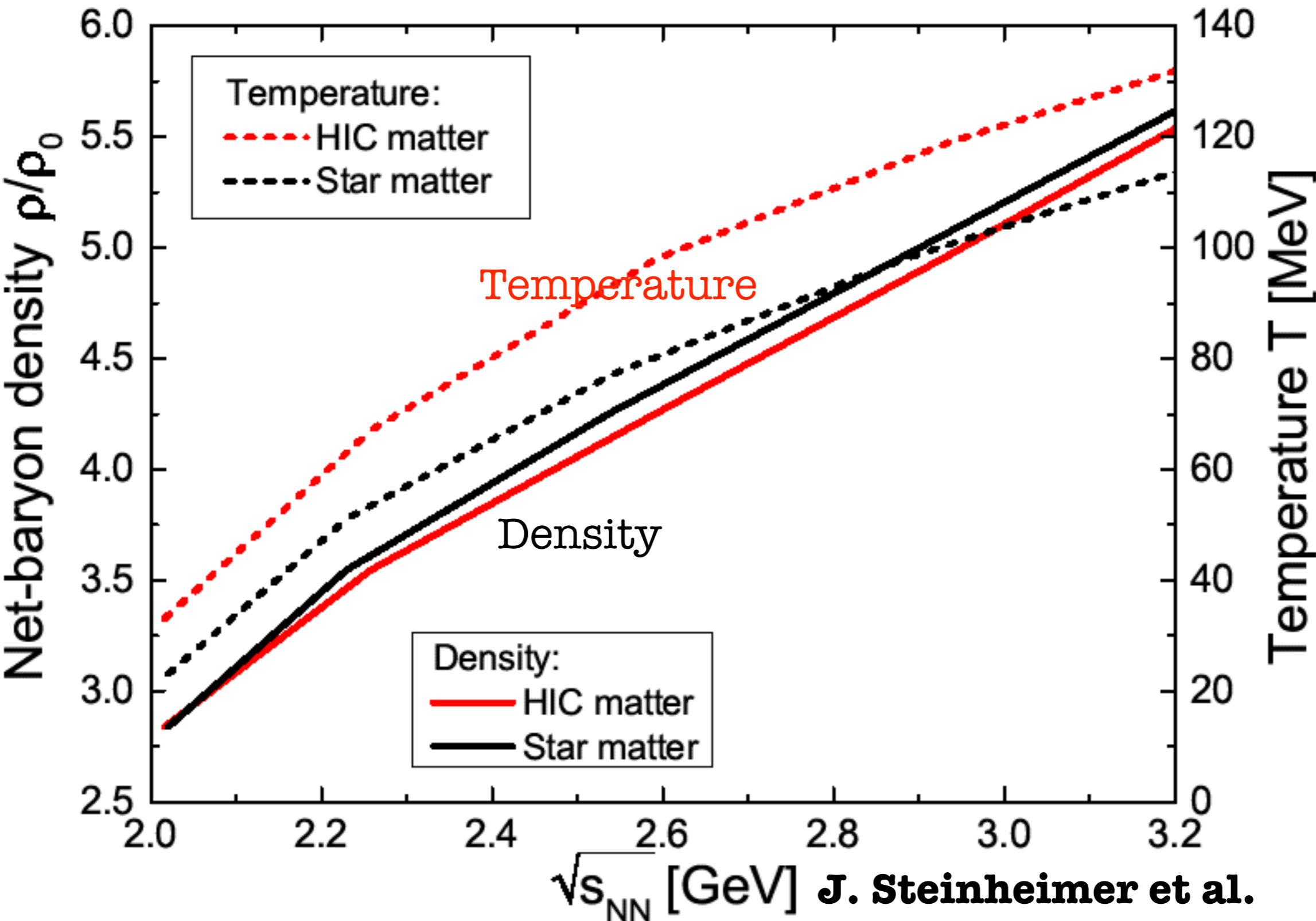
Temperature





# Neutron Star merger vs. heavy ion collisions: Which initial Densities and Temperatures are reached?

+ initialize by Relativistic Rankine Hugoniot Taub Adiabats with Relativistic CMF- EoS



**J. Steinheimer et al.**

Compare central heavy ion collisions with head-on neutron star collisions:  
Rankine Hugoniot Taub Adiabate  
conserve baryon number and energy momentum current densities across shock front yields 1-Dim, stationary hydrodynamical equation for  $n, p$  vs  $E_{cm}=E$ :  
 $E^2 - E_0^2 = (p-p_0)(E/n - E_0/n_0)$



# Neutron Star mergers vs. Heavy Ion collisions: No Difference in Hydro-Dynamics? Really? Why?

- Hydro-Dynamics is scale invariant !
- System Size: Kilometers vs. Femtometers - does not matter !
- Evolution time: Milliseconds vs. fm/c - does not matter !
- Chemical Equilibrium & Phase-Equilibrium vs. Non-Equilibrium ?
- Gravity is relevant ! Attraction** is enormous- Special Relativity vs. GR: BHs
- Relativistic Hydro-Dynamics the theory for both SR & GR!
- Relativistic nuclear **Equation of State** must be conform to QCD- Thermodyn.
- EoS most important input for Relativistic Hydrodynamics, SR and GR



# ”The Death Star machine!” (The Times of India)

FAIR and NICA ideally equipped for precision studies  
to compare relativistic collisions between  
**heavy ions and neutron stars**

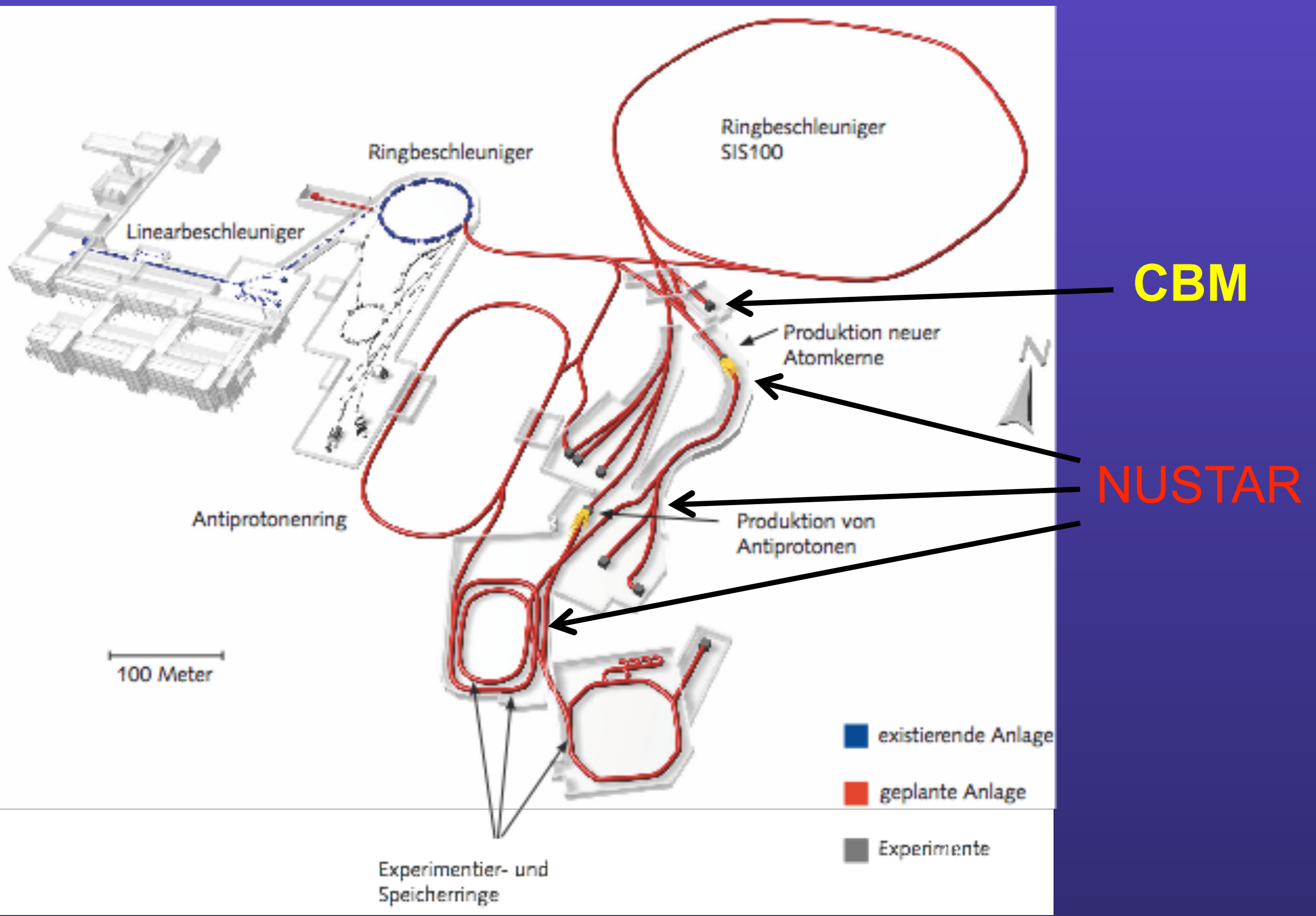
- **Consistent theoretical treatment:**

**Relativistic EoS** Equation of State of dense QCD Matter  
input into

General **Relativistic** 3+1 Dim **Hydro**dynamical Transport

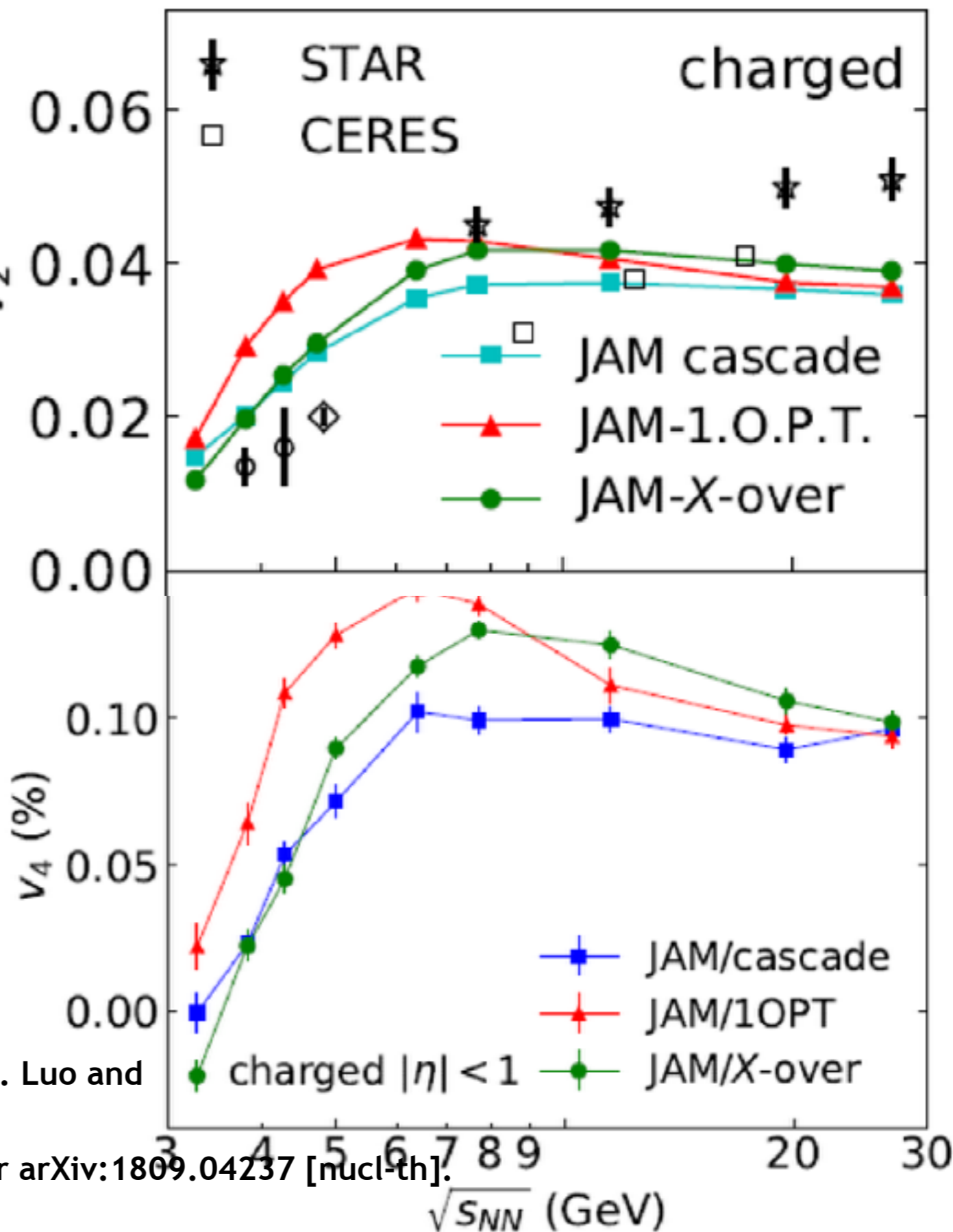
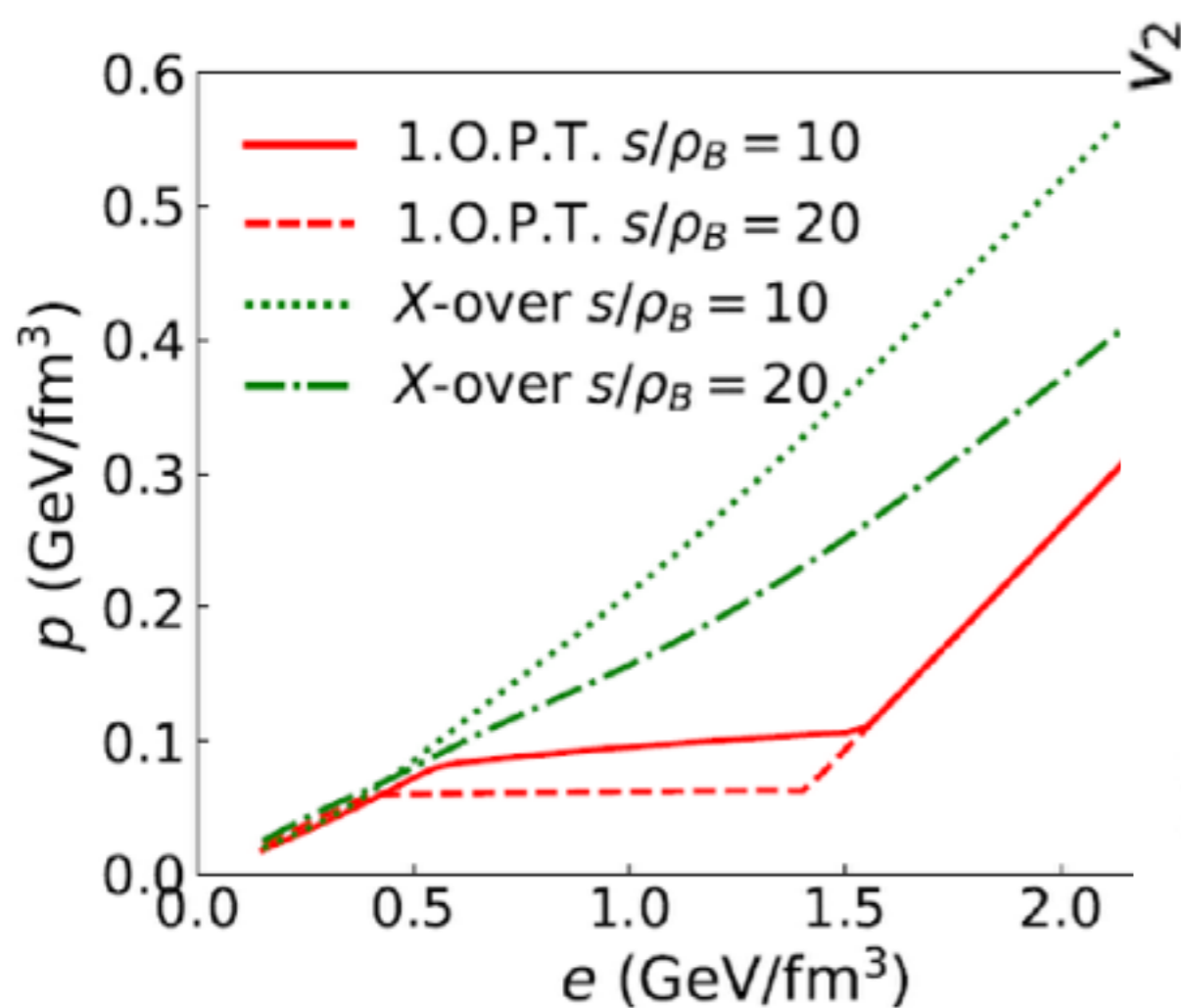
- **Predict and compare to observational data -**

