

# Are Neutrinos different ?

## Outline (maybe for a longer talk ... )

- Who thought neutrinos should be massless?
- Neutrino masses: Majorana, Dirac ...
- $\nu_R$  ? Magnetic moments?
- Oscillations, free vs in matter
- Why don't we look for neutrino-antineutrino oscillations?
- How to generate mass
- Mass patterns ... a challenging model
- $R$  neutrinos put to use : leptogenesis – falsifiable by light  $W_R$
- $R$  neutrinos as Dark Matter and detection with light  $W_R$
- For fun... neutrino lensing

## Facts

- Masses are very small (one could even vanish) ; we only know the differences of their squares.
- « Cabibbo » mixing is important, might even be more complicated (extra phases if Majorana, mixing with steriles)
- We don't even know the number of degrees of freedom (Majorana vs Dirac)
- They violate the **separate** conservation of electron, muon and tau numbers

## Conjectures

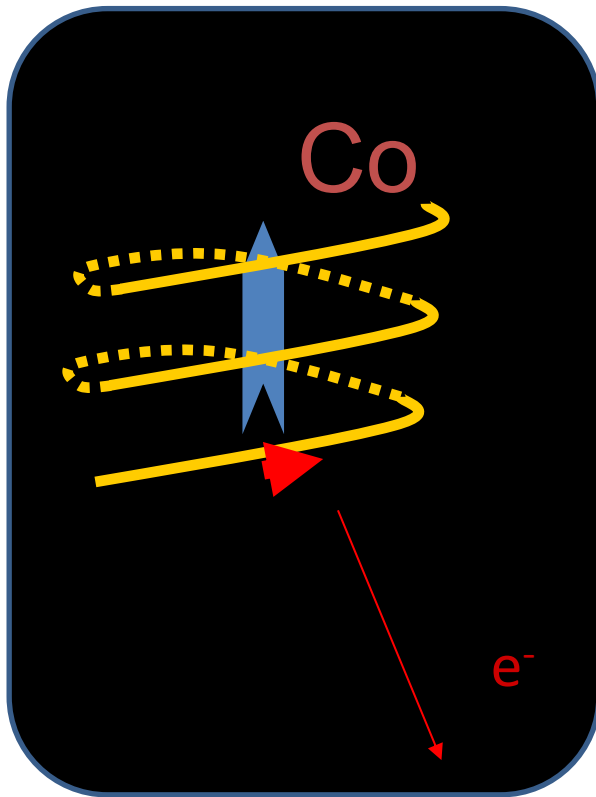
- *They might violate the **global** lepton number (neutrinoless double beta)*
- *they could explain the Defeat of Antimatter (leptogenesis)*
- *They suggest (via See-Saw or other) the presence of new particles, new scales, and could even accomodate extra dimensions*

They pester us with re-learning about  
Dirac, Majorana, degrees of freedom, oscillations, ...

while the rest of the fermions seem so simple  
by comparison!

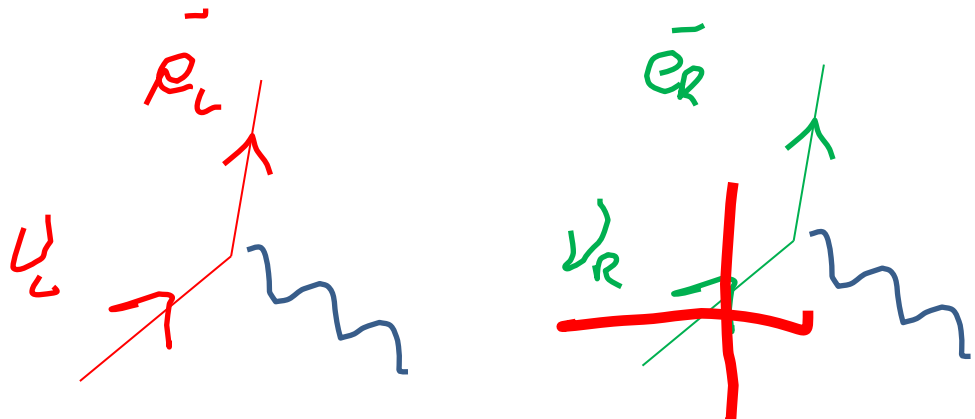
# Should neutrinos have been massless ?

*Once upon a time (has it completely ended? ) people used to blame P violation on the absence of right-handed neutrinos ...*

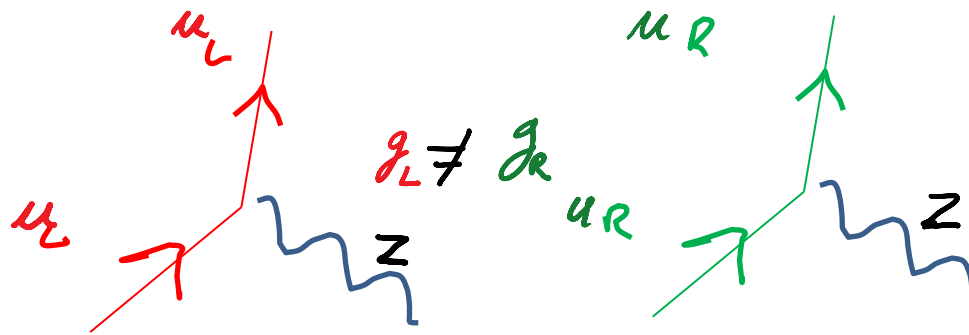


P violation was clearly demonstrated in the Wu experiment ..

It is easy to explain if only left-handed electrons are produced in a charged vector current.



*Killing the right-handed neutrino allows for parity violation in charged currents, even if the coupling is pure vector*



*Killing the right-handed neutrino allows for parity violation in charged currents, even if the coupling is pure vector*

**This was NEVER a solution ... Assuming the whole world to be symmetrical under P, and taking the right-handed neutrino as the BAD GUY was NO SOLUTION.**

- Not a solution today : we know the the Standard Model has neutral currents which violate P (parity violation in atoms, asymmetrical couplings of Z to quarks ..
- Even at the time of Wu's experiment, it was not a solution ... this experiment was only a confirmation, a demonstration of P violation, known from the  $K \rightarrow 2 \pi$  and  $K \rightarrow 3 \pi$  (the  $\Theta \tau$  puzzle )

*Still, in a way the doublet  $(\nu_L e_L)$  was at the basis of the Standard Model, but the actual symmetry was experimentally found to be  $SU(2)_L$ , applied to all known fermions, including quarks*

## From the «absence of $\nu_R$ » to « massless neutrinos »

The «absence of  $\nu_R$  » meant that « ordinary » (Dirac) masses were excluded ...

This fitted well the fact that very small neutrino masses (at least for the electron neutrino) were requested from  $\beta$  decay kinematics.

...and this lead to the legend that neutrinos had to be massless in the Standard Model

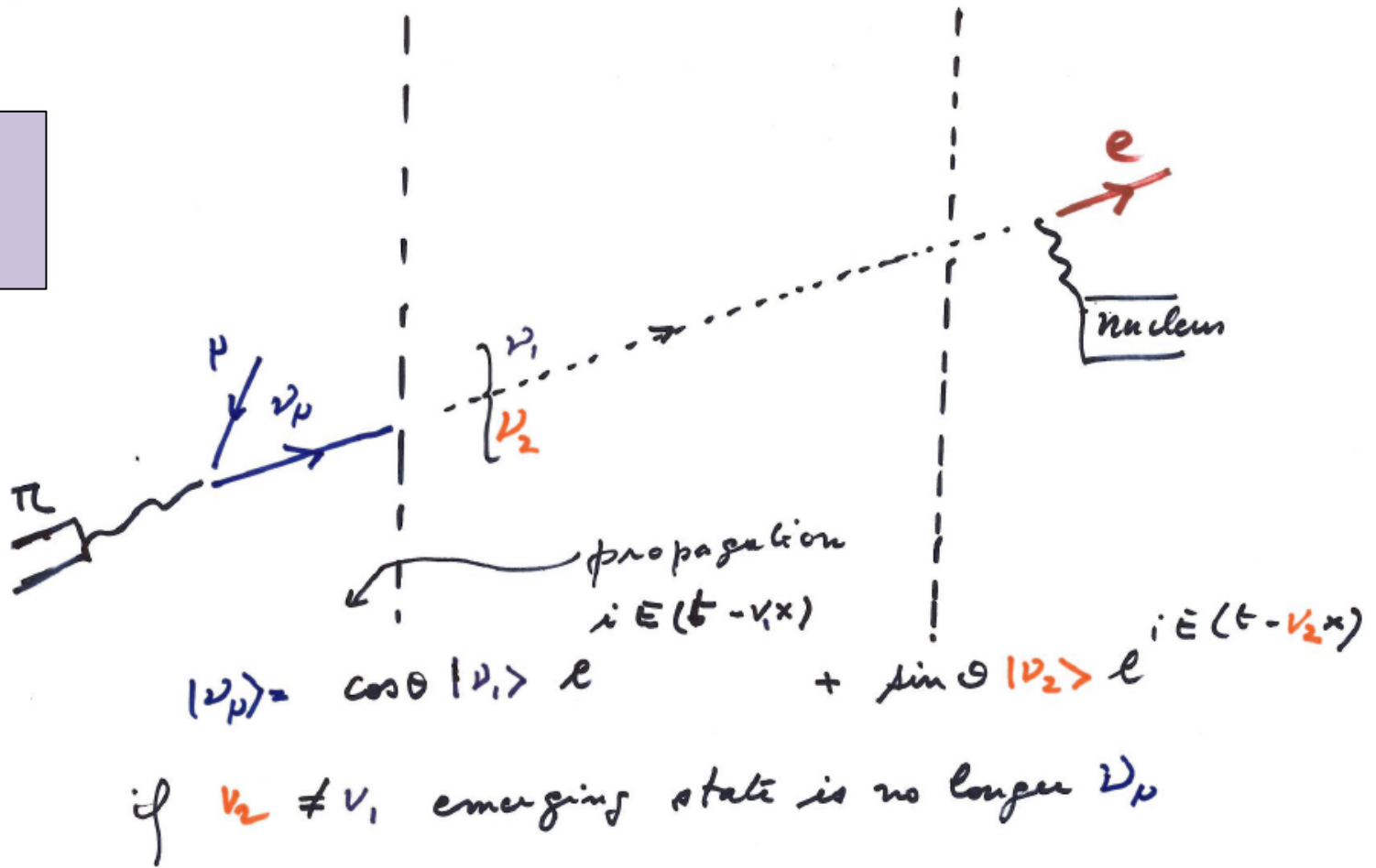
In fact, masses were simply omitted in the first version  
(which also lacked quarks, families, CP violation..)

But .. Evidence for neutrino masses!

But .. Evidence for neutrino masses! (?)

