



# SURFACE DEFECTS IN MASSIVE IIA

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# Introduction and Motivations

- Some branes (or their bound states) include closed string AdS vacua in their near-horizon.
- **AdS/CFT correspondence:** Dual description of AdS vacua at the horizon as RG fixed point of the worldvolume QFT of the brane. These fixed points are given by strongly-coupled SCFTs in the large  $N$  limit.  
[Maldacena. 1997.] [Witten. 1998.].
- Consistent truncations to  $d$ -dimensional gauged supergravities  $\longrightarrow$  RG flow across dimensions, conformal defects...  
[Boonstra, Skenderis, Townsend. 1998.] [Maldacena, Nunez. 2000.]  
[Karch, Randall. 2001.].

# Outline

- Conformal defects and holography.
- Gauged Supergravity Setup.
- Solutions with non-trivial p-form gauge potentials.
- Charged DW in  $d = 7$ :  $\text{AdS}_3$  slicing and brane picture in massive IIA.
- Defect  $\text{SCFT}_2$  within the  $\mathcal{N} = (1, 0)$   $\text{SCFT}_6$ .

# Holographic Defects

We want to describe the physics of some branes ending on a known brane intersection featured by an AdS vacuum at the horizon.

## Supergravity Picture of a Conformal Defect

Asymptotically  $\text{AdS}_d$  warped solutions  $\text{AdS}_{p+2} \times_w \mathcal{M}_{d-p-2}$  in a  $d$ -dimensional gauged supergravity are dual to defect  $\text{SCFT}_{p+1}$  within the  $\text{SCFT}_{d-1}$  dual to the  $\text{AdS}_d$  in the asymptotics. [Karch, Randall. 2001.].

$$ds_d^2 = e^{2U(r)} ds_{\text{AdS}_{p+2}}^2 + e^{2V(r)} dr^2 + e^{2W(r)} ds_{d-p-3}^2.$$

# Supergravity Setup

We consider massive IIA string theory and the following consistent truncations:

- **NS5-D6-D8** and  $\text{AdS}_7 \times_w \tilde{S}^3$  vacua  $\rightarrow$  minimal  $\mathcal{N} = 1$  gauged supergravity in  $d = 7$ :  $(g_{\mu\nu}, X, B_{(3)}, A^i)$ .  
[Townsend, van Nieuwenhuizen. 1983.] [Hanany, Zaffaroni. 1998] [Imamura, 2001]  
[Apruzzi, Fazzi, Rosa, Tomasiello. 2013.] [Gaiotto, Tomasiello. 2014.] [Passias, Rota, Tomasiello. 2015.]
- **D4-D8** and  $\text{AdS}_6 \times_w S^4$  vacua  $\rightarrow$  minimal  $\mathcal{N} = (1, 1)$   $F(4)$  gauged supergravity in  $d = 6$ :  $(g_{\mu\nu}, X, B_{(2)}, A^0, A^i)$ .  
[Romans. 1984.] [Seiberg. 1996.] [Brandhuber, Oz. 1999.] [Ferrara, Kehagias, Partuche, Zaffaroni. 1998.] [Cvetic, Lu, Pope. 1999.] [Jafferis, Pufu. 2012.]

# Bulk Geometry with p-Forms

- Backgrounds BPS/2 with AdS<sub>7</sub> asymptotics:

$$ds_7^2 = e^{2U(r)} ds_{\text{AdS}_3}^2 + e^{2V(r)} dr^2 + e^{2W(r)} ds_{\Sigma_3}^2,$$

$$B_{(3)} = k(r) \text{vol}_{\text{AdS}_3} + l(r) \text{vol}_{\Sigma_3},$$

$$X = X(r),$$

where  $\Sigma_3 = \{\mathbb{R}^3, S^3\}$ . [Dibitetto, N.P. 2017.]

- Backgrounds BPS/2 with AdS<sub>6</sub> asymptotics:

$$ds_6^2 = e^{2U(r)} ds_{\text{AdS}_3}^2 + e^{2V(r)} dr^2 + e^{2W(r)} ds_{\Sigma_2}^2,$$

$$B_{(2)} = b(r) \text{vol}_{\Sigma_2}$$

$$X = X(r)$$

where  $\Sigma_2 = \{\mathbb{R}^2, S^2\}$ . [Dibitetto, N.P. 2018.]

## An Example: Charged DW in $d = 7$

- The Killing spinor is very simple (8 supercharges):  $\epsilon(r) = Y(r) \epsilon_0$ .

$$ds_7^2 = e^{2U(r)} (ds_{\text{AdS}_3}^2 + ds_{S^3}^2) + e^{2V(r)} dr^2,$$

$$B_{(3)} = k(r) (\text{vol}_{\text{AdS}_3} + \text{vol}_{S^3}).$$

- BPS flow with  $r \in (0, 1)$ :

$$e^{2U} = \frac{2^{-1/4}}{\sqrt{g}} \left( \frac{r}{1 - r^5} \right)^{1/2}, \quad e^{2V} = \frac{25}{2g^2} \frac{r^6}{(1 - r^5)^2},$$

$$Y = \frac{2^{-1/16}}{g^{1/8}} \left( \frac{r}{1 - r^5} \right)^{1/8}, \quad k = -\frac{2^{1/4} R_{\text{AdS}_3}}{g^{3/2}} \left( \frac{r^5}{1 - r^5} \right)^{1/2},$$

$$X = r.$$

- UV regime: locally  $\text{AdS}_7$  with  $X = 1$  and  $\mathcal{F}_{(4)0123} = \mathcal{F}_{(4)3456} = 0$ .
- IR regime: Generic singularity. We want to give the physical interpretation of this singularity!

