

Introduction to SUSY and MSSM

CORFU SUMMER INSTITUTE

School and Workshop on Standard Model and Beyond

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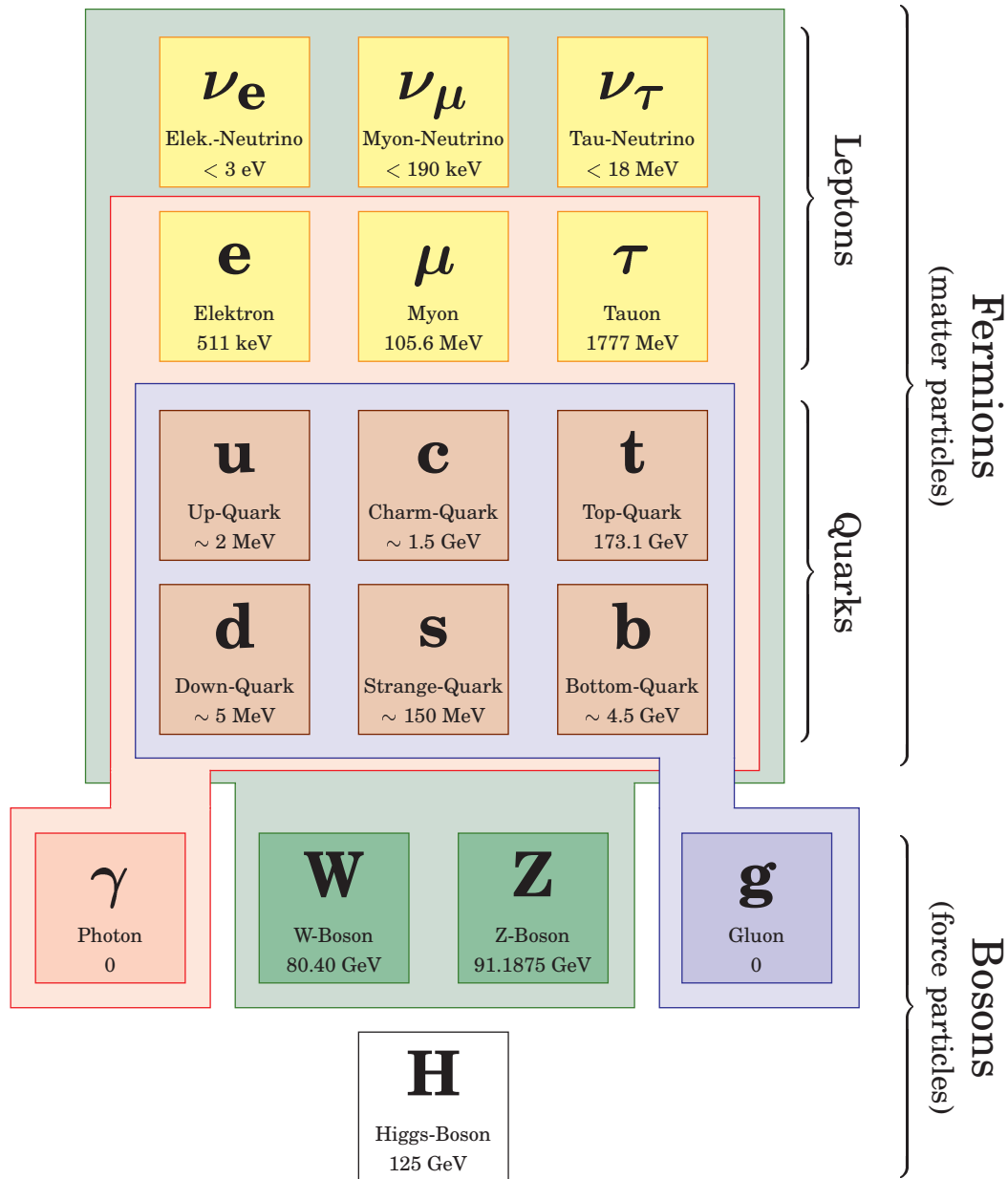
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Standard Model input is now completely determined



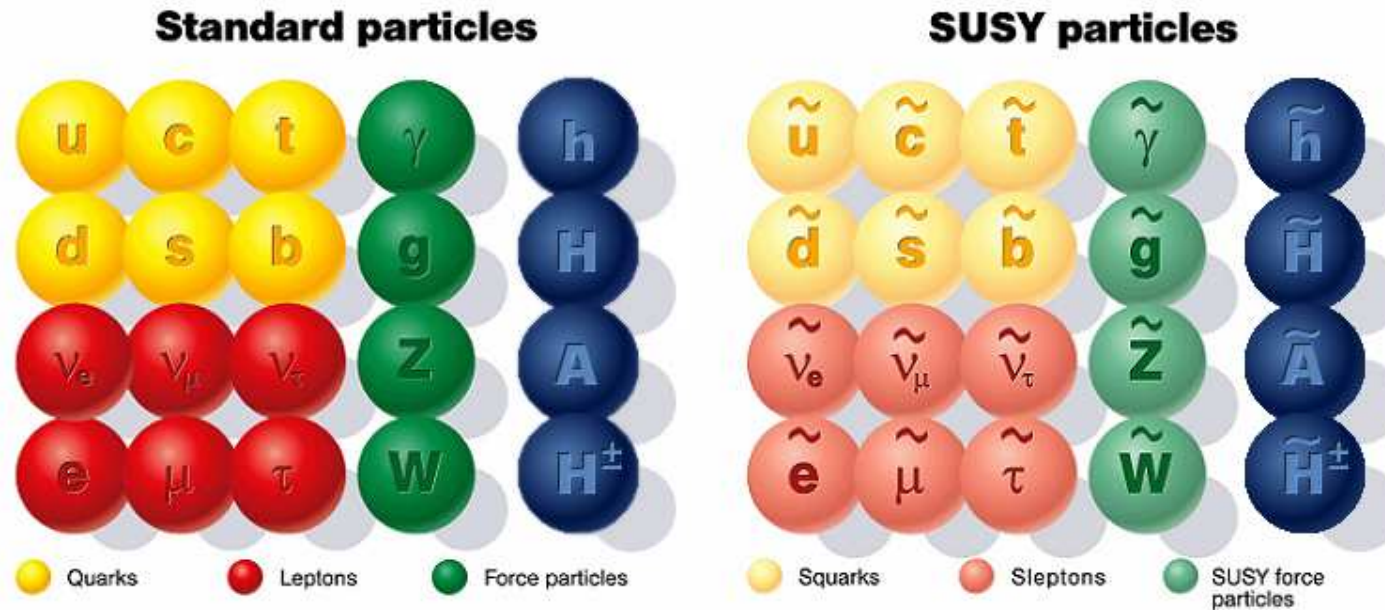
Why physics beyond the Standard Model?

many open issues

- hierarchy problem $v \ll M_{\text{Pl}}, \quad M_H \ll M_{\text{Pl}}$
- large number of free parameters $g_1, g_2, v, m_f, V_{\text{CKM}}$
- no further unification of forces
- missing link to gravity

- nature of dark matter?
- baryon asymmetry of the universe?

Supersymmetry



- gauge coupling unification
- dark matter candidate (lightest SUSY particle, LSP)
- physical Higgs bosons: h^0, H^0, A^0, H^\pm
lightest Higgs boson $h^0 < 130 \text{ GeV}$

Outline

1. SUSY algebra and representations
2. SUSY fields and Lagrangians
3. MSSM, formulation and content
4. Tests of the MSSM

1. SUSY algebra and representations

1.1. Space-time symmetry

Poincaré transformations

- translations a^μ , P^μ
 - rotations $\alpha \vec{n}$, \vec{J}
 - boosts $\phi \vec{n}$, \vec{K}
 - reflexions
- generators

Generators: $P^\mu, J^{\mu\nu}$

$$J^{12} = J^3, \quad J^{23} = J^1, \quad J^{31} = J^2$$

$$J^{0k} = K^k$$

Poincaré Algebra

$$[J^{\mu\nu}, J^{\sigma\rho}] = i(g^{\mu\sigma}J^{\nu\rho} - g^{\mu\rho}J^{\nu\sigma} + g^{\nu\sigma}J^{\mu\rho} - g^{\nu\rho}J^{\mu\sigma})$$

$$[P^\mu, J^{\nu\rho}] = i(g^{\mu\nu}P^\rho - g^{\mu\rho}P^\nu)$$

$$[P^\mu, P^\nu] = 0$$

invariant operators

(Casimir operators)

commute with $\mathfrak{E}^{\mu\nu}$, P^μ

$$(i) \quad P^2 = P_\mu P^\mu \quad \rightarrow \text{mass}$$

$$(ii) \quad W^2 = W_\mu W^\mu, \quad W^\mu = \frac{1}{2} \varepsilon^{\mu\nu\rho\sigma} \mathfrak{J}_{\nu\rho} P_\sigma$$

\rightarrow spin

Eigenspaces of Casimir operators
are the irreducible
representations of the
Lie algebra

[Schur's Lemma]

\rightarrow 1-particle spaces according
to m, s

Internal symmetries

e.g. gauge symmetries

additional symmetry group G

with Lie-Algebra

$$[T_a, T_b] = i f_{abc} T_c$$

commute with P.A.

$$[P^\mu, T_a] = [J^{\mu\nu}, T_a] = 0$$

direct product $P \times G$
of Poincare Group and
internal symmetry group G

only possibility to merge P
with other symmetries
containing $[,]$

[Coleman-Mandula Theorem]

can be circumvented if the
extra symmetry contains

$\{ \dots \}$ instead of $[\dots, \dots]$

anti-commutators

$$\{ F_1, F_2 \} = F_1 F_2 + F_2 F_1$$

→ graded Lie Algebra:

$$[B, B'] = B''$$

Lie - Algebra

lin. space L_0

$$[\ , \] \in L_0$$

$$\{ F, F' \} = B$$

$F \in L_1$

linear space

$$\{ \ , \ } \in L_0$$



$$[B, F] = F' \in L_1$$

1.2. Spinors

Generators of Lorentz Group

$$J^l, K^l \rightarrow$$

$$A^l = \frac{1}{2} (J^l + iK^l)$$

$$B^l = \frac{1}{2} (J^l - iK^l)$$

Lie Algebra:

$$[A^k, A^l] = i \varepsilon^{klm} A^m$$

$$[B^k, B^l] = i \varepsilon^{klm} B^m$$

$$[A^l, B^k] = 0$$

$$\boxed{SU(2) \times SU(2)}$$

irreducible representations:

$$(j_1, j_2), \quad j = 0, \frac{1}{2}, \dots$$

spinor representations

$$\underline{j_1 = \frac{1}{2}, j_2 = 0:} \quad \vec{A} = \frac{1}{2} \vec{\sigma}, \quad \vec{B} = 0$$

$$\vec{J} = \frac{1}{2} \vec{\sigma}, \quad \vec{K} = -\frac{i}{2} \vec{\sigma}$$

2x2-matrices,

act on 2-comp. spinor

$$\psi = \begin{pmatrix} \psi_1 \\ \psi_2 \end{pmatrix} \quad \text{Weyl spinor}$$

Lorentz transformation Λ :

$$\psi \xrightarrow{\Lambda} \psi' = D(\Lambda) \psi$$

$$D(\Lambda) = \begin{cases} e^{-\frac{i}{2} \alpha \vec{n} \cdot \vec{\sigma}} & \text{rotation} \\ e^{-\frac{1}{2} \phi \vec{n} \cdot \vec{\sigma}} & \text{boost} \end{cases}$$

$$\underline{j_1=0, j_2=\frac{1}{2}}: \quad \vec{A}=0, \quad \vec{B}=\frac{1}{2}\vec{\sigma}$$

$$\vec{J}=\frac{1}{2}\vec{\sigma}, \quad \vec{K}=\frac{i}{2}\vec{\sigma}$$

operate on 2-dim. space,

spinor $\bar{\chi} = \begin{pmatrix} \bar{\chi}^1 \\ \bar{\chi}^2 \end{pmatrix}$

components: $\bar{\chi}^a$ (often $\bar{\chi}^{\dot{a}}$)

Lorentz transf. Λ :

$$\bar{\chi} \xrightarrow{\Lambda} \bar{\chi}' = \bar{D}(\Lambda) \bar{\chi}$$

$$\bar{D}(\Lambda) = \begin{cases} e^{-\frac{i}{2} \alpha \vec{n} \cdot \vec{\sigma}} & \text{rotation} \\ e^{+\frac{1}{2} \phi \vec{n} \cdot \vec{\sigma}} & \text{boost} \end{cases}$$

D and \bar{D} are inequivalent:

$$\bar{D} = T D^* T^{-1}, \quad T = i\sigma^2$$

$$\bar{D}^\dagger = D^{-1}, \quad \psi \rightarrow \bar{\psi} = -i\sigma^2 \psi^*$$

Pauli matrices: $\vec{\sigma} = (\sigma^1, \sigma^2, \sigma^3)$

with $\sigma^0 := 1 \Rightarrow \sigma^\mu = (\sigma^0, \vec{\sigma})$

$$\bar{\sigma}^\mu = (\sigma^0, -\vec{\sigma})$$

4-vectors:

$$X^\mu = \bar{\chi}^\dagger \sigma^\mu \bar{\chi} = (\bar{\chi}^{\dagger 1}, \bar{\chi}^{\dagger 2}) \sigma^\mu \begin{pmatrix} \bar{\chi}^1 \\ \bar{\chi}^2 \end{pmatrix}$$

$$\bar{X}^\mu = \psi^\dagger \bar{\sigma}^\mu \psi = (\psi_1^\dagger, \psi_2^\dagger) \bar{\sigma}^\mu \begin{pmatrix} \psi_1 \\ \psi_2 \end{pmatrix}$$

Scalars:

$$\begin{aligned} \bar{\chi}^\dagger \psi &\xrightarrow{\wedge} (\bar{D}\bar{\chi})^\dagger (D\psi) \\ \psi^\dagger \bar{\chi} &= \bar{\chi}^\dagger \underbrace{\bar{D}^\dagger D}_{=1} \psi \end{aligned}$$

more spinor notations and conventions

definition: $\psi^1 = -\psi_2, \quad \psi^2 = \psi_1$

$$\bar{\psi}_1 = \bar{\psi}^2, \quad \bar{\psi}_2 = -\bar{\psi}^1$$

$$\Rightarrow \boxed{\bar{\psi}_a = \psi_a^*, \quad \bar{\psi}^a = \psi^{a*}}$$

\Rightarrow *compact notations for Lorentz covariants*

$$\bar{\chi}^+ \psi = \chi^a \psi_a \equiv \chi \psi$$

$$\psi^+ \bar{\chi} = \bar{\psi}_a \bar{\chi}^a \equiv \bar{\psi} \bar{\chi}$$

$$\bar{\psi}^+ \sigma^\mu \bar{\psi} = \psi \sigma^\mu \bar{\psi}$$

$$\psi^+ \bar{\sigma}^\mu \psi = \bar{\psi} \bar{\sigma}^\mu \psi$$

4-component spinors

$$\Psi = \begin{pmatrix} \psi \\ \bar{\chi} \end{pmatrix} \xrightarrow{\Lambda} \begin{pmatrix} D(\Lambda) & 0 \\ 0 & \bar{D}(\Lambda) \end{pmatrix} \begin{pmatrix} \psi \\ \bar{\chi} \end{pmatrix}$$