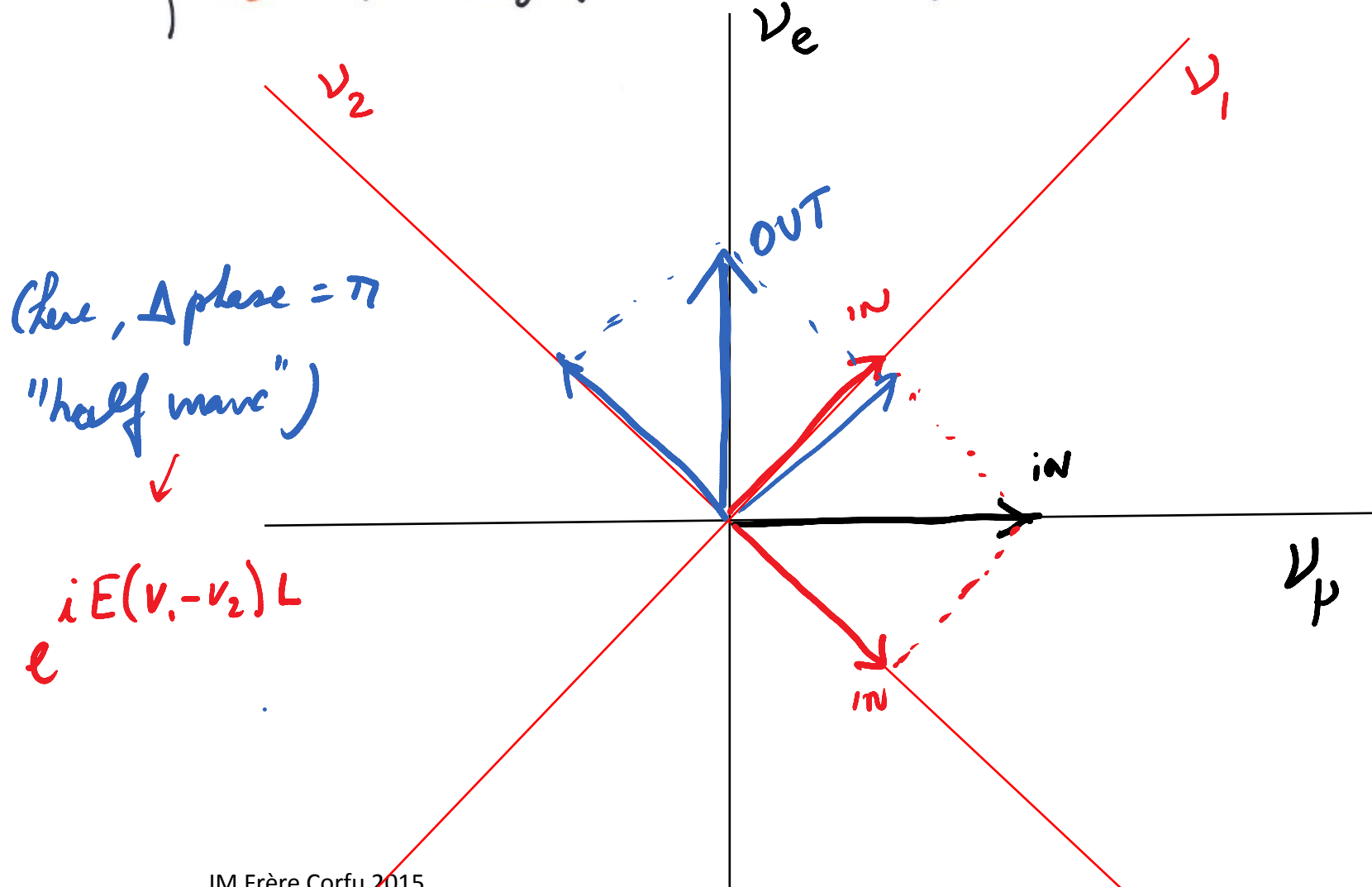
Neutrino oscillations prove that the « propagation states »  
are different from the « creation » and « detection » states.

See  
Polarization  
demo



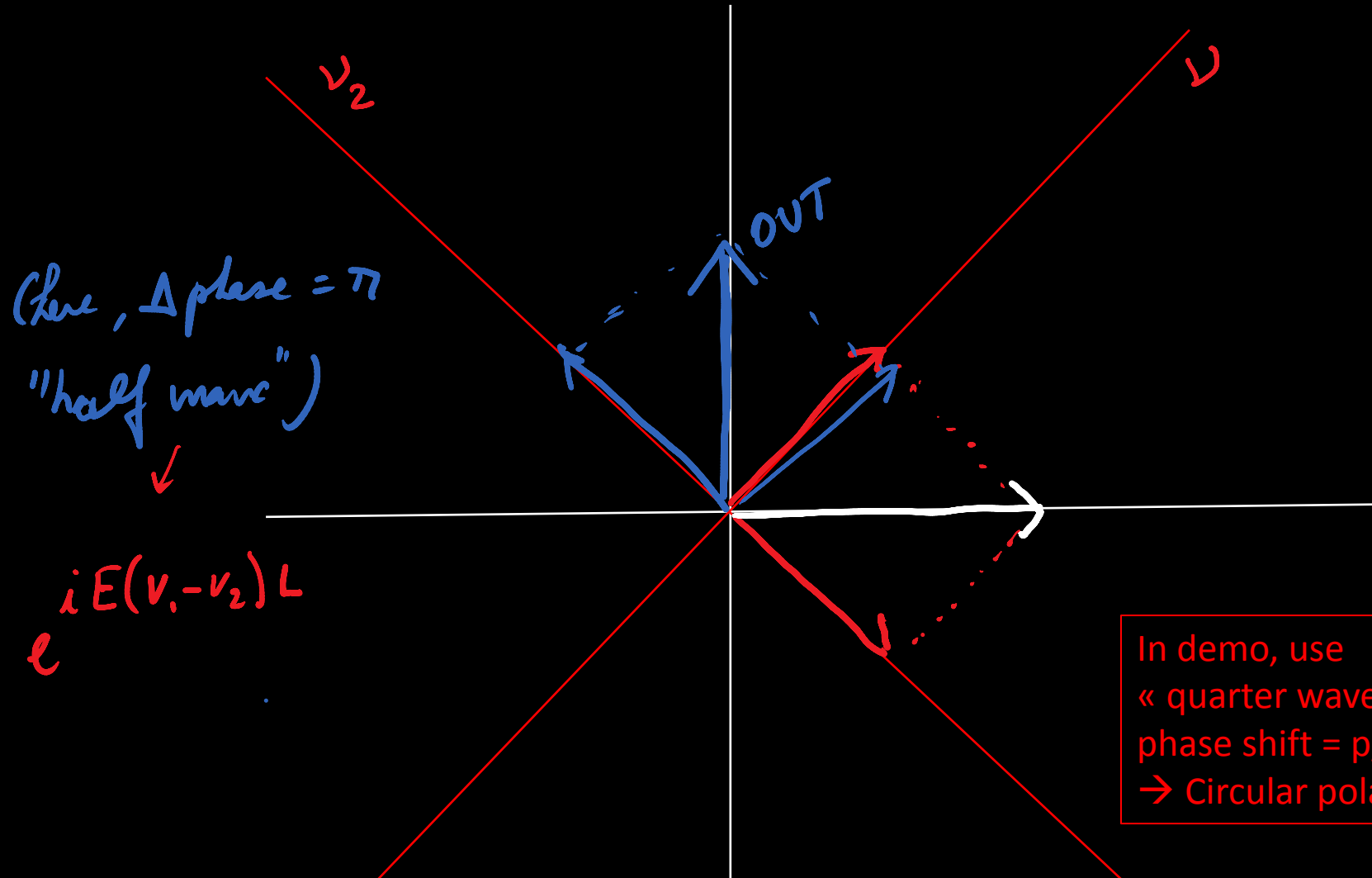
$$|\nu_p\rangle = \cos\theta |\nu_1\rangle e^{iE(t-\nu_1 x)} + \sin\theta |\nu_2\rangle e^{iE(t-\nu_2 x)}$$

if  $\nu_2 \neq \nu_1$ , emerging state is no longer  $\nu_p$





(almost) Black slide during demonstration



In demo, use  
« quarter wave plate »,  
phase shift =  $\pi/2$   
→ Circular polarization,

Why would be the propagation speed of neutrinos 1 and 2 differ?

It could be MASS,

$$\begin{aligned} E^2 &= \vec{p}^2 + m^2 \\ v &= |\vec{p}|/E \\ v &= \sqrt{1 - (m/E)^2} \\ (v_1 - v_2) L &= \frac{(m_2^2 - m_1^2) L}{2E} \end{aligned}$$

*The effect is the same for neutrinos and antineutrinos,  
does not depend on the type of mass (Majorana or Dirac)*

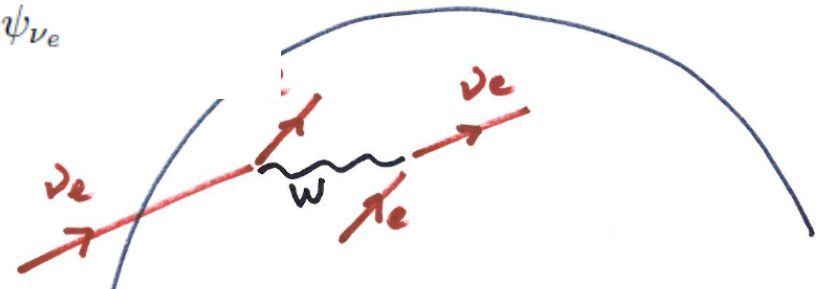
But also any kind of interaction affecting differently 1 and 2  
Well-known example : MSW effect

But also any kind of interaction affecting differently 1 and 2  
Well-known example : MSW effect

$$\begin{aligned} \text{Lagrangian} &\supset \bar{\psi}_{\nu_e}(p^0\gamma^0 - \vec{p}\cdot\vec{\gamma})\psi_{\nu_e} - V \\ V &\supset \kappa G_F \bar{\psi}_{\nu_e}\gamma^\mu\psi_e \psi_e\gamma_\mu\psi_{\nu_e} \end{aligned}$$

After Fierzing,

$$\begin{aligned} \kappa G_F \bar{\psi}_{\nu_e}\gamma^\mu\psi_e \psi_e\gamma_\mu\psi_{\nu_e} &= \kappa' G_F \bar{\psi}_{\nu_e}\gamma^\mu L\psi_{\nu_e}\psi_e \psi_e\gamma_\mu L\psi_e \\ &= \kappa'' \bar{\psi}_{\nu_e}\gamma^0 L\psi_{\nu_e} G_F \rho_e \end{aligned}$$



matter.

$\nu_e, \nu_\mu$   
 $\nu_{\text{sterile}}$   
have  $\neq$  interactions  
in matter.