# AdS<sub>7</sub>/CFT<sub>6</sub> in Massive IIA

- Massive type IIA with AdS<sub>7</sub> ×<sub>w</sub>  $\tilde{S}^3$  vacuum →  $\mathcal{N} = 1$  minimal gauged supergravity in  $d = 7$ . [Apruzzi, Fazzi, Rosa, Tomasiello. 2013.] [Passias, Rota, Tomasiello. 2015.].
- Branes' intersection NS5-D6-D8. [Hanany, Zaffaroni. 1998.] [Imamura. 2001].
- AdS<sub>7</sub> ×<sub>w</sub>  $\tilde{S}^3$  "near-horizon" of NS5-D6-D8 with 16 supercharges. [Gaiotto, Tomasiello. 2014.] [Bobev, Dibiteto, Gautason, Truijen. 2016.].
- Non-lagrangian theory arising as the fixed point of the 6d worldvolume QFT. [Hanany, Zaffaroni. 1998.].
- Dual to  $\mathcal{N} = (1, 0)$  SCFT<sub>6</sub>. [Gaiotto, Tomasiello. 2014.].



# AdS<sub>3</sub> Slicing and its Massive IIA Interpretation

- In the UV the solution is dual to the  $\mathcal{N} = (1, 0)$  SCFT<sub>6</sub>: it describes the near-horizon of NS5-D6-D8.
- What happens in the IR? The singular behavior and the dyonic profile of  $\mathcal{F}_{(4)}$  in  $d = 7$  hints the presence of D2 and D4-branes filling the AdS<sub>3</sub> and intersecting the bound state NS5-D6-D8!

branes	$t$	$y$	$\rho$	$\varphi^1$	$\varphi^2$	$\varphi^3$	$z$	$r$	$\theta^1$	$\theta^2$
NS5	×	×	×	×	×	×	—	—	—	—
D6	×	×	×	×	×	×	×	—	—	—
D8	×	×	×	×	×	×	—	×	×	×
D2	×	×	—	—	—	—	×	—	—	—
D4	×	×	—	—	—	—	—	×	×	×

# The Brane Picture of D2-D4-NS5-D6-D8

- Imamura solution for NS5-D6-D8  $\rightarrow S(r, z), K(r, z)$ . [Imamura. 2001].
- "Non-standard" intersection with D2-D4.  
(see [Boonstra, Peeters, Skenderis. 1998.]).

$$ds_{10}^2 = S^{-1/2} H_{D2}^{-1/2} H_{D4}^{-1/2} ds_{\mathbb{R}^{1,1}}^2 + S^{-1/2} H_{D2}^{1/2} H_{D4}^{1/2} (d\rho^2 + \rho^2 ds_{S^3}^2) \\ + K S^{-1/2} H_{D2}^{-1/2} H_{D4}^{1/2} dz^2 + K S^{1/2} H_{D2}^{1/2} H_{D4}^{-1/2} (dr^2 + r^2 ds_{S^2}^2),$$

$$e^\Phi = g_s K^{1/2} S^{-3/4} H_{D2}^{1/4} H_{D4}^{-1/4},$$

$$H_3 = \frac{\partial}{\partial z} (KS) \text{vol}_3 - dz \wedge \star_3 dK, \quad F_0 = m, \quad F_2 = -g_s^{-1} \star_3 dS$$

$$F_{(4)} = g_s^{-1} \text{vol}_{\mathbb{R}^{1,1}} \wedge dz \wedge dH_{D2}^{-1} + \star_{10} (\text{vol}_{\mathbb{R}^{1,1}} \wedge \text{vol}_3 \wedge dH_{D4}^{-1}),$$

$$\text{where} \quad mg_s K - \frac{\partial S}{\partial z} = 0, \quad r^{-2} \partial_r (r^2 \partial_r S) + \frac{1}{2} \frac{\partial^2 S}{\partial z^2} S^2 = 0,$$

$$H_{D2}(\rho, r) = \left(1 + \frac{Q_{D4}}{\rho^2}\right) \left(1 + \frac{Q_{D6}}{r}\right), \quad H_{D4}(\rho) = \left(1 + \frac{Q_{D4}}{\rho^2}\right).$$

# The Near-Horizon

- Near-horizon:  $z, r \rightarrow \infty$  with  $\frac{r}{z^2}$  finite.
- Far from the defect  $\rho \rightarrow \infty$  (i.e.  $H_{D4} \rightarrow 1$  and  $H_{D2} \rightarrow H_{D6}$ ):

$$ds_{10}^2 \sim 2 \cos \alpha \left( \tan \alpha ds_{\text{AdS}_7}^2 + \tan \alpha d\alpha^2 + \frac{1}{4} \sin^2 \alpha ds_{S^2}^2 \right).$$

$$\implies \text{AdS}_7 \times_w \tilde{S}^3 \longleftrightarrow \mathcal{N} = (1, 0) \text{ SCFT}_6.$$

- Zooming on the defect  $\rho \rightarrow 0 \rightarrow$  warped  $\text{AdS}_3 \times I_\zeta \times S^3 \times I_\alpha \times S^2$  with 7d part:

$$ds_7^2 \sim \zeta^{-1/4} \underbrace{\left( \frac{\rho^2}{Q_{D4}} ds_{\mathbb{R}^{1,1}}^2 + \frac{Q_{D4}}{\rho^2} d\rho^2 \right)}_{ds_{\text{AdS}_3}^2} + \frac{d\zeta^2}{\zeta^2} + Q_{D4} \zeta^{-1/4} ds_{S^3}^2,$$

$$\implies \text{this is our 7d CDW!} \longleftrightarrow \text{defect } \mathcal{N} = (4, 0) \text{ SCFT}_2$$