

Observable windows for Axions as Hot Relics

Alessio Notari ¹

Universitat de Barcelona

talk @ Workshop on the Standard Model and Beyond,
Corfu 2018.

¹ In collaboration with Ricardo Z. Ferreira, F. D'Eramo, J.L. Bernal

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

The **QCD Axion** (a) is a very light particle that

- Solves the “**Strong CP problem**” via coupling to gluons

$$\mathcal{L}_a = \frac{\alpha_s}{8\pi} \frac{a}{f} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

The **QCD Axion** (a) is a very light particle that

- Solves the “**Strong CP problem**” via coupling to gluons

$$\mathcal{L}_a = \frac{\alpha_s}{8\pi} \frac{a}{f} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

- Integrating by parts: $\mathcal{L}_a = \frac{\alpha_s}{8\pi} \frac{\partial_\mu a}{f} K^\mu$,
 \implies continuous shift symmetry $a \rightarrow a + c$

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

The **QCD Axion** (a) is a very light particle that

- Solves the “**Strong CP problem**” via coupling to gluons

$$\mathcal{L}_a = \frac{\alpha_s}{8\pi} \frac{a}{f} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

- Integrating by parts: $\mathcal{L}_a = \frac{\alpha_s}{8\pi} \frac{\partial_\mu a}{f} K^\mu$,
 \implies continuous shift symmetry $a \rightarrow a + c$
- **But:** boundary term sensitive to QCD Instantons,
 - 1 breaks to discrete $\frac{a}{f} \rightarrow \frac{a}{f} + 2\pi$.
 - 2 Induces a mass $m_a \approx \frac{\Lambda_{\text{QCD}}^2}{f}$

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

The **QCD Axion** (a) is a very light particle that

- Solves the “**Strong CP problem**” via coupling to gluons

$$\mathcal{L}_a = \frac{\alpha_s}{8\pi} \frac{a}{f} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

- Integrating by parts: $\mathcal{L}_a = \frac{\alpha_s}{8\pi} \frac{\partial_\mu a}{f} K^\mu$,
 \implies continuous shift symmetry $a \rightarrow a + c$
- **But:** boundary term sensitive to QCD Instantons,
 - 1 breaks to discrete $\frac{a}{f} \rightarrow \frac{a}{f} + 2\pi$.
 - 2 Induces a mass $m_a \approx \frac{\Lambda_{\text{QCD}}^2}{f}$
- Present bounds on $f \implies m_a \ll 0.1 \text{ eV}$ (or even less)

Axion: constraints

Axions as Hot Relics

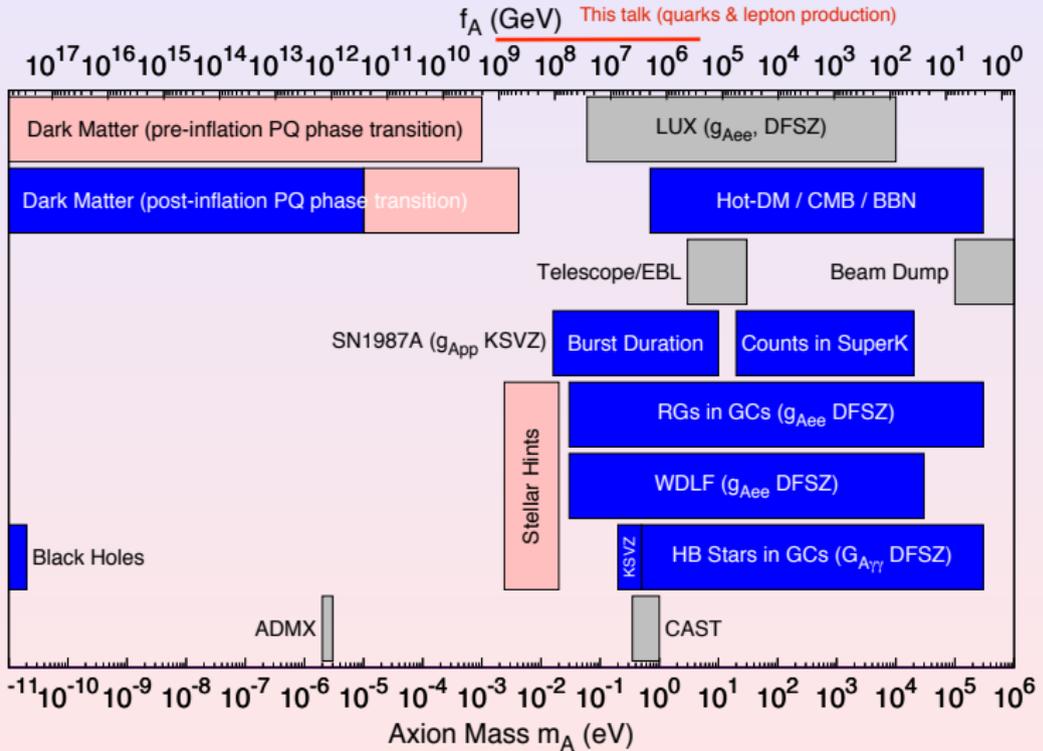
The QCD Axion

Axions via Gluons

Axion via Quarks

Axion via Leptons

The H_0 tension



QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- **Axions:**
 - 1 couple with continuous shift symmetry with **all SM**
 - 2 **Only** breaking: Instanton-induced (tiny) mass