This means that we simply replace  
 $(p^0)^2 - \vec{p}^2 = m^2$  by

$$E^2 - 2p^0\kappa''G_F - \vec{p}^2 = m^2$$

And get an effective mass ..

which differs for neutrino  
and antineutrino (CPT violation ...  
we interact with MATTER

$$m^2 \rightarrow m^2 + 2p^0\kappa''G_F\rho_e$$

$$\nu \quad p^0 > 0$$

$$\bar{\nu} \quad p^0 < 0$$

Even if we should keep in mind that interactions rather than masses can generate oscillations, let us now concentrate on masses.

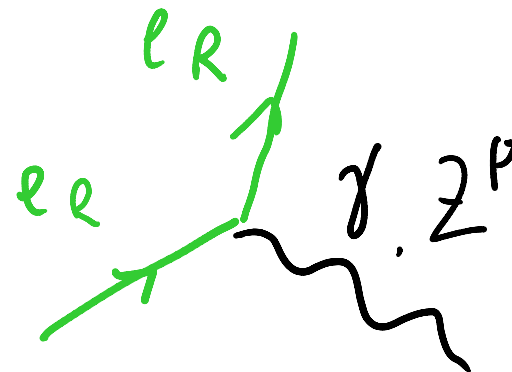
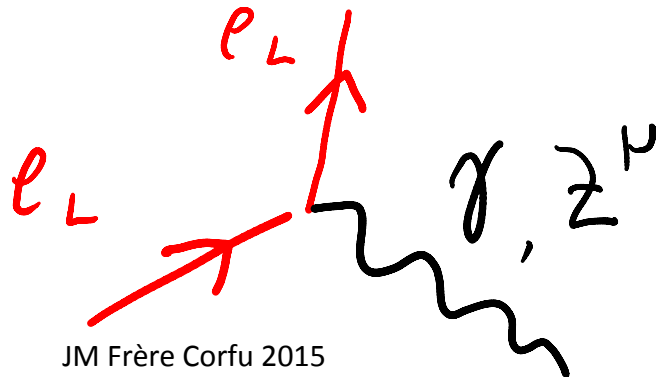
For questions of language, it is easier to speak of the electron + positron...

$$\begin{pmatrix} e_L \\ e_R \end{pmatrix} = \begin{pmatrix} e_{L1} \\ e_{L2} \\ e_{R1} \\ e_{R2} \end{pmatrix}$$

The Dirac spinor breaks down into 2 « Weyl » spinors,

$$\begin{pmatrix} \xi_L \\ \eta_R \end{pmatrix}$$

Gauge interactions talk separately to the L (left-handed) and R (right-handed)



$e_L$  Describes 2 things : the destruction of a L-handed electron and the creation of a R-handed positron

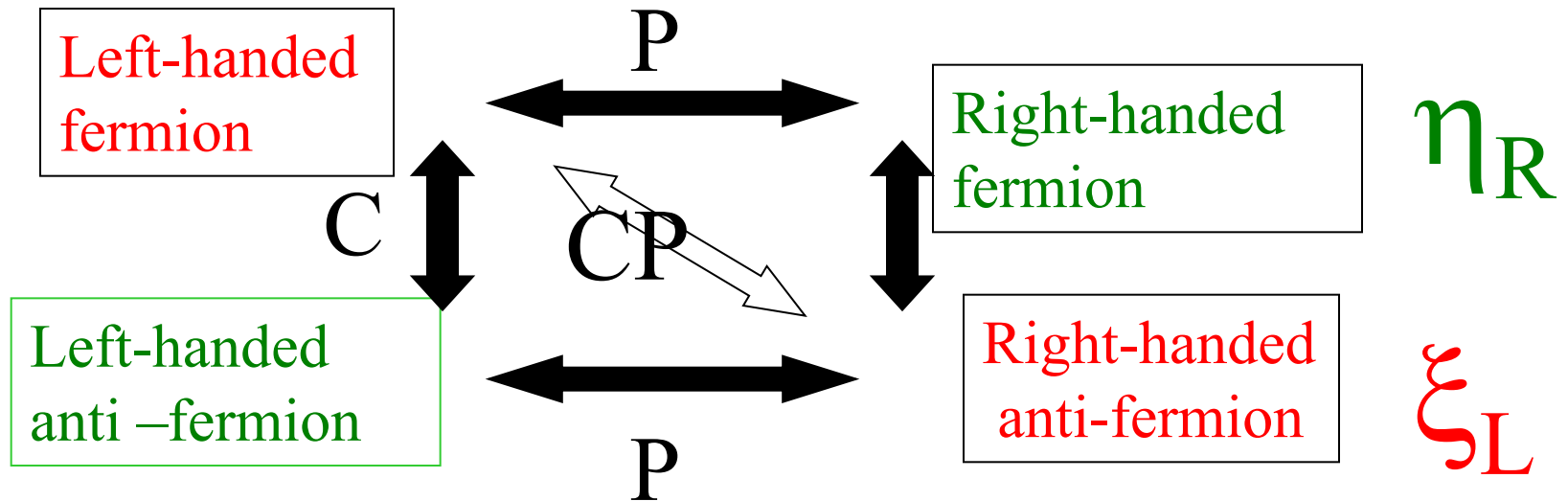
These 2 are CP conjugates (not C !)

$e_L$   $\longrightarrow$   $e_L^c$

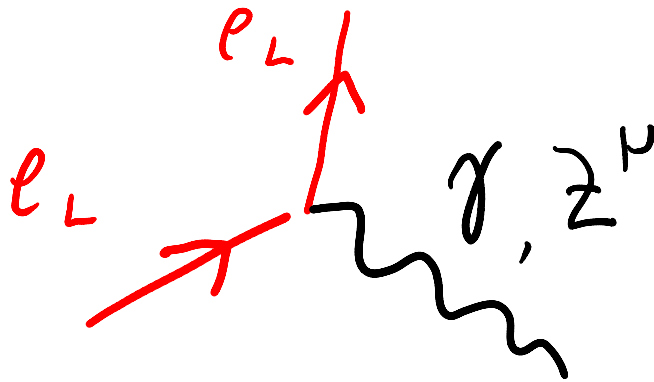
+

But  $e_L$  does not describe the other 2 states ..

JM Frère Corfu 2015



The simplest coupling only introduces the left-handed Weyl spinor, C and P are violated, but CP is conserved : this is THE symmetry of gauge interactions,



# How can we write a mass term ?

A « mass » term must be invariant under proper Lorentz transformations (but we don't impose P or C, which are broken in the SM).

Equations of motion must lead to

$$p^2 = |m|^2$$

$$\begin{pmatrix} \psi_L \\ 0 \end{pmatrix} = \begin{pmatrix} \psi_{L1} \\ \psi_{L2} \\ 0 \end{pmatrix} \quad \begin{pmatrix} \xi_L \\ 0 \end{pmatrix}$$

*We introduce here 2 spinors,  
We assume both to be L,  
(if not, perform a CP transformation)*

The Lorentz invariant then reads

$$\psi_{L1} \xi_{L2} - \psi_{L2} \xi_{L1} = \epsilon_{ij} \psi_{Li} \xi_{Lj}$$

... if we limit ourselves to rotations, this is just the spin singlet !

This expression covers ALL cases!

$$\uparrow \downarrow - \downarrow \uparrow$$

$$\psi_{L1}\xi_{L2} - \psi_{L2}\xi_{L1} = \epsilon_{ij} \psi_{Li}\xi_{Lj}$$

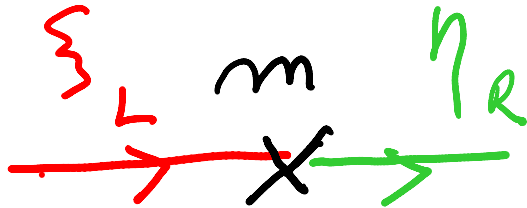
2 special cases :

$$\psi_L = \xi_L$$



$$\epsilon_{ij}\xi_{Li}\xi_{Lj}$$

Creates (or destroys) 2 units  
of fermionic number :  
« Majorana mass »



$$\psi_{Li} = \epsilon_{ik} \overline{\eta_{Rk}}$$

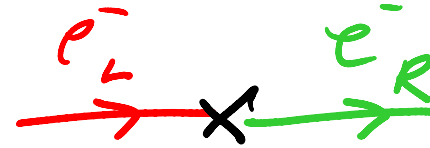
« Dirac mass term »

$$m \overline{\eta_{Rk}} \xi_{Lk}$$

If we can assign the same fermionic number  
to  $\eta$  and  $\xi$ ,  
Fermion number is now conserved



For the electron, only the « Dirac » mass term is allowed – the « Majorana » one does not even conserve electric charge!



On the other hand, for the neutrino, charge is not a problem, and we can use the « Majorana » mass. It violates leptonic number, but if the mass is small enough, this escapes detection.

It is thus possible to have Neutrino masses without introducing the right-handed neutrino

The sign (or phase) of the mass.



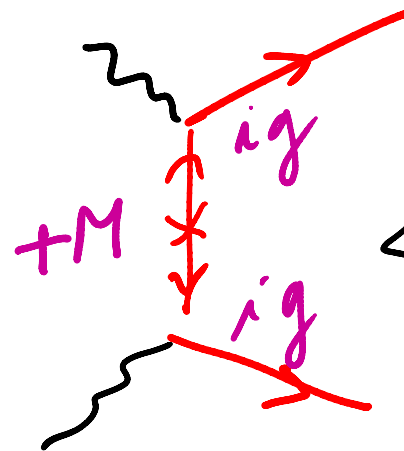
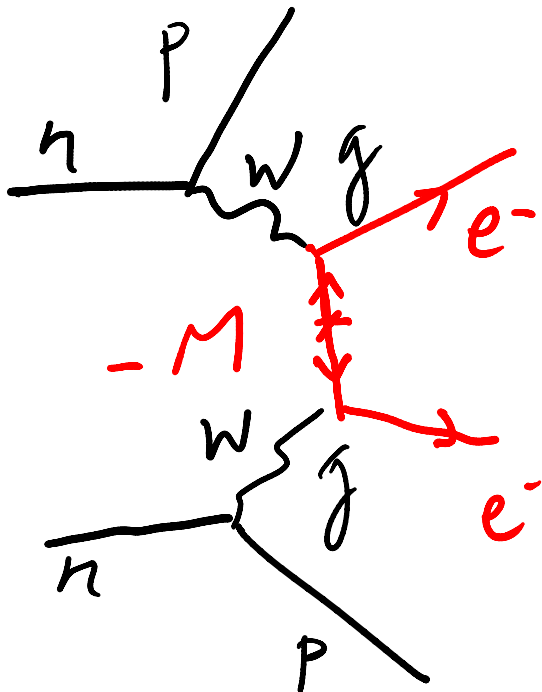
The parameter  $m$  in the Lagrangian is in general a complex number. In the case of one family, in the Dirac case, we can always re-define  $m$  to be real, just by changing the sign of  $\eta_R$ , which does not couple to anyone.