# Neutron Star matter in CBM @FAiR-GSI Helmholtzcentre



# 1.st, 2.nd and 4.th order coefficient of FLOW can signal a 1.Order phase transition

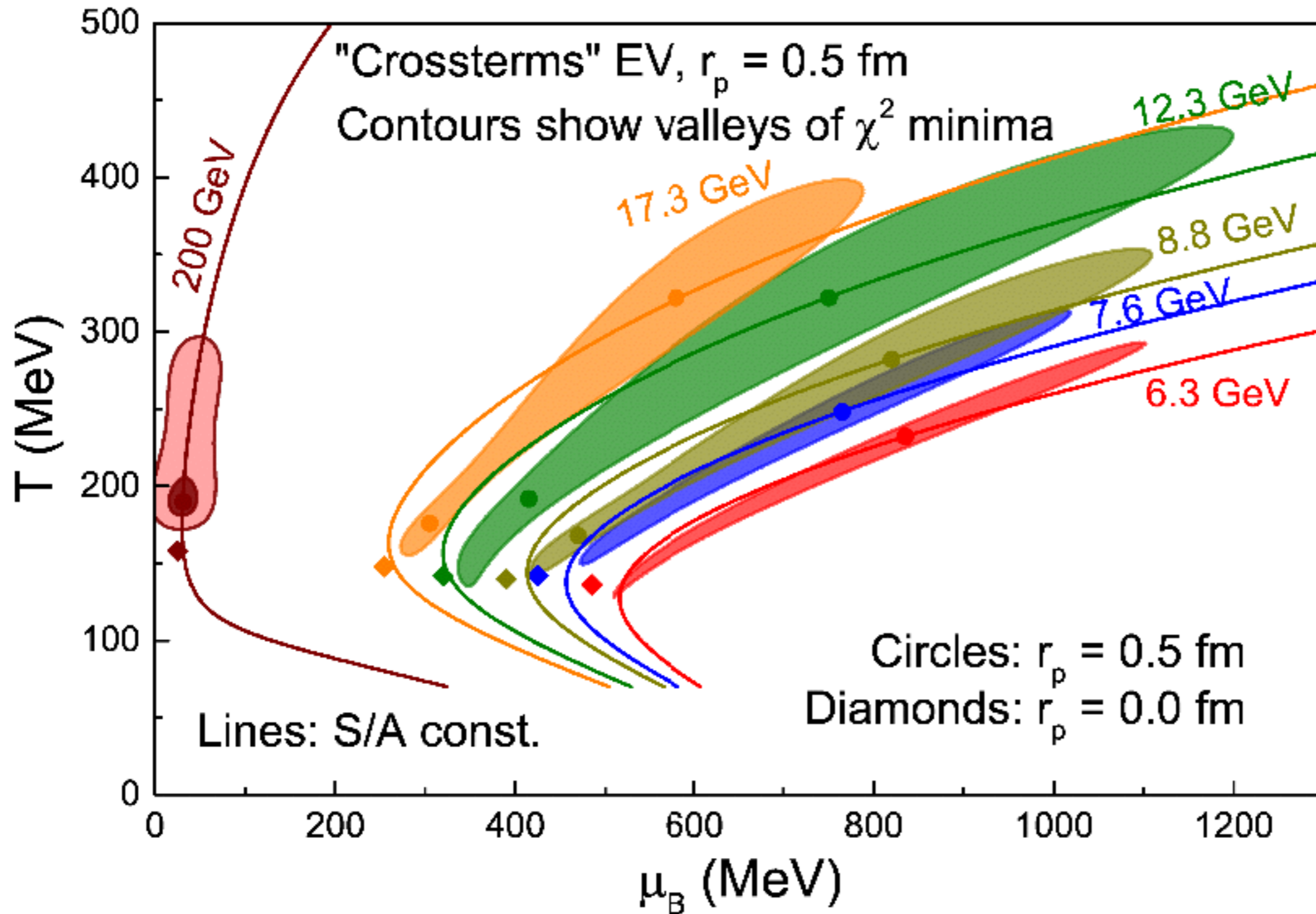
- JAM relativistic transport model
- EoS introduced via azimuthal scat angle
- IF there is a 1. order phase transition?
- Then=>  $v_1$  Drop &  $v_2$  and  $v_4$  PEAK



Y. Nara, H. Niemi, A. Ohnishi, J. Steinheimer, X. Luo and H. Stöcker, Eur. Phys. J. A 54, no. 2, 18 (2018)

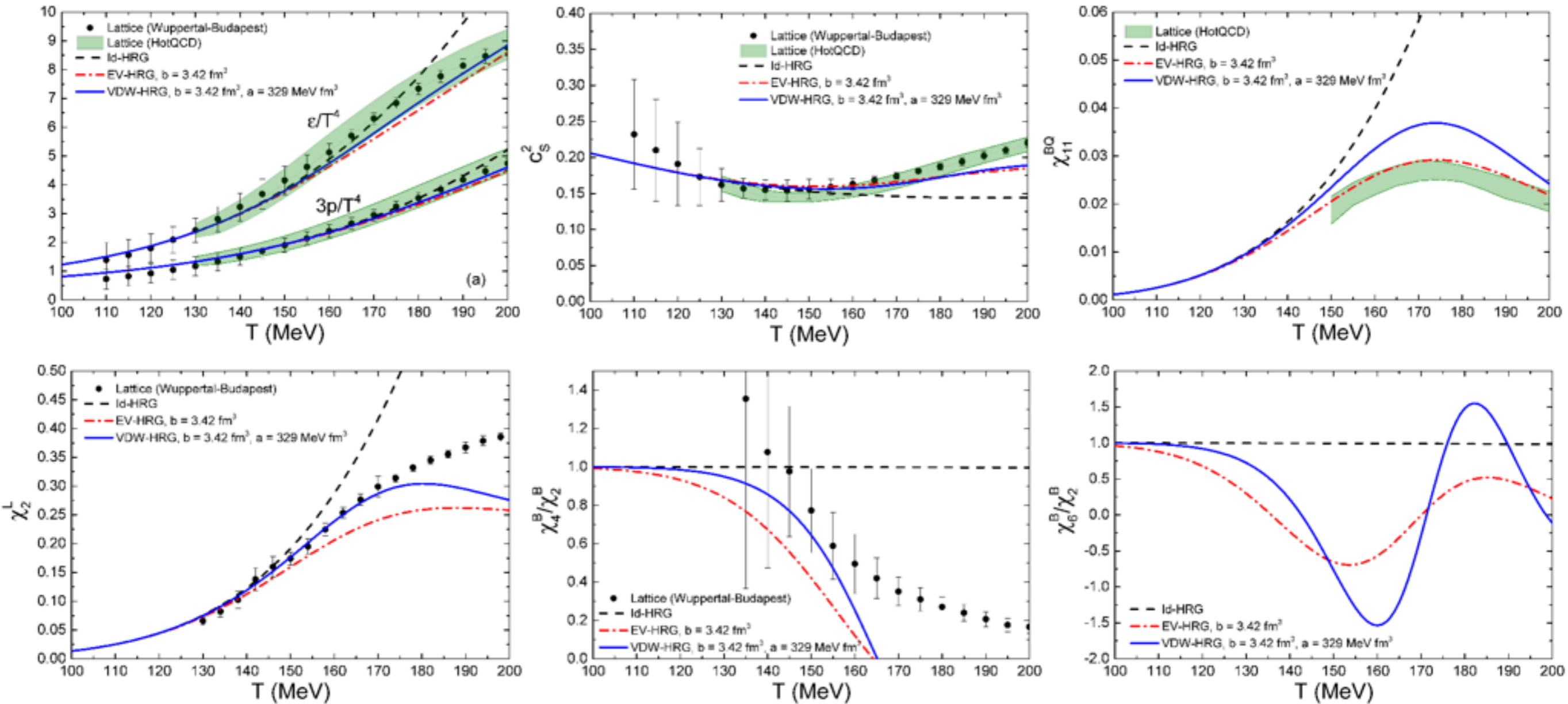
Yasushi Nara, J. Steinheimer and H. Stoecker arXiv:1809.04237 [nucl-th].

QvdW-Excluded-volume interactions have a **surprisingly large** effect on thermal fits



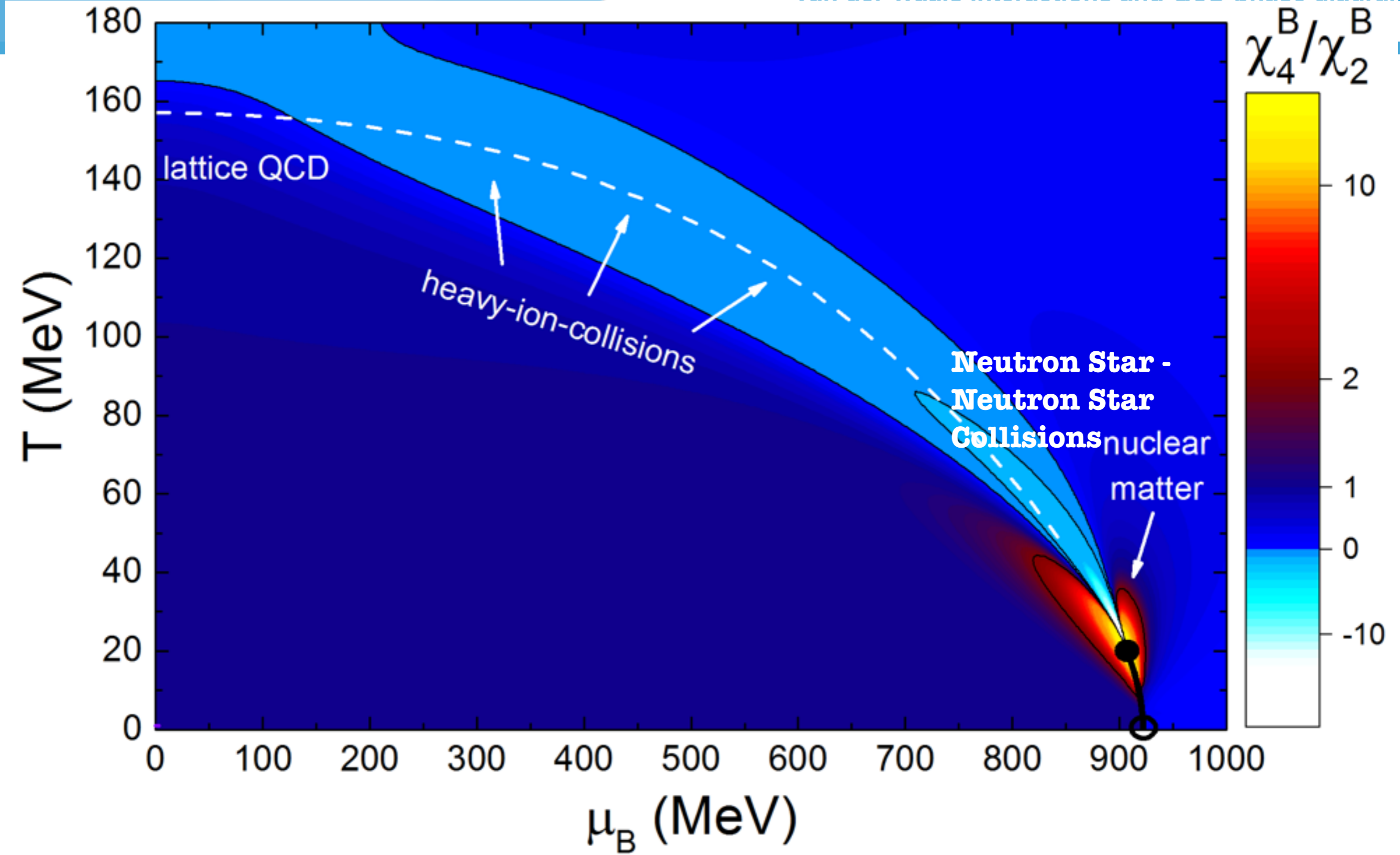


Quantum van der Waals terms for baryons: parameter-free LQCD data description



QvdW can- beyond LQCD- explore high baryochemical potential and neutron star matter at high density, needs little computing power

Quantum van der Waals describes HR-Fluid at non- zero net-baryon density  
 van der Waals interactions and QCD phase diagram



Nuclear matter **shines brightly** across **whole phase diagram** probed in HIC & NsNs

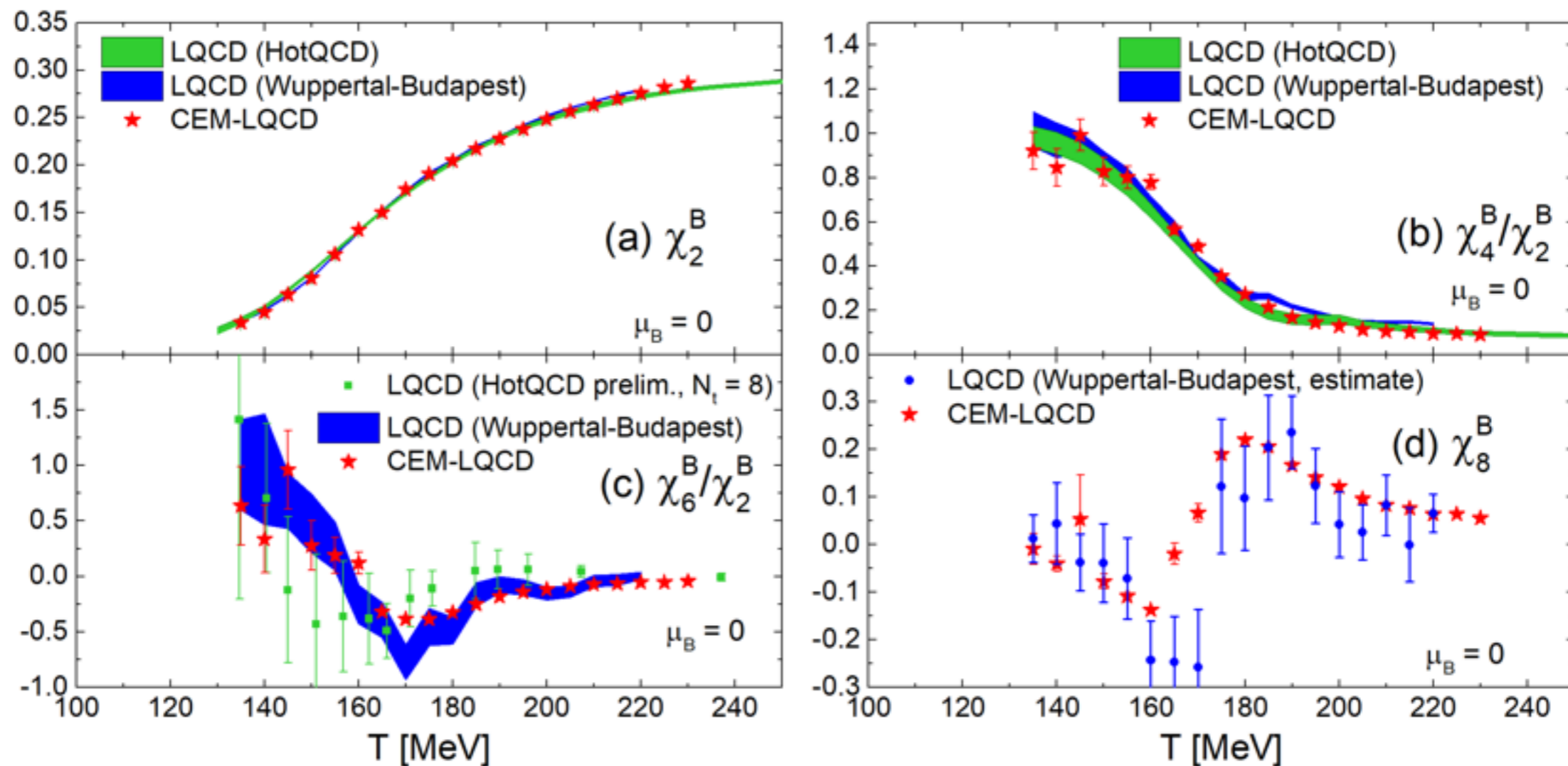
V. Vovchenko, M.I. Gorenstein, H. Stoecker, Phys. Rev. Lett. (2017), 1609.03975