[Weyl representation]

$$\gamma^\mu = \begin{pmatrix} 0 & \sigma^\mu \\ \bar{\sigma}^\mu & 0 \end{pmatrix}, \quad \gamma_5 = \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$$

$\bar{\psi} \neq \bar{\chi}$: Dirac spinor

$\bar{\psi} = \bar{\chi}$: Majorana spinor

$$P_L = \frac{1}{2}(1 - \gamma_5) = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \quad \text{projects on } \psi$$

$$P_R = \frac{1}{2}(1 + \gamma_5) = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix} \quad \text{projects on } \bar{\chi}$$

$\begin{pmatrix} \psi \\ 0 \end{pmatrix}$: eigenstate of P_L , left-chiral

$\begin{pmatrix} 0 \\ \bar{\chi} \end{pmatrix}$: eigenstate of P_R , right-chiral

1.3. Poincaré Algebra \rightarrow SUSY P.A.

introduce additional
spinor charges Q, \bar{Q}

$$Q = \begin{pmatrix} Q_1 \\ Q_2 \end{pmatrix}, \quad \bar{Q} = \begin{pmatrix} \bar{Q}^1 \\ \bar{Q}^2 \end{pmatrix}$$

transform like Weyl spinors $\psi, \bar{\psi}$
under Lorentz transform.

$$Q \leftrightarrow D(\Lambda), \quad \bar{Q} \leftrightarrow \bar{D}(\Lambda)$$

$$\bar{Q} = -i\sigma^2 Q^\dagger$$

$$\begin{pmatrix} \bar{Q}^1 \\ \bar{Q}^2 \end{pmatrix} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} Q_1^\dagger \\ Q_2^\dagger \end{pmatrix}$$

$$\bar{Q}_a = Q_a^\dagger \quad (a=1,2)$$

[generalization: $Q^L, L=1..N$]

SUSY Poincaré Algebra

Poincaré Algebra (N=1)

$$[Q, \mathcal{F}^{\mu\nu}] = \sigma^{\mu\nu} Q$$

$$[\bar{Q}, \mathcal{F}^{\mu\nu}] = \bar{\sigma}^{\mu\nu} \bar{Q}$$

$$[Q, P^\mu] = [\bar{Q}, P^\mu] = 0$$

$$\{Q_a, Q_b\} = \{\bar{Q}_a, \bar{Q}_b\} = 0$$

$$\{Q_a, \bar{Q}_b\} = 2(\sigma^\mu)_{ab} P_\mu$$

$$\sigma^{\mu\nu} = \frac{i}{4} (\sigma^\mu \bar{\sigma}^\nu - \sigma^\nu \bar{\sigma}^\mu)$$

$$\bar{\sigma}^{\mu\nu} = \frac{i}{4} (\bar{\sigma}^\mu \sigma^\nu - \bar{\sigma}^\nu \sigma^\mu)$$

1.4. Irreducible representations

Casimir operators \rightarrow

eigenspaces = irreducible reps.

- $P^2 = P_\mu P^\mu$ invariant under SUSY-P.A.

\Rightarrow mass m defines irr. rep.

- $W^2 = W_\mu W^\mu$ no Casimir operator of SUSY-P.A.

$$W^\mu = \frac{1}{2} \varepsilon^{\mu\nu\rho\sigma} F_{\nu\rho} P_\sigma$$

- instead: $Y^\mu = W^\mu - \frac{1}{4} X^\mu$

$$\begin{aligned} X^\mu &= Q^a \sigma_{ab}^\mu \bar{Q}^b \equiv Q \sigma^\mu \bar{Q} \\ &= P^\mu - \bar{Q} \sigma^\mu Q \end{aligned}$$

Commutator:

$$[Y^\mu, Y^\nu] = i \varepsilon^{\mu\nu\rho\sigma} P_\rho Y_\sigma$$

rest system: $P_0 = m$, $\vec{P} = 0$

$$[Y^k, Y^l] = i m \varepsilon^{klj} Y^j$$

\vec{Y}^2 has eigenvalues

$$m^2 y(y+1), \quad y = 0, \frac{1}{2}, 1, \dots$$

Casimir operator: $C^2 = C_{\mu\nu} C^{\mu\nu}$

$$C^{\mu\nu} = Y^\mu P^\nu - Y^\nu P^\mu$$

$$\text{check: } [C^{\mu\nu}, P^\rho] = 0$$

$$[C^{\mu\nu}, Q] = 0$$

$$[C^2, \exists^{\mu\nu}] = 0$$

C^2 invariant \rightarrow rest frame

$$C^2 = 2m^2 Y^2 - 2(Y_\mu P^\mu)$$

$$\begin{aligned} &\rightarrow 2m^2 Y^2 - 2m^2(Y_0)^2 \\ &= 2m^2(Y^2 - Y_0^2) = 2m^2(-\vec{Y}^2) \end{aligned}$$

eigenvalues: $-2m^4 \cdot y(y+1)$

$$[y = 0, \frac{1}{2}, 1, \dots]$$

irreducible representations
are classified by m, y

states: $|m, y; \vec{p}, y_3, \dots\rangle$

Spin?

action of Q, \bar{Q} ?

continue in rest frame, $P^M = (m, \vec{0})$

$$\{Q_a, \bar{Q}_b\} = 2(\sigma^0)_{ab} m = 2m \delta_{ab}$$

define $f_a^- = \frac{1}{\sqrt{2m}} Q_a \quad (a=1,2)$

$$f_a^+ = \frac{1}{\sqrt{2m}} \bar{Q}_a$$

$$\{f_a^-, f_b^+\} = \delta_{ab}$$

$$\{f_a^-, f_b^-\} = \{f_a^+, f_b^+\} = 0$$

anti-commutators for creation (f_a^+)
and annihilation (f_a^-) operators
of fermions

- vacuum (0-fermion state) $|\Omega\rangle$

$$f_a^- |\Omega\rangle = 0$$

- $f_a^+ |\Omega\rangle$ are 1-fermion states

- $f_1^+ f_2^+ |\Omega\rangle$ 2-fermion state

4 linearly independent states:

$$|\Omega\rangle, f_a^+ |\Omega\rangle, f_1^+ f_2^+ |\Omega\rangle$$

for the same value γ_3

$$[\text{based on } [Q, Y^3] = [\bar{Q}, Y] = 0]$$

$$Y^3 |\Omega\rangle = \gamma_3 |\Omega\rangle$$

$$Y^3 f_a^+ |\Omega\rangle = f_a^+ Y^3 |\Omega\rangle = \gamma_3 f_a^+ |\Omega\rangle$$

$$\begin{aligned} Y^3 f_1^+ f_2^+ |\Omega\rangle &= f_1^+ f_2^+ Y^3 |\Omega\rangle \\ &= \gamma_3 f_1^+ f_2^+ |\Omega\rangle \end{aligned}$$

\Rightarrow each γ_3 occurs as
4-fold degenerate

$$\begin{aligned} & \text{dimension of irred. rep.} \\ & = 4 \cdot (2\gamma + 1) \end{aligned}$$

Values of S^3 :

rest frame: $W^3 = m S^3$

$$X^k = -\bar{Q} \sigma^k Q \Rightarrow X^k |\Omega\rangle = 0$$

1) state $|\Omega\rangle$:

$$Y^3 |\Omega\rangle = m \gamma_3 |\Omega\rangle$$

$$= \left(W^3 - \frac{1}{4} X^3 \right) |\Omega\rangle = m S^3 |\Omega\rangle$$

$$\boxed{S_3 = \gamma_3}$$

2) states $f_a^+ |\Omega\rangle$:

$$W^3 f_1^+ |\Omega\rangle = m \left(y_3 + \frac{1}{2} \right) f_1^+ |\Omega\rangle$$

$$W^3 f_2^+ |\Omega\rangle = m \left(y_3 - \frac{1}{2} \right) f_2^+ |\Omega\rangle$$

$$S_3 = y_3 \pm \frac{1}{2}$$

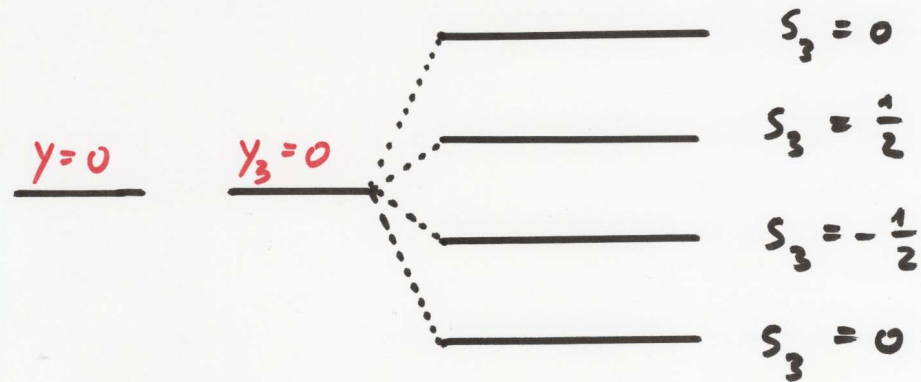
3) state $f_1^+ f_2^+ |\Omega\rangle$:

$$W^3 |.. \rangle = m y_3 |.. \rangle$$

$$S_3 = y_3$$

\Rightarrow different spins in
an irred. rep.

$\gamma=0$ chiral multiplet

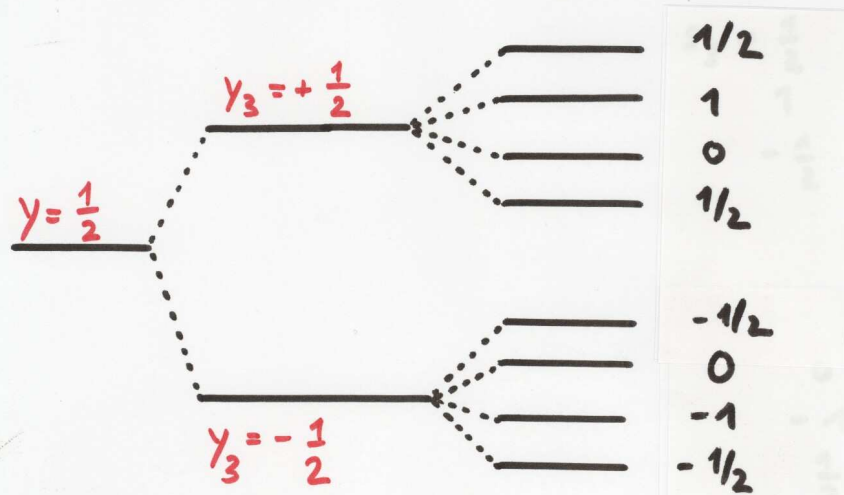


2 bosons with spin 0

1 fermion with spin $\frac{1}{2}$

$$y = \frac{1}{2}$$

vector multiplet



2 fermions with spin $\frac{1}{2}$

1 boson with spin 1

1 boson with spin 0

Appendix to Section1

Useful formulae for spinors

Weyl-spinors with components ψ_a ($a = 1, 2$)

$$\psi = \begin{pmatrix} \psi_1 \\ \psi_2 \end{pmatrix}$$

form a 2-dimensional representation of the Lorentz Group. They transform under Lorentz transformations Λ according to

$$\Lambda : \quad \psi \rightarrow D(\Lambda) \psi$$

with the matrix

$$D(\Lambda) = \begin{cases} e^{-\frac{i}{2}\alpha \vec{n}\vec{\sigma}} & \text{rotation} \\ e^{-\frac{1}{2}\phi \vec{n}\vec{\sigma}} & \text{boost.} \end{cases}$$

$\vec{\sigma} = (\sigma^1, \sigma^2, \sigma^3)$ denote the Pauli matrices.

Weyl-spinors with components $\bar{\chi}^a$ ($a = 1, 2$)

$$\bar{\chi} = \begin{pmatrix} \bar{\chi}^1 \\ \bar{\chi}^2 \end{pmatrix}$$

belong to another, not equivalent, 2-dimensional representation of the Lorentz Group. Under the same Lorentz transformation Λ as above they transform according to

$$\Lambda : \quad \bar{\chi} \rightarrow \bar{D}(\Lambda) \bar{\chi}$$

with the matrix

$$D(\Lambda) = \begin{cases} e^{-\frac{i}{2}\alpha \vec{n}\vec{\sigma}} & \text{rotation} \\ e^{+\frac{1}{2}\phi \vec{n}\vec{\sigma}} & \text{boost.} \end{cases}$$

The representation matrices are connected via

$$\bar{D} = T D^* T^{-1}, \quad T = i\sigma^2$$

and fulfill the relation

$$D^{-1} = \bar{D}^+.$$

For each ψ transforming with D , a $\bar{\psi}$ can be found transforming with \bar{D} , namely

$$\bar{\psi} = -i \sigma^2 \psi^*,$$

or explicitly,

$$\begin{pmatrix} \bar{\psi}^1 \\ \bar{\psi}^2 \end{pmatrix} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} \psi_1^* \\ \psi_2^* \end{pmatrix}$$

The Pauli matrices, together with

$$\sigma^0 := \mathbf{1} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

can be summarized in terms of a 4-component quantity,

$$\sigma^\mu = (\sigma^0, \vec{\sigma}).$$

In addition, one defines

$$\bar{\sigma}^\mu = (\sigma^0, -\vec{\sigma}).$$

Lorentz covariants:

scalars:

$$\begin{aligned} \bar{\chi}^+ \psi & \quad \text{mit} \quad \bar{\chi}^+ = (\bar{\chi}^{1*}, \bar{\chi}^{2*}) \\ \psi^+ \bar{\chi} & \quad \text{mit} \quad \psi^+ = (\psi_1^*, \psi_2^*). \end{aligned}$$

4-vectors:

$$\begin{aligned} X^\mu &= \bar{\chi}^+ \sigma^\mu \bar{\chi}, \\ \bar{X}^\mu &= \psi^+ \bar{\sigma}^\mu \psi. \end{aligned}$$