## The sign of the fermion mass – Majorana case

$$-M \quad \epsilon_{ij} \xi_{Li} \xi_{Lj}$$

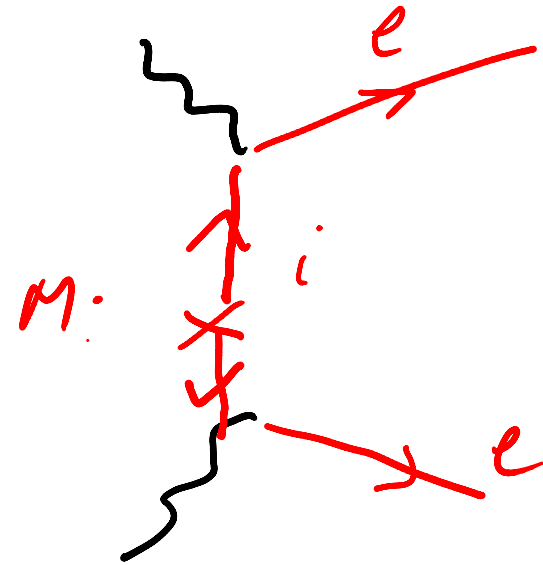
Here, we cannot re-define the sign of the mass without affecting the interactions ... we can bring  $m$  to be real by re-defining  $\xi \rightarrow i \xi$

But in any case, the sign of the amplitude remains



$$\Leftrightarrow \frac{-M g^2}{q^2 - M^2}$$

Neutrinoless Double Beta decay is sensitive to the weighted sum of masses, including Majorana phases



$$\sum \left( \frac{M_i}{q^2 - M_i^2} \cdot g^2 V_{ei}^2 \right)$$

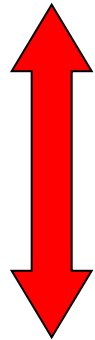
$$\sum M_i = 0$$

Special case : for one flavor,  
Dirac can be seen as 2 semi-spinors with  
equal but opposite masses and equal couplings

For later use : the cancellation occurs not in one family, but across families  
« Pseudo-Dirac »

An aside : A Dirac spinor can indeed be seen as the sum of 2 Majorana spinors of equal and opposite masses ..

$$m \bar{\Psi} \Psi$$



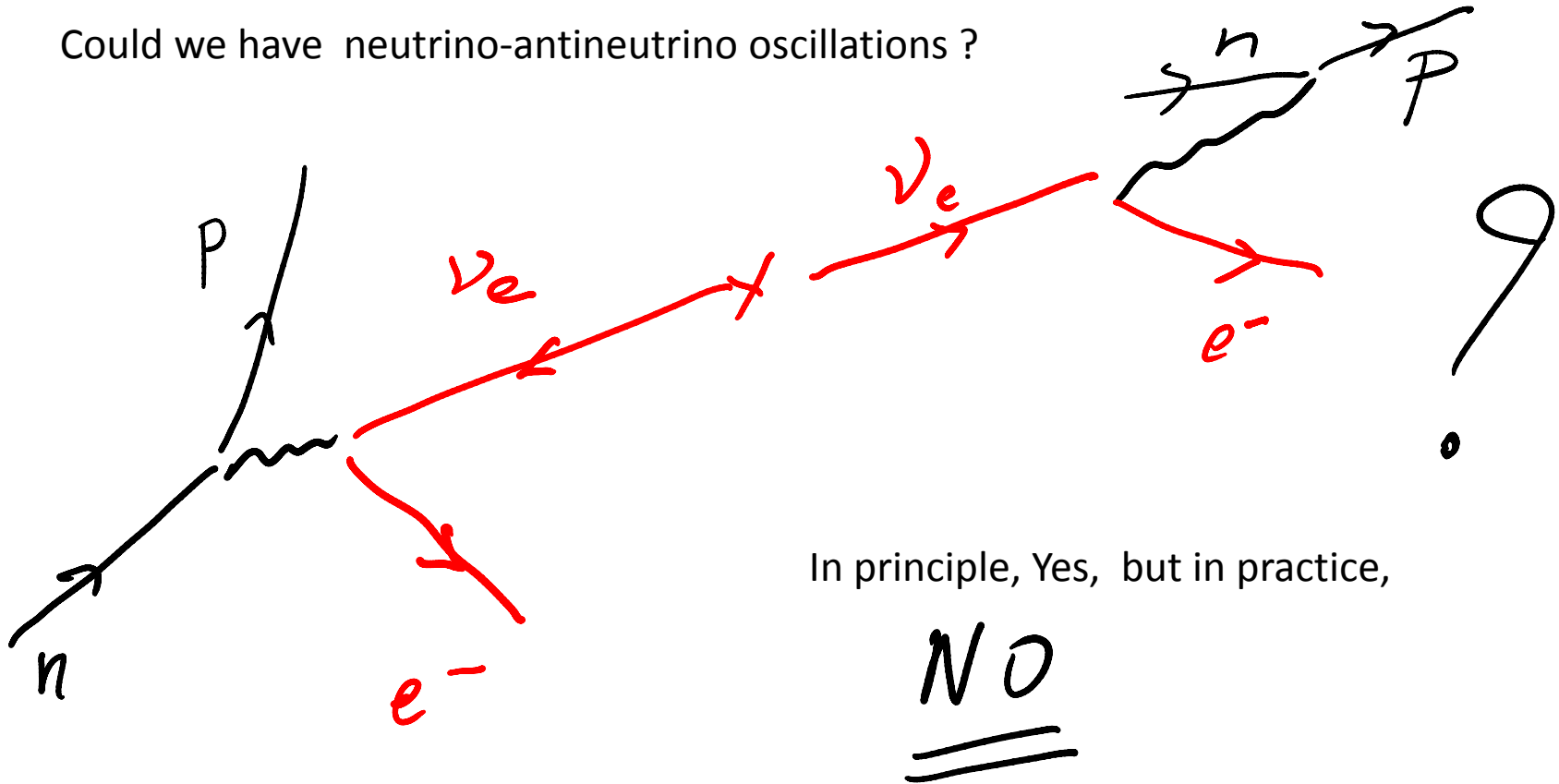
$$\chi = \frac{1}{\sqrt{2}}(\Psi + \Psi^c)$$

$$\lambda = i\frac{1}{\sqrt{2}}(\Psi - \Psi^c)$$

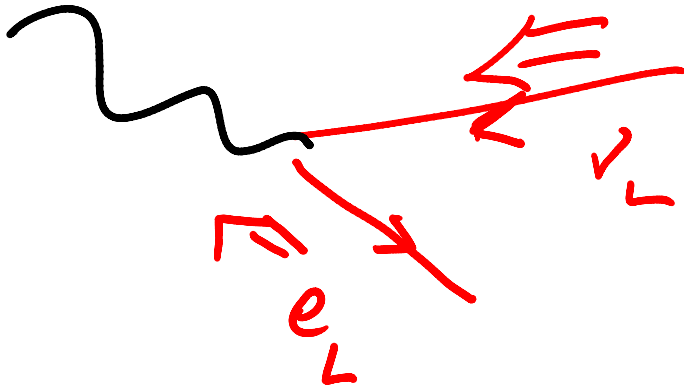
$$\frac{m}{2}\bar{\chi}^c\chi - \frac{m}{2}\bar{\lambda}^c\lambda$$

# Beyond the Neutrinoless Double beta decay, Can we probe the Majorana nature of neutrino masses?

Could we have neutrino-antineutrino oscillations ?

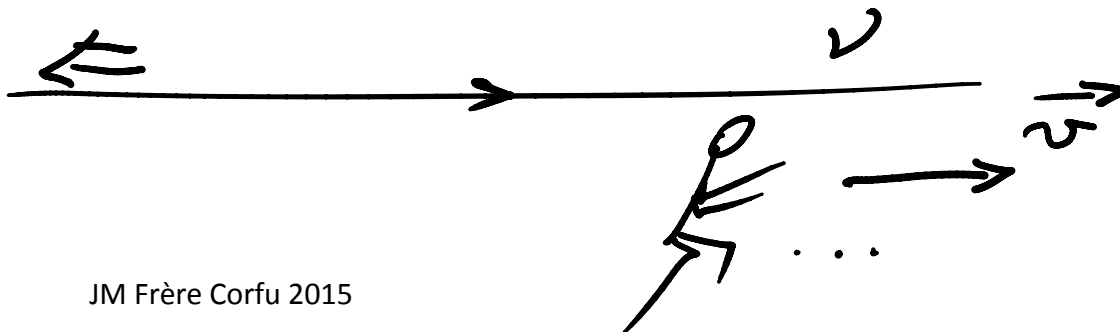


Even though the lepton number is not conserved, angular momentum suppresses this reaction