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- **Axions:**
 - ① couple with continuous shift symmetry with **all SM**
 - ② **Only** breaking: Instanton-induced (tiny) mass

- **Terminology:**
 - ① If it couples to $G\tilde{G} \implies$ "QCD Axion"
 - ② If not: \implies Axion-Like Particle ("ALP")

QCD Axion production in Early Universe

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Due to $\frac{\alpha_s}{8\pi} \frac{a}{f} G_{\mu\nu} \tilde{G}^{\mu\nu}$ QCD Axions can be produced by gluon scatterings in the Early Universe

QCD Axion production in Early Universe

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Due to $\frac{\alpha_s}{8\pi} \frac{a}{f} G_{\mu\nu} \tilde{G}^{\mu\nu}$ QCD Axions can be produced by gluon scatterings in the Early Universe
- Can be produced at high T and decouples at $T \lesssim T_{DEC}$
→ **hot relic (dark radiation)**
(M.Turner, 1987; Masso, F. Rota, and G. Zsembinszki, 2003, Salvio, Strumia, Xue, 2014)

QCD Axion production in Early Universe

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Due to $\frac{\alpha_s}{8\pi} \frac{a}{f} G_{\mu\nu} \tilde{G}^{\mu\nu}$ QCD Axions can be produced by gluon scatterings in the Early Universe
- Can be produced at high T and decouples at $T \lesssim T_{DEC}$
→ hot relic (dark radiation)
(M.Turner, 1987; Masso, F. Rota, and G. Zsembinszki, 2003, Salvio, Strumia, Xue, 2014)
- Scattering rate (via gluons) vs. Hubble

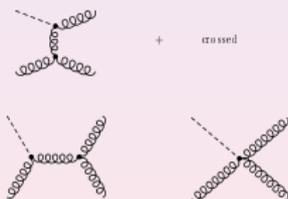


Figure: (Massò et al. Phys.Rev. D66 (2002).).

$$\Gamma_s \equiv \langle \sigma v \rangle \cdot n_g^{EQ} = \left(\frac{\alpha_s}{2\pi f} \right)^2 g_s^2 \cdot T^3$$

QCD Axion production in Early Universe

Axions as Hot Relics

The QCD Axion

Axions via Gluons

Axion via Quarks

Axion via Leptons

The H_0 tension

- Due to $\frac{\alpha_s}{8\pi} \frac{a}{f} G_{\mu\nu} \tilde{G}^{\mu\nu}$ QCD Axions can be produced by gluon scatterings in the Early Universe
- Can be produced at high T and decouples at $T \lesssim T_{DEC}$
→ hot relic (dark radiation)
(M.Turner, 1987; Masso, F. Rota, and G. Zsembinszki, 2003, Salvio, Strumia, Xue, 2014)
- Scattering rate (via gluons) vs. Hubble

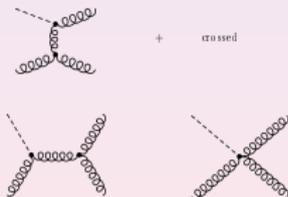


Figure: (Massò et al. Phys.Rev. D66 (2002).).

$$\Gamma_s \equiv \langle \sigma v \rangle \cdot n_g^{EQ} = \left(\frac{\alpha_s}{2\pi f} \right)^2 g_s^2 \cdot T^3 \text{ vs. } H \approx \frac{T^2}{M_{Pl}}.$$

QCD Axion thermalization and decoupling

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Scattering rate (via gluons) vs. Hubble

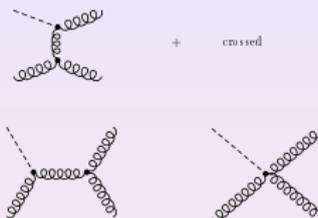


Figure: (Massò et al. Phys.Rev. D66 (2002).).

$$\Gamma_s = \left(\frac{\alpha_s}{2\pi f}\right)^2 g_s^2 T^3 \text{ vs. } H \approx \frac{T^2}{M_{Pl}}.$$

QCD Axion thermalization and decoupling

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Scattering rate (via gluons) vs. Hubble

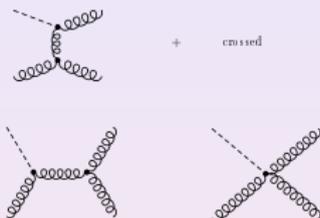


Figure: (Massò et al. Phys.Rev. D66 (2002).).

$$\Gamma_s = \left(\frac{\alpha_s}{2\pi f}\right)^2 g_s^2 T^3 \text{ vs. } H \approx \frac{T^2}{M_{Pl}}.$$

- At $T > T_{DEC} \equiv$ thermal equilibrium

QCD Axion thermalization and decoupling

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Scattering rate (via gluons) vs. Hubble

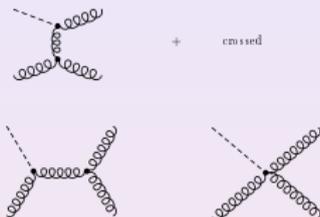


Figure: (Massò et al. Phys.Rev. D66 (2002).).

$$\Gamma_s = \left(\frac{\alpha_s}{2\pi f}\right)^2 g_s^2 T^3 \text{ vs. } H \approx \frac{T^2}{M_{Pl}}.$$