Spinor notations:

In addition to the components $\psi_a, \bar{\psi}^a$ one defines:

$$\begin{aligned} \psi^1 &= -\psi_2 & \psi^2 &= \psi_1 \\ \bar{\psi}_1 &= \bar{\psi}^2 & \bar{\psi}_2 &= -\bar{\psi}^1. \end{aligned}$$

This yields

$$\bar{\psi}_a = \psi_a^*, \quad \bar{\psi}^a = \psi^{a*}$$

and a compact notations for the Lorentz covariants:

$$\begin{aligned} \bar{\chi}^+ \psi &= \chi^1 \psi_1 + \chi^2 \psi_2 \equiv \chi^a \psi_a \equiv \chi \psi \\ \psi^+ \bar{\chi} &= \bar{\psi}_1 \bar{\chi}^1 + \bar{\psi}_2 \bar{\chi}^2 \equiv \bar{\psi}_a \bar{\chi}^a \equiv \bar{\psi} \bar{\chi} \\ \bar{\psi}^+ \sigma^\mu \bar{\psi} &= \psi^a (\sigma^\mu)_{ab} \bar{\psi}^b \equiv \psi \sigma^\mu \bar{\psi} \\ \psi^+ \bar{\sigma}^\mu \psi &= \bar{\psi}_a (\bar{\sigma}^\mu)^{ab} \psi_b \equiv \bar{\psi} \bar{\sigma}^\mu \psi \end{aligned}$$

The spinor products, expressed in terms of the original components, read

$$\begin{aligned} \chi \psi &= \chi_1 \psi_2 - \chi_2 \psi_1 \\ \bar{\psi} \bar{\chi} &= \bar{\psi}^2 \bar{\chi}^1 - \bar{\psi}^1 \bar{\chi}^2. \end{aligned}$$

4-component spinors:

A Dirac spinor is composed of 2 Weyl spinors according to (Weyl representation)

$$\Psi = \begin{pmatrix} \psi \\ \bar{\chi} \end{pmatrix}$$

Under a Lorentz transformation Λ , it transforms as follows,

$$\Lambda : \quad \Psi \rightarrow \begin{pmatrix} D(\Lambda) & \mathbf{0} \\ \mathbf{0} & \bar{D}(\Lambda) \end{pmatrix} \Psi$$

Dirac-Matrices in Weyl representation:

$$\gamma^\mu = \begin{pmatrix} \mathbf{0} & \sigma^\mu \\ \bar{\sigma}^\mu & \mathbf{0} \end{pmatrix}, \quad \gamma_5 = i\gamma^0\gamma^1\gamma^2\gamma^3 = \begin{pmatrix} -\mathbf{1} & \mathbf{0} \\ \mathbf{0} & \mathbf{1} \end{pmatrix}$$

Chirale projektors:

$$\mathbf{P}_L = \frac{1 - \gamma_5}{2} = \begin{pmatrix} \mathbf{1} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{pmatrix}$$
$$\mathbf{P}_R = \frac{1 + \gamma_5}{2} = \begin{pmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{1} \end{pmatrix}$$

The spinors

$$\begin{pmatrix} \psi \\ 0 \end{pmatrix}, \quad \begin{pmatrix} 0 \\ \bar{\chi} \end{pmatrix}$$

are eigenspinors of \mathbf{P}_L (left-chiral) and \mathbf{P}_R (right-chiral). The representations D and \bar{D} are thus left- and right-chiral representations

A Majorana spinor is a 4-component spinor with $\bar{\chi} = \bar{\psi}$:

$$\Psi_M = \begin{pmatrix} \psi \\ \bar{\psi} \end{pmatrix}$$

It obeys

$$\bar{\Psi}_M = \mathbf{C} \bar{\Psi}_M^T$$

with

$$\bar{\Psi} = \Psi^\dagger \gamma^0, \quad \mathbf{C} = \begin{pmatrix} i\sigma^2 & \mathbf{0} \\ \mathbf{0} & -i\sigma^2 \end{pmatrix}$$

2. SUSY fields and Lagrangians

2.1. Superspace

representation of Poincaré' transf.

$$e^{-i\omega_{\mu\nu} J^{\mu\nu} - ia_{\mu} P^{\mu}}$$

translation:

$$\phi(x) \rightarrow \phi(x+a) = \phi(x) + a^{\mu} \frac{\partial \phi}{\partial x^{\mu}} + \dots$$

$$= (1 - ia^{\mu} P_{\mu}) \phi(x)$$

$$P_{\mu} = i \frac{\partial}{\partial x^{\mu}} \equiv i \partial_{\mu}$$

Lie Algebra \longrightarrow Group

$$[T_k, T_l] = \dots$$

$$e^{ia_k T_k}$$

$$e^A e^B =$$

$$\sum [\dots [T_k, T_l] \dots]$$

SUSY algebra contains $\{\dots, \dots\}$
→ group? group elements?

strategy: multiply Q, \bar{Q} by
anti-commuting variables

$$\{, \} \rightarrow [,]$$

New spinorial variables

$$\epsilon = \begin{pmatrix} \epsilon_1 \\ \epsilon_2 \end{pmatrix}, \quad \bar{\epsilon} = \begin{pmatrix} \bar{\epsilon}^1 \\ \bar{\epsilon}^2 \end{pmatrix}, \quad \theta = \begin{pmatrix} \theta_1 \\ \theta_2 \end{pmatrix} \dots$$

$$\text{with } \{\epsilon_a, \epsilon_b\} = \{\bar{\epsilon}_a, \bar{\epsilon}_b\} = 0$$

Grassmann variables

$$\text{and } [\epsilon, P_\mu] = [\bar{\epsilon}, P_\mu] = 0$$

$$\{Q_a, \epsilon_b\} = \{\bar{Q}_a, \bar{\epsilon}_b\} = \dots = 0$$

$$\text{then: } \{Q, \bar{Q}\} \rightarrow [\epsilon Q, \bar{\epsilon} \bar{Q}]$$

group element:

$$e^{-i\xi^\mu P_\mu + i\epsilon Q + i\bar{\epsilon}\bar{Q}} \equiv g(\xi, \epsilon, \bar{\epsilon})$$

operates on a space with
"coordinates" $\{x^\mu, \theta, \bar{\theta}\}$

Superspace

• group multiplication:

$$g(0, \epsilon, \bar{\epsilon}) g(x^\mu, \theta, \bar{\theta}) = g(x^\mu + a^\mu, \theta + \epsilon, \bar{\theta} + \bar{\epsilon})$$

$$\text{with } a^\mu = i(\theta\sigma^\mu\bar{\epsilon} - \epsilon\sigma^\mu\bar{\theta})$$

\equiv shift in parameter space

function in superspace:

$$F(x^r, \theta, \bar{\theta})$$

differentiation:

$$\frac{\partial}{\partial x^r} = \partial_r, \quad \frac{\partial}{\partial \theta^a} = \partial_a, \quad \frac{\partial}{\partial \bar{\theta}^a} = \bar{\partial}_a$$

basic rules:

$$\frac{\partial}{\partial \theta^a} \theta^b = \delta_a^b, \quad \frac{\partial}{\partial \bar{\theta}^a} \bar{\theta}^b = \delta_a^b$$

$$\frac{\partial}{\partial \theta^a} \bar{\theta}^b = 0, \quad \frac{\partial}{\partial \bar{\theta}^a} \theta^b = 0$$

note: $F(x, \theta, \bar{\theta})$ is a
polynomial in $\theta, \bar{\theta}$:

$$\begin{aligned} &\theta, \bar{\theta}, \theta\theta, \bar{\theta}\bar{\theta}, (\theta\bar{\theta})\bar{\theta} \\ &\quad (\theta\bar{\theta})\theta, \\ &\quad (\theta\theta)(\bar{\theta}\bar{\theta}) \end{aligned}$$

pure SUSY transformation:

$$g(0, \epsilon, \bar{\epsilon}) = e^{i(\epsilon Q + \bar{\epsilon} \bar{Q})}$$

generates translations

$$F(x, \theta, \bar{\theta}) \rightarrow g(0, \epsilon, \bar{\epsilon}) F(x, \theta, \bar{\theta})$$

$$= F(x+a, \theta+\epsilon, \bar{\theta}+\bar{\epsilon})$$

$$a^\mu = i(\theta \sigma^\mu \bar{\epsilon} - \epsilon \sigma^\mu \bar{\theta})$$

infinitesimal parameters:

$$F(x+a, \theta+\epsilon, \bar{\theta}+\bar{\epsilon})$$

$$= a^\mu \frac{\partial F}{\partial x^\mu} + \epsilon^a \frac{\partial F}{\partial \theta^a} + \bar{\epsilon}^a \frac{\partial F}{\partial \bar{\theta}^a}$$

$$= (1 + i\epsilon^a Q_a + i\bar{\epsilon}^a \bar{Q}^a) F$$

$\Rightarrow Q_a, \bar{Q}_a$ as diff-operators

$$iQ_a = \frac{\partial}{\partial \theta^a} - i \sigma_{ab}^\mu \bar{\theta}^b \partial_\mu$$

$$i\bar{Q}_a = -\frac{\partial}{\partial \bar{\theta}^a} + i \theta^b \sigma_{ba}^\mu \partial_\mu$$

define *covariant derivative*

$$D_a = \frac{\partial}{\partial \theta^a} + i \sigma_{ab}^\mu \bar{\theta}^b \partial_\mu$$

$$\bar{D}_a = -\frac{\partial}{\partial \bar{\theta}^a} - i \theta^b \sigma_{ba}^\mu \partial_\mu$$

- D_a, \bar{D}_a invariant under susy

$$[\epsilon Q + \bar{\epsilon} \bar{Q}, D_a] = 0$$

$$[\epsilon Q + \bar{\epsilon} \bar{Q}, \bar{D}_a] = 0$$

2.2. Superfields

superfield = Lorentz scalar
on superspace

$\Phi(x, \theta, \bar{\theta})$ polynomial in
 $\theta, \bar{\theta}$

general form:

$$\begin{aligned}\Phi = & \varphi(x) + \theta^a \psi_a(x) + \bar{\theta}_a \bar{\chi}^a(x) \\ & + (\theta\theta) F(x) + (\bar{\theta}\bar{\theta}) H(x) \\ & + (\theta\sigma^\mu\bar{\theta}) A_\mu(x) \\ & + (\theta\theta) \bar{\theta}_a \bar{\lambda}^a(x) + (\bar{\theta}\bar{\theta}) \theta^a \xi_a(x) \\ & + (\theta\theta) (\bar{\theta}\bar{\theta}) D(x)\end{aligned}$$

φ, F, H, D : scalars
 A_μ : vector
 $\psi, \bar{\chi}, \bar{\lambda}, \xi$: spinors

} components
of Φ

general Φ is reducible

Irreducible superfields by
suitable conditions (have to
be invariant under susy transf.)

Conditions:

$\bar{D}_a \Phi = 0$: (left-)chiral SF

$D_a \bar{\Phi}^\dagger = 0$: (right-)chiral SF

$\Phi = \bar{\Phi}^\dagger$: vector SF

$$\boxed{\bar{D}_a \Phi = 0}$$

left-chiral SF

$$\Phi \Big|_{\bar{D}_a \Phi = 0} = \phi(z, \theta)$$

$$= \varphi(z) + \sqrt{2} \theta \psi(z) + \theta\theta F(z)$$

with $z^\mu = x^\mu + i \theta \sigma^\mu \bar{\theta}$

φ, F : scalars

ψ : Weyl spinor (left)

inf. SUSY transf. $1 + i\epsilon Q + i\bar{\epsilon} \bar{Q}$
 \Rightarrow transformation of components

$$\delta\varphi = \sqrt{2} \epsilon \psi$$

$$\delta\psi = i\sqrt{2} \sigma^\mu \bar{\epsilon} \partial_\mu \varphi + \sqrt{2} \epsilon F$$

$$\delta F = i\sqrt{2} \underbrace{\partial_\mu (\bar{\epsilon} \bar{\sigma}^\mu \psi)}$$

4-divergence

$$\boxed{D_a \Phi^+ = 0}$$

right-chiral SF

$$\Phi \Big|_{D_a \Phi^+ = 0} = \Phi^+(\bar{z}^\mu, \bar{\theta})$$

$$= \varphi^*(\bar{z}) + \sqrt{2} \bar{\theta} \bar{\psi}(\bar{z}) + \bar{\theta} \bar{\theta} F^*(\bar{z})$$

$$\text{with } \bar{z} = x^\mu - i \theta \sigma^\mu \bar{\theta}$$

$\bar{\psi}$: Weyl spinor (right-chiral)

$$V = V^\dagger$$

vector SF

$$\Phi = V(x^\mu, \theta, \bar{\theta}), \quad V = V^\dagger$$

has full expansion in $\theta, \bar{\theta}$
with constraints on components

φ, D : real scalar fields

$F = H^*$: scalar field

A_μ : vector field

$\psi = \chi, \xi = \lambda$: Weyl spinors

number of components can be
reduced by

susy gauge transformations

SUSY gauge transformation

$$V \rightarrow V' = V + (\phi + \phi^\dagger)$$

$$\phi = a + \sqrt{2} \theta \xi + \theta \theta G$$

chiral SF

$$V = V^\dagger \rightarrow V' = (V')^\dagger$$

components of V' :

$$\varphi' = \varphi + 2 \operatorname{Re} a$$

$$\psi' = \psi + \sqrt{2} \xi$$

$$F' = F + G$$

$$A'_\mu = A_\mu - \partial_\mu (2 \operatorname{Im} a)$$

$$\lambda' = \lambda + \frac{i}{\sqrt{2}} \sigma^\mu \partial_\mu \bar{\xi}$$

$$D' = D - \frac{1}{2} \square (2 \operatorname{Re} a)$$

eliminate $\varphi', \psi', F' \leftrightarrow \operatorname{Re} a, \xi, G$

in the gauge without the
 φ, ψ, F components

$$\begin{aligned} V' = & (\theta \sigma^\mu \bar{\theta}) A'_\mu(x) \\ & + (\theta \theta) \bar{\theta} \bar{\lambda}'(x) \\ & + (\bar{\theta} \bar{\theta}) \theta \lambda'(x) \\ & + (\theta \theta) (\bar{\theta} \bar{\theta}) D'(x) \end{aligned}$$

Wess-Zumino gauge

in the following to be used

(drop')

SUSY-transf. $\delta_\epsilon V$, $\delta_\epsilon = i\epsilon Q + i\bar{\epsilon} \bar{Q}$

$$\Rightarrow \delta A_\mu = \dots, \quad \delta \lambda = \dots,$$

$$\delta D = \frac{i}{2} \partial_\mu (\epsilon \sigma^\mu \bar{\lambda} - \lambda \sigma^\mu \bar{\epsilon})$$