# Cluster Expansion Model

A state-of-the-art lattice based model for QCD EoS at finite density

$$\frac{\rho(T, \mu_B)}{T^4} = p_0(T) - \frac{2}{27\pi^2} \frac{\hat{b}_1^2}{\hat{b}_2} \left\{ 4\pi^2 [\text{Li}_2(x_+) + \text{Li}_2(x_-)] + 3 [\text{Li}_4(x_+) + \text{Li}_4(x_-)] \right\}$$



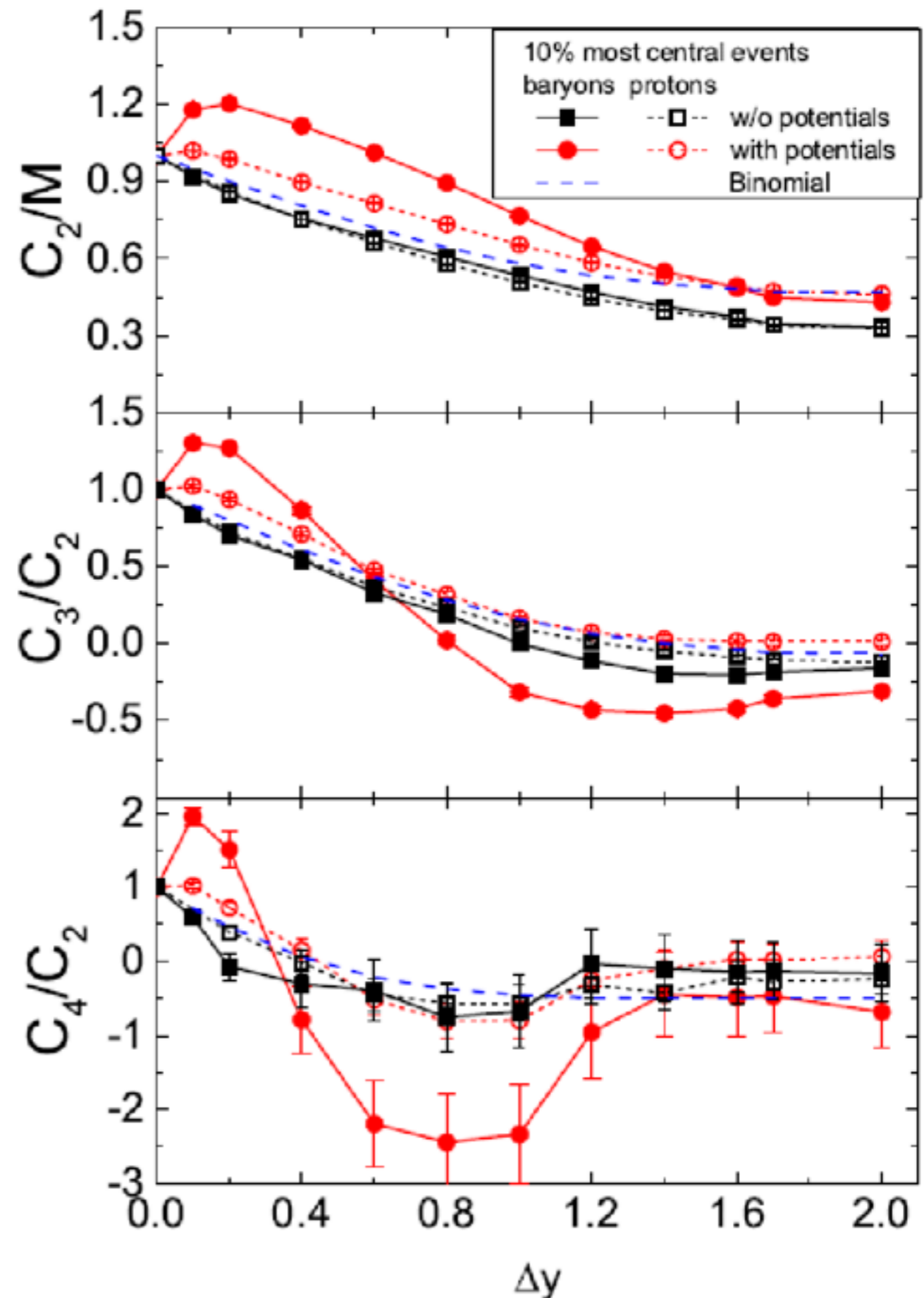
V. Vovchenko, J. Steinheimer, O. Philipsen, *HSt*, *Phys. Rev. D* 97, 114030 (2018)

# Baryon number fluctuations reveal the attr.-rep. nuclear interactions

- Simulations of central Au+Au collisions with UrQMD at HADES/GSI SIS18 beam energy.
- Either use cascade mode or include Skyrme potentials.
- Calculations with potentials see an significant increase of all cumulant ratios, at small rapidity windows
- Can we find effects of the nuclear L-G critical point?
- Work in progress.

J. Steinheimer, Y. Wang, A. Mukherjee, Y. Ye, C. Guo, Q. Li and H. Stoecker Phys. Lett. B785,40(2018)

Y. Ye et al. arXiv:1808.06342[nucl-th].



# EoS by SU(3) Parity-doublet Quark-Hadron Chiral Mean Field CMF

A. Motornenko, P. Rau, J. Steinheimer, S. Schramm, H. ST.

**.... includes consistently main aspects of QCD phenomenology**

Unified effective QCD approach and thermodynamics in a wide range of scales.

- **PDG** vacuum hadrons - plus quarks and gluons
- Proper description of nuclei, hypernuclei, single particle states, SHE
- nuclear and neutron star matter, cold and hot
- Chiral crossover: Parity partners' masses become equal
- **Deconfinement: comes separate at higher energy densities**

**A realistic and relativistic EOS**

**for Heavy Ion Collisions at FAIR/NICA and  
for NS (T=0) and binary NS mergers (T~70 MeV)**

P. Papazoglou, S. Schramm et al., Phys. Rev. C 57, 2576 (1998).

P. Papazoglou, D. Zschiesche S. Schramm et al., Phys. Rev. C 59, 411 (1999).

J. Steinheimer, S. Schramm, H. Stoecker, Phys.Rev. C84 045208 (2011)

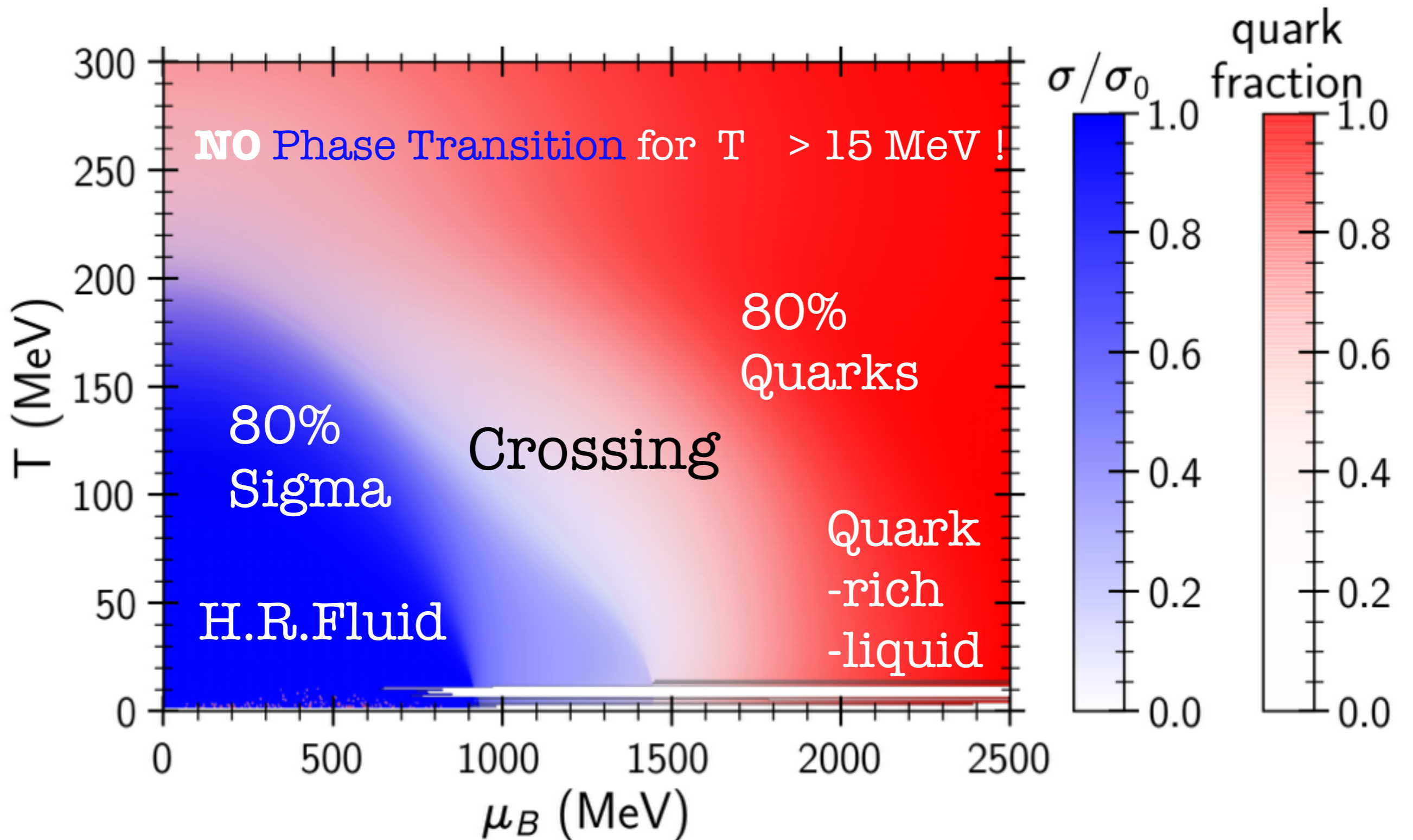
P. Rau, J. Steinheimer, S. Schramm, H. Stoecker, Phys.Lett. B733 (2014) 176-182

A. Mukherjee, J. Steinheimer, S. Schramm, Phys.Rev. C96 (2017) no.2, 025205

A. Motornenko, V. Vovchenko, J. Steinheimer, S. Schramm, H. Stoecker, 1809.02000

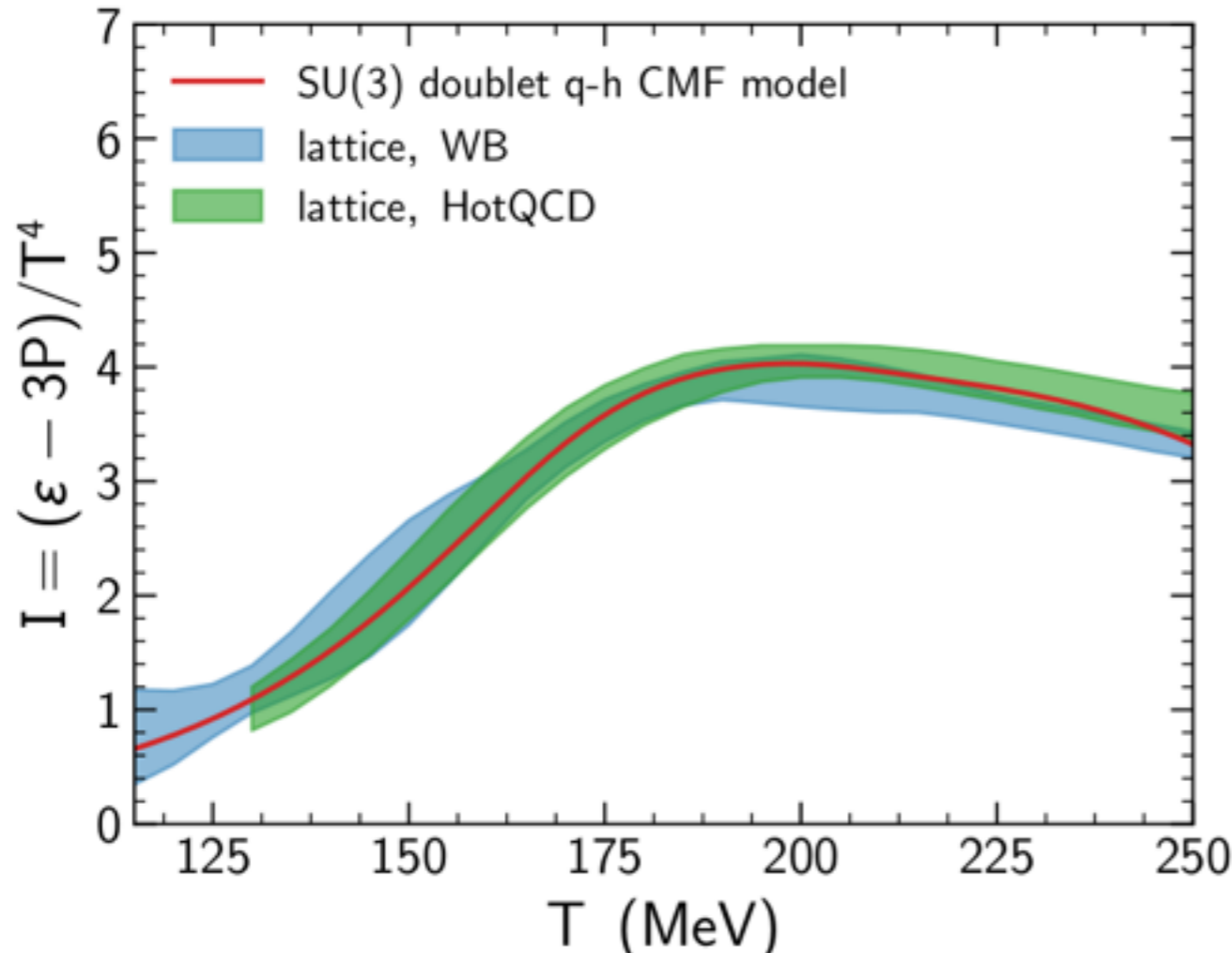
# Phase diagram from relativistic Chiral Mean Field CMF