- At $T > T_{DEC} \equiv$ thermal equilibrium

- **Example:**

① $f = 10^9 \text{ GeV} \implies T_{DEC} \approx 10 \text{ TeV}$

② $f = 10^{10} \text{ GeV} \implies T_{DEC} \approx 10^4 \text{ TeV}$

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If a particle:

- 1 Was in equilibrium at $T > T_{DEC}$
- 2 Decouples at some $T \lesssim T_{DEC}$
- 3 Has negligible mass

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If a particle:
 - 1 Was in equilibrium at $T > T_{DEC}$
 - 2 Decouples at some $T \lesssim T_{DEC}$
 - 3 Has negligible mass
- After decoupling $n_a \propto a^{-3}$ and $\rho_a \propto a^{-4}$, acts as a **hot relic** (like neutrinos)
- Affects Matter-Radiation equality (if $m \ll \mathcal{O}(0.1 \sim 1 \text{eV})$)
 \implies **Observable by CMB** (and BBN)

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If a particle:
 - 1 Was in equilibrium at $T > T_{DEC}$
 - 2 Decouples at some $T \lesssim T_{DEC}$
 - 3 Has negligible mass
- After decoupling $n_a \propto a^{-3}$ and $\rho_a \propto a^{-4}$, acts as a **hot relic** (like neutrinos)
- Affects Matter-Radiation equality (if $m \ll \mathcal{O}(0.1 \sim 1 \text{ eV})$)
 \implies **Observable by CMB** (and BBN)
- Traditionally parameterized by **effective neutrino number**
- $N_{\text{eff}} = 3.046 + \Delta N_{\text{eff}}$

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If a particle:
 - 1 Was in equilibrium at $T > T_{DEC}$
 - 2 Decouples at some $T \lesssim T_{DEC}$
 - 3 Has negligible mass
- After decoupling $n_a \propto a^{-3}$ and $\rho_a \propto a^{-4}$, acts as a **hot relic** (like neutrinos)
- Affects Matter-Radiation equality (if $m \ll \mathcal{O}(0.1 \sim 1 \text{ eV})$)
 \implies **Observable by CMB** (and BBN)
- Traditionally parameterized by **effective neutrino number**
- $N_{\text{eff}} = 3.046 + \Delta N_{\text{eff}}$

$$\Delta N_{\text{eff}} \approx \frac{13.6}{g_{*,DEC}^{4/3}}$$

QCD Axion through N_{eff}

Axions as Hot
Relics

- $$\Delta N_{\text{eff}} \approx \frac{13.6}{g_{*,\text{DEC}}^{4/3}}$$

- If $T_{\text{DEC}} \gg 100\text{GeV}$ we only know

$$g_{*,\text{DEC}} \geq g_{*,\text{DEC}}^{\text{SM}} = 106.75$$

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

QCD Axion through N_{eff}

Axions as Hot
Relics

- $$\Delta N_{\text{eff}} \approx \frac{13.6}{g_{*,\text{DEC}}^{4/3}}$$

The QCD
Axion

- If $T_{\text{DEC}} \gg 100\text{GeV}$ we only know

$$g_{*,\text{DEC}} \geq g_{*,\text{DEC}}^{\text{SM}} = 106.75$$

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- $\Rightarrow \Delta N_{\text{eff}} \lesssim 0.027$ (only upper bound!)

QCD Axion through N_{eff}

Axions as Hot Relics

The QCD Axion

Axions via Gluons

Axion via Quarks

Axion via Leptons

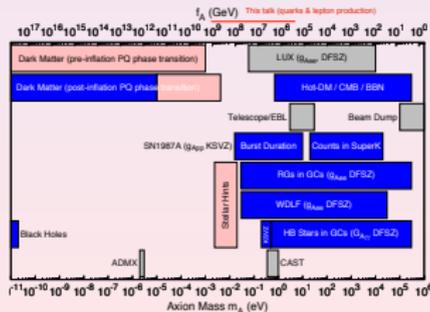
The H_0 tension

- $$\Delta N_{\text{eff}} \approx \frac{13.6}{g_{*,\text{DEC}}^{4/3}}$$

- If $T_{\text{DEC}} \gg 100\text{GeV}$ we only know

$$g_{*,\text{DEC}} \geq g_{*,\text{DEC}}^{\text{SM}} = 106.75$$

- $\Rightarrow \Delta N_{\text{eff}} \lesssim 0.027$ (only upper bound!)



- Let's study $f \lesssim 10^9 \text{ GeV}$

$$\Rightarrow T_{\text{DEC}} \leq \text{Electroweak scale}$$

QCD Axion through N_{eff}

Axions as Hot
Relics

- Below EW scale ($f \lesssim 10^9$ GeV) dominant channels are via **quarks & leptons** (A.N. & R.Z.Ferreira, PRL 2018)