SUSY field strength

use covariant derivative $\mathcal{D}, \bar{\mathcal{D}}$

$$W_a := -\frac{1}{4} (\bar{\mathcal{D}} \bar{\mathcal{D}}) \mathcal{D}_a V(x, \theta, \bar{\theta})$$

- $\bar{\mathcal{D}}_a W_a = 0$
- invariant under SUSY-transf.
- components:

$$W_a = i \lambda_a(x) - 2 \theta_a \mathcal{D}(x)$$

$$- (\sigma^{\mu\nu} \theta)_a F_{\mu\nu}(x)$$

$$- (\theta \theta) (\sigma^\mu \partial_\mu \bar{\lambda})_a$$

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

2.3. SUSY Lagrangians

Lagrangian \mathcal{L} : scalar, hermitean

action: $S = \int d^4x \mathcal{L}$

SUSY: \mathcal{L} resp. S
invariant under
SUSY-transf.

$$\mathcal{L} \xrightarrow{\text{SUSY}} \mathcal{L} + \underbrace{\partial_\mu K^\mu}_{\rightarrow 0 \text{ in } S}$$

products of $SF = SF$
highest component in $\theta, \bar{\theta}$
 $\xrightarrow{\text{SUSY}} + \partial_\mu (\dots)$

under $\delta_\epsilon = i(\epsilon Q + \bar{\epsilon} \bar{Q})$:

$$(\theta\theta) F \rightarrow \delta F = \partial_\mu (\dots)$$

$$(\theta\theta)(\bar{\theta}\bar{\theta}) D \rightarrow \delta D = \partial_\mu (\dots)$$

examples:

$$\phi = \varphi + \sqrt{2} \theta \psi + (\theta\theta) F$$

$$\phi^2 = \varphi^2 + 2\sqrt{2} \varphi \theta \psi + (\theta\theta) \underline{\underline{(2F\varphi - \psi\psi)}}$$

$$\phi^3 = \varphi^3 + \dots + (\theta\theta) \cdot \underline{\underline{3(\varphi^2 F - \varphi\psi\psi)}}$$

$$\phi^\dagger \phi = \dots + (\theta\theta)(\bar{\theta}\bar{\theta}) \cdot [\dots]$$

$$[\dots] = (\partial_\mu \varphi)^* (\partial^\mu \varphi)$$

$$-\frac{i}{2} (\bar{\psi} \bar{\sigma}^\mu \partial_\mu \psi + \psi \sigma^\mu \partial_\mu \bar{\psi})$$

$$+ F^* F$$

Lagrangian:

$$\mathcal{L} = \underbrace{\phi^\dagger \phi}_{\text{kinetic}} - \underbrace{\frac{m}{2} \phi^2}_{\text{mass}} - \underbrace{\frac{g}{3} \phi^3}_{\text{interaction}}$$

$$\begin{aligned} &= |\partial_\mu \psi|^2 - \frac{i}{2} (\bar{\psi} \gamma^\mu \partial_\mu \psi + \psi \gamma^\mu \partial_\mu \bar{\psi}) + F^* F \\ &+ \frac{m}{2} (\psi \psi + \bar{\psi} \bar{\psi}) - m (\psi F + \psi^* F^*) \\ &+ g (\psi \psi \psi + \psi^* \bar{\psi} \bar{\psi} - \psi^2 F - \psi^{*2} F^*) \end{aligned}$$

F : no dynamical field ("auxiliary field")

eq. of motion for F :

$$\frac{\partial \mathcal{L}}{\partial F^*} = 0 : \quad F - m \psi^* - g \psi^{*2} = 0$$

$$F = m \psi^* + g \psi^{*2}$$

insert in $\mathcal{L} \rightarrow$

$$\mathcal{L} = |\partial_\mu \varphi|^2 - m^2 \varphi^* \varphi$$

$$- \frac{i}{2} (\bar{\psi} \overline{\sigma}_\mu \partial_\mu \psi + \psi \sigma_\mu \partial_\mu \bar{\psi}) + \frac{m}{2} (\psi \psi + \bar{\psi} \bar{\psi})$$

$$+ g (\varphi \psi \psi + \varphi^* \bar{\psi} \bar{\psi})$$

$$- m g (\varphi^* \varphi) (\varphi + \varphi^*) - g (\varphi^* \varphi)^2$$

- scalar field φ
 - spinor field ψ
 - Yukawa interaction $\varphi - \psi - \psi$
 - scalar self interaction
 - universal coupling
- } equal mass

("Wess Zumino model")

4-component notation:

$$\Psi = \begin{pmatrix} \psi \\ \bar{\psi} \end{pmatrix}, \quad \psi\psi = \bar{\Psi} \mathbb{P}_L \Psi$$

$$\bar{\psi}\bar{\psi} = \bar{\Psi} \mathbb{P}_R \Psi$$

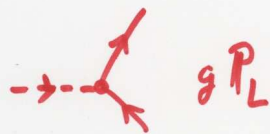
$$\psi \sigma^\mu \partial_\mu \bar{\psi} + \bar{\psi} \bar{\sigma}^\mu \partial_\mu \psi = \bar{\Psi} \gamma^\mu \partial_\mu \Psi$$

$$\mathcal{L} = |\partial_\mu \varphi|^2 - m^2 |\varphi|^2$$

$$- \frac{i}{2} \bar{\Psi} (i \gamma^\mu \partial_\mu - m) \Psi$$

$$+ g (\varphi \bar{\Psi} \mathbb{P}_L \Psi + \varphi^* \bar{\Psi} \mathbb{P}_R \Psi)$$

$$- mg (\varphi^* \varphi) (\varphi + \varphi^*) - g |\varphi|^4$$



example for vector field

components A_μ, λ, D

$$\mathcal{L} = \frac{1}{4} W^a W_a \Big|_{\theta\theta} + \text{h.c.}$$

$$= -\frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

$$- \frac{i}{2} \left(\lambda \bar{\sigma}^\mu \partial_\mu \bar{\lambda} + \bar{\lambda} \sigma^\mu \partial_\mu \lambda \right)$$

$$+ 2 D^2$$

D : auxiliary,
eliminate
($D=0$)

A_μ : photon

λ : photino

$$\Psi = \begin{pmatrix} \lambda \\ \bar{\lambda} \end{pmatrix} :$$

$$\frac{1}{2} \bar{\Psi} i \gamma^\mu \partial_\mu \Psi$$

mass = 0

2.4. SUSY gauge theories

2.4.1. Abelian case

chiral SF ϕ , $\bar{D}_a \phi = 0$

- SUSY gauge transf. $\phi \rightarrow \phi' = e^{-i\Lambda(x)} \phi$

$$\bar{D}_a \phi' = 0 \Leftrightarrow \bar{D}_a \Lambda = 0$$

Λ chiral SF

- with $\phi^{+'} = \phi^+ e^{i\Lambda^+}$
the kinetic term of \mathcal{L} changes:

$$\mathcal{L}_{\text{kin}} = \phi^+ \phi \Big|_{\theta\theta\bar{\theta}\bar{\theta}} \rightarrow \phi^+ e^{i(\Lambda^+ - \Lambda)} \phi \Big|_{\theta\theta\bar{\theta}\bar{\theta}}$$

- get invariance by introducing vector field V in \mathcal{L}_{kin} :

$$\rightarrow \mathcal{L}_{\text{kin}} = \phi^+ e^{2gV} \phi \Big|_{\theta\theta\bar{\theta}\bar{\theta}}$$

$$\text{with } V \rightarrow V' = V + \frac{i}{2g} (\Lambda - \Lambda^+)$$

local susy gauge transf.

$$\begin{aligned}\phi &\rightarrow e^{-i\Lambda(x)} \phi \\ V &\rightarrow V + \frac{i}{2g} (\Lambda - \Lambda^\dagger)\end{aligned}$$

$$e^{2gV} = 1 + 2gV + 2g^2 VV$$

$$\mathcal{L}_{kin} = \underbrace{\phi^\dagger \phi \Big|_{\theta\theta\bar{\theta}\bar{\theta}}}_{\text{free kin. Term } \mathcal{L}_0} + \underbrace{\phi^\dagger (2gV + 2g^2 V^2) \phi \Big|_{\theta\theta\bar{\theta}\bar{\theta}}}_{\text{interaction term } \mathcal{L}_1}$$

$$\begin{aligned}\mathcal{L}_0 + \mathcal{L}_1 &= |D_\mu \phi|^2 - \frac{i}{2} (\bar{\Psi} \bar{\sigma}^\mu D_\mu \psi + \psi \sigma^\mu D_\mu \bar{\Psi}) \\ &\quad + ig\sqrt{2} (\phi^* \psi \lambda - \phi \bar{\Psi} \bar{\lambda}) \\ &\quad + FF^* + 2g(\phi^* \phi) D\end{aligned}$$

$$\text{with } D_\mu = \partial_\mu - igA_\mu$$

* add kinetic term for V
photon A_μ , photino λ

* 4-component notation

$$\Psi = \begin{pmatrix} \psi \\ \bar{\psi} \end{pmatrix}, \quad \chi = \begin{pmatrix} \lambda \\ \bar{\lambda} \end{pmatrix}$$

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} \bar{\chi} i \gamma^\mu \partial_\mu \chi \\ & + |D_\mu \varphi|^2 - \frac{1}{2} \bar{\Psi} i \gamma^\mu D_\mu \Psi \\ & + ig\sqrt{2} (\bar{\Psi} P_L \chi \varphi^* - \bar{\Psi} P_R \chi \varphi) \\ & + FF^* + 2g(\varphi^* \varphi) D + 2D^2 \end{aligned}$$

* eliminate F, D

$$\frac{\partial \mathcal{L}}{\partial F^*} = 0 \Rightarrow F = 0$$

$$\frac{\partial \mathcal{L}}{\partial D} = 0 \Rightarrow D = -\frac{g}{2} (\varphi^* \varphi)$$

$|\varphi|^4$
term

SUSY-QED

needs 2 chiral SF: ϕ_+, ϕ_-

$$\phi_{\pm} \rightarrow e^{\mp i\Lambda(x)} \phi_{\pm}$$

$$\left. \begin{array}{l} \phi_+ : \varphi_+, \psi_+, F_+ \\ \phi_- : \varphi_-, \psi_-, F_- \end{array} \right\} \Psi = \begin{pmatrix} \psi_+ \\ \bar{\psi}_- \end{pmatrix}$$

$$\begin{aligned} \mathcal{L}_{SQED} &= \frac{1}{4} W^a W_a \Big|_{\theta\theta} \\ &+ \phi_+^\dagger e^{2eV} \phi_+ \Big|_{\theta\theta\bar{\theta}\bar{\theta}} + \phi_-^\dagger e^{-2eV} \phi_- \Big|_{\theta\theta\bar{\theta}\bar{\theta}} \\ &- \frac{m}{2} \left(\phi_+ \phi_- \Big|_{\theta\theta} + \phi_-^\dagger \phi_+^\dagger \Big|_{\bar{\theta}\bar{\theta}} \right) \end{aligned}$$

eliminate F_+, F_-, D fields \rightarrow

in 4-component notation:

$$\begin{aligned} \mathcal{L}_{\text{SQED}} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} \bar{\chi} i \gamma^\mu \partial_\mu \chi \\ & + |D_\mu \varphi_+|^2 - m^2 |\varphi_+|^2 - \bar{\Psi} (i \gamma^\mu D_\mu - m) \Psi \\ & + |D_\mu \varphi_-|^2 - m^2 |\varphi_-|^2 \\ & - \frac{e^2}{2} (|\varphi_+|^2 - |\varphi_-|^2)^2 \\ & - e\sqrt{2} (\bar{\chi} P_L \Psi \varphi_+^* + \bar{\Psi} P_R \chi \varphi_+) \\ & + e\sqrt{2} (\bar{\Psi} P_L \chi \varphi_-^* + \bar{\chi} P_R \Psi \varphi_-) \end{aligned}$$

m : mass of e^- , e^+

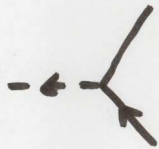
and of $\underbrace{\tilde{e}_L^-, \tilde{e}_L^+}_{\varphi_+}$, $\underbrace{\tilde{e}_R^-, \tilde{e}_R^+}_{\varphi_-^*}$

fermion-scalar interactions

\longrightarrow e^\pm --- χ

$\text{---}\longrightarrow\text{---}$ φ_+, φ_-

Vertices:

$\varphi_+ \text{---}\longleftarrow$  $-ie\sqrt{2} P_L$

$\varphi_+ \text{---}\longrightarrow$  $-ie\sqrt{2} P_R$

$\varphi_- \text{---}\longrightarrow$  $ie\sqrt{2} P_R$

$\varphi_- \text{---}\longleftarrow$  $ie\sqrt{2} P_L$

2.4.2. Non-Abelian case

gauge group G , generators T_1, \dots, T_N

$$[T_a, T_b] = i f_{abc} T_c$$

matter: $\psi = \begin{pmatrix} \psi_1 \\ \vdots \\ \psi_n \end{pmatrix}$ n -dim.
rep. of G

gauge fields: W_μ^α , $\alpha = 1, \dots, N$

field strength: $W_{\mu\nu}^\alpha = \partial_\mu W_\nu^\alpha - \partial_\nu W_\mu^\alpha$
 $+ g f_{abc} W_\mu^b W_\nu^c$

cov. derivative: $D_\mu = \partial_\mu - ig T_\alpha W_\mu^\alpha$

$$\mathcal{L} = -\frac{1}{4} (W_{\mu\nu}^\alpha)^2 + \bar{\Psi} i \gamma^\mu D_\mu \Psi + |D_\mu \psi|^2$$
$$- m \bar{\Psi} \Psi - m^2 \psi^\dagger \psi$$

SW SY version

- matter fields

$$\Phi_{\pm} = \begin{pmatrix} \Phi_{1,\pm} \\ \vdots \\ \Phi_{n,\pm} \end{pmatrix} \quad \begin{array}{l} \text{superfields} \\ \text{(chiral)} \end{array}$$

$$\Phi_{k,\pm} = \varphi_{k,\pm} + \sqrt{2} \theta \psi_{k,\pm} + (\theta\theta) F_{k,\pm}$$

- gauge fields V^1, \dots, V^N
vector SF

$$V^{\alpha} = (\theta\sigma^{\mu}\bar{\theta}) W_{\mu}^{\alpha} + (\bar{\theta}\bar{\theta})(\theta\lambda^{\alpha}) + \dots$$

$$\alpha = 1, \dots, N$$

gauge index

[$a=1,2$: spinor ind.]