A. Motornenko - talk Wednesday

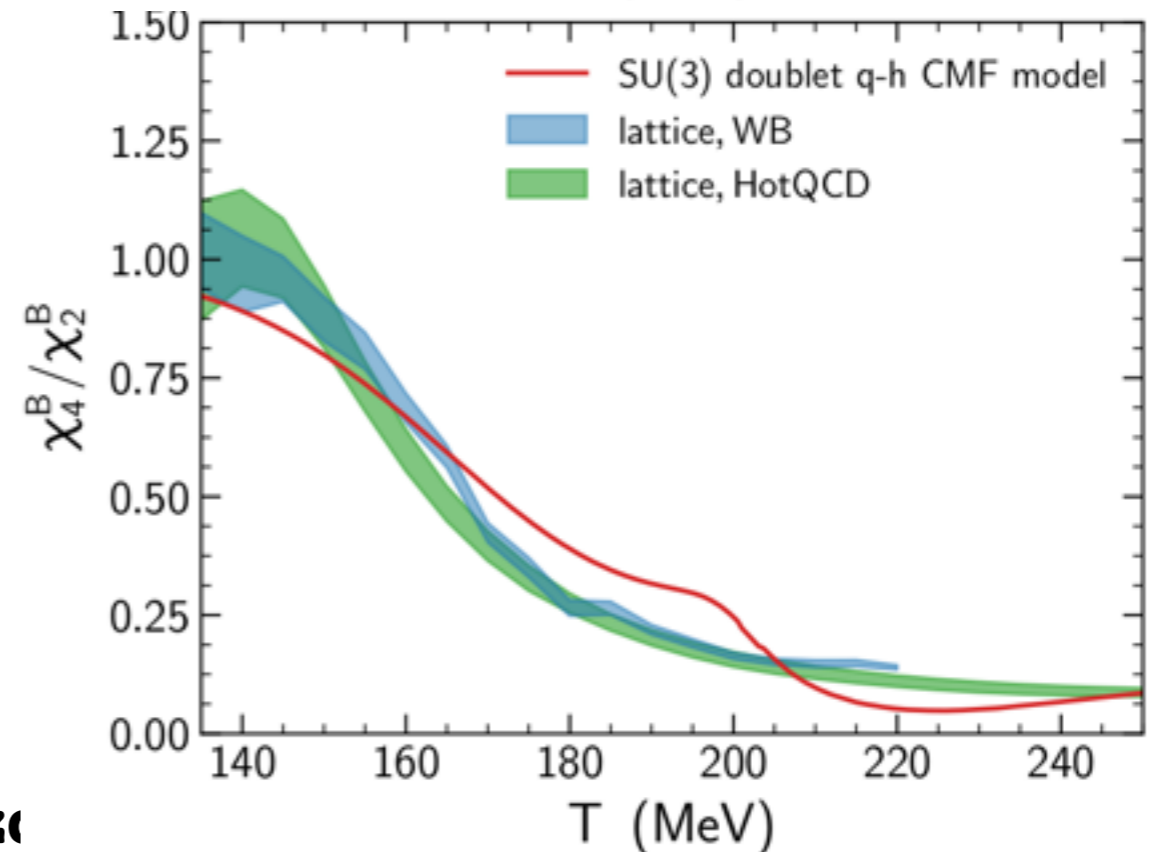
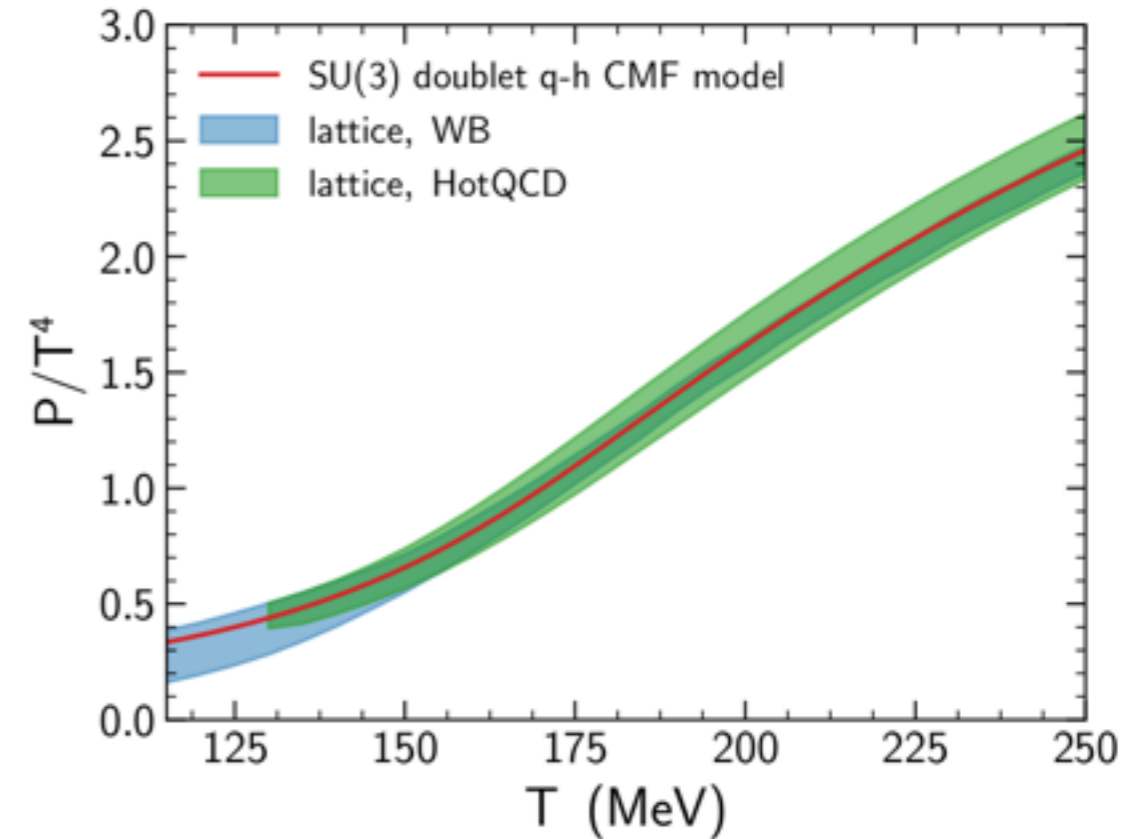


# Quark-Hadron-EoS of CMF -fits to Lattice QCD data

A, Motornenko et al., 1809.02000

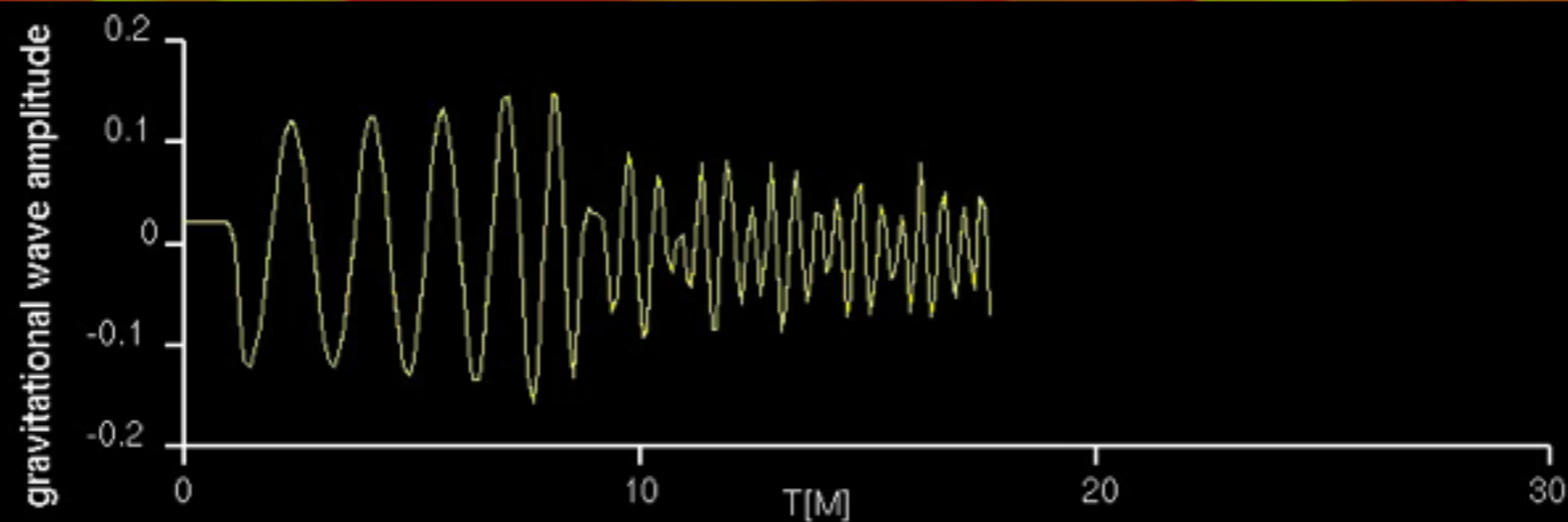
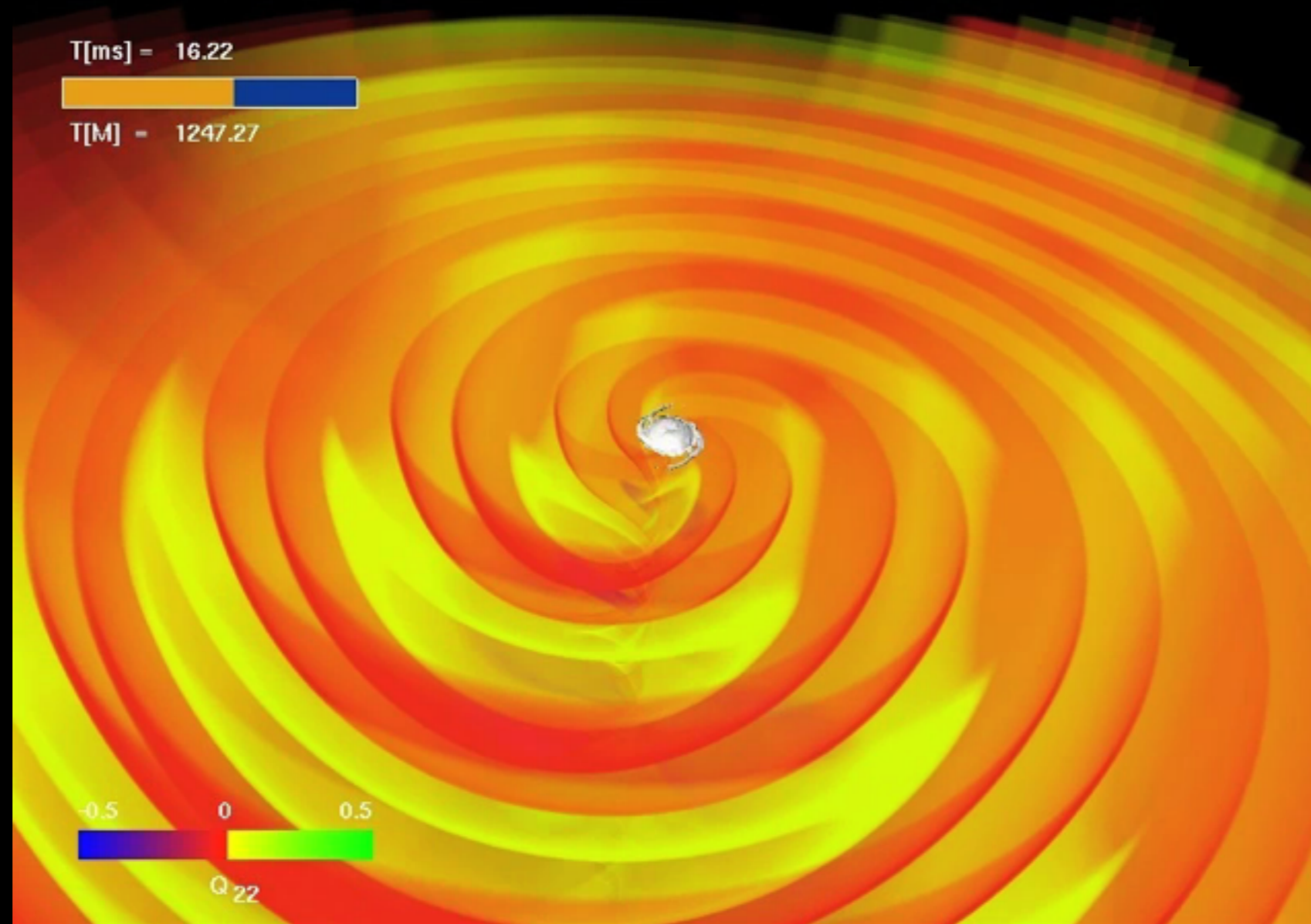


Wuppertal-Budapest collaboration, 1112.4416, 1309.5258, 1507.04627  
 HotQCD collaboration, 1203.0784, 1407.6387, 1701.04325



Model successfully reproduces lattice QCD data

# Gravitational waves: Einstein's last prediction



# Über Gravitationswellen.

Von A. EINSTEIN.

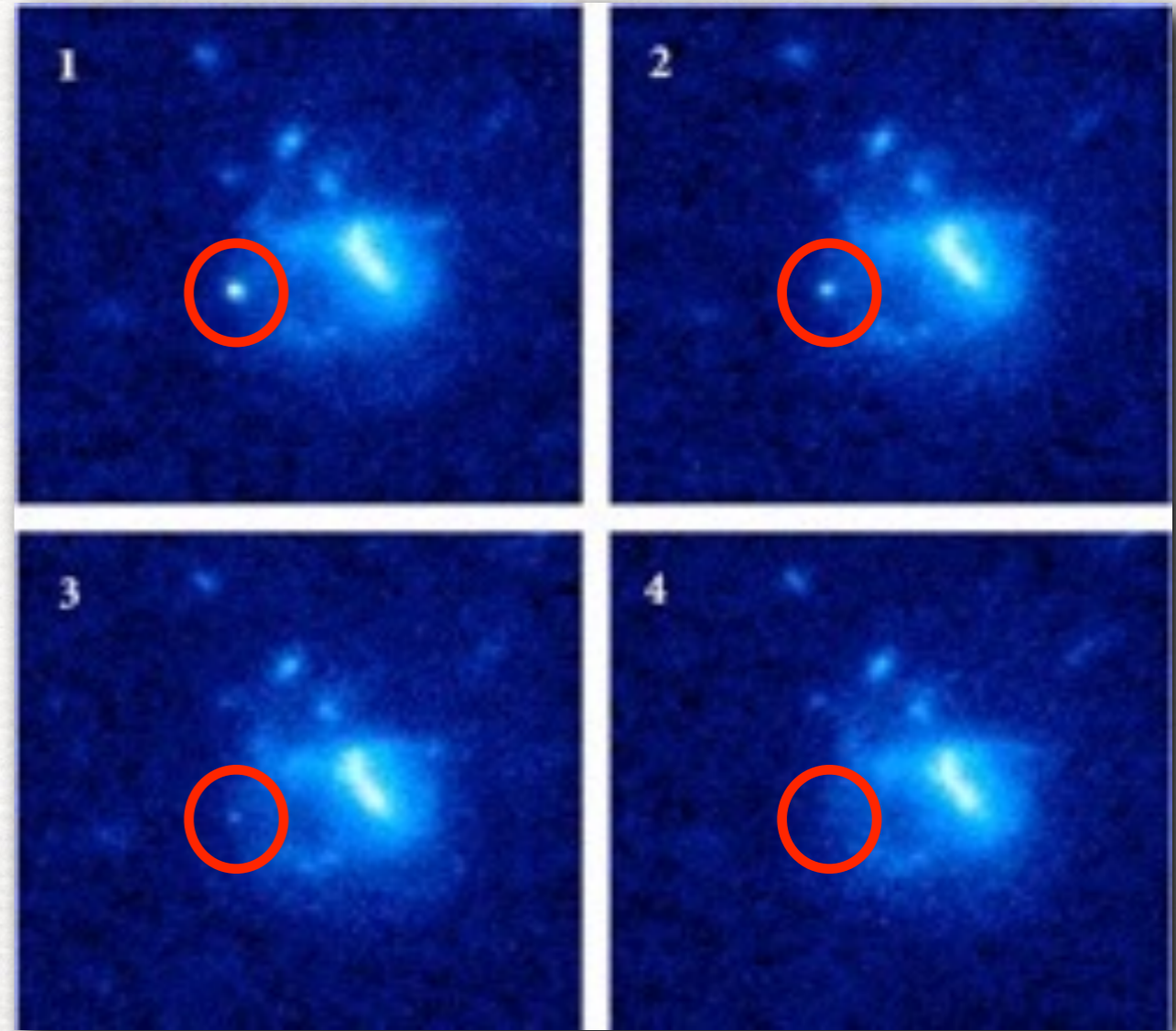
(Vorgelegt am 31. Januar 1918 [s. oben S. 79].)

Die wichtige Frage, wie die Ausbreitung der Gravitationsfelder erfolgt, ist schon vor anderthalb Jahren in einer Akademiearbeit von mir behandelt worden<sup>1</sup>. Da aber meine damalige Darstellung des Gegenstandes nicht genügend durchsichtig und außerdem durch einen bedauerlichen Rechenfehler verunstaltet ist, muß ich hier nochmals auf die Angelegenheit zurückkommen.

Sitzungsberichte der Königlich-Preussischen Akademie der Wissenschaften  
Einstein's First work on Gravitational Waves, Juni 1916, was ...**wrong**...