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

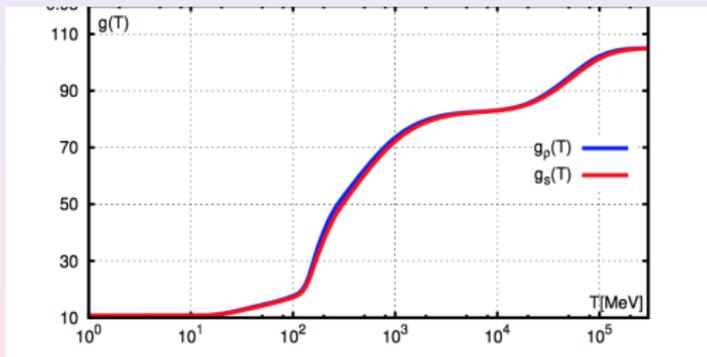
Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Below EW scale ($f \lesssim 10^9$ GeV) dominant channels are via **quarks & leptons** (A.N. & R.Z.Ferreira, PRL 2018)



QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

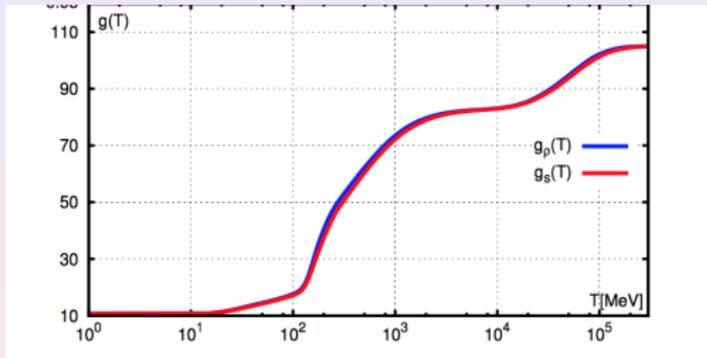
Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Below EW scale ($f \lesssim 10^9$ GeV) dominant channels are via **quarks & leptons** (A.N. & R.Z.Ferreira, PRL 2018)



ADVANTAGES:

- 1 g_*^{SM} is smaller \implies **larger N_{eff}**
- 2 Here we are confident on $g_*^{SM} \implies$ **Precise predictions**
- 3 Lower $f \implies$ more accessible by **direct** searches
(**CAST, IAXO**)

QCD Axion through N_{eff}

Axions as Hot
Relics

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{C_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, *e.g.* $qg \leftrightarrow qa$) vs. Hubble



QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

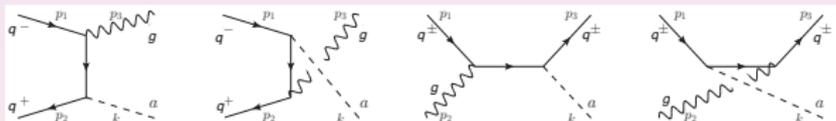
Axion via
Leptons

The H_0
tension

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g. $qg \leftrightarrow qa$) vs. Hubble



- If $m_q = 0 \implies$ the **vertex vanishes**

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

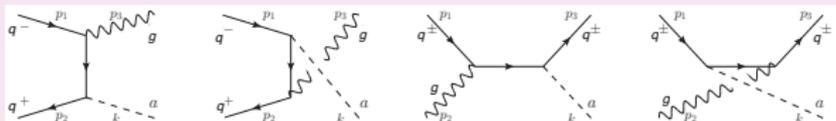
Axion via
Leptons

The H_0
tension

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g. $qg \leftrightarrow qa$) vs. Hubble



- If $m_q = 0 \implies$ the **vertex vanishes**
- In fact:

- This coupling can be **rotated away** $q \rightarrow e^{i\frac{c_j a}{f}} \gamma^5 q$
- But it **reappears in the mass term** $m_q \bar{q} q$

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

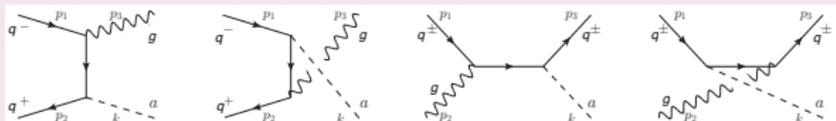
Axion via
Leptons

The H_0
tension

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g. $qg \leftrightarrow qa$) vs. Hubble



- If $m_q = 0 \implies$ the **vertex vanishes**
- In fact:
 - This coupling can be **rotated away** $q \rightarrow e^{i\frac{c_i a}{f}} \gamma^5 q$
 - But it **reappears in the mass term** $m_q \bar{q} q$

$$\Gamma_s = \left(\frac{c_i}{f}\right)^2 g_s^2 m_q^2 T$$

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

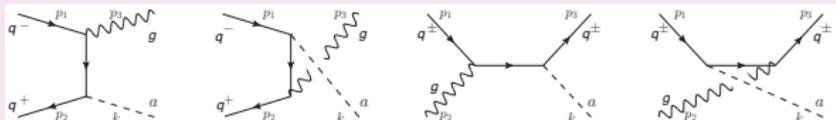
Axion via
Leptons

The H_0
tension

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g. $qg \leftrightarrow qa$) vs. Hubble



- If $m_q = 0 \implies$ the **vertex vanishes**
- In fact:
 - This coupling can be **rotated away** $q \rightarrow e^{i\frac{c_i a}{f}} \gamma^5 q$
 - But it **reappears in the mass term** $m_q \bar{q} q$

$$\Gamma_s = \left(\frac{c_i}{f}\right)^2 g_s^2 m_q^2 T \cdot e^{-\frac{m_q}{T}}$$

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{C_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

QCD Axion through N_{eff}

Axions as Hot
Relics

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g. $qg \leftrightarrow qa$) vs. Hubble
- $\Gamma_s = \left(\frac{c_i}{f}\right)^2 g_s^2 m_q^2 T \cdot e^{-\frac{m_q}{T}}$ vs. $H \approx \frac{T^2}{M_{Pl}}$.