W_{μ}^{α} : vector bosons,

λ^{α} : gauginos

$$V = T_{\alpha} V^{\alpha} \quad n \times n \text{ matrix}$$

- gauge transformation

$$\Phi'_+ = e^{-i\Lambda} \Phi_+, \quad \Lambda = T_\alpha \Lambda^\alpha(x)$$

$$\Phi'_- = e^{i\Lambda} \Phi_-$$

- $\mathcal{L}_{\text{matter}} =$

$$\Phi_+^\dagger e^{2gV} \Phi_+ + \Phi_-^\dagger e^{-2gV} \Phi_-$$

$$(\phi_{+1}^\dagger, \dots, \phi_{+n}^\dagger) (n \times n) \begin{pmatrix} \phi_{+1} \\ \vdots \\ \phi_{+n} \end{pmatrix}$$

• $\mathcal{L}_{\text{gauge}}$:

$$W_a = -\frac{1}{4} (\bar{D}\bar{D}) e^{-2gV} D_a e^{2gV}$$

field strength

$$\mathcal{L}_{\text{gauge}} = \frac{1}{4} W_a W^a \Big|_{\theta\theta} + \text{h.c.}$$

$$= -\frac{1}{4} W_{\mu\nu}^\alpha W^{\mu\nu, \alpha}$$

$$- \frac{i}{2} \left(\bar{\lambda}^\alpha \bar{\sigma}^\mu D_\mu \lambda^\alpha + \lambda^\alpha \sigma^\mu D_\mu \bar{\lambda}^\alpha \right)$$

$$+ 2 (D^\alpha)^2$$

choose $G = SU(3)$:

SUSY-QCD

2.5. SUSY breaking

physics: $m_{\text{bos}} \neq m_{\text{ferm}}$

SUSY partners of standard particles
heavy, need extra mass terms

here: formal description
[can be realized in models]

soft breaking:

- $M_{ij}^2 \phi_i^+ \phi_j$ mass for scalars
- $B_{ij} \phi_i \phi_j + A_{ijk} \phi_i \phi_j \phi_k + \text{h.c.}$
for scalars
- $\frac{1}{2}(M_\lambda \lambda \lambda + \text{h.c.})$ mass for gauginos

do not lead to quadratic
divergences in loop contributions
to masses, renormalizable

SUSY formulation

soft terms = part of SUSY
interaction terms

introduce external chiral SF
"spurion field"

$$\eta(z, \theta) = a(z) + \sqrt{2} \theta \chi(z) + \theta \theta \hat{f}(z)$$

$$\hat{f}(z) = f_0 + f(z), \quad f_0 \text{ const}$$

- $\tilde{M}_{ij}^2 \eta^+ \eta \Phi_i^+ e^{2gV} \Phi_j \Big|_{\theta\theta\bar{\theta}\bar{\theta}}$
 $\rightarrow \tilde{M}_{ij}^2 f_0^2 \phi_i^+ \phi_j$ for $a=\chi=f=0$
- $\tilde{B}_{ij} \eta \Phi_i \Phi_j + \tilde{A}_{ijk} \eta \Phi_i \Phi_j \Phi_k \Big|_{\theta\theta} + \text{h.c.}$
 $\tilde{B}_{ij} f_0 \phi_i \phi_j + \tilde{A}_{ijk} f_0 \phi_i \phi_j \phi_k$
- $\frac{1}{2} \tilde{M}_\lambda \eta W_\alpha W^\alpha \Big|_{\theta\theta} + \text{h.c.}$
 $\tilde{M}_\lambda f_0 (\lambda_\alpha \lambda_\alpha + \bar{\lambda}_\alpha \bar{\lambda}_\alpha)$

$$\dim[\eta] = 0$$

interaction terms are
supersymmetric and
(power-counting) renormalizable

useful for quantization
and proof of renormalizability

3. MSSM: formulation and content

gauge boson content

$SU(2)_I$: generators $T_I^1, T_I^2, T_I^3, T_I^a = \frac{1}{2}\sigma_a$

gauge fields $W_\mu^1, W_\mu^2, W_\mu^3$

also: $W_\mu^\pm = \frac{1}{\sqrt{2}} (W_\mu^1 \mp i W_\mu^2), W_\mu^3$

$U(1)_Y$: generator Y

gauge field B_μ

$SU(3)_C$: generators $T^a = \frac{1}{2}\lambda_a \quad (a = 1, \dots, 8)$

gauge fields $G_\mu^a, \quad (a = 1, \dots, 8)$

matter fields and quantum numbers

$SU(2)_I$: weak isospin, generators $T_I^a = \frac{1}{2} \sigma^a$ for L , $= 0$ for R

$U(1)_Y$: weak hypercharge, generator Y

$$T_I^3 + Y/2 = Q$$

fermion content (ignoring possible right-handed neutrinos)

				T_I^3	Y	
leptons:	$\Psi_L^L =$	$\begin{pmatrix} \nu_e^L \\ e^L \end{pmatrix}$	$\begin{pmatrix} \nu_\mu^L \\ \mu^L \end{pmatrix}$	$\begin{pmatrix} \nu_\tau^L \\ \tau^L \end{pmatrix}$	$+\frac{1}{2}$	-1
	$\psi_l^R =$	e^R	μ^R	τ^R	0	-2
quarks:	$\Psi_Q^L =$	$\begin{pmatrix} u^L \\ d^L \end{pmatrix}$	$\begin{pmatrix} c^L \\ s^L \end{pmatrix}$	$\begin{pmatrix} t^L \\ b^L \end{pmatrix}$	$+\frac{1}{2}$	$+\frac{1}{3}$
	$\psi_u^R =$	u^R	c^R	t^R	0	$+\frac{4}{3}$
	$\psi_d^R =$	d^R	s^R	b^R	0	$-\frac{2}{3}$

Particle Content of the MSSM

Superfield	Bosons		Fermions		$SU_c(3)$	$SU_L(2)$	$U_Y(1)$		
Gauge									
\mathbf{G}^a	gluon	g^a	gluino	\tilde{g}^a	8	1	0		
\mathbf{V}^k	Weak	$W^k (W^\pm, Z)$	wino, zino	$\tilde{w}^k (\tilde{w}^\pm, \tilde{z})$	1	3	0		
\mathbf{V}'	Hypercharge	$B (\gamma)$	bino	$\tilde{b}(\tilde{\gamma})$	1	1	0		
Matter									
\mathbf{L}_i	sleptons	{	leptons	{	1	2	-1		
\mathbf{E}_i					$\tilde{L}_i = (\tilde{\nu}, \tilde{e})_L$	$L_i = (\nu, e)_L$	1	1	2
\mathbf{Q}_i	squarks	{	quarks	{	3	2	1/3		
\mathbf{U}_i					$\tilde{E}_i = \tilde{e}_R$	$E_i = e_R$	3^*	1	-4/3
\mathbf{D}_i					$\tilde{Q}_i = (\tilde{u}, \tilde{d})_L$	$Q_i = (u, d)_L$	3^*	1	2/3
Higgs									
\mathbf{H}_1	Higgses	{	higgsinos	{	1	2	-1		
\mathbf{H}_2					H_1	\tilde{H}_1	1	2	1

superfields for matter

$$\mathbf{Q} = \begin{pmatrix} \mathbf{Q}^1 \\ \mathbf{Q}^2 \end{pmatrix}, \mathbf{U}, \mathbf{D} \text{ (quarks)} \quad \mathbf{L} = \begin{pmatrix} \mathbf{L}^1 \\ \mathbf{L}^2 \end{pmatrix}, \mathbf{E} \text{ (leptons)}$$

$$\mathbf{Q}^i = \tilde{Q}^i + \sqrt{2} (\theta q_L^i) + (\theta\theta) F_L^i$$

$$\mathbf{U} = \tilde{U} + \sqrt{2} (\theta u_R) + (\theta\theta) F_R^u$$

$$\mathbf{U}^\dagger = \tilde{U}^* + \sqrt{2} (\bar{\theta} \bar{u}_R) + (\bar{\theta}\bar{\theta}) F_R^{u*}$$

scalar *spinor* *auxiliary*

$\tilde{Q}^i = \tilde{q}_L^i$: *u- and d-squarks, "left-handed"*

$\tilde{U}^* = \tilde{u}_R$, *u-squark, "right-handed"*

4-component quark spinors: $\Psi_u = \begin{pmatrix} u_L \\ \bar{u}_R \end{pmatrix}, \quad \Psi_u^c = \begin{pmatrix} u_R \\ \bar{u}_L \end{pmatrix}$

(analogous for d-quarks and leptons)

superfields for Higgs

$$\mathbf{H}_1 = \begin{pmatrix} \mathbf{H}_1^1 \\ \mathbf{H}_1^2 \end{pmatrix} \quad \text{with } Y = -1, \quad \mathbf{H}_2 = \begin{pmatrix} \mathbf{H}_2^1 \\ \mathbf{H}_2^2 \end{pmatrix} \quad \text{with } Y = +1$$

$$\mathbf{H}_i^k = H_i^k + \sqrt{2} (\theta \psi_{H_i^k}) + (\theta\theta) F_i^k$$

scalar *spinor* *auxiliary*
(Higgs) *(Higgsino)*

superfields for Higgs

$$\mathbf{H}_1 = \begin{pmatrix} \mathbf{H}_1^1 \\ \mathbf{H}_1^2 \end{pmatrix} \quad \text{with } Y = -1, \quad \mathbf{H}_2 = \begin{pmatrix} \mathbf{H}_2^1 \\ \mathbf{H}_2^2 \end{pmatrix} \quad \text{with } Y = +1$$

$$\mathbf{H}_i^k = \underbrace{H_i^k}_{\substack{\text{scalar} \\ \text{(Higgs)}}} + \sqrt{2} \underbrace{(\theta \psi_{H_i^k})}_{\substack{\text{spinor} \\ \text{(Higgsino)}}} + (\theta\theta) \underbrace{F_i^k}_{\text{auxiliary}}$$

electric charge: $\mathbf{Q}_{H_1} = \begin{pmatrix} 0 & 0 \\ 0 & -1 \end{pmatrix}, \quad \mathbf{Q}_{H_2} = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$

$$\Rightarrow \mathbf{H}_1 = \begin{pmatrix} \mathbf{H}_1^0 \\ \mathbf{H}_1^- \end{pmatrix}, \quad \mathbf{H}_2 = \begin{pmatrix} \mathbf{H}_2^+ \\ \mathbf{H}_2^0 \end{pmatrix}$$

constructing the MSSM Lagrangian

$$[\textit{notation: } \mathbf{V}_i = T_\alpha \mathbf{V}_i^\alpha, \quad \mathbf{W}_a = T_\alpha \mathbf{W}_a^\alpha]$$

$$\sum_{SU(3), SU(2), U(1)} \frac{1}{4} \text{Tr}(\mathbf{W}_a \mathbf{W}^a) + h.c.$$

$$+ \sum_{\text{matter}} \Phi_i^\dagger e^{2(g_3 \mathbf{V}_3 + g_2 \mathbf{V}_2 + g_1 \mathbf{V}_1)} \Phi_i$$

$$+ \sum_{\text{Higgs}} \mathbf{H}_i^\dagger e^{2(g_2 \mathbf{V}_2 + g_1 \mathbf{V}_1)} \mathbf{H}_i$$

$$+ \mathcal{W} \quad \text{superpotential}$$

$$\mathcal{W} = \varepsilon_{ij} \mu \mathbf{H}_1^i \mathbf{H}_2^j$$

$$+ \varepsilon_{ij} (Y_U \mathbf{Q}^j \mathbf{U} \mathbf{H}_2^i + Y_D \mathbf{Q}^j \mathbf{D} \mathbf{H}_1^i + Y_E \mathbf{L}^j \mathbf{E} \mathbf{H}_1^i)$$

- \mathcal{W} conserves **R-parity**: $P_R = (-1)^{3(B-L)+2s}$
- P_R -violating interactions
 - induce baryon- or lepton-number violating processes
 - interactions must be suppressed
 - interactions are absent if P_R -conservation is postulated
- phenomenologically, P_R -violating terms can be present, with couplings (small) as free parameters
- minimal choice (MSSM) contains only R-parity conserving terms
- all SM particles have even, all SUSY particles have odd $P_R \Rightarrow$
 - SUSY-particles can only be produced in pairs
 - lightest SUSY particle (“**LSP**”) is stable

soft breaking terms

$$\begin{aligned}\mathcal{L}_{\text{soft}} = & \sum_i m_i^2 |\varphi_i|^2 \\ & + \sum_{SU(3), SU(2), U(1)} \frac{1}{2} M_\lambda \lambda_\alpha \lambda_\alpha \\ & + B \varepsilon_{ij} H_1^i H_2^j + h.c. \\ & + \varepsilon_{ij} (A_U \tilde{Q}^j \tilde{U} H_2^i + A_D \tilde{Q}^j \tilde{D} H_1^i + A_E \tilde{L}^j \tilde{E} H_1^i)\end{aligned}$$

φ_i : all scalar fields

λ_α : all gaugino fields

$\tilde{U}, \tilde{D}, \tilde{E}$: scalar quark/lepton fields

\tilde{Q}, \tilde{E} : doublets of scalar quarks/leptons

general: coefficients A are 3×3 -matrices in generation space

- essentially all masses and mixings of superpartners are free parameters
- soft parameters can be treated as independent free parameters
- or: fixed by some (ad-hoc) assumptions
- or: derived from specific models of SUSY breaking

- essentially all masses and mixings of superpartners are free parameters
 - soft parameters can be treated as independent free parameters
 - or: fixed by some ad-hoc/ well motivated assumptions
 - or: derived from specific models of SUSY breaking
-

- parameters M_λ, A_f can be complex
- new sources of CP -violation
- phenomenological constraints from electric dipole moments and from flavor physics

Higgs fields

two scalar doublets from $\mathbf{H}_1, \mathbf{H}_2$ superfields:

$$H_1 = \begin{pmatrix} H_1^1 \\ H_1^2 \end{pmatrix} = \begin{pmatrix} H_1^0 \\ \phi_1^- \end{pmatrix}, \quad \langle H_1 \rangle_0 = \begin{pmatrix} v_1 \\ 0 \end{pmatrix}$$

$$H_2 = \begin{pmatrix} H_2^1 \\ H_2^2 \end{pmatrix} = \begin{pmatrix} \phi_2^+ \\ H_2^0 \end{pmatrix}, \quad \langle H_2 \rangle_0 = \begin{pmatrix} 0 \\ v_2 \end{pmatrix}$$

$$V_H^{\text{susy}} = \mu^2 H_1^\dagger H_1 + \mu^2 H_2^\dagger H_2 + \frac{g_1^2 + g_2^2}{8} (H_1^\dagger H_1 - H_2^\dagger H_2)^2 + \frac{g_2^2}{2} |H_1^\dagger H_2|^2,$$

$$V_H^{\text{soft}} = m_1^2 H_1^\dagger H_1 + m_2^2 H_2^\dagger H_2 - m_3^2 \varepsilon_{ij} (H_1^i H_2^j + h.c.)$$