# Probe the EoS in collisions of binary neutron stars

- We know they exist - among the strongest sources of GWs
- We expect them related to SGRBs:
- energies released are huge:  
 $10^{48-50}$  erg.
- Equivalent to what is released by the whole Galaxy over  $\sim 1$  year!



short GRB,  
artist impression  
(NASA)

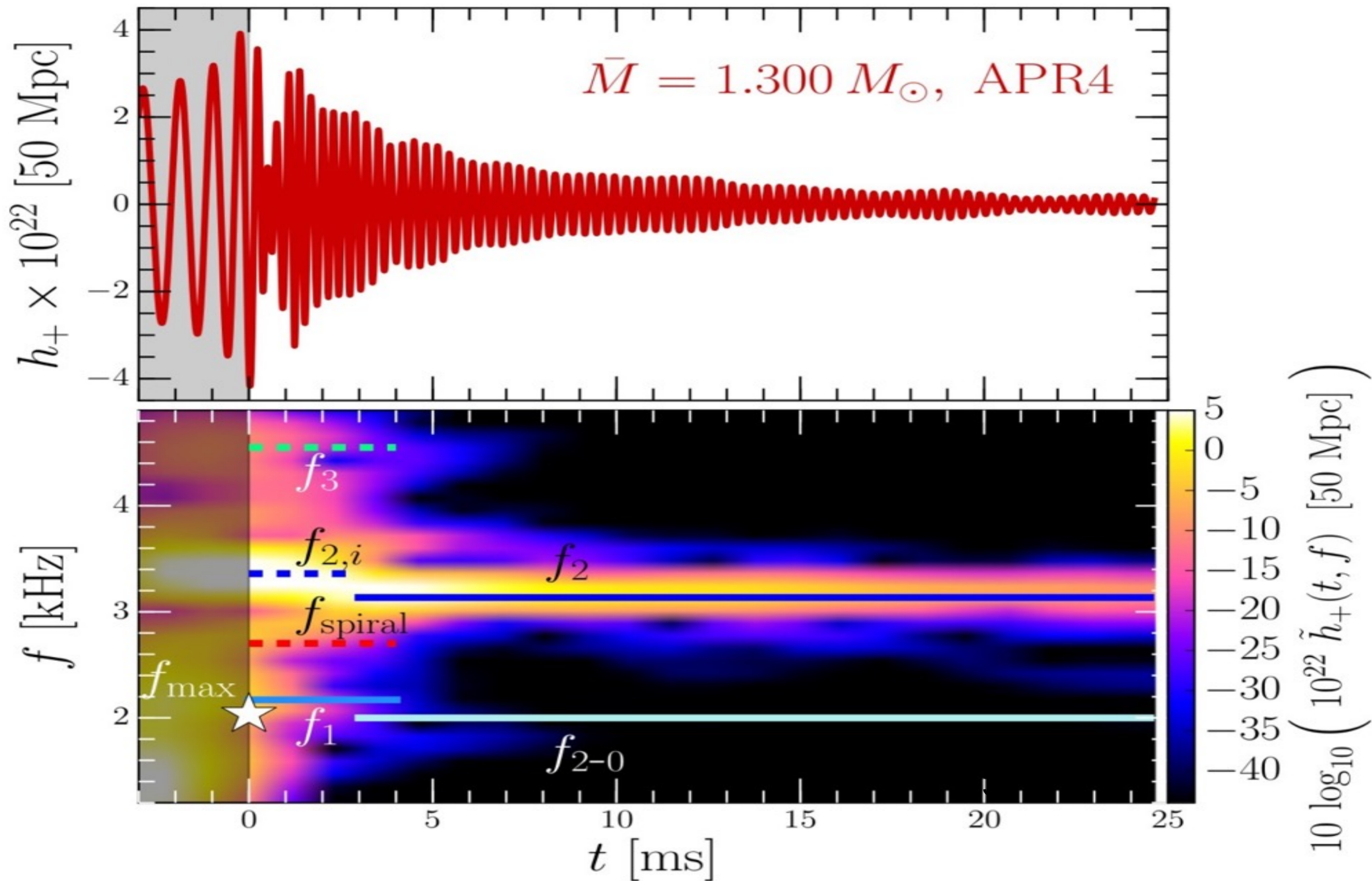
- Despite decades of observations no self-consistent model has yet been produced to explain SGRBs.



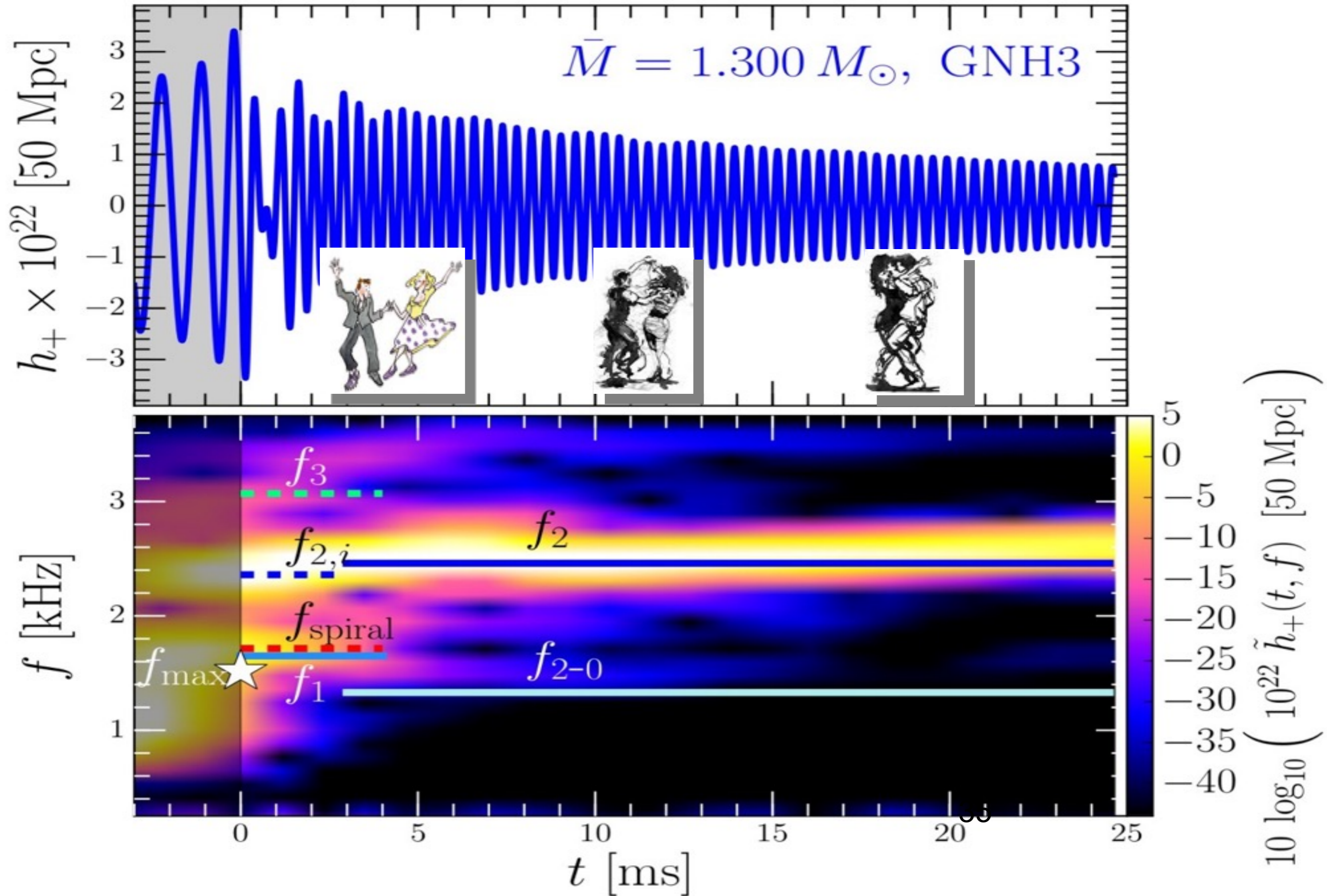
How to constrain the EOS  
of superdense neutron star matter  
by relativistic binary neutron star - collisions

- and the EoS of superdense hot nuclear matter  
by relativistic heavy ion - collisions

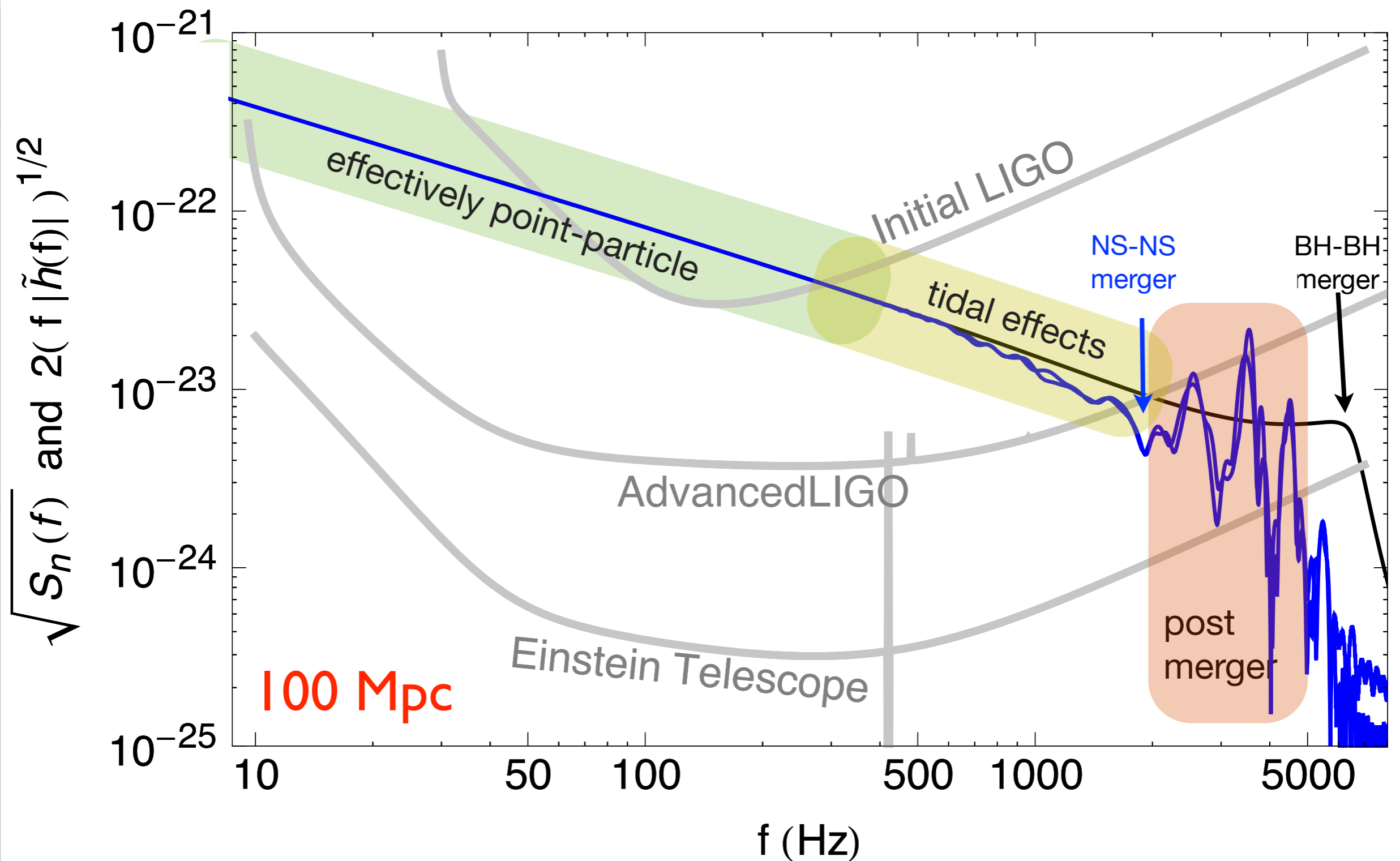
# G-Wave Frequency Spectrum depends on EoS: **soft** nuclear matter EoS