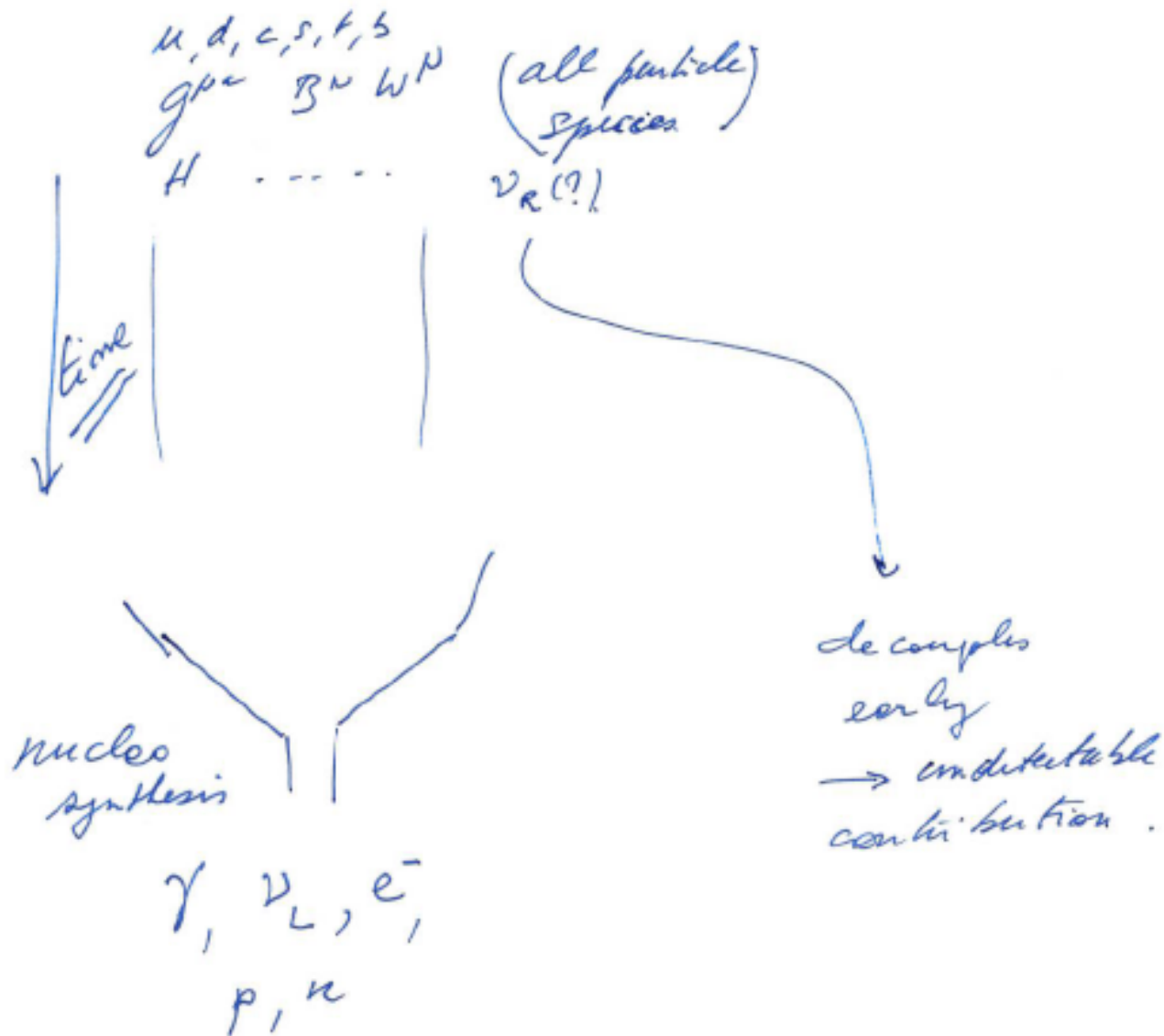


The  $\nu_L$  stays linked to  $e_L^-$ , and not to  $e_R^+$  by the  $W$ 's in the SM

*As long as the detector and emitter don't have large relative speeds (in comparison to the neutrino), helicity is conserved up to factor of  $m/E$  in amplitude. Even for 1MeV neutrinos, this gives a suppression of  $10^{-12}$  in probability*



# Could the cosmological counting of neutrinos help us ?





# Magnetic moments?

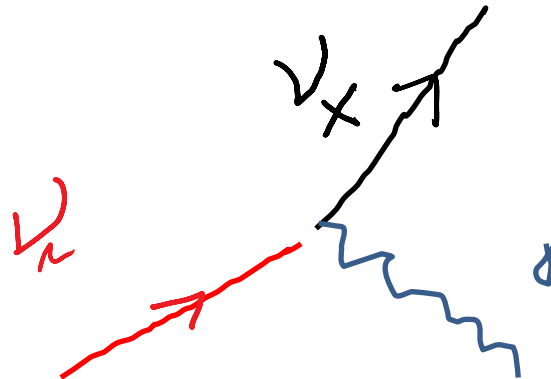
For ONE Weyl neutrino, a magnetic moment is forbidden by Fermi statistics ..

Is it a way to exclude Majorana masses?



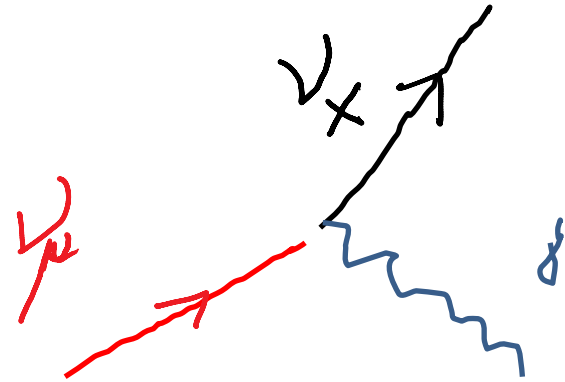
**NO**, TRANSITION magnetic moments are still allowed ...

and undistinguishable!



$$H_{\text{eff}} = \frac{\mu_{IJ}}{2} \bar{\nu}_I^c \sigma_{\alpha\beta} P_L \nu_J F^{\alpha\beta} + \text{h.c.},$$

effective  
moment  
for  $\nu_\mu$



$$\sqrt{|\mu_{e\mu}|^2 + |\mu_{\tau\mu}|^2} (\bar{\nu}_X^c \sigma_{\alpha\beta} \nu_\mu F^{\alpha\beta}),$$

$$\bar{\nu}_X^c \equiv \frac{(\mu_{e\mu} \bar{\nu}_e^c + \mu_{\tau\mu} \bar{\nu}_\tau^c)}{\sqrt{|\mu_{e\mu}|^2 + |\mu_{\tau\mu}|^2}}.$$

Effective electromagnetic moment for the muon neutrino :

$$|\mu_{\nu_\mu}| \equiv \sqrt{|\mu_{e\mu}|^2 + |\mu_{\tau\mu}|^2}$$

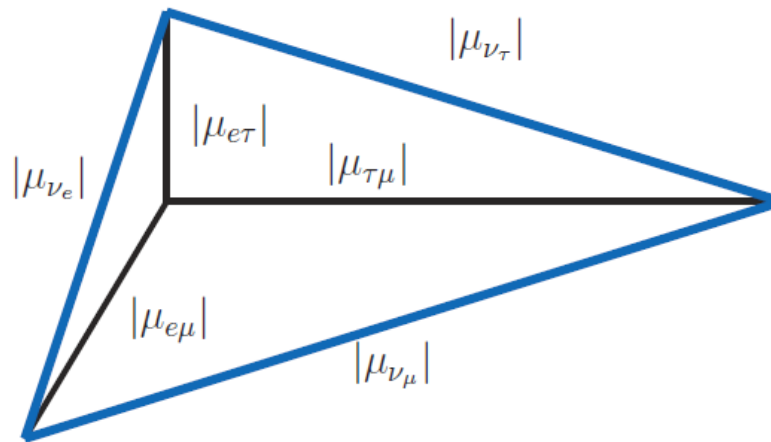


Figure 1:  $|\mu_{\nu_J}|$  forms a right triangle with  $|\mu_{IJ}|$  and  $|\mu_{KJ}|$  (for  $I \neq J \neq K$ ).  $|\mu_{\nu_{I,J,K}}|$  thus also form a triangle (shown in thick blue), in general not with right angles.

JMF, J Heeck, S Mollet arXiv:1506.02964 to appear in PRD

It is then easy to work out the inequalities ..

$$|\mu_{\nu_\tau}|^2 \leq |\mu_{\nu_e}|^2 + |\mu_{\nu_\mu}|^2 ,$$

$$|\mu_{\nu_\mu}|^2 \leq |\mu_{\nu_\tau}|^2 + |\mu_{\nu_e}|^2 ,$$

$$|\mu_{\nu_e}|^2 \leq |\mu_{\nu_\mu}|^2 + |\mu_{\nu_\tau}|^2 ,$$

These are stronger than the more obvious « triangle inequalities »:

(none of the angles can be  $> 90^\circ$ )  $||\mu_{\nu_J}| - |\mu_{\nu_K}|| \leq |\mu_{\nu_I}| \leq |\mu_{\nu_J}| + |\mu_{\nu_K}|$

Current limits (terrestrial)

$$|\mu_{\nu_e}| < 2.9 \times 10^{-11} \mu_B , \quad |\mu_{\nu_\mu}| < 6.8 \times 10^{-10} \mu_B , \quad |\mu_{\nu_\tau}| < 3.9 \times 10^{-7} \mu_B .$$

Perspectives : SHiP (CERN SPS ) could improve considerably the  $\tau$  neutrino limit ...

## Current limits (terrestrial)

$$|\mu_{\nu_e}| < 2.9 \times 10^{-11} \mu_B, \quad |\mu_{\nu_\mu}| < 6.8 \times 10^{-10} \mu_B, \quad |\mu_{\nu_\tau}| < 3.9 \times 10^{-7} \mu_B.$$

## Current limits (astrophysics – in fact sum over all neutrinos)

$$4.5 \times 10^{-12} \mu_B$$

Hopeless for terrestrial measurements?

NO ...

if there is a 4th light (sterile) neutrino, with mass  $> \text{keV}$ ,

astro limits don't apply

and a large electromagnetic moment could be observed ... SHiP is in business !

(by the way, light extra neutrinos are considered as components of Dark Matter...)

## Neutrinos masses in the Standard Model .. And a bit beyond...

The simplest...

Just treat them like other fermions,

Introduce  $\nu_R$  and a Yukawa coupling  $\lambda$

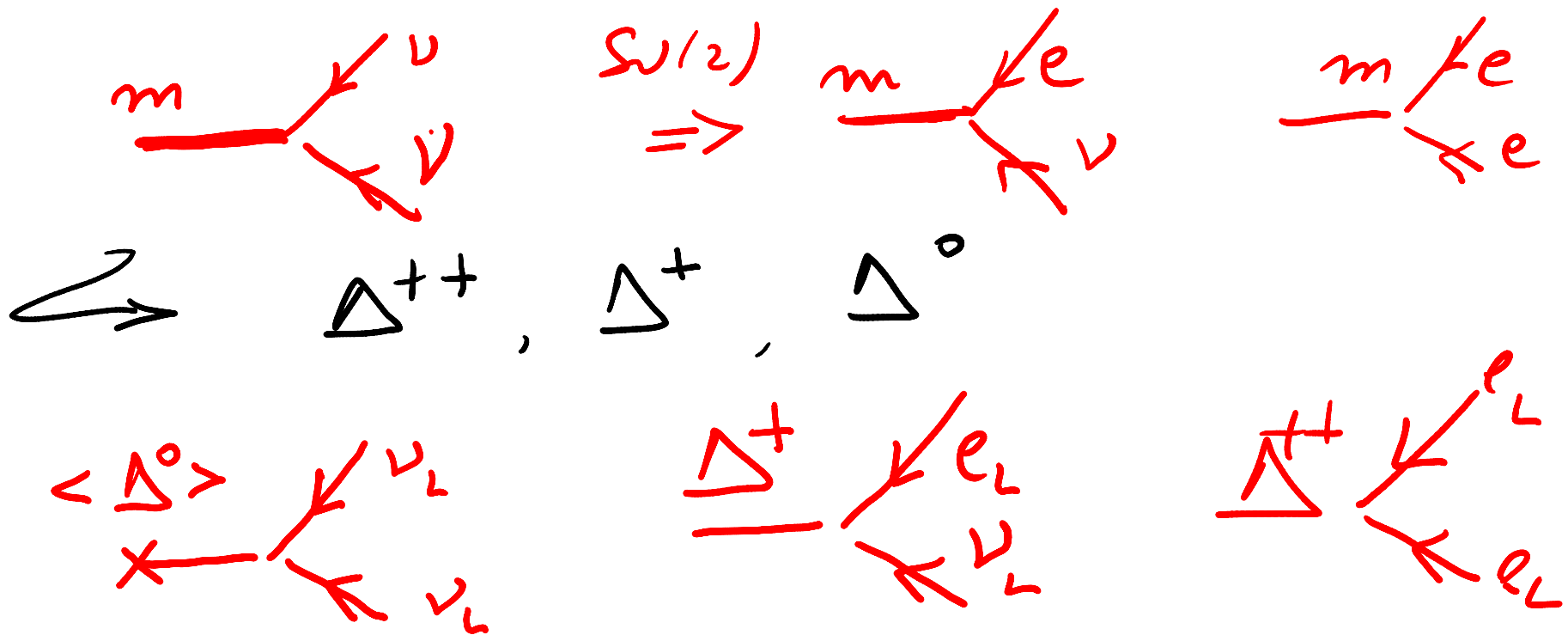
$$\lambda < m_\nu / m_W < 10^{-11}$$

A bit inelegant, but there are other large/small Yukawa ratios in the SM (top/ electron =  $3 \cdot 10^5$ )

In this context, the  $\nu_R$  is all but unobservable, as its sole role is in giving mass .