Higgs potential:

$$V_H = V_H^{\text{susy}} + V_H^{\text{soft}}$$

$$= (\mu^2 + m_1^2) H_1^\dagger H_1 + (\mu^2 + m_2^2) H_2^\dagger H_2 - m_3^2 \varepsilon_{ij} (H_1^i H_2^j + h.c.)$$

$$+ \frac{g_1^2 + g_2^2}{8} (H_1^\dagger H_1 - H_2^\dagger H_2)^2 + \frac{g_2^2}{2} |H_1^\dagger H_2|^2$$

EW symmetry breaking: minimum of V_H at

$$H_1^0 = v_1 \neq 0, \quad H_2^0 = v_2 \neq 0, \quad \Phi_1^- = 0, \quad \Phi_2^+ = 0$$

necessary condition: $m_3^4 > (\mu^2 + m_1^2)(\mu^2 + m_2^2)$
 requires $m_3^2 \neq 0$

- SUSY breaking required for EW symmetry breaking

Higgs potential: $V_H = V_H^{\text{susy}} + V_H^{\text{soft}}$

$$= (\mu^2 + m_1^2) H_1^\dagger H_1 + (\mu^2 + m_2^2) H_2^\dagger H_2 - m_3^2 \varepsilon_{ij} (H_1^i H_2^j + h.c.)$$

$$+ \frac{g_1^2 + g_2^2}{8} (H_1^\dagger H_1 - H_2^\dagger H_2)^2 + \frac{g_2^2}{2} |H_1^\dagger H_2|^2$$

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necessary condition: $m_3^4 > (\mu^2 + m_1^2)(\mu^2 + m_2^2)$
 requires $m_3^2 \neq 0$

- SUSY breaking required for EW symmetry breaking

SM particle masses:

$$M_{W,Z}^2 \sim v_1^2 + v_2^2, \quad m_d, m_e \sim v_1, \quad m_u \sim v_2$$

new parameter: $\tan \beta = \frac{v_2}{v_1}$

mass spectrum: 3 unphysical + 5 physical degrees of freedom

- 3 Goldstone bosons G^0, G^\pm
- 2 neutral CP -even Higgs bosons h^0, H^0
- 1 neutral CP -odd Higgs boson A^0 “pseudoscalar”
$$M_A^2 = m_3^2 (\cot \beta + \tan \beta)$$

conventional input parameters: $M_A, \tan \beta = \frac{v_2}{v_1}$

other masses m_h, m_H, m_{H^\pm} predicted, not independent

mass eigenstates are linear combinations of the doublet components, with $\phi_1^+ = (\phi_1^-)^\dagger, \phi_2^- = (\phi_2^+)^\dagger$

$$H_1^0 = v_1 + \frac{1}{\sqrt{2}} (\phi_1 + i\chi_1)$$

$$H_2^0 = v_2 + \frac{1}{\sqrt{2}} (\phi_2 + i\chi_1)$$

$$\begin{pmatrix} H^0 \\ h^0 \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \phi_1 \\ \phi_2 \end{pmatrix}$$

$$\begin{pmatrix} G^0 \\ A^0 \end{pmatrix} = \begin{pmatrix} \cos \beta & \sin \beta \\ -\sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix}$$

$$\begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix} = \begin{pmatrix} \cos \beta & \sin \beta \\ -\sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} \phi_1^\pm \\ \phi_2^\pm \end{pmatrix}$$

$$\tan 2\alpha = \tan 2\beta \frac{M_A^2 + M_Z^2}{M_A^2 - M_Z^2}, \quad -\frac{\pi}{2} < \alpha < 0$$

- predictions for dependent masses (tree-level):

$$m_{H^\pm}^2 = M_A^2 + M_W^2$$

$$m_{H,h}^2 = \frac{1}{2} \left(M_A^2 + M_Z^2 \pm \sqrt{(M_A^2 + M_Z^2)^2 - 4M_A^2 M_Z^2 \cos^2 2\beta} \right)$$

$$m_h < M_Z |\cos(2\beta)| < M_Z \quad (!)$$

- substantial higher-order corrections:

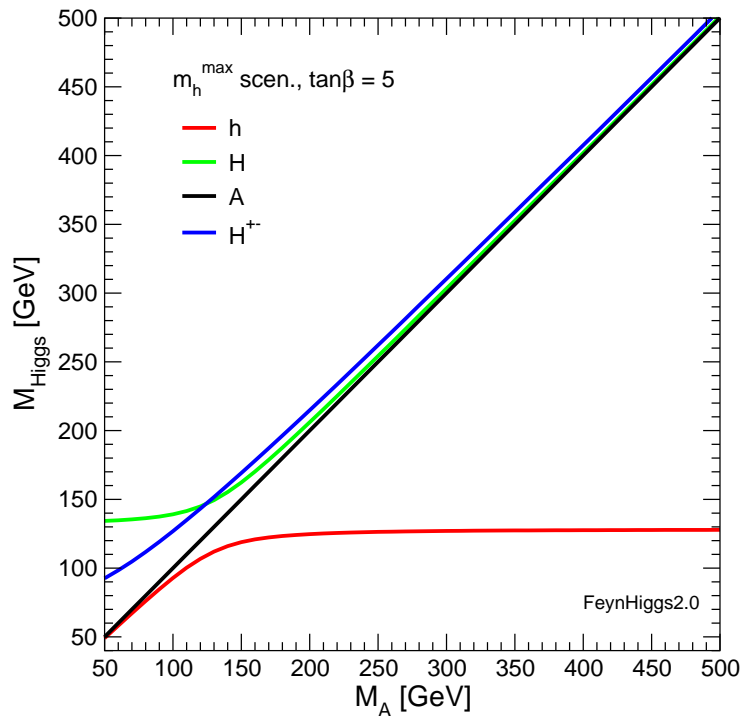
dominant one-loop term $\Delta m_h^2 \sim G_F m_t^4 \log(m_{\tilde{t}}^2/m_t^2)$

from the Yukawa sector

all other sectors also contribute

$m_h =$ observable sensitive to (still) unknown SUSY particles

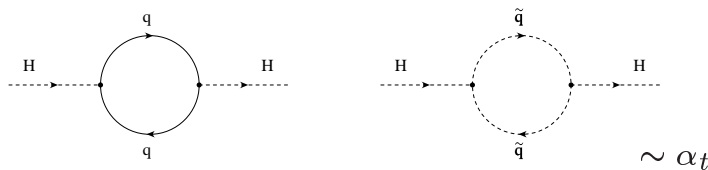
Higgs bosons in the MSSM: h^0, H^0, A^0, H^\pm



- *light Higgs boson h^0*

$$m_h \leq m_Z |\cos(2\beta)| + \Delta m_{h^0}$$
- *for heavy A^0, H^0, H^\pm :*
 h^0 like Standard Model Higgs boson

m_h^0 strongly influenced by quantum effects, e.g. t, \tilde{t}



gauginos and Higgsinos

mass terms = bilinear terms in gaugino and Higgsino fields

notation: *gluino* \tilde{g}_a , *winos* $\tilde{W}^\pm, \tilde{W}^3$, *bino* \tilde{B}^0 , *Higgsinos* $\tilde{H}_{1,2}^{\pm,0}$

$$\mathcal{L}_{\text{gaugino,Higgsino}} = \frac{1}{2} M_3 \tilde{g}_a \tilde{g}_a + \frac{1}{2} \chi^T \mathbf{M}^{(0)} \chi + \psi_-^T \mathbf{M}^{(c)} \psi_+ + \text{h.c.}$$

$\mathbf{M}^{(c)}$, $\mathbf{M}^{(0)}$ non diagonal in the components

$$\psi_+ = \begin{pmatrix} \tilde{W}^+ \\ \tilde{H}_2^+ \end{pmatrix}, \quad \psi_- = \begin{pmatrix} \tilde{W}^- \\ \tilde{H}_1^- \end{pmatrix}, \quad \chi = \begin{pmatrix} \tilde{B}^0 \\ \tilde{W}^3 \\ \tilde{H}_1^0 \\ \tilde{H}_2^0 \end{pmatrix}$$

diagonalization \rightarrow mass eigenstates:

- charginos $\chi_{1,2}^\pm$, neutralinos $\chi_{1,2,3,4}^0$

● **chargino masses:** $m_{\tilde{\chi}_{1,2}^{\pm}}$ from M_2, μ

$$\begin{pmatrix} M_2 & \sqrt{2}M_W \sin \beta \\ \sqrt{2}M_W \cos \beta & \mu \end{pmatrix}$$

● **neutralino masses:** $m_{\tilde{\chi}_{1,2,3,4}^0}$ from M_1, M_2, μ

$$\begin{pmatrix} M_1 & 0 & -M_Z s_W \cos \beta & M_Z s_W \sin \beta \\ 0 & M_2 & M_Z c_W \cos \beta & -M_Z c_W \sin \beta \\ -M_Z s_W \cos \beta & M_Z c_W \cos \beta & 0 & -\mu \\ M_Z s_W \sin \beta & -M_Z c_W \sin \beta & -\mu & 0 \end{pmatrix}$$

● sfermion masses: $m_{\tilde{f}_{1,2}}$ from $M_L, M_{\tilde{f}_R}, A_f$

$$\begin{pmatrix} m_f^2 + M_L^2 + M_Z^2 c_{2\beta} (I_f^3 - Q_f s_W^2) & m_f (A_f - \mu \kappa) \\ m_f (A_f - \mu \kappa) & m_f^2 + M_{\tilde{f}_R}^2 + M_Z^2 c_{2\beta} Q_f s_W^2 \end{pmatrix}$$

with

$$\kappa = \{\cot \beta; \tan \beta\} \quad \text{for } f = \{u, d\}$$

note: M_L equal for both \tilde{u} and \tilde{d} of a doublet

$$M_L, M_{\tilde{u}_R}, A_u \rightarrow m_{\tilde{u}_{1,2}}, \theta_u$$

$$M_L, M_{\tilde{d}_R}, A_d \rightarrow m_{\tilde{d}_{1,2}}, \theta_d$$

$$\Rightarrow m_{\tilde{u}_{1,2}}, m_{\tilde{d}_{1,2}} \text{ not independent}$$

Quantization and renormalization

conventional gauge theories

gauge group G , generators T_a , structure constants f_{abc}

for quantization: $\mathcal{L} = \mathcal{L}_{\text{sym}} + \mathcal{L}_{\text{fix}} + \mathcal{L}_{\text{ghost}}$

$$\mathcal{L}_{\text{fix}} = \frac{1}{2} F_a^2, \quad F_a = \partial_\mu W^{a,\mu}$$

requires ghost fields c_a and anti-ghosts \bar{c}_a

$$\mathcal{L}_{\text{ghost}} = (\partial^\mu \bar{c}_a) (D_\mu^{\text{adj}})_{ab} c_b, \quad D_\mu^{\text{adj}} = \partial_\mu - ig W_\mu^r T_r^{\text{adj}}$$

• \mathcal{L} is symmetric under BRS transformations

$$sW_\mu^a = (D_\mu^{\text{adj}})_{ab} c_b \quad [sW_\mu^a \equiv \delta W_\mu^a \quad \text{etc.}]$$

$$sc_a = -\partial^\nu W_\nu^a, \quad s\bar{c}_a = -\frac{1}{2}g f_{abc} c_b c_c$$

BRS [*Becchi, Rouet, Stora*] symmetry guarantees

- renormalizability
- gauge invariant and unitary S matrix

important: ST identities = symmetry relations between Green functions, valid to all orders

basic quantity: effective action $\Gamma(\mathcal{L})$
generating functional of vertex functions

$$\frac{\delta\Gamma}{\delta\varphi_i\delta\varphi_j\dots} = \Gamma_{\varphi_i\varphi_j\dots}$$

classical action: $\Gamma_{\text{cl}}(\mathcal{L}) = \int d^4x \mathcal{L}$
 \Rightarrow tree level vertices

general: vertex functions with loop contributions,
building blocks for renormalization

BRS symmetry: invariance of Γ under BRS transformations,

$$S(\Gamma) = \int d^4x \left[\frac{\delta\Gamma}{\delta\varphi_i} s\varphi_i + \dots \right] = 0 \quad S: \text{ST-operator}$$

$$\Rightarrow \frac{\delta S(\Gamma)}{\delta\varphi_{j\dots}} = 0 \quad \text{relations between vertex functions}$$

ST identities

\Rightarrow all UV divergences in vertex functions can be removed by (multiplicative) renormalization of parameters and fields in the classical Lagrangian/action

SUSY gauge theories

SUSY transformation modify BRS transformations,

$$\mathcal{L}_{\text{fix}} + \mathcal{L}_{\text{ghost}}$$

not invariant under SUSY transformations

- BRS transformations \rightarrow **SUSY-BRS transformations**

combine BRS and SUSY transformations

SUSY gauge theories

SUSY transformation modify BRS transformations,

$$\mathcal{L}_{\text{fix}} + \mathcal{L}_{\text{ghost}}$$

not invariant under SUSY transformations

- BRS transformations \rightarrow **SUSY-BRS transformations**

combine BRS and SUSY transformations

SUSY BRS symmetry \Rightarrow ST identities

ST id must be fulfilled at any order, including counterterms

\Rightarrow structure of counterterms

result:

⇒ all UV divergences in vertex functions can be removed by (multiplicative) renormalization of parameters and fields in the classical Lagrangian/action.