# The G-Wave Spectrum for a **HARD** nuclear EoS

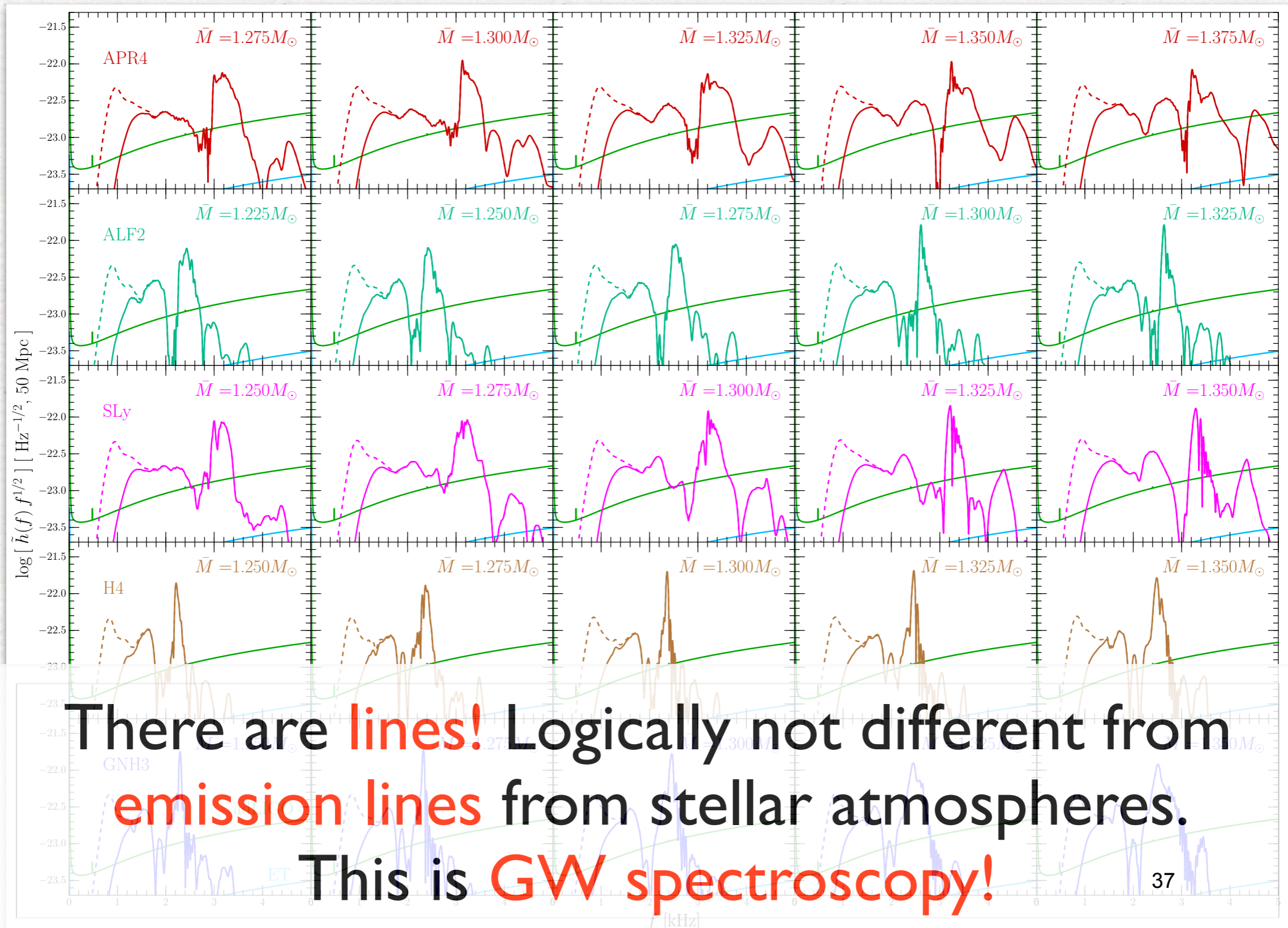


# In frequency space



# Extracting information from the EOS

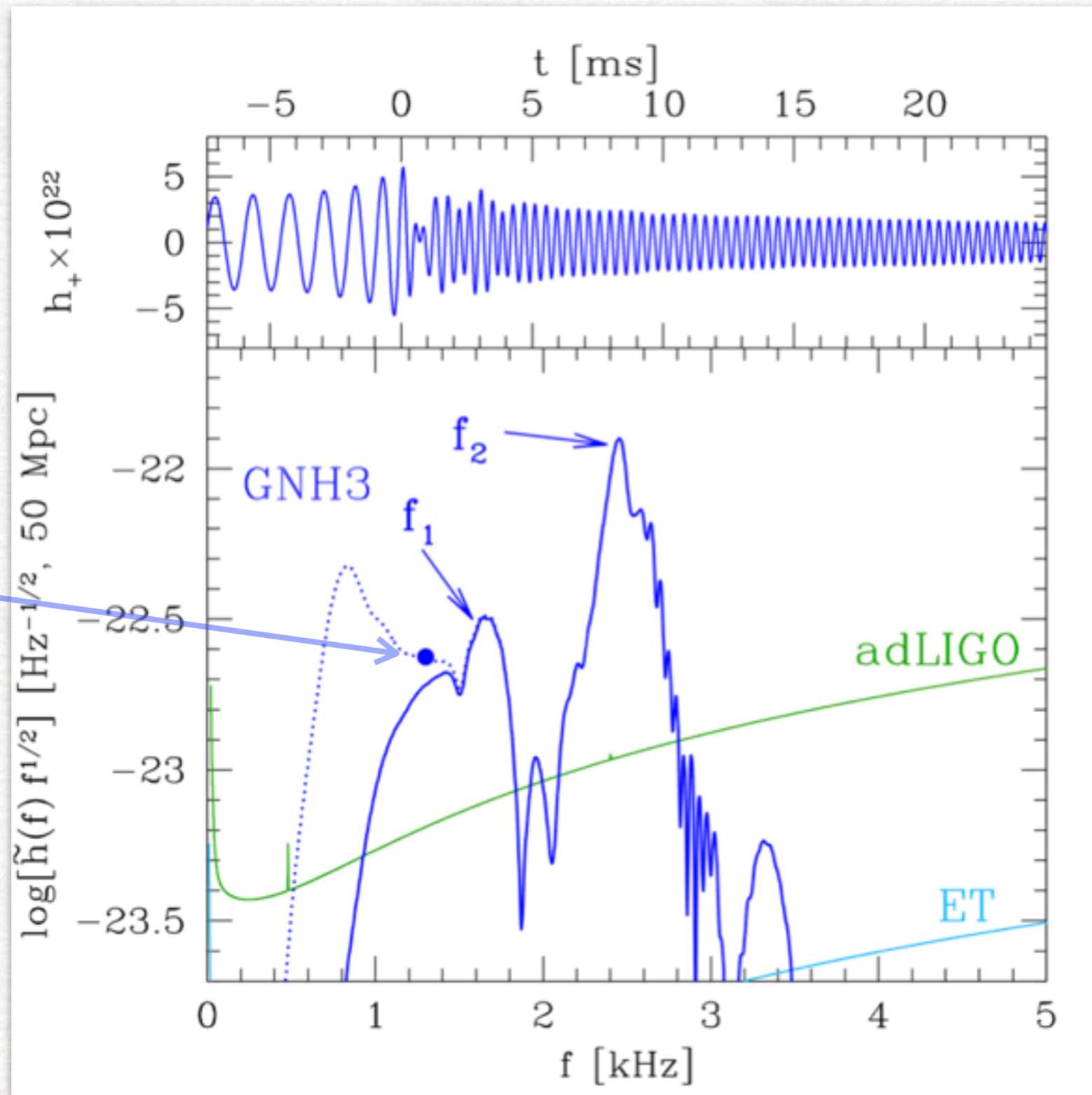
Takami, LR, Baiotti (2014, 2015), LR+ (2016)



# A new approach to constrain the EOS

Oechslin+2007, Baiotti+2008, Bauswein+ 2011, 2012, Stergioulas+ 2011, Hotokezaka+ 2013, Takami 2014, 2015, Bernuzzi 2014, 2015, Bauswein+ 2015, LR+2016...

merger  
frequency



# How to constrain the EOS by GW high freq.s

Oechslin+2007,

Baiotti+2008,

Bauswein+  
2011, 2012,

Stergioulas+  
2011,  
Hotokezaka+  
2013,

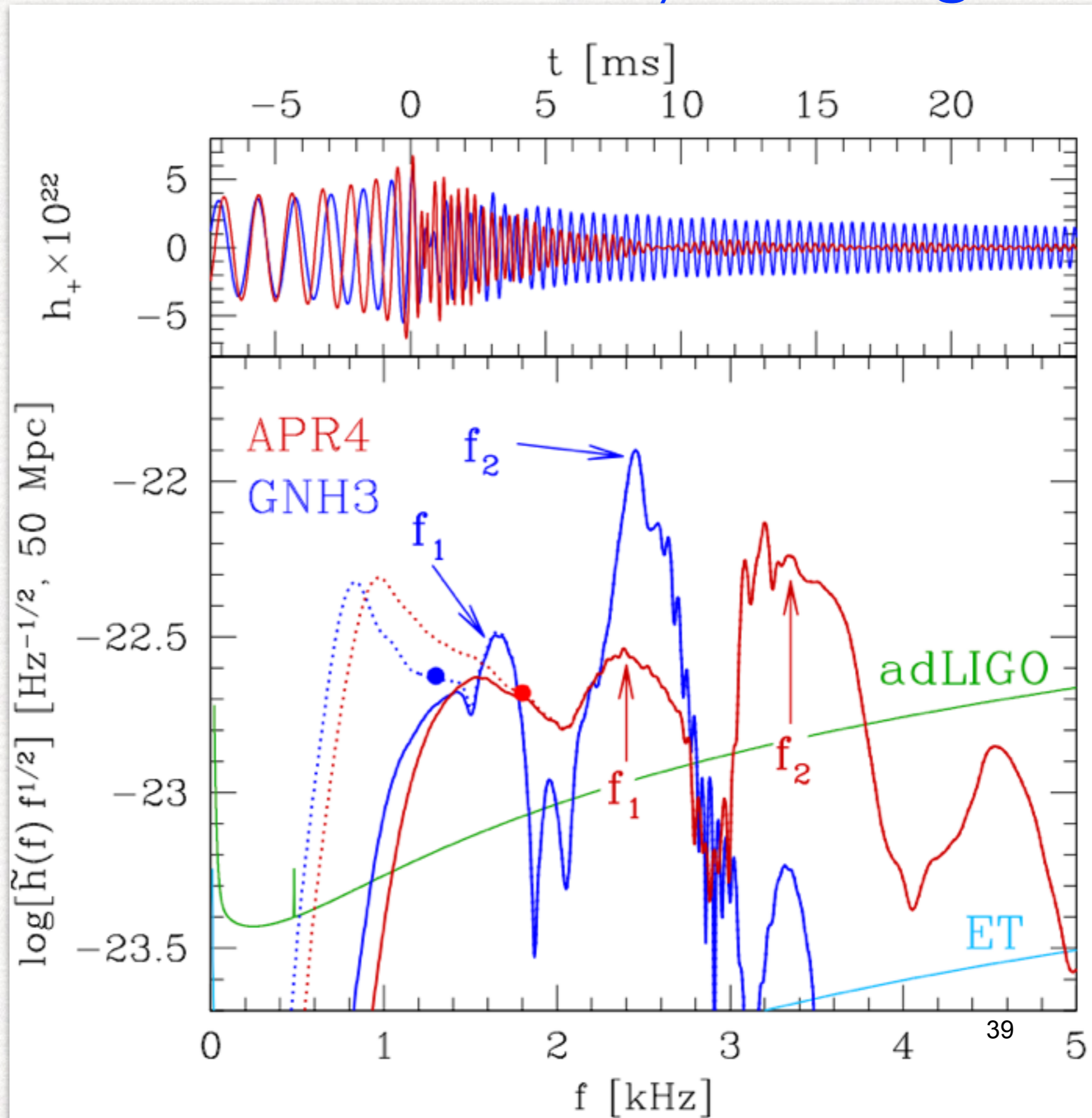
Takami 2014,  
2015,

Bernuzzi 2014,  
2015,

Bauswein+  
2015,

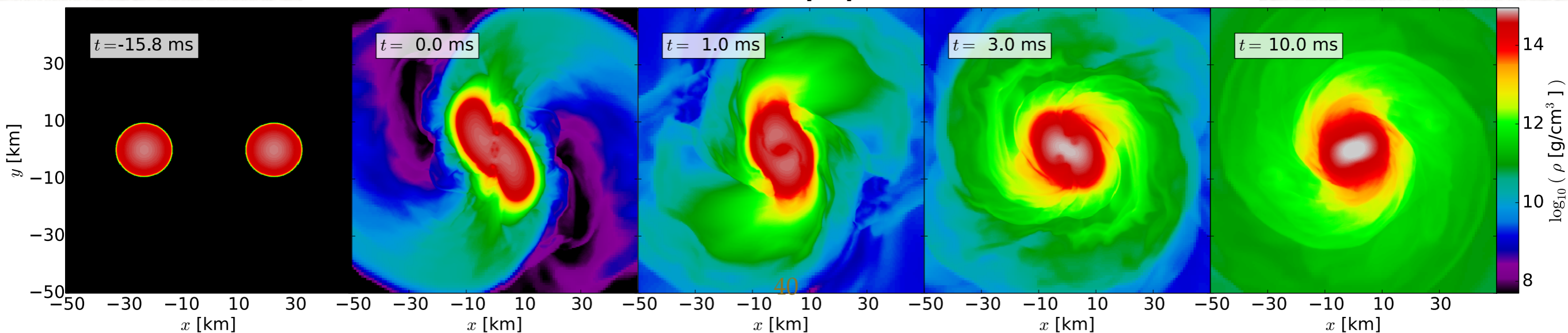
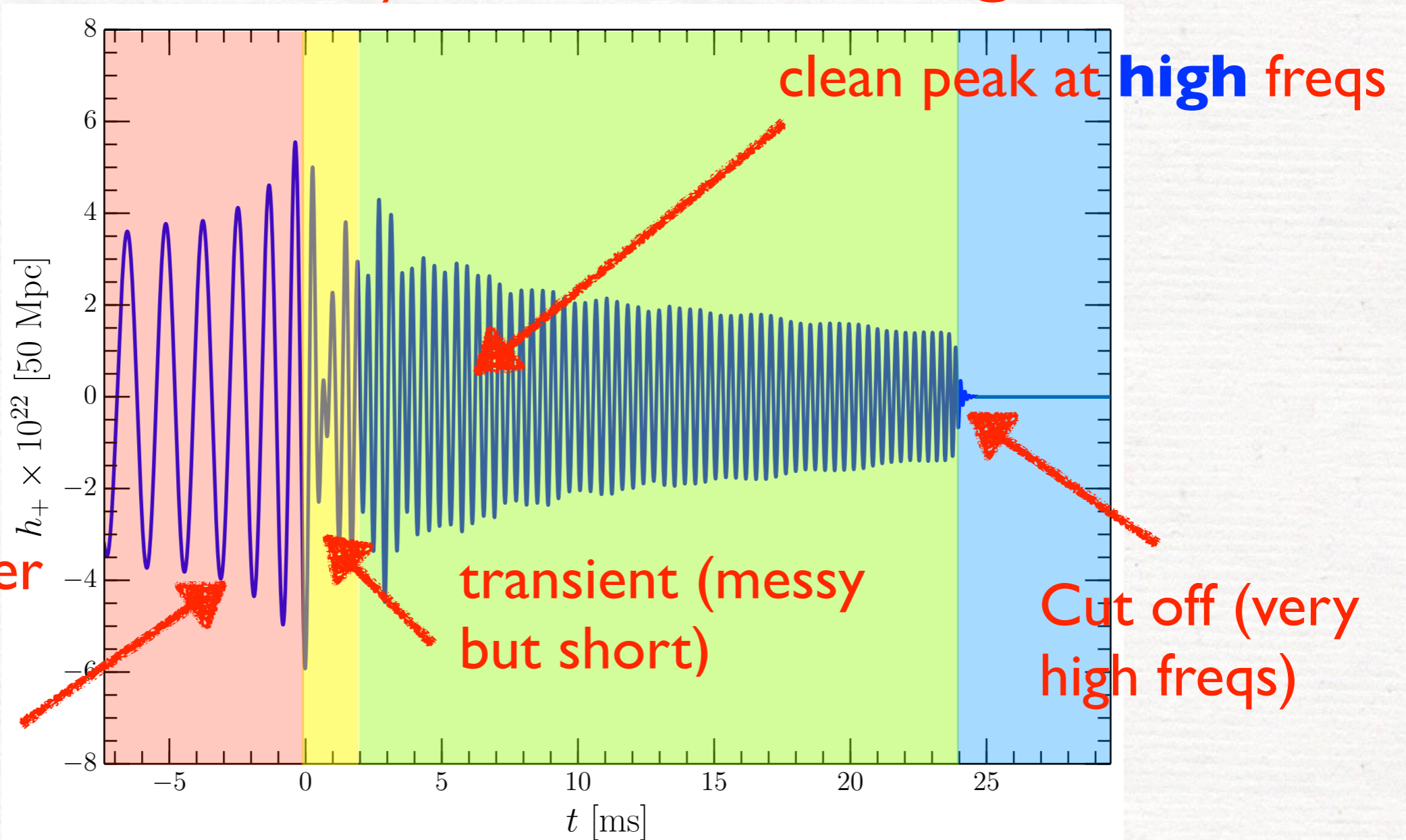
LRezzolla+2016

...



# Anatomy of the GW signal

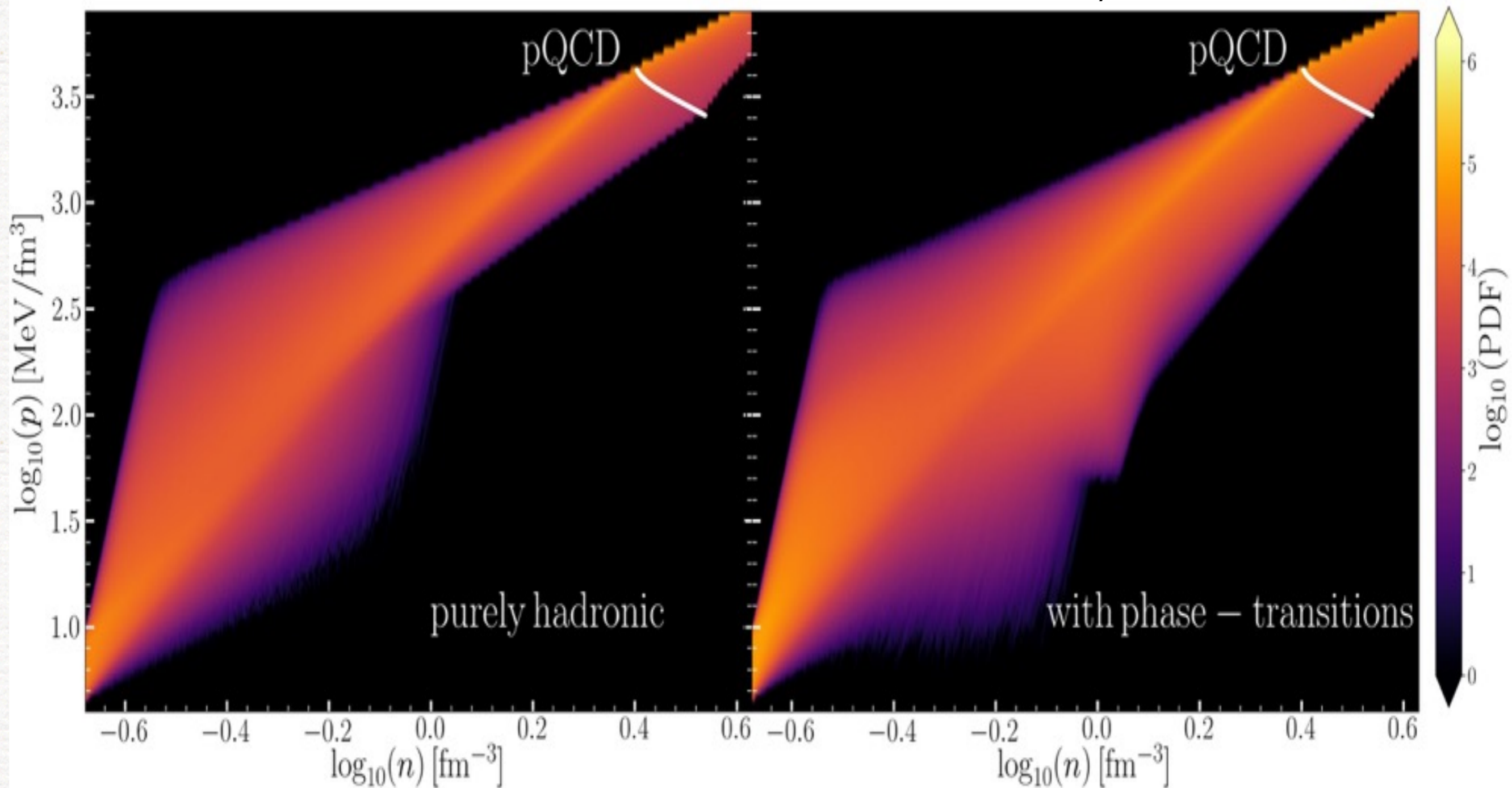
Chirp signal  
(track from **low** to higher frequencies)