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

QCD Axion through N_{eff}

Axions as Hot
Relics

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g. $qg \leftrightarrow qa$) vs. Hubble
- $\Gamma_s = \left(\frac{c_i}{f}\right)^2 g_s^2 m_q^2 T \cdot e^{-\frac{m_q}{T}}$ vs. $H \approx \frac{T^2}{M_{Pl}}$.
- Ratio peaks at $T \approx m_q$

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g. $qg \leftrightarrow qa$) vs. Hubble
- $\Gamma_s = \left(\frac{c_i}{f}\right)^2 g_s^2 m_q^2 T \cdot e^{-\frac{m_q}{T}}$ vs. $H \approx \frac{T^2}{M_{Pl}}$.

- Ratio peaks at $T \approx m_q$
- Axions produced **dominantly** via quarks

$$1 \text{ GeV} \lesssim T \lesssim 100 \text{ GeV}$$

$$\text{(for } 10^7 \text{ GeV} \lesssim f/c_i \lesssim 10^9 \text{ GeV)}^2$$

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g. $qg \leftrightarrow qa$) vs. Hubble
- $\Gamma_s = \left(\frac{c_i}{f}\right)^2 g_s^2 m_q^2 T \cdot e^{-\frac{m_q}{T}}$ vs. $H \approx \frac{T^2}{M_{Pl}}$.

- Ratio peaks at $T \approx m_q$
- Axions produced **dominantly** via quarks

$$1 \text{ GeV} \lesssim T \lesssim 100 \text{ GeV}$$

(for $10^7 \text{ GeV} \lesssim f/c_i \lesssim 10^9 \text{ GeV}$)²

- Range interesting for direct detection (e.g. IAXO),
 $m_a \approx 10^{-2} \sim 10^{-3} \text{ eV}$,

²R.Ferreira & A.N., PRL 2018. See also Turner PRL 1987, Brust et al. JHEP 2013, Baumann et al. PRL 2016.

QCD Axion through N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If a is directly coupled to **heavy quarks** (c, b, t):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g. $qg \leftrightarrow qa$) vs. Hubble

- $\Gamma_s = \left(\frac{c_i}{f}\right)^2 g_s^2 m_q^2 T \cdot e^{-\frac{m_q}{T}}$ vs. $H \approx \frac{T^2}{M_{Pl}}$.

- Ratio peaks at $T \approx m_q$

- Axions produced **dominantly** via quarks

$$1 \text{ GeV} \lesssim T \lesssim 100 \text{ GeV}$$

$$\text{(for } 10^7 \text{ GeV} \lesssim f/c_i \lesssim 10^9 \text{ GeV)}^2$$

- Range interesting for direct detection (e.g. IAXO),
 $m_a \approx 10^{-2} \sim 10^{-3} \text{ eV}$, (+ Hints from stellar cooling)

²R.Ferreira & A.N., PRL 2018. See also Turner PRL 1987, Brust et al. JHEP 2013, Baumann et al. PRL 2016.

QCD Axion through N_{eff}

Axions as Hot
Relics

- $g_{*,DEC}$ is smaller at $1 \text{ GeV} \lesssim T \lesssim 100 \text{ GeV}$
- **Prediction:** larger $N_{\text{eff}} \lesssim 0.05 - 0.06$
(*Not just upper bound!*)

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

QCD Axion through N_{eff}

Axions as Hot Relics

The QCD Axion

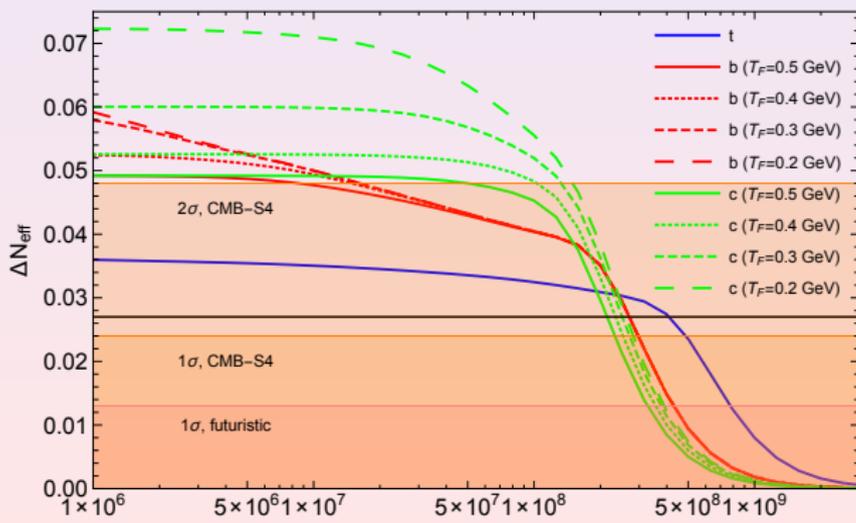
Axions via Gluons

Axion via Quarks

Axion via Leptons

The H_0 tension

- $g_{*,DEC}$ is smaller at $1 \text{ GeV} \lesssim T \lesssim 100 \text{ GeV}$
- **Prediction:** larger $N_{\text{eff}} \lesssim 0.05 - 0.06$
(*Not just upper bound!*)
- Solving Boltzmann equations for n_a :