We can also try to do without the  $\nu_R$ , and use a Majorana mass for the sole  $\nu_L$

-- But such a term breaks SU(2) invariance, and we would need a scalar triplet, with a vev through spontaneous symmetry breaking.



Such a breaking  $V_L$  would upset the mass ratio  $W/Z$

But is acceptable if small enough, for instance ..

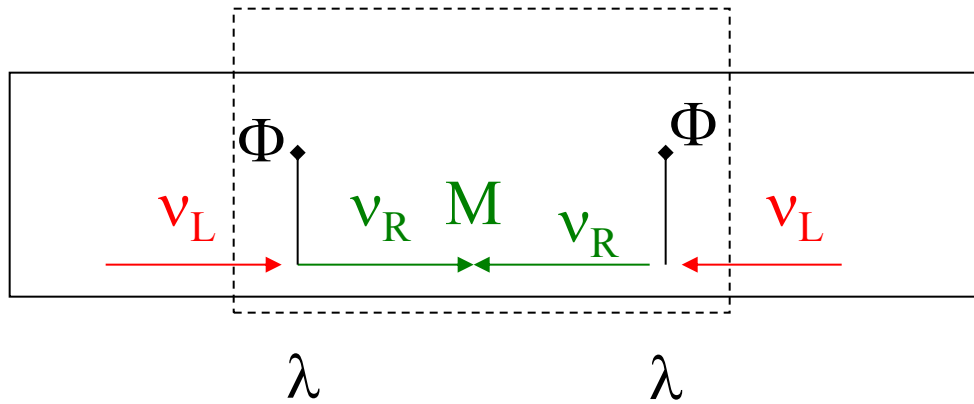
$$\langle \Delta^0 \rangle = v_L < v/100 \quad \frac{g v}{2} = m_W$$

This solution is not more costly in terms of « degrees of freedom » than the introduction of right – handed neutrinos, ... it deserves study at the LHC



## A poor man's triplet

We can build an « effective triplet » from the Standard Model doublet, and, right-handed neutrinos ..



**After diagonalization,**

**2 Weyl spinors**

**SU(2) imposes  $M_1 = 0$**

**For  $m = \lambda v \ll M_2 = M$  we get**

$$|m_1| \approx m/M^2$$

$$|m_2| \approx M$$

	$\xi_{Li}$	$\epsilon_{ik}\eta_{Rk}^+$
$\epsilon_{il}\xi_{Ll}$	$M_1$	$m$
$\eta_{Ri}^+$	$m$	$M_2$

$$\lambda_1 \approx \xi_L - m/M \epsilon \cdot \eta_R^+$$

$$\lambda_2 \approx \eta_R + m/M \epsilon \cdot \xi_L^+$$


$$\lambda_1 \approx \xi_L - m/M \epsilon \cdot \eta_R^+$$

$$\lambda_2 \approx \eta_R + m/M \epsilon \cdot \xi_L^+$$

We end up with something close to a low Majorana mass left-handed neutrino, In principle, such schemes could be differentiated from the triplet by the small admixture of the R mode , which leads to a departure from unitarity in the mixing matrix .. However such effects are of order  $m/M$  and thus unobservable.

Some models may make this presence detectable, they tend however to be quite artificial ... for instance :

« Double see-saw »

$$M_\nu = \begin{pmatrix} \overset{\nu_L}{0} & \overset{\nu_R}{m} & \overset{\nu_S}{0} \\ m^T & 0 & M^T \\ 0 & M & m_\sigma \end{pmatrix} \quad \xrightarrow{\text{2 singlets}}$$


$$m = \lambda v$$

$\lambda$  can then be large, and lead to observable effects, since the light neutrino mass is proportional to  $m_\sigma$

$$m_{\nu_1} \approx (m/M)^2 m_\sigma, \quad m_{\nu_{2,3}} \approx M \pm m_\sigma/2,$$

*(remark : this is an example of « pseudo-Dirac »,  
since  $\nu_R + \nu_S$  act as a Dirac pair, whose contributions to the light  
neutrino compensate.)*

(an old idea, .. Langacker, Mohapatra, Antoniadis, 1986-88, jmf+Liu,  
recently revived...)

## Mass models

Many attempts have been made at « predicting » or more often « postdicting » quark and lepton masses.

A frequent approach is based on « textures », for instance imposing a certain number of vanishing elements in the mass matrices (hopefully in a basis-independent way), possibly via discrete symmetries ( $A_3$ ,  $A_4$ ,...)

Most have failed. (and nobody predicted the top quark in non-suspect time).

A model inspired from extra dimensions

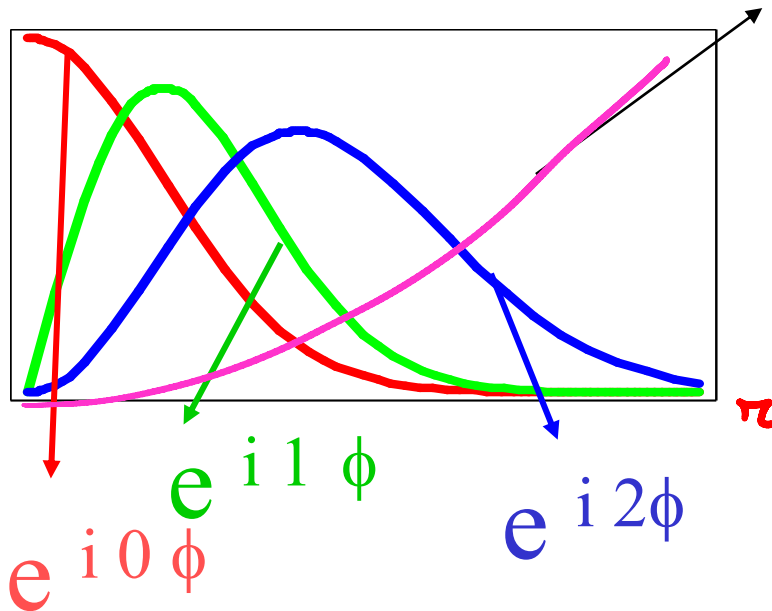
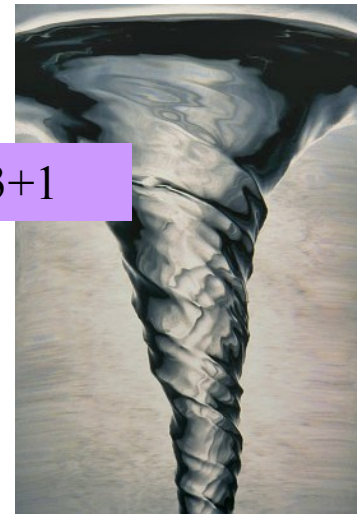
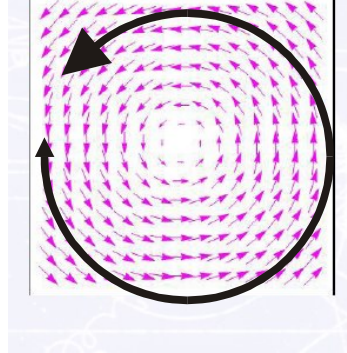
3+1 +2 dim

1family in 6D  $\rightarrow$  3 families in 4D

Vortex with winding number  $n$  localizes  $n$  chiral massless fermion modes in 3+1

Vortex Profile  $e^{i3\phi}$

$$\Phi = e^{i n \phi}$$



The 3 fermion modes have different shapes in  $r$ , and different winding properties in the extra dimension variable  $\phi$

Generic prediction (quarks) :

- nearly diagonal mass matrices
- Strong hierarchy of masses linked to the overlaps at the origin

**Generic prediction (neutrinos) :**

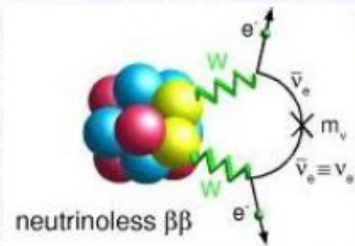
- **large mixings,**
- **inverted hierarchy**
- **suppressed neutrinoless double beta decay**

**Generic prediction :** large mixings,  
inverted hierarchy  
suppressed neutrinoless double beta decay

## NEUTRINOS MASSES

### Consequences of this structure

#### $0\nu\beta\beta$ decay

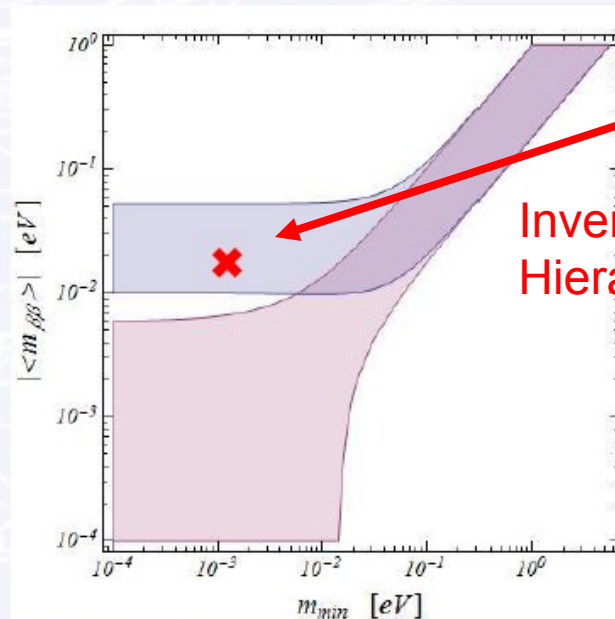


partial suppression

$$|\langle m_{\beta\beta} \rangle| \simeq \frac{1}{3} \sqrt{\Delta m_{\oplus}^2}$$

$$M_{\nu} \sim \begin{pmatrix} \cdot & \cdot & \times \\ \cdot & \cdot & \cdot \\ \times & \cdot & \cdot \end{pmatrix}$$