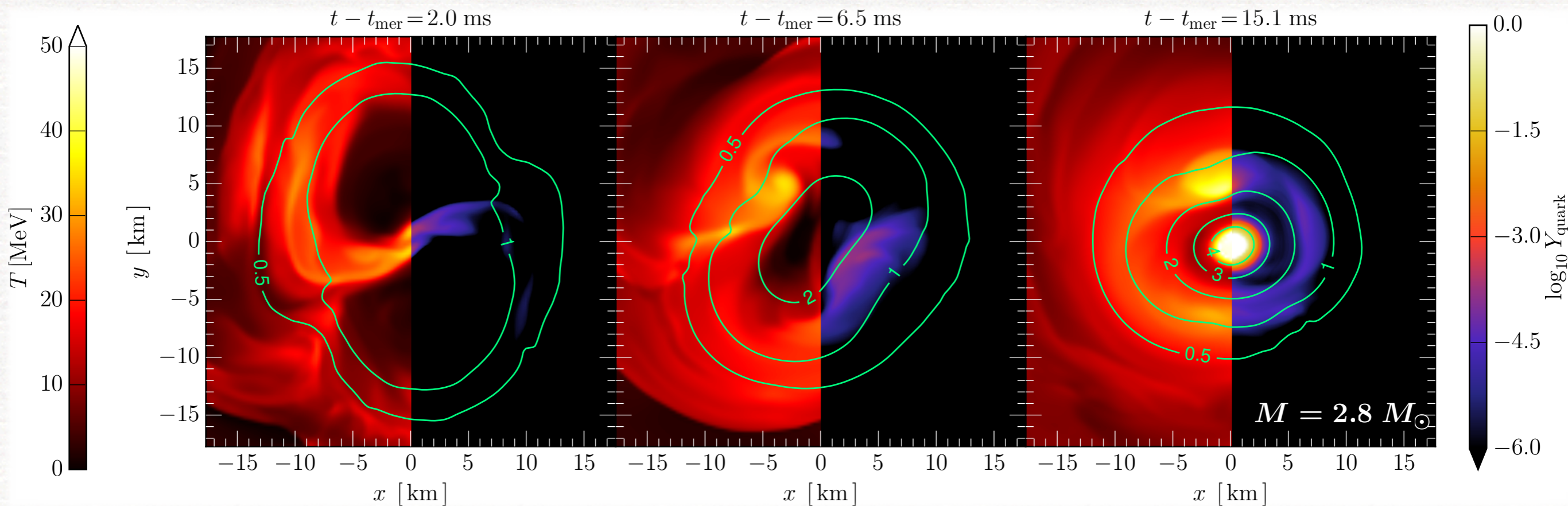
# What about Quark Matter phase transition?

- All EOSs so far purely hadronic - a conservative, but at high density un-**reasonable** assumption.
- What about the possibility of **H-QM-phase transition**? These are not trivial, and difficult to model consistently relativistic.



# Formation of a quark core in BNS mergers

- Small quark fraction present in regions of high temperature (cross-over phase transition)

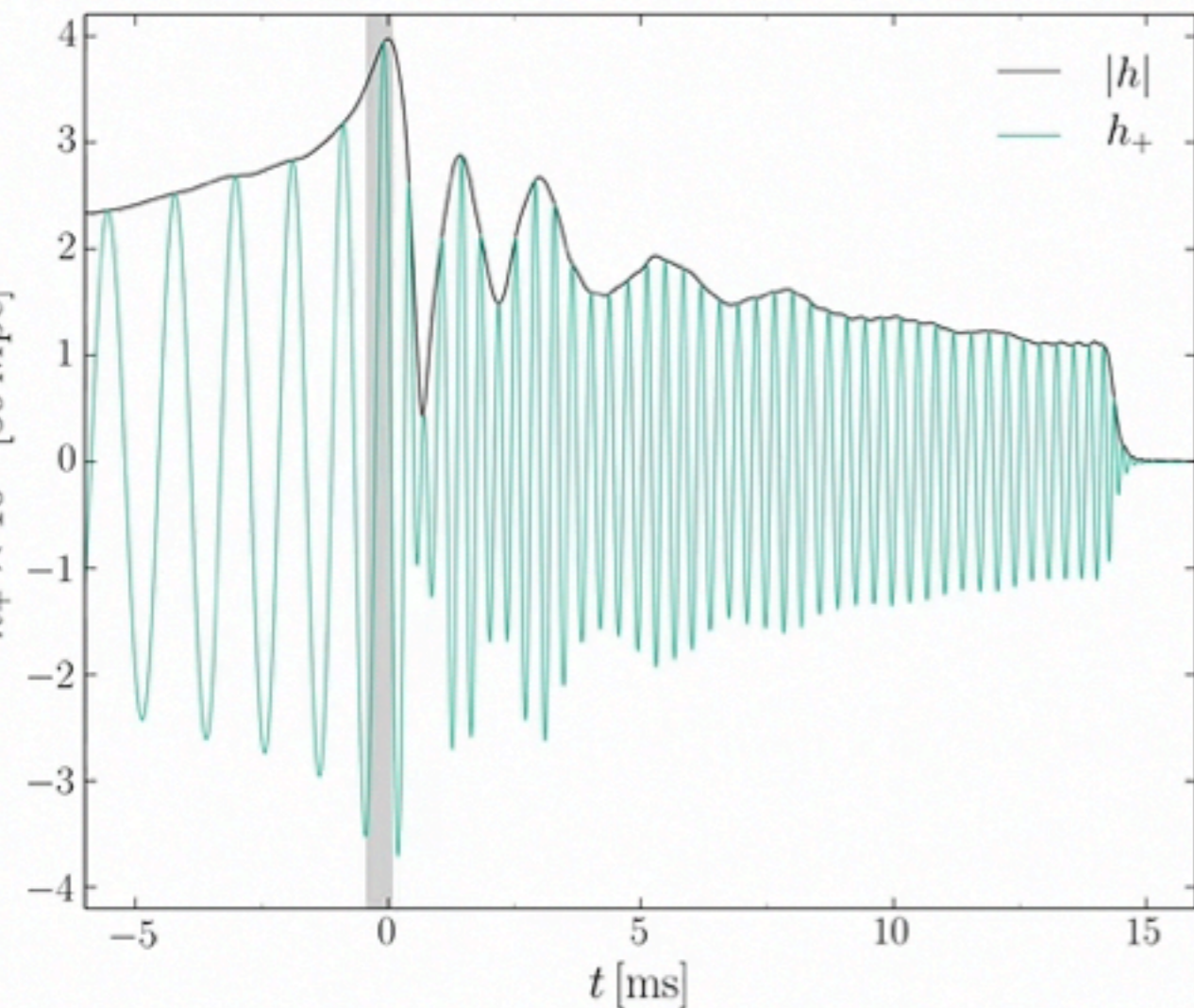


First order phase transition produces hot (unstable) quark core in the centre of the remnant

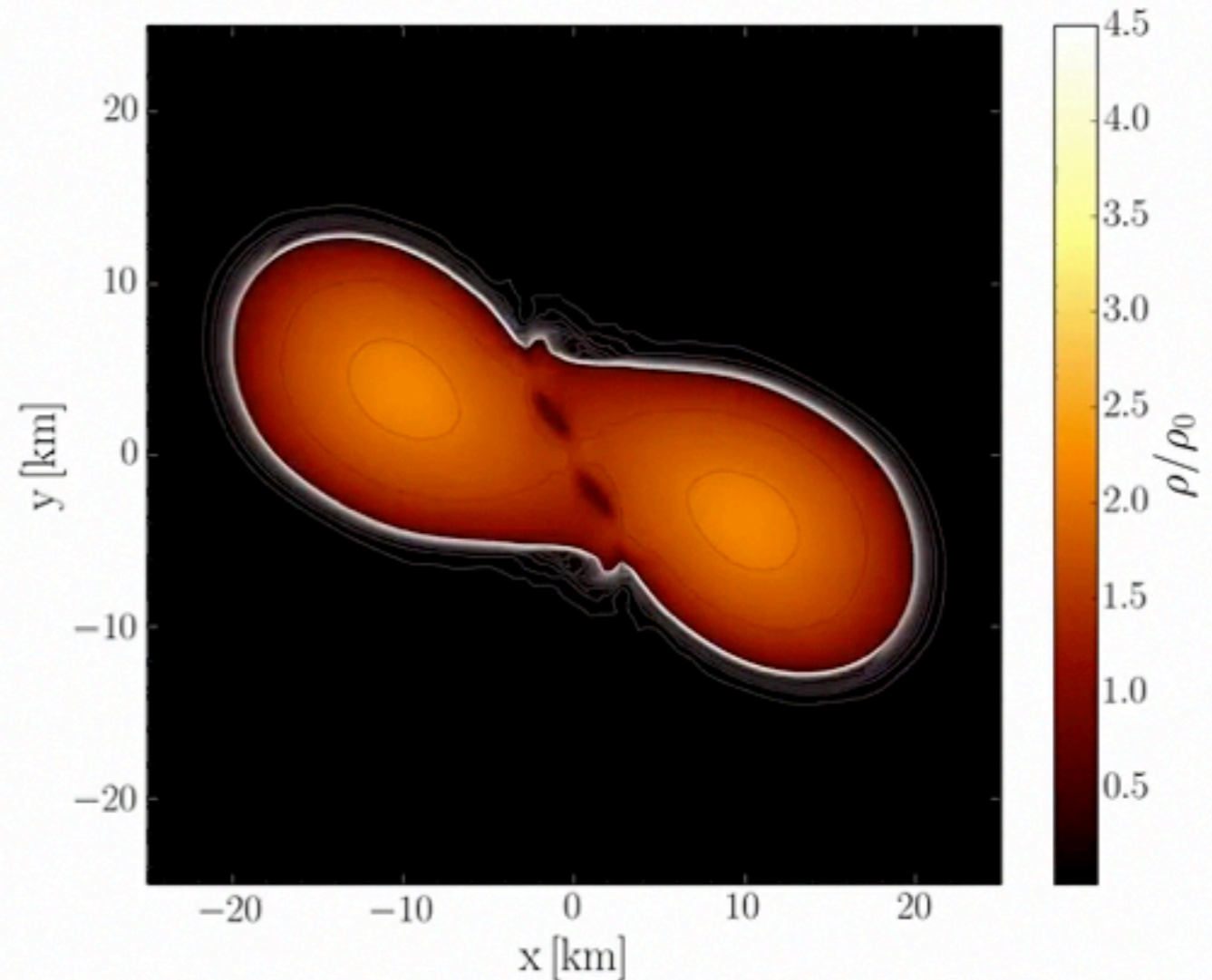
# Hypermassive Neutronstar GR-Hydro: Making **Quarkmatter BHs**

EoS Contains Neutrons, Protons, Electrons, Hyperons, Muons

**Quarkmatter at high** net baryon density ( $3\rho_0$ ) ! Each NS:  $M = 1.35$  Solar Mass



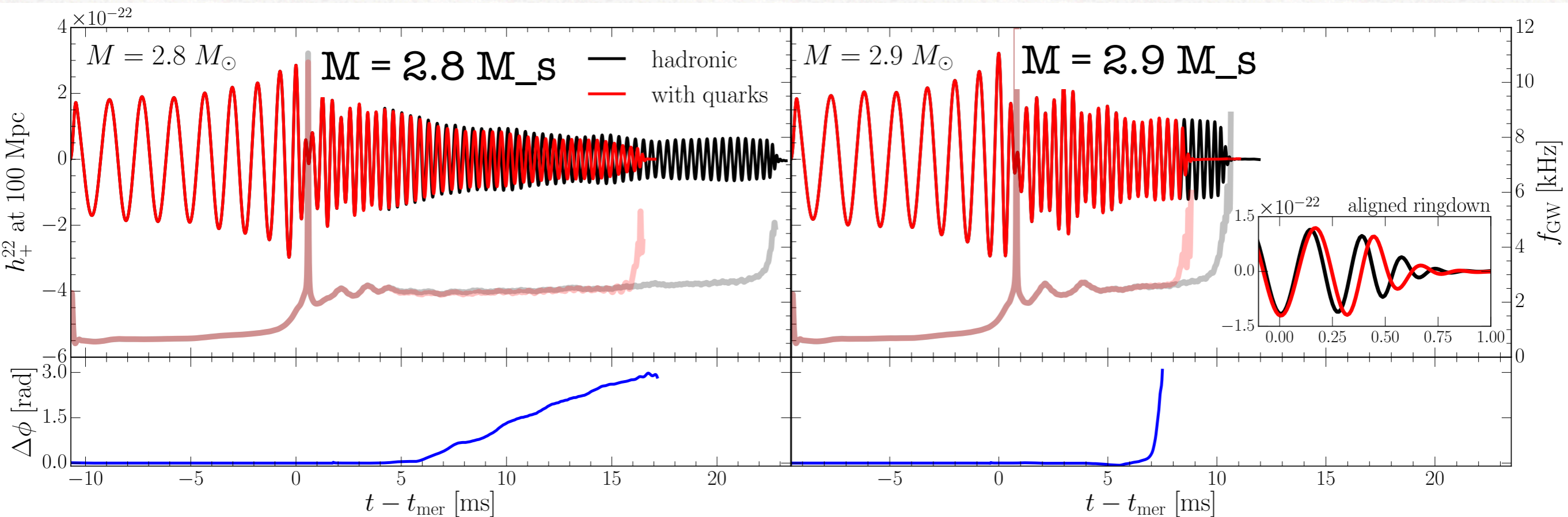
Amplitude of the emitted  
Gravitational Wave  
at a distance of 50 Mpc



particle density  $\rho(x,y)$   
in the equatorial slice in Units of normal  
nuclear groundstate density  $\rho_0$

# Quark Matter seen in gravitational waves?

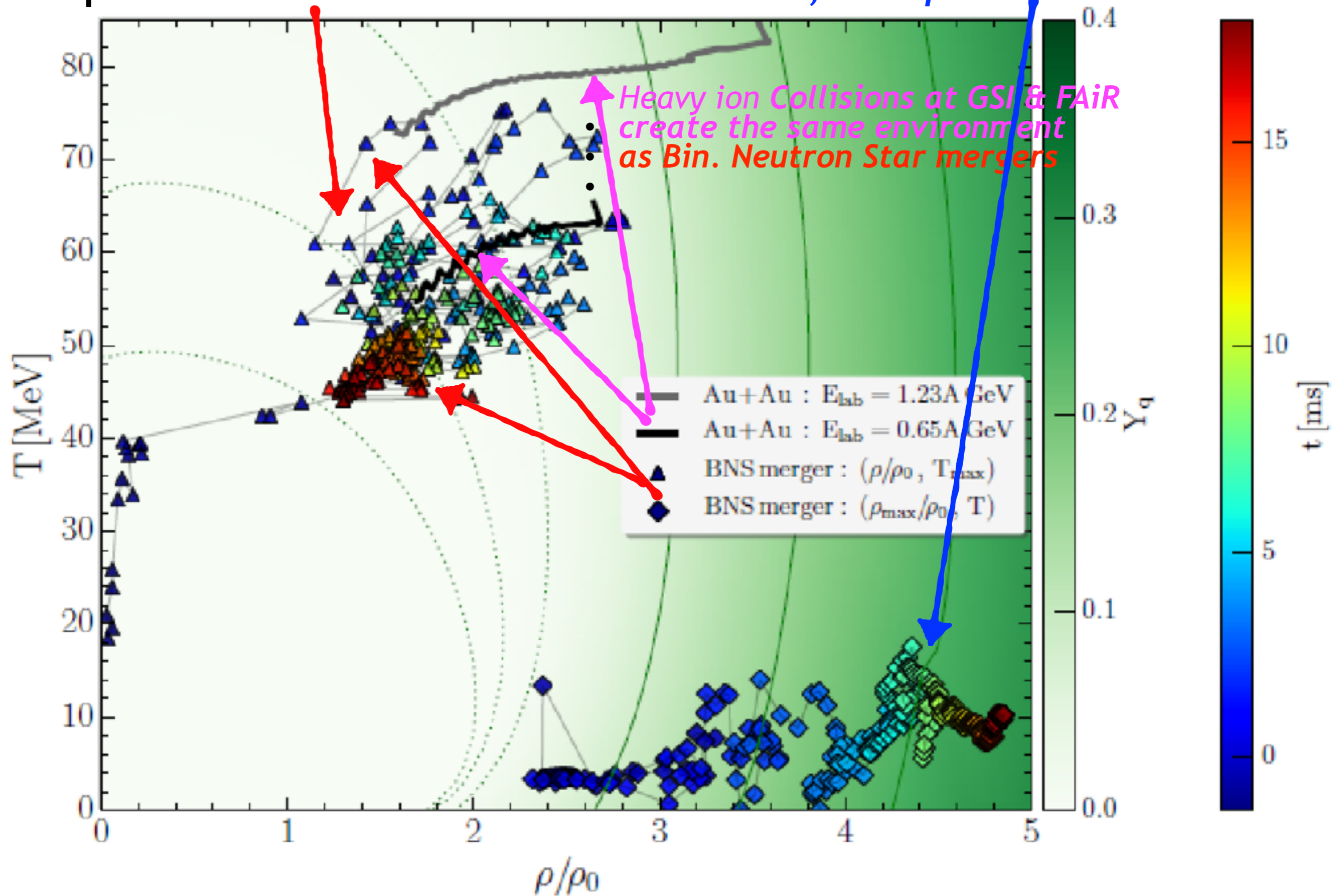
- No quarks are present in the inspiral phase !