Hot Axions via lepton scatterings

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- The same can be done with leptons (μ and τ)³
- a -electron uninteresting (strongly constrained)

³arxiv:., F.D'Eramo, A.N.,R.Z.Ferreira, J.L.Bernal 

Hot Axions via lepton scatterings

Axions as Hot Relics

The QCD Axion

Axions via Gluons

Axion via Quarks

Axion via Leptons

The H_0 tension

- The same can be done with leptons (μ and τ)³
- a -electron uninteresting (strongly constrained)
- Direct coupling to **heavy leptons** (μ, τ):

$$\mathcal{L}_{a-l} = \partial_\mu a \sum_i \frac{C_i}{2f} \bar{l}_i \gamma^\mu \gamma^5 l_i,$$



³arxiv.: F.D'Eramo, A.N., R.Z.Ferreira, J.L.Bernal

Hot Axions via lepton scatterings

Axions as Hot Relics

The QCD Axion

Axions via Gluons

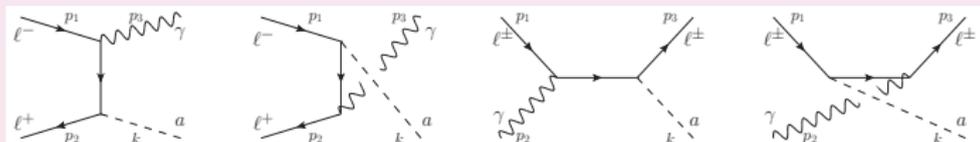
Axion via Quarks

Axion via Leptons

The H_0 tension

- The same can be done with leptons (μ and τ)³
- a -electron uninteresting (strongly constrained)
- Direct coupling to **heavy leptons** (μ, τ):

$$\mathcal{L}_{a-l} = \partial_\mu a \sum_i \frac{C_i}{2f} \bar{l}_i \gamma^\mu \gamma^5 l_i,$$



- Slightly smaller f/c_ℓ
- Ratio peaks at $T \approx m_\ell \implies$ **Larger N_{eff}**

³arxiv.: F.D'Eramo, A.N.,R.Z.Ferreira, J.L.Bernal

Hot Axions via lepton scatterings

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

**Axion via
Leptons**

The H_0
tension

Hot Axions via lepton scatterings

Axions as Hot
Relics

The QCD
Axion

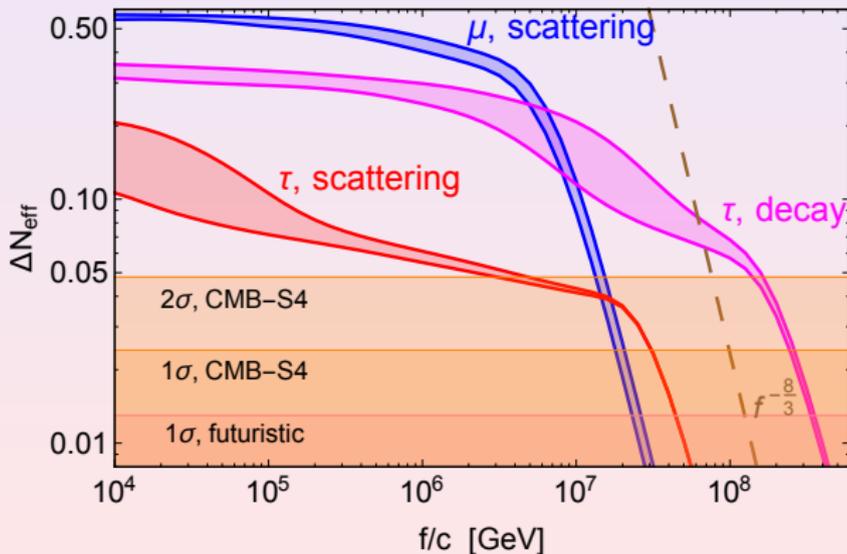
Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Smaller $f/c_i \lesssim \text{few} \cdot 10^7 \text{ GeV}$
- Ratio peaks at $T \approx m_\ell \Rightarrow$ Larger N_{eff}



Hot Axions via lepton Decays

Axions as Hot
Relics

- $a - \ell$ interaction can be **flavor non-diagonal**

$$\mathcal{L}_{a-\ell} = \partial_\mu \mathbf{a} \sum_{\ell \neq \ell'} \bar{\ell}' \gamma^\mu (\mathcal{V}_{\ell'\ell} + \mathcal{A}_{\ell'\ell} \gamma^5) \ell + \text{h.c.} ,$$