Parameters to be renormalized:

supersymmetric and soft-breaking parameters.

counterterms fulfill the ST id \Leftrightarrow the regularization scheme for loop calculations is symmetric

otherwise: symmetry-restoring counterterms needed, determined by the ST id

- important for practical calculations

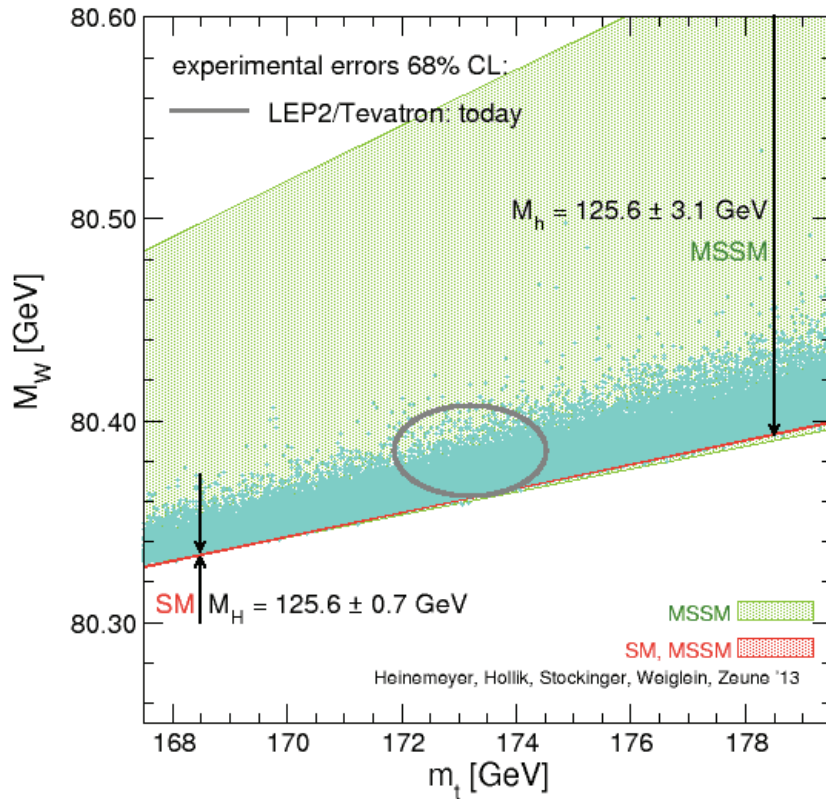
practical calculations are done in

- dimensional regularization D_{reg} :
 $p^\mu, A^\mu, \gamma^\mu, g_{\mu\nu}$ in D dimensions
not supersymmetric,
needs symmetry-restoring counterterms
- dimensional reduction D_{red} :
only momenta in D dimensions,
no symmetry-restoring counterterms needed (at
one-loop), beyond one-loop no general proof yet

4. Tests of the MSSM

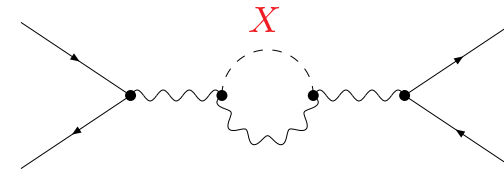
- SUSY parameters → mass spectrum + mixing matrices
- interaction terms → Feynman rules for the MSSM
- calculate processes with SUSY particles
 - production cross sections for colliders
 - decay widths/ branching ratiosin terms of the model parameters
- confront predictions with experimental results: **direct searches**
- calculate electroweak precision observables (PO) with virtual SUSY particles M_W , Z observables, muon $g - 2$, and M_h (!)
- compare predictions with experimental results for PO:
indirect searches

indirect: precision observables with SUSY quantum loops



dark: $m_{\tilde{t}}, m_{\tilde{b}} > 500 \text{ GeV}$
 $m_{\tilde{q}}, m_{\tilde{g}} > 1200 \text{ GeV}$

muon decay $\mu^- \rightarrow e^- \nu_\mu \bar{\nu}_e$

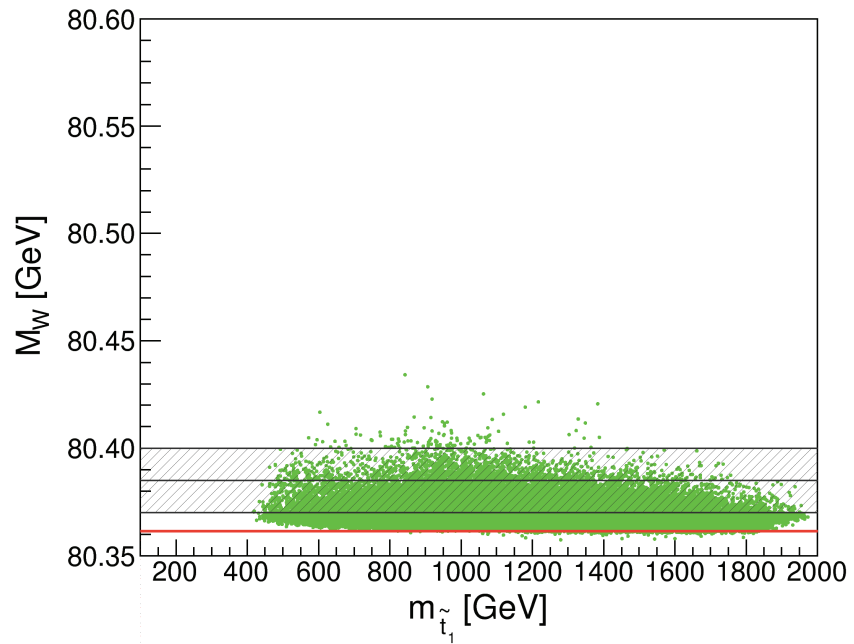


$X = \text{Higgs bosons, SUSY particles}$

$$\frac{G_F}{\sqrt{2}} = \frac{\pi\alpha}{M_W^2 (1 - M_W^2/M_Z^2)} \cdot [1 + \Delta r(m_t, X)]$$

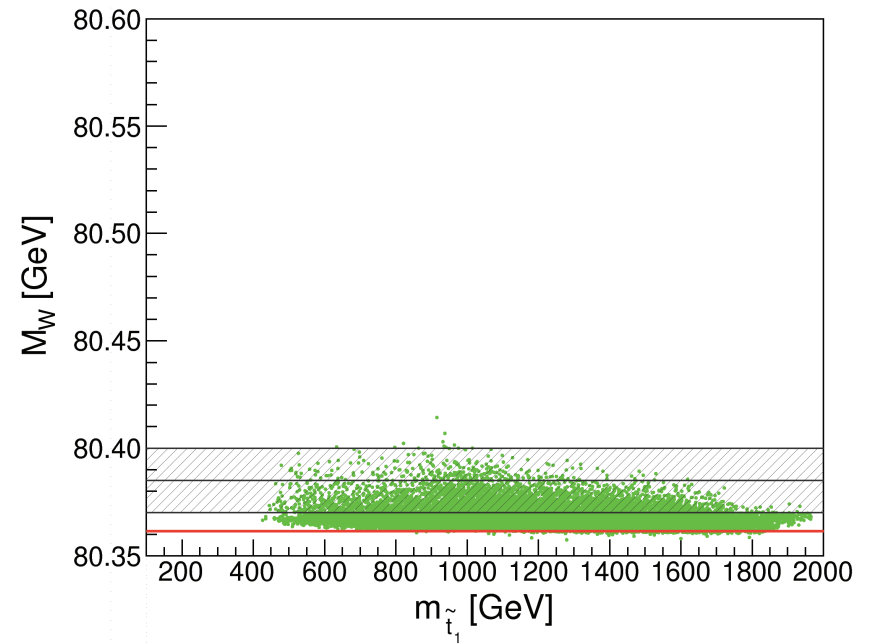
determines W mass

$$M_W = M_W(\alpha, G_F, M_Z, m_t, X)$$



$$m_{\tilde{t}}, m_{\tilde{b}} > 1000 \text{ GeV}$$

$$(m_{\tilde{q}}, m_{\tilde{g}} > 1200 \text{ GeV})$$



+ *charginos and sleptons above 500 GeV*

muon $g - 2$

new contributions from virtual SUSY partners of μ , ν_μ and of W^\pm , Z



extra terms

$$+ \frac{\alpha}{\pi} \frac{m_\mu^2}{M_{\text{SUSY}}^2} \cdot \frac{v_2}{v_1}$$

can provide missing contribution for

$$M_{\text{SUSY}} = 200 - 600 \text{ GeV}$$

direct: SUSY searches at the LHC

> at the LHC sparticles are pair produced

- dominantly squarks and gluinos via the strong interaction
- they decay via cascades into the stable LSP (neutralino or gravitino), assuming R-parity conservation

> common signature:

- multiple, high energetic jets and transverse missing momentum
- distinguish final states by additional particles

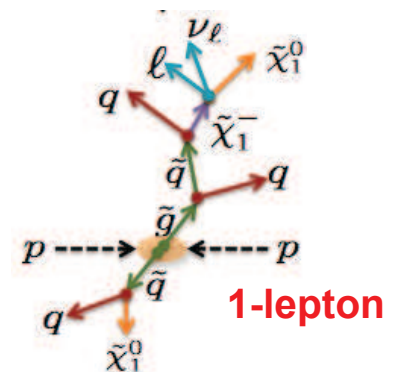
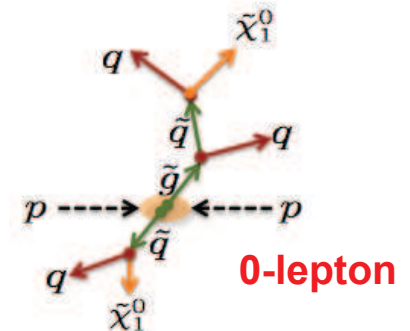
zero, one, two, .. leptons (e, μ), two photons, ...

b-jets if 3rd generation squarks are lighter than other generation squarks

> incomplete event reconstruction due to LSP

→ *distributions of jets (and leptons)*

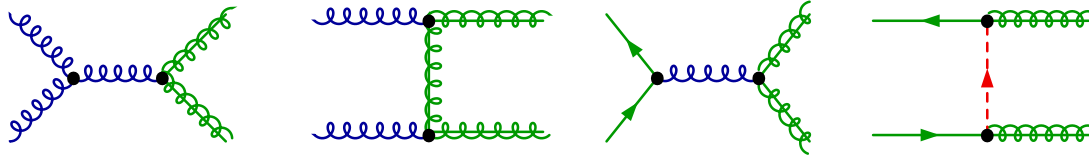
- searches need predictions for production and decays of SUSY particles



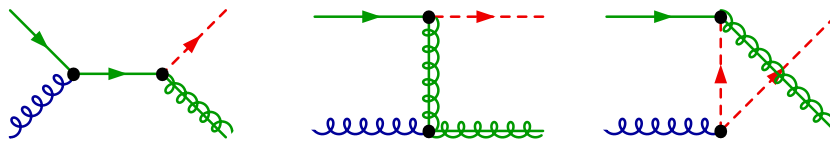
- **LHC:** LO contributions to squark pair production (QCD tree level)

cross sections depend essentially only on α_s and s -particle masses

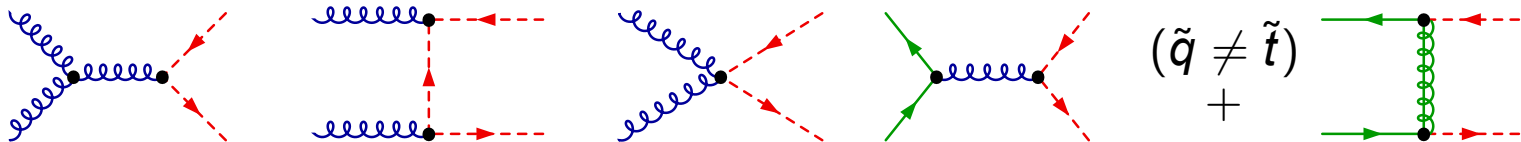
- $\mathcal{O}(\alpha_s^2)$: – $\tilde{g}\tilde{g}$ production



- $\tilde{g}\tilde{q}$ production



- $\tilde{q}\tilde{q}^*$, $\tilde{b}_i\tilde{b}_i^*$, $\tilde{t}_i\tilde{t}_i^*$ production; $\tilde{q}\tilde{q}$ production