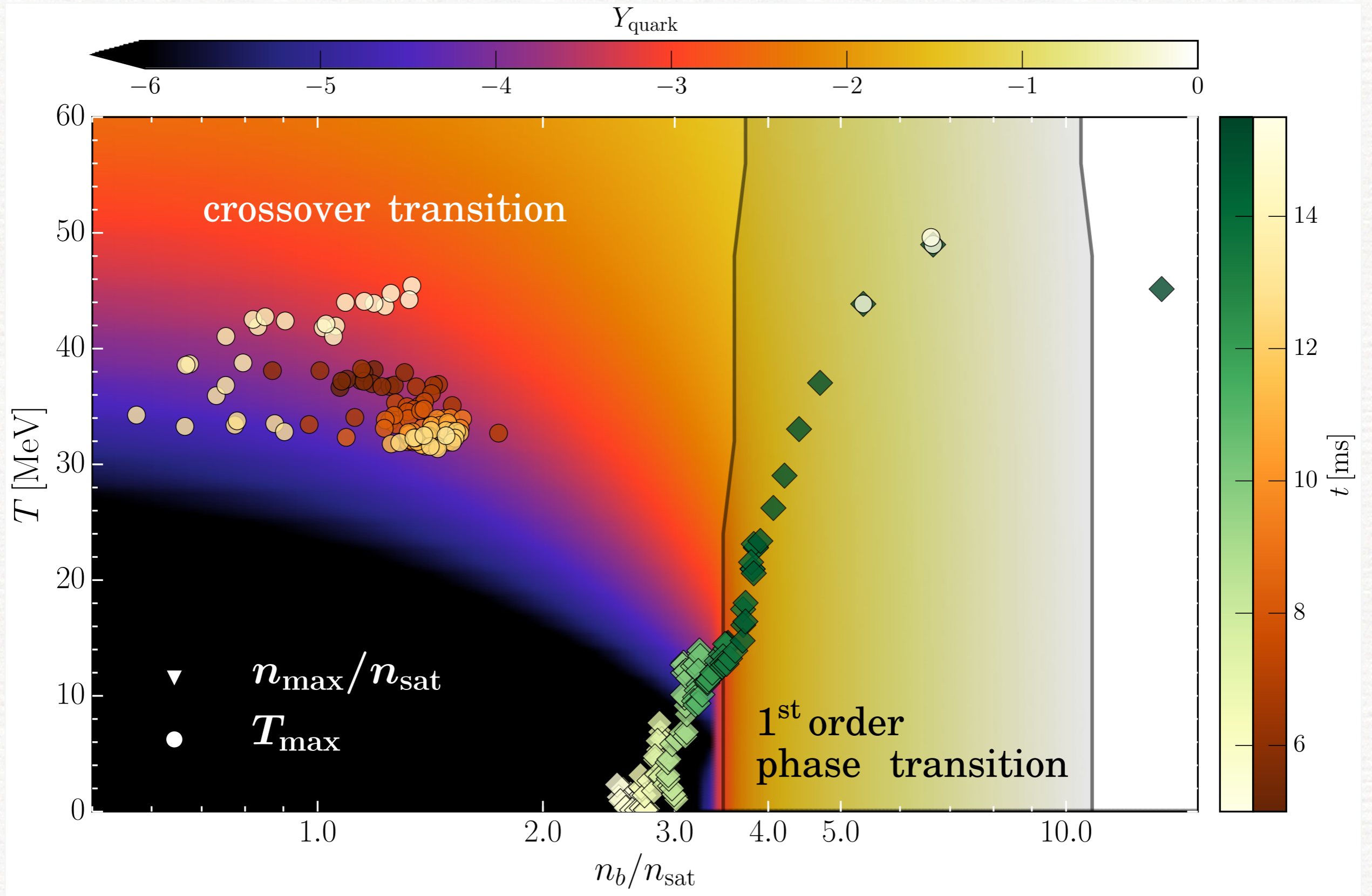
Continued presence of small quark fraction leads to a de-phasing of the waveform in the post merger

# Where it's hot and dense in neutron star mergers

- Separation of **hot hadronic corona** and **dense, cold quark matter core**



# Observing a 1. Order phase transition ?



Most Dexheimer Schramm Rezzolla H.ST. et al 2018

\*more to come

\*Spectra of post-merger shows peaks, some "quasi-universal".

\*When used together with tens of observations, they will set tight constraints on EOS: radius known with  $\sim 1$  km precision.

\*Magnetic fields unlikely to be detected during the inspiral but **important** after the merger: instabilities and EM counterparts.

\***Mergers** lead to tiny but important ejected matter and kilo-/macro-nova emission - "**high-A**" nucleosynthesis very robust.

\***GW170817** provided new limits on **maximum mass** and **radii**:

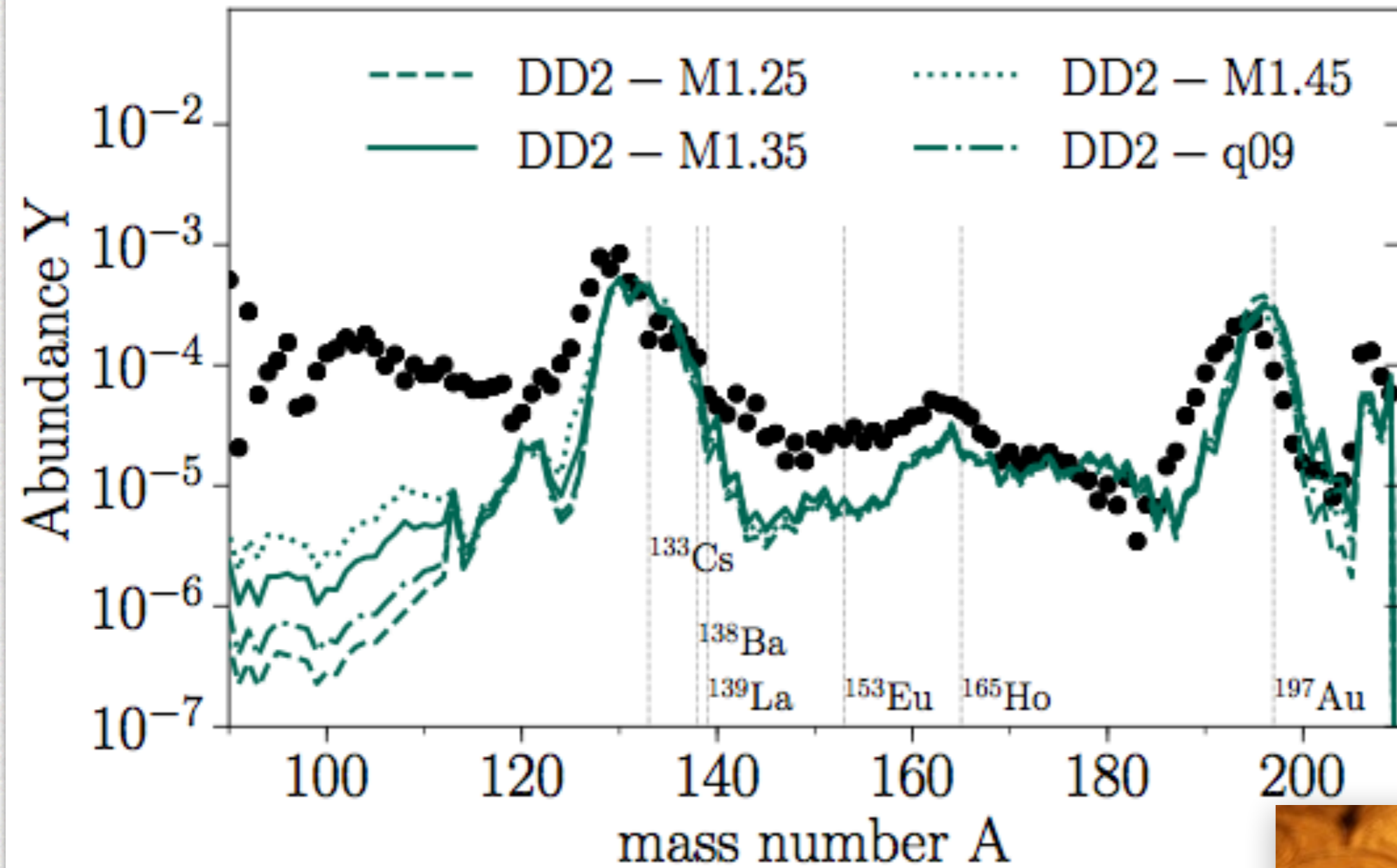
$$2.01_{-0.04}^{+0.04} \leq M_{\text{TOV}}/M_{\odot} \lesssim 2.16_{-0.15}^{+0.17}$$

$$12.00 < R_{1.4}/\text{km} < 13.45 \quad \bar{R}_{1.4} = 12.45 \text{ km} \quad \text{hadronic EOSs}$$

$$8.53 < R_{1.4}/\text{km} < 13.74 \quad \bar{R}_{1.4} = 13.06 \text{ km} \quad \text{phase transitions}$$

Merging binaries of NSs are Einstein's **richest laboratory**:

GWs, nuclear physics, astrophysics: more to come!...



Relative Abundance of cosmic elements - Simulation vs. Observation - T. Kodama '77 GW170817 produces lots of Gold, Platinum: 10x M\_earth !

Tell Your politicians !





# The "Death-Star- Machines" FAIR and NICA: Neutron-Star matter by Nuclear Collisions in the Lab

!

## Charm and Beauty of International Collaboration



Observers

- 
- 
- 
- 

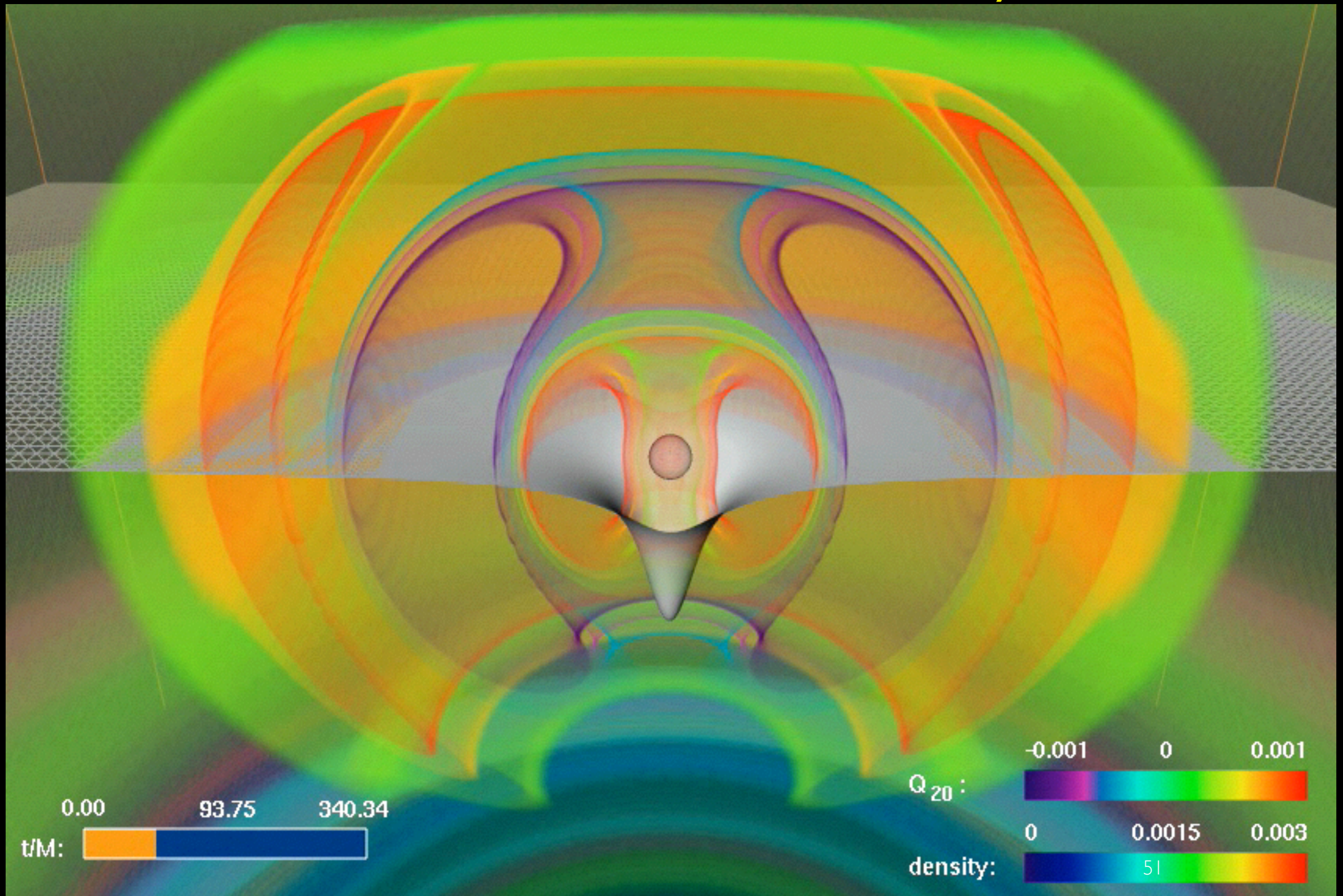


2/27/2018

- Austria
- Czech
- China
- Hungary
- Finland
- France
- Germany
- India
- Italy
- Poland
- Slovenia
- Spain
- Sweden
- Romania
- Russia
- Rosatom
- UK



# Numerical Relativity



# Supercomputers as “astrophysical laboratories”

The complexity of the Einstein equations and the absence of symmetries force the use of parallel supercomputers.

In essence the problem at any time is broken in many smaller pieces, one for each of the many processors. If necessary, data can be exchanged between neighbouring processors



We also employ **AMR** (adaptive mesh refinement) to increase the resolution where needed

## Typical simulation:

- 500 processors
- 1 TB memory
- 4-6 weeks of running time
- 3-4 TB of data produced

Damiana @ AEI, LCSC,  
Green Cube at GSI

# Numerical Relativity: probing the extreme

- Einstein equations are **highly nonlinear** and so are the equations of relativistic hydrodynamics and MHD in conditions where **shocks** are expected to develop =>CBM.
- Furthermore, the need to compute gravitational waves requires that we consider highly non-symmetrical configurations, eg binaries. This implies that we need to solve the equations in **3 spatial dimensions plus time (3+1)**
- Numerical relativity is focussed on solving Einstein equations and those of relativistic hydrodynamics and MHD in those regimes in which no approximation holds: eg in the **most nonlinear regimes** of the theory.

Special Programs for **Junior Researchers** at FAIR and **FIAS** :

Support of international Ph.D.- Students and Postdocs through GSI, Helmholtz, BMBF and HIC for FAIR @ **FIAS**

Helmholtz Graduate School **HIRE for FAIR@FIAS**

Large inter-university Graduate School with excellent connections to GSI

Education and training of young researchers: one of key pillars at FIAS !!

- Large number of **international doctoral students**
- Numerous power weeks and workshop-type events - every year
- Handling of scholarships of various funding sources by FIAS

Support international young investigators: key advantage for FAIR@ FIAS

Large highly visible activities, including public outreach, every year at FIAS