- Decays $\tau \rightarrow \mu + \mathbf{a}$, $\tau \rightarrow e + \mathbf{a}$

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

Hot Axions via lepton Decays

Axions as Hot Relics

The QCD Axion

Axions via Gluons

Axion via Quarks

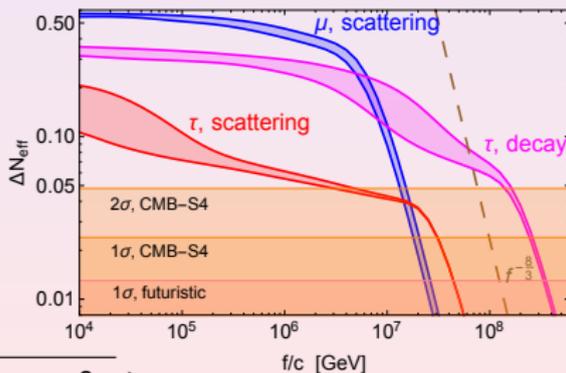
Axion via Leptons

The H_0 tension

- $a - \ell$ interaction can be **flavor non-diagonal**

$$\mathcal{L}_{a-\ell} = \partial_\mu a \sum_{\ell \neq \ell'} \bar{\ell}' \gamma^\mu (\mathcal{V}_{\ell'\ell} + \mathcal{A}_{\ell'\ell} \gamma^5) \ell + \text{h.c.},$$

- Decays $\tau \rightarrow \mu + a$, $\tau \rightarrow e + a$



$$(c_{\ell\ell'} \equiv \sqrt{\mathcal{V}_{\ell'\ell}^2 + \mathcal{A}_{\ell'\ell}^2})$$

Hot Axions via lepton Decays

Axions as Hot Relics

The QCD Axion

Axions via Gluons

Axion via Quarks

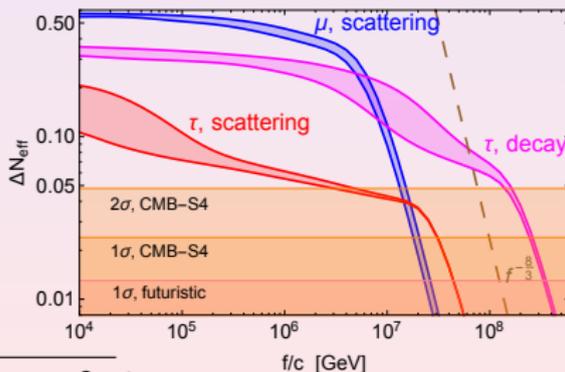
Axion via Leptons

The H_0 tension

- $a - \ell$ interaction can be **flavor non-diagonal**

$$\mathcal{L}_{a-\ell} = \partial_\mu a \sum_{\ell \neq \ell'} \bar{\ell}' \gamma^\mu (\mathcal{V}_{\ell'\ell} + \mathcal{A}_{\ell'\ell} \gamma^5) \ell + \text{h.c.},$$

- Decays $\tau \rightarrow \mu + a$, $\tau \rightarrow e + a$



$$(c_{\ell\ell'} \equiv \sqrt{\mathcal{V}_{\ell'\ell}^2 + \mathcal{A}_{\ell'\ell}^2})$$

- More efficient** than scatterings (**larger f/c**)

H_0 tension

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Planck CMB data (2015 and recent 2018)
- Measured H_0 in tension with direct local measurements from SN

H_0 tension

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Planck CMB data (2015 and recent 2018)
- Measured H_0 in tension with direct local measurements from SN
 - $H_0 = 67.27 \pm 0.60 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (CMB)
 - $H_0 = 73.52 \pm 1.62 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (SN)
- Tension at 3.6σ (3.46σ including BAO)

H_0 vs N_{eff}

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- It is known that $\Delta N_{eff} > 0$ correlates with a higher Hubble constant H_0 from CMB

H_0 vs N_{eff}

Axions as Hot
Relics

The QCD
Axion

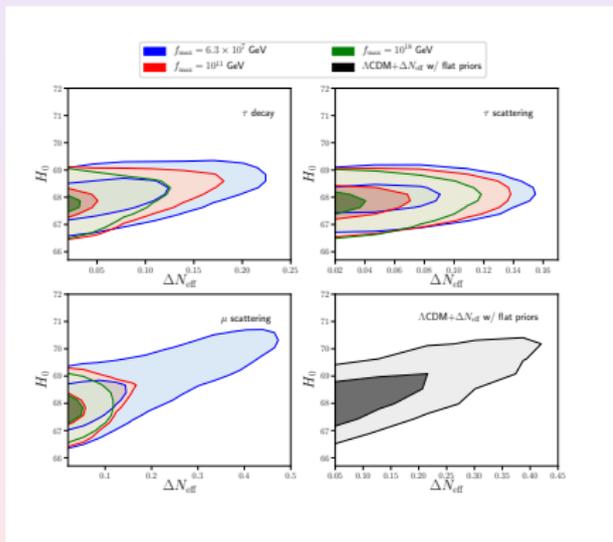
Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- It is known that $\Delta N_{\text{eff}} > 0$ correlates with a higher Hubble constant H_0 from CMB



H_0 vs N_{eff}

Axions as Hot
Relics

The QCD
Axion

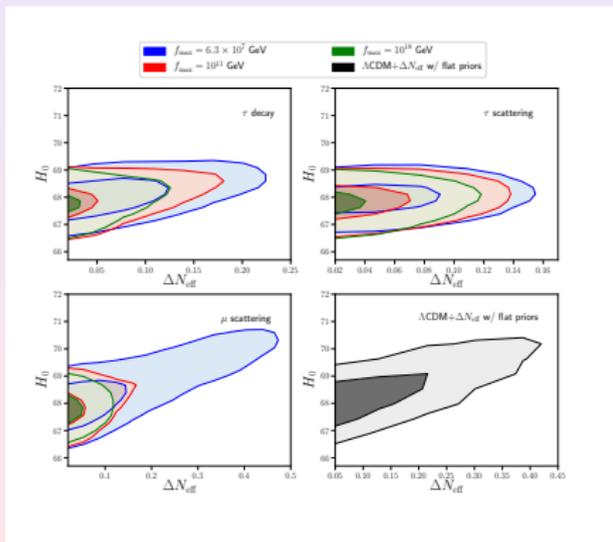
Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- It is known that $\Delta N_{\text{eff}} > 0$ correlates with a higher Hubble constant H_0 from CMB