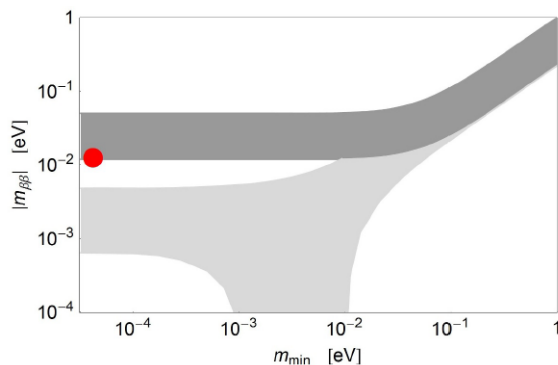
Automatically  
get



Inverted  
Hierarchy

Mass scale

Neutrino masses		
$m_1$	$5.46 \cdot 10^{-2} \text{ eV}$	—
$m_2$	$5.53 \cdot 10^{-2} \text{ eV}$	—
$m_3$	$4.17 \cdot 10^{-5} \text{ eV}$	—
$\Delta m_{21}^2$	$7.96 \cdot 10^{-5} \text{ eV}^2$	$(7.50 \pm 0.185) \cdot 10^{-5} \text{ eV}^2$
$\Delta m_{13}^2$	$2.98 \cdot 10^{-3} \text{ eV}^2$	$(2.47^{+0.069}_{-0.067}) \cdot 10^{-3} \text{ eV}^2$
Lepton mixing matrix		
$ U_{\text{PMNS}} $	$\begin{pmatrix} 0.76 & 0.63 & 0.13 \\ 0.39 & 0.58 & 0.72 \\ 0.52 & 0.52 & 0.68 \end{pmatrix}$	$\simeq \begin{pmatrix} 0.795 - 0.846 & 0.513 - 0.585 & 0.126 - 0.178 \\ 0.205 - 0.543 & 0.416 - 0.730 & 0.579 - 0.808 \\ 0.215 - 0.548 & 0.409 - 0.725 & 0.567 - 0.800 \end{pmatrix}$
$\langle m_{\beta\beta} \rangle$	$0.013 \text{ eV}$	$\lesssim 0.3 \text{ eV}$ [31]
J	$0.019$	$\lesssim 0.036$
$\theta_{12}$	$39.7^\circ$	$\simeq (31.09^\circ - 35.89^\circ)$
$\theta_{23}$	$46.5^\circ$	$\simeq (35.8^\circ - 54.8^\circ)$
$\theta_{13}$	$7.2^\circ$	$\simeq (7.19^\circ - 9.96^\circ)$



JM Frère Corfu 2015

*JMF, M Libanov, FS Ling, S Mollet, S Troitsky*

Note a non-vanishing  $\theta_{13}$  was predicted  
(in previous version) *before observation*



## Back to oscillations

3 families of neutrinos : 3 mixing angles, 1 « CKM-like » phase  
 IF Majorana : 2 additional phases (impossible to determine by oscillations,  
 only in neutrinoless double beta (and leptogenesis))

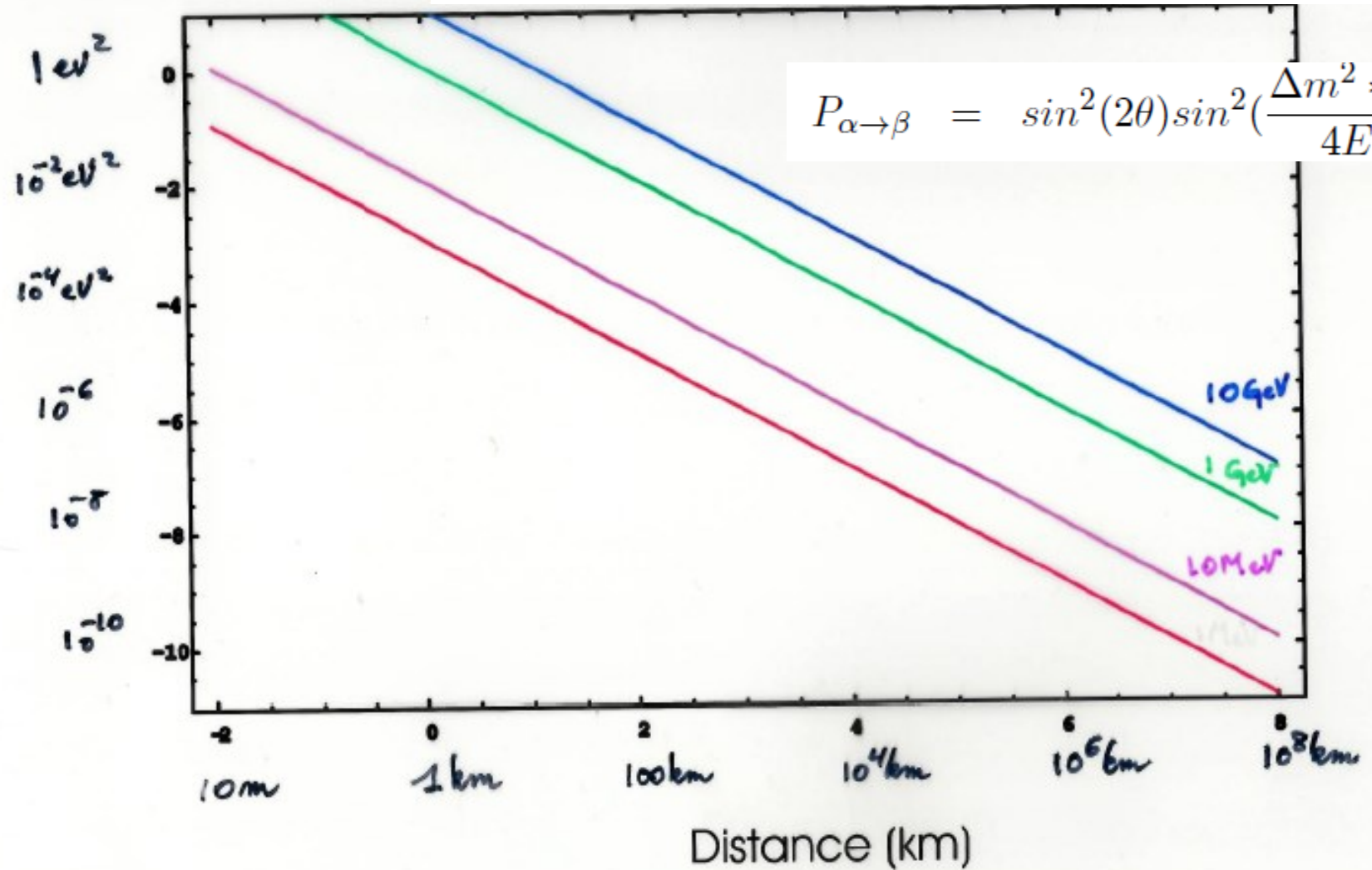
See Eligio Lisi's talk !

$$\begin{aligned}
 U &= \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix} \\
 &= \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_1/2} & 0 \\ 0 & 0 & e^{i\alpha_2/2} \end{bmatrix} \\
 &= \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_1/2} & 0 \\ 0 & 0 & e^{i\alpha_2/2} \end{bmatrix}
 \end{aligned}$$

(Pasted from wikipedia )

$\Delta m^2 \text{ (eV}^2\text{)}$

$$P_{\alpha \rightarrow \beta} = \sin^2(2\theta) \sin^2\left(1.27 \frac{\Delta m^2 * L}{4E} (\text{eV}^2 \text{ km/GeV})\right)$$



## Short distance oscillations, « Reactor anomaly »

At short distance (or  $\Delta m^2 = 1 \text{ eV}^2$ ) the situation is extremely confused, with contradictory claims from LSND, Mini-Boone, Karmen ..

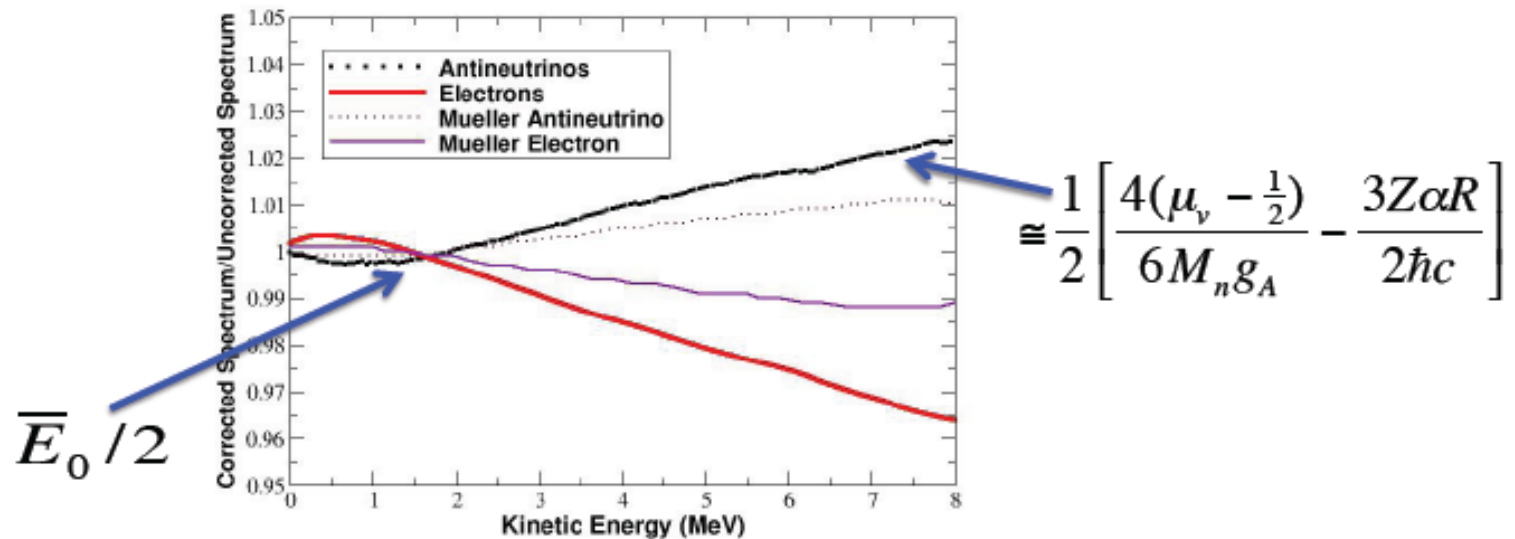
More recently, a re-examination of neutrino fluxes from nuclear power plants has led to the claim of an « anomaly » (approx. 5% more neutrinos expected than from previous calculations, and above observations).