- *decay modes depend in detail on model parameters and chiralities*

- *simplifying assumptions for experimental analyses*

ATLAS SUSY Searches* - 95% CL Lower Limits

Status: August 2016

ATLAS Preliminary

$\sqrt{s} = 7, 8, 13$ TeV

Model	e, μ, τ, γ	Jets	E_T^{miss}	$[\mathcal{L} dt[\text{fb}^{-1}]$	Mass limit	$\sqrt{s} = 7, 8$ TeV	$\sqrt{s} = 13$ TeV	Reference	
Inclusive Searches	MSUGRA/CMSSM	0-3 e, μ /1-2 τ	2-10 jets/3 b	Yes	20.3	\tilde{q}, \tilde{g}	1.85 TeV	$m(\tilde{q})=m(\tilde{g})$	1507.05525
	$\tilde{q}\tilde{q}, \tilde{q} \rightarrow q\tilde{\chi}_1^0$	0	2-6 jets	Yes	13.3	\tilde{q}	1.35 TeV	$m(\tilde{\chi}_1^0) < 200$ GeV, $m(1^{st} \text{ gen. } \tilde{q})=m(2^{nd} \text{ gen. } \tilde{q})$	ATLAS-CONF-2016-078
	$\tilde{q}\tilde{q}, \tilde{q} \rightarrow q\tilde{\chi}_1^{\pm}$ (compressed)	mono-jet	1-3 jets	Yes	3.2	\tilde{q}	608 GeV	$m(\tilde{q})-m(\tilde{\chi}_1^0) < 5$ GeV	1604.07773
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^0$	0	2-6 jets	Yes	13.3	\tilde{g}	1.86 TeV	$m(\tilde{\chi}_1^0)=0$ GeV	ATLAS-CONF-2016-078
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^{\pm}$	0	2-6 jets	Yes	13.3	\tilde{g}	1.83 TeV	$m(\tilde{\chi}_1^0) < 400$ GeV, $m(\tilde{\chi}_1^{\pm})=0.5(m(\tilde{\chi}_1^0)+m(\tilde{g}))$	ATLAS-CONF-2016-078
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}(\ell\ell/\nu\nu)\tilde{\chi}_1^0$	3 e, μ	4 jets	-	13.2	\tilde{g}	1.7 TeV	$m(\tilde{\chi}_1^0) < 400$ GeV	ATLAS-CONF-2016-037
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}WZ\tilde{\chi}_1^0$	2 e, μ (SS)	0-3 jets	Yes	13.2	\tilde{g}	1.6 TeV	$m(\tilde{\chi}_1^0) < 500$ GeV	ATLAS-CONF-2016-037
	GMSB ($\tilde{\ell}$ NLSP)	1-2 τ + 0-1 ℓ	0-2 jets	Yes	3.2	\tilde{g}	2.0 TeV	$c\tau(\text{NLSP}) < 0.1$ mm	1607.05979
	GGM (bino NLSP)	2 γ	-	Yes	3.2	\tilde{g}	1.65 TeV	$c\tau(\text{NLSP}) < 0.1$ mm	1606.09150
	GGM (higgsino-bino NLSP)	γ	1 b	Yes	20.3	\tilde{g}	1.37 TeV	$m(\tilde{\chi}_1^0) < 950$ GeV, $c\tau(\text{NLSP}) < 0.1$ mm, $\mu < 0$	1507.05493
	GGM (higgsino-bino NLSP)	γ	2 jets	Yes	13.3	\tilde{g}	1.8 TeV	$m(\tilde{\chi}_1^0) > 680$ GeV, $c\tau(\text{NLSP}) < 0.1$ mm, $\mu > 0$	ATLAS-CONF-2016-066
	GGM (higgsino NLSP)	2 e, μ (Z)	2 jets	Yes	20.3	\tilde{g}	900 GeV	$m(\text{NLSP}) > 430$ GeV	1503.03290
Gravitino LSP	0	mono-jet	Yes	20.3	$\mu^{1/2}$ scale	865 GeV	$m(\tilde{G}) > 1.8 \times 10^{-4}$ eV, $m(\tilde{g})=m(\tilde{q})=1.5$ TeV	1502.01518	
3rd gen. \tilde{g} med.	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$	0	3 b	Yes	14.8	\tilde{g}	1.89 TeV	$m(\tilde{\chi}_1^0)=0$ GeV	ATLAS-CONF-2016-052
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$	0-1 e, μ	3 b	Yes	14.8	\tilde{g}	1.89 TeV	$m(\tilde{\chi}_1^0)=0$ GeV	ATLAS-CONF-2016-052
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow b\tilde{t}\tilde{\chi}_1^0$	0-1 e, μ	3 b	Yes	20.1	\tilde{g}	1.37 TeV	$m(\tilde{\chi}_1^0) < 300$ GeV	1407.06000
3rd gen. squarks direct production	$\tilde{b}_1\tilde{b}_1, \tilde{b}_1 \rightarrow b\tilde{\chi}_1^0$	0	2 b	Yes	3.2	\tilde{b}_1	840 GeV	$m(\tilde{\chi}_1^0) < 100$ GeV	1606.08772
	$\tilde{b}_1\tilde{b}_1, \tilde{b}_1 \rightarrow t\tilde{\chi}_1^0$	2 e, μ (SS)	1 b	Yes	13.2	\tilde{b}_1	325-685 GeV	$m(\tilde{\chi}_1^0) < 150$ GeV, $m(\tilde{\chi}_1^{\pm})=m(\tilde{\chi}_1^0)+100$ GeV	ATLAS-CONF-2016-037
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow b\tilde{\chi}_1^0$	0-2 e, μ	1-2 b	Yes	4.7/13.3	\tilde{t}_1	170 GeV	$m(\tilde{\chi}_1^0)=2m(\tilde{\chi}_1^{\pm}), m(\tilde{\chi}_1^0)=55$ GeV	1209.2102, ATLAS-CONF-2016-077
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow Wb\tilde{\chi}_1^0$ or $\tilde{\chi}_1^0$	0-2 e, μ	0-2 jets/1-2 b	Yes	4.7/13.3	\tilde{t}_1	90-198 GeV	$m(\tilde{\chi}_1^0)=1$ GeV	1506.08616, ATLAS-CONF-2016-077
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow c\tilde{\chi}_1^0$	0	mono-jet	Yes	3.2	\tilde{t}_1	90-323 GeV	$m(\tilde{\chi}_1^0)-m(\tilde{\chi}_1^{\pm})=5$ GeV	1604.07773
	$\tilde{t}_1\tilde{t}_1$ (natural GMSB)	2 e, μ (Z)	1 b	Yes	20.3	\tilde{t}_1	150-600 GeV	$m(\tilde{\chi}_1^0) > 150$ GeV	1403.5222
	$\tilde{t}_2\tilde{t}_2, \tilde{t}_2 \rightarrow \tilde{t}_1 + Z$	3 e, μ (Z)	1 b	Yes	13.3	\tilde{t}_2	290-700 GeV	$m(\tilde{\chi}_1^0) < 300$ GeV	ATLAS-CONF-2016-038
$\tilde{t}_2\tilde{t}_2, \tilde{t}_2 \rightarrow \tilde{t}_1 + h$	1 e, μ	6 jets + 2 b	Yes	20.3	\tilde{t}_2	320-620 GeV	$m(\tilde{\chi}_1^0)=0$ GeV	1506.08616	
EW direct	$\tilde{\chi}_{1,R}^{\pm}\tilde{\chi}_{1,R}^{\mp}, \tilde{\chi}_{1,R}^{\pm} \rightarrow \tilde{\chi}_1^0$	2 e, μ	0	Yes	20.3	$\tilde{\chi}_{1,R}^{\pm}$	90-335 GeV	$m(\tilde{\chi}_1^0)=0$ GeV	1403.5294
	$\tilde{\chi}_{1,R}^{\pm}\tilde{\chi}_{1,R}^{\mp}, \tilde{\chi}_{1,R}^{\pm} \rightarrow \tilde{\nu}(\tilde{\nu})$	2 e, μ	0	Yes	20.3	$\tilde{\chi}_{1,R}^{\pm}$	140-475 GeV	$m(\tilde{\chi}_1^0)=0$ GeV, $m(\tilde{\nu}, \tilde{\nu})=0.5(m(\tilde{\chi}_1^{\pm})+m(\tilde{\chi}_1^0))$	1403.5294
	$\tilde{\chi}_{1,R}^{\pm}\tilde{\chi}_{1,R}^{\mp}, \tilde{\chi}_{1,R}^{\pm} \rightarrow \tilde{\tau}(\tilde{\tau})$	2 τ	-	Yes	20.3	$\tilde{\chi}_{1,R}^{\pm}$	355 GeV	$m(\tilde{\chi}_1^0)=0$ GeV, $m(\tilde{\tau}, \tilde{\nu})=0.5(m(\tilde{\chi}_1^{\pm})+m(\tilde{\chi}_1^0))$	1407.0350
	$\tilde{\chi}_{1,R}^{\pm}\tilde{\chi}_{1,R}^{\mp}, \tilde{\chi}_{1,R}^{\pm} \rightarrow \tilde{\nu}_i \nu_j^{\pm} \ell(\tilde{\nu}_i), \tilde{\nu}_j^{\pm} \ell(\tilde{\nu}_i)$	3 e, μ	0	Yes	20.3	$\tilde{\chi}_{1,R}^{\pm}, \tilde{\chi}_{1,R}^{\mp}$	715 GeV	$m(\tilde{\chi}_1^0)=m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0)=0, m(\tilde{\nu}, \tilde{\nu})=0.5(m(\tilde{\chi}_1^{\pm})+m(\tilde{\chi}_1^0))$	1402.7029
	$\tilde{\chi}_{1,R}^{\pm}\tilde{\chi}_{1,R}^{\mp}, \tilde{\chi}_{1,R}^{\pm} \rightarrow W\tilde{\chi}_1^0 Z\tilde{\chi}_1^0$	2-3 e, μ	0-2 jets	Yes	20.3	$\tilde{\chi}_{1,R}^{\pm}, \tilde{\chi}_{1,R}^{\mp}$	425 GeV	$m(\tilde{\chi}_1^0)=m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0)=0, \tilde{\ell}$ decoupled	1403.5294, 1402.7029
	$\tilde{\chi}_{1,R}^{\pm}\tilde{\chi}_{1,R}^{\mp}, \tilde{\chi}_{1,R}^{\pm} \rightarrow W\tilde{\chi}_1^0 h\tilde{\chi}_1^0, h \rightarrow b\tilde{b}/WW/\tau\tau/\gamma\gamma$	e, μ, γ	0-2 b	Yes	20.3	$\tilde{\chi}_{1,R}^{\pm}, \tilde{\chi}_{1,R}^{\mp}$	270 GeV	$m(\tilde{\chi}_1^0)=m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0)=0, \tilde{\ell}$ decoupled	1501.07110
	$\tilde{\chi}_{2,3}^0\tilde{\chi}_{2,3}^0 \rightarrow \tilde{\chi}_1^0 \tilde{g}$	4 e, μ	0	Yes	20.3	$\tilde{\chi}_{2,3}^0$	635 GeV	$m(\tilde{\chi}_2^0)=m(\tilde{\chi}_3^0), m(\tilde{\chi}_1^0)=0, m(\tilde{\nu}, \tilde{\nu})=0.5(m(\tilde{\chi}_2^0)+m(\tilde{\chi}_1^0))$	1405.5086
	GGM (wino NLSP) weak prod.	1 $e, \mu + \gamma$	-	Yes	20.3	\tilde{W}	115-370 GeV	$c\tau < 1$ mm	1507.05493
	GGM (bino NLSP) weak prod.	2 γ	-	Yes	20.3	\tilde{W}	590 GeV	$c\tau < 1$ mm	1507.05493
	Long-lived particles	Direct $\tilde{\chi}_1^{\pm}\tilde{\chi}_1^{\mp}$ prod., long-lived $\tilde{\chi}_1^{\pm}$	Disapp. trk	1 jet	Yes	20.3	$\tilde{\chi}_1^{\pm}$	270 GeV	$m(\tilde{\chi}_1^{\pm})-m(\tilde{\chi}_1^0) \sim 160$ MeV, $\tau(\tilde{\chi}_1^{\pm})=0.2$ ns
Direct $\tilde{\chi}_1^{\pm}\tilde{\chi}_1^{\mp}$ prod., long-lived $\tilde{\chi}_1^{\pm}$		dE/dx trk	-	Yes	18.4	$\tilde{\chi}_1^{\pm}$	495 GeV	$m(\tilde{\chi}_1^{\pm})-m(\tilde{\chi}_1^0) \sim 160$ MeV, $\tau(\tilde{\chi}_1^{\pm}) < 15$ ns	1506.05332
Stable, stopped \tilde{g} R-hadron		0	1-5 jets	Yes	27.9	\tilde{g}	850 GeV	$m(\tilde{\chi}_1^0)=100$ GeV, $10 \mu\text{s} < \tau(\tilde{g}) < 1000$ s	1310.6584
Stable \tilde{g} R-hadron		trk	-	-	3.2	\tilde{g}	1.58 TeV	$m(\tilde{\chi}_1^0)=100$ GeV, $\tau > 10$ ns	1606.05129
Metastable \tilde{g} R-hadron		dE/dx trk	-	-	3.2	\tilde{g}	1.57 TeV	$m(\tilde{\chi}_1^0)=100$ GeV, $\tau > 10$ ns	1604.04520
GMSB, stable $\tilde{\tau}, \tilde{\chi}_1^0 \rightarrow \tilde{\tau}(\tilde{\nu}, \tilde{\mu}) + \tau(e, \mu)$		1-2 μ	-	-	19.1	$\tilde{\chi}_1^0$	537 GeV	$1 < \tau(\tilde{\chi}_1^0) < 3$ ns, SPS8 model	1411.6795
GMSB, $\tilde{\chi}_1^0 \rightarrow \gamma\tilde{G}$, long-lived $\tilde{\chi}_1^0$		2 γ	-	Yes	20.3	$\tilde{\chi}_1^0$	440 GeV	$7 < c\tau(\tilde{\chi}_1^0) < 740$ mm, $m(\tilde{g})=1.3$ TeV	1409.5542
GGM $\tilde{g}\tilde{g}, \tilde{\chi}_1^0 \rightarrow Z\tilde{G}$		displ. $ee/\mu\mu/\mu\nu$	-	-	20.3	$\tilde{\chi}_1^0$	1.0 TeV	$6 < c\tau(\tilde{\chi}_1^0) < 480$ mm, $m(\tilde{g})=1.1$ TeV	1504.05162
RPV	LFB $pp \rightarrow \tilde{\nu}_\tau + X, \tilde{\nu}_\tau \rightarrow e\mu/\tau\mu$	$e\mu, e\tau, \mu\tau$	-	-	3.2	$\tilde{\nu}_\tau$	1.9 TeV	$\lambda_{111}^0=0.11, \lambda_{132/133/233}=0.07$	1607.08079
	Bilinear RPV CMSSM	2 e, μ (SS)	0-3 b	Yes	20.3	\tilde{q}, \tilde{g}	1.45 TeV	$m(\tilde{q})=m(\tilde{g}), c\tau_{\text{LSP}} < 1$ mm	1404.2500
	$\tilde{\chi}_1^{\pm}\tilde{\chi}_1^{\mp}, \tilde{\chi}_1^{\pm} \rightarrow W\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow ee\nu, e\mu\nu, \mu\mu\nu$	4 e, μ	-	Yes	13.3	$\tilde{\chi}_1^{\pm}$	1.14 TeV	$m(\tilde{\chi}_1^0) > 400$ GeV, $\lambda_{12k} \neq 0$ ($k=1, 2$)	ATLAS-CONF-2016-075
	$\tilde{\chi}_1^{\pm}\tilde{\chi}_1^{\mp}, \tilde{\chi}_1^{\pm} \rightarrow W\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow \tau\nu_e, e\tau\nu_\tau$	3 $e, \mu + \tau$	-	Yes	20.3	$\tilde{\chi}_1^{\pm}$	450 GeV	$m(\tilde{\chi}_1^0) > 0.2m(\tilde{\chi}_1^{\pm}), \lambda_{133} \neq 0$	1405.5086
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow qq$	0	4-5 large- R jets	-	14.8	\tilde{g}	1.08 TeV	$\text{BR}(\tilde{g})=\text{BR}(b)=\text{BR}(c)=0\%$	ATLAS-CONF-2016-057
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow qq$	0	4-5 large- R jets	-	14.8	\tilde{g}	1.55 TeV	$m(\tilde{\chi}_1^0)=800$ GeV	ATLAS-CONF-2016-057
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow t\tilde{t}, \tilde{t}_1 \rightarrow bs$	2 e, μ (SS)	0-3 b	Yes	13.2	\tilde{g}	1.3 TeV	$m(\tilde{t}_1) < 750$ GeV	ATLAS-CONF-2016-037
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow bs$	0	2 jets + 2 b	-	15.4	\tilde{t}_1	410 GeV	$\text{BR}(\tilde{t}_1 \rightarrow b\ell/\mu) > 20\%$	ATLAS-CONF-2016-022, ATLAS-CONF-2016-084
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow b\ell$	2 e, μ	2 b	-	20.3	\tilde{t}_1	0.4-1.0 TeV	$\text{BR}(\tilde{t}_1 \rightarrow b\ell/\mu) > 20\%$	ATLAS-CONF-2015-015
	Other	Scalar charm, $\tilde{c} \rightarrow c\tilde{\chi}_1^0$	0	2 c	Yes	20.3	\tilde{c}	510 GeV	$m(\tilde{\chi}_1^0) < 200$ GeV

*Only a selection of the available mass limits on new states or phenomena is shown.

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Mass scale [TeV]