- Flat prior on $\log(f/c_i) \implies$ some prior dependence
- μ production can significantly increase H_0

Hot axions and H_0 tension

Axions as Hot Relics

The QCD Axion

Axions via Gluons

Axion via Quarks

Axion via Leptons

The H_0 tension

- Tension remains, but can be **alleviated** to 3σ level

Model	Coupling	Prior $(f/c)_{\max}$ [GeV]	H_0 [km s $^{-1}$ Mpc $^{-1}$]	Tension (σ)
Λ CDM+ ΔN_{eff}	μ scattering	3×10^7	$68.0^{+0.8}_{-0.7} (+2.3_{-1.1})$	3.06 (2.75*)
		10^{11}	$67.8^{+0.6}_{-0.5} (+1.4_{-1.1})$	3.36
		10^{18}	$67.7^{+0.5}_{-0.4} (+1.2_{-1.0})$	3.38
	τ decay	6.3×10^7 GeV	$68.1^{+0.6}_{-0.5} (+1.2_{-1.0})$	3.18
		10^{11}	$67.8^{+0.6}_{-0.5} (+1.2_{-0.9})$	3.35
		10^{18}	$67.7^{+0.5}_{-0.4} (+1.1_{-0.9})$	3.39
	τ scattering	5×10^8	$68.0^{+0.5}_{-0.5} (+1.0_{-1.0})$	3.25
		10^{11}	$67.8^{+0.5}_{-0.5} (+1.1_{-1.0})$	3.33
		10^{18}	$67.7^{+0.5}_{-0.5} (+1.1_{-0.9})$	3.39
		Flat prior on N_{eff}	-	$68.3^{+0.8}_{-0.7} (+1.8_{-1.2})$
Λ CDM	No coupling	-	$67.7^{+0.5}_{-0.4} (+0.9_{-0.9})$	3.46

Conclusions

Axions as Hot
Relics

- If $f \lesssim \mathcal{O}(10^9)$ GeV, coupling with **quarks and leptons** (with $c_i = \mathcal{O}(1)$) dominates over $\frac{\alpha_s}{8\pi} \frac{a}{f} G\tilde{G}$

The QCD
Axion

Axion via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- Efficiency peaks at $T \approx m_f$

Conclusions

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If $f \lesssim \mathcal{O}(10^9)$ GeV, coupling with **quarks and leptons** (with $c_i = \mathcal{O}(1)$) dominates over $\frac{\alpha_s}{8\pi} \frac{a}{f} G\tilde{G}$
- Efficiency peaks at $T \approx m_f$
- For **quarks** (t, b, c) $\implies N_{\text{eff}} \lesssim 0.05 - 0.07$ (measurable at 2σ by CMB S4)
- For **leptons** (μ, τ) $\implies N_{\text{eff}} \lesssim 0.6 - 0.15$ (measurable by CMB S4)
- Non-diagonal couplings \implies production via **Decays** at slightly higher f/c_i

Conclusions

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If $f \lesssim \mathcal{O}(10^9)$ GeV, coupling with **quarks and leptons** (with $c_i = \mathcal{O}(1)$) dominates over $\frac{\alpha_s}{8\pi} \frac{a}{f} G\tilde{G}$
- Efficiency peaks at $T \approx m_f$
- For **quarks** (t, b, c) $\implies N_{\text{eff}} \lesssim 0.05 - 0.07$ (measurable at 2σ by CMB S4)
- For **leptons** (μ, τ) $\implies N_{\text{eff}} \lesssim 0.6 - 0.15$ (measurable by CMB S4)
- Non-diagonal couplings \implies production via **Decays** at slightly higher f/c_i
- μ production can **alleviate H_0 tension to 3σ level**

Conclusions

Axions as Hot
Relics

The QCD
Axion

Axions via
Gluons

Axion via
Quarks

Axion via
Leptons

The H_0
tension

- If $f \lesssim \mathcal{O}(10^9)$ GeV, coupling with **quarks and leptons** (with $c_i = \mathcal{O}(1)$) dominates over $\frac{\alpha_s}{8\pi} \frac{a}{f} G\tilde{G}$
- Efficiency peaks at $T \approx m_f$
- For **quarks** (t, b, c) $\implies N_{\text{eff}} \lesssim 0.05 - 0.07$ (measurable at 2σ by CMB S4)
- For **leptons** (μ, τ) $\implies N_{\text{eff}} \lesssim 0.6 - 0.15$ (measurable by CMB S4)
- Non-diagonal couplings \implies production via **Decays** at slightly higher f/c_i
- μ production can **alleviate H_0 tension to 3σ level**
- **Future CMB experiments** will tell in a few years about the **Axion** (and H_0)