**In fact, it is not really the NUMBER of neutrinos which changes, but their energy distribution.**

The following is based on Anna Hayes 's talk at Moriond 2015

<https://indico.in2p3.fr/event/10819/session/0/contribution/74/material/slides/0.pdf>

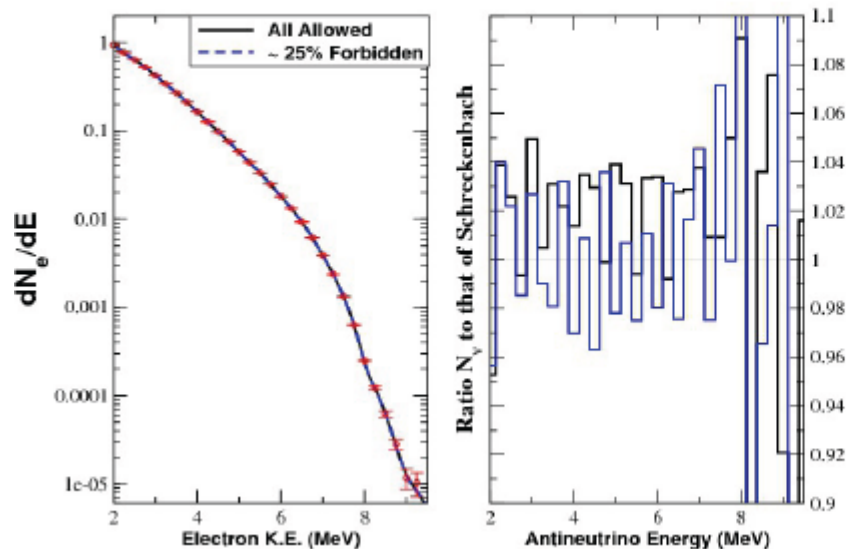
**If all forbidden transitions are treated as allowed GT, the corrections lead to an anomaly - the  $\nu_e$  spectrum is shifted to higher energy**



Based on Anna Hayes 's talk at Moriond 2015

<https://indico.in2p3.fr/event/10819/session/0/contribution/74/material/slides/0.pdf>

## Fit to Schreckenbach's beta spectrum



If all allowed:

$\Rightarrow +2.2\%$  antineutrinos

If 25% forbidden transitions

$\Rightarrow +0.06\%$  antineutrinos

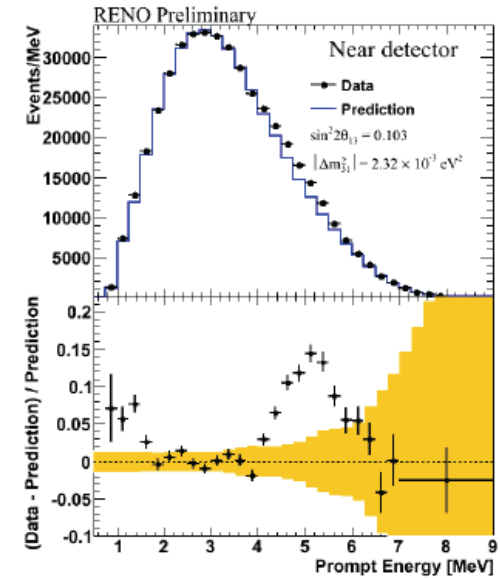
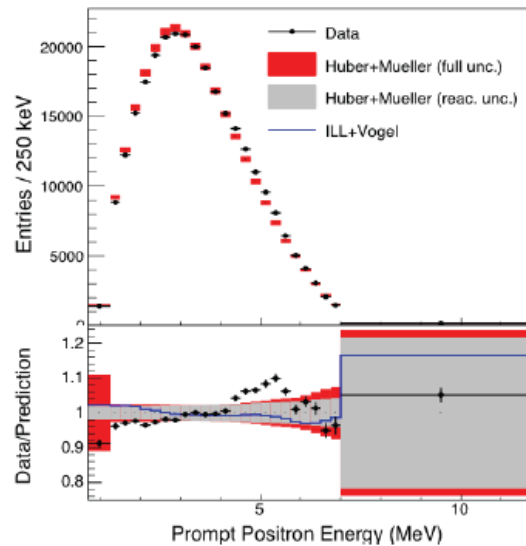
**Changes in the antineutrino spectrum range from 0-4%**

**Problem arises because of lack of knowledge on how to treat forbidden transitions**

Based on Anna Hayes 's talk at Moriond 2015

<https://indico.in2p3.fr/event/10819/session/0/contribution/74/material/slides/0.pdf>

**Significant Shoulder seen in the Near Detector at  $E_{\text{prompt}} \sim 4-6.5$  MeV  
at both Dayabay and RENO. Also seen in the far detectors**



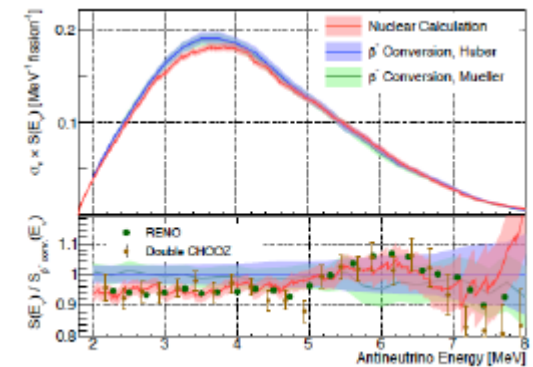
Not foreseen by the Muller  
and Huber calculations ..

Can be accounted for ..

Based on some data bases, but not others.

Dwyer+Langford, **arXiv:1407:1281**

The only way to know the neutrino flux  
measure it ... (2 detectors experiments)



Can we test the « fast oscillations » scheme?

$$P_{\alpha \rightarrow \beta} = \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 * L}{4E}\right)$$

$$P_{\alpha \rightarrow \beta} = \sin^2(2\theta) \sin^2\left(1.27 \frac{\Delta m^2 * L}{4E} (eV^2 m / MeV)\right)$$

To get a suppression by 5% with unresolved oscillations, need  
 $\sin^2(2\theta) > 0.1$

Could we get very fast oscillations (say  $< 1m$ ) which could escape planned detectors?

Would need  $m > 10 eV$  ... but with such large mixing, excluded by nucleosynthesis !

→ Currently built reactor experiments will tell us the answer !

# What are Right-handed neutrinos good for?

Heavy  $\nu_R$  ( $= N$ ) are found in grand unified theories like  $SO(10)$  and above,  
But are specially usefull for inducing the DEFEAT OF ANTIMATTER

CP violating decay creates  $L < 0$ , converted into  $B > 0$  by an anomaly-related mechanism (instantons)

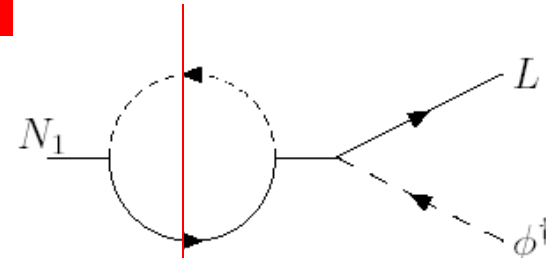
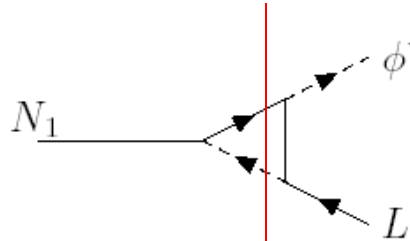
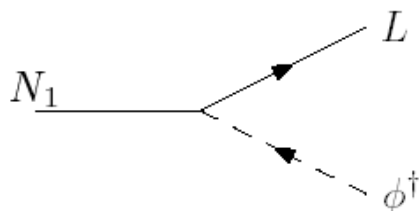


# How leptogenesis works....

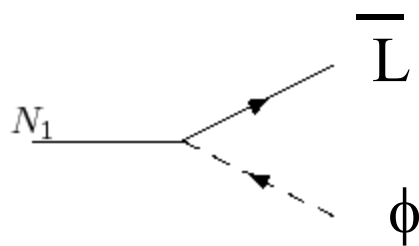
Assume that we have some population of heavy  $N$  particles...  
(either initial thermal population, or re-created after inflation) ; due to their heavy mass and relatively small coupling,  $N$  become easily relic particles.

## Generation of lepton number

$L = +1$



$N$  can decay to Lepton  $L + \phi^\dagger$  as above, or to the opposite channel  $\bar{L}\phi$



CP violation +  
Interference term leads  
to excess of  $L$  or anti- $L$

$L = -1$

Possible unitarity  
cuts

# Constraints:

Heavy neutrinos must decay out of equilibrium

$$\tau(X) \gg H^{-1}$$

$H = \dot{a}/a$  is the Hubble constant,

$$\tau^{-1} = \Gamma \cong g^2 M$$

$$H = \sqrt{g^*} \frac{T^2}{10^{19} \text{GeV}}$$

$g^*$  is the number of degrees of freedom at the time

at decay :  $T \approx M$  ,

Need enough CP violation;

for large splitting between neutrino masses, get

$$\epsilon_i^\phi = -\frac{3}{16\pi} \frac{1}{[\lambda_\nu \lambda_\nu^\dagger]_{ii}} \sum_{j \neq i} \text{Im} \left( [\lambda_\nu \lambda_\nu^\dagger]_{ij}^2 \right) \frac{M_i}{M_j}.$$

Some rough estimations...

...What are the suitable values of  $\lambda$  and  $M$ ?

Assume there is only one generic value of  $\lambda$  (in reality, a matrix)

$$\epsilon < \lambda^4 / \lambda^2 \approx \lambda^2 > 10^{-8}$$

$$m_\nu = m^2 / M \approx \lambda^2 / M \approx .01 eV$$

rough estimate of  $M$  scale  
(in GeV) needed...

similar to  $\tau$  lepton  $\longrightarrow$

At the difference of  
baryogenesis, the Yukawa  
matrix  $\lambda$  leaves a lot of  
freedom

$\lambda$	light neutrino .01 eV $M \sim$	decay out of equil. $M >$	enough CP viol
.0000 1	$10^7$	$10^8$	need tuning
.0001	$10^9$	$10^{10}$	
.001	$10^{11}$	$10^{12}$	
.01	$10^{13}$	$10^{14}$	
.1	$10^{15}$	$10^{16}$	
1	$10^{17}$	$10^{18}$	large

# Can leptogenesis be falsified ?

In general, no, since most mass ranges are inaccessible.

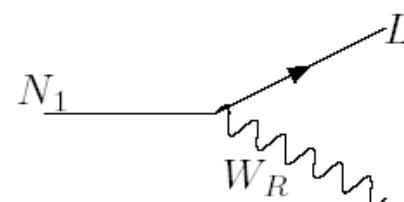
But .. Presence of  $\nu_R$  suggest a larger symmetry, like  $SO(10)$  or  $SU(2)_L \times SU(2)_R$

with the gauge inclusion

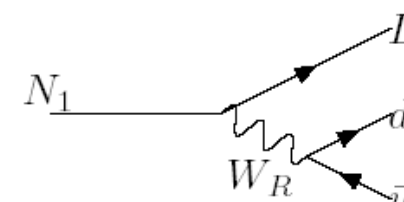
$$\epsilon_1 = \frac{\epsilon_1^0}{1 + X}$$

diluted CP asymmetry

$M_{W_R} < M_{N_1}$



$M_{W_R} > M_{N_1}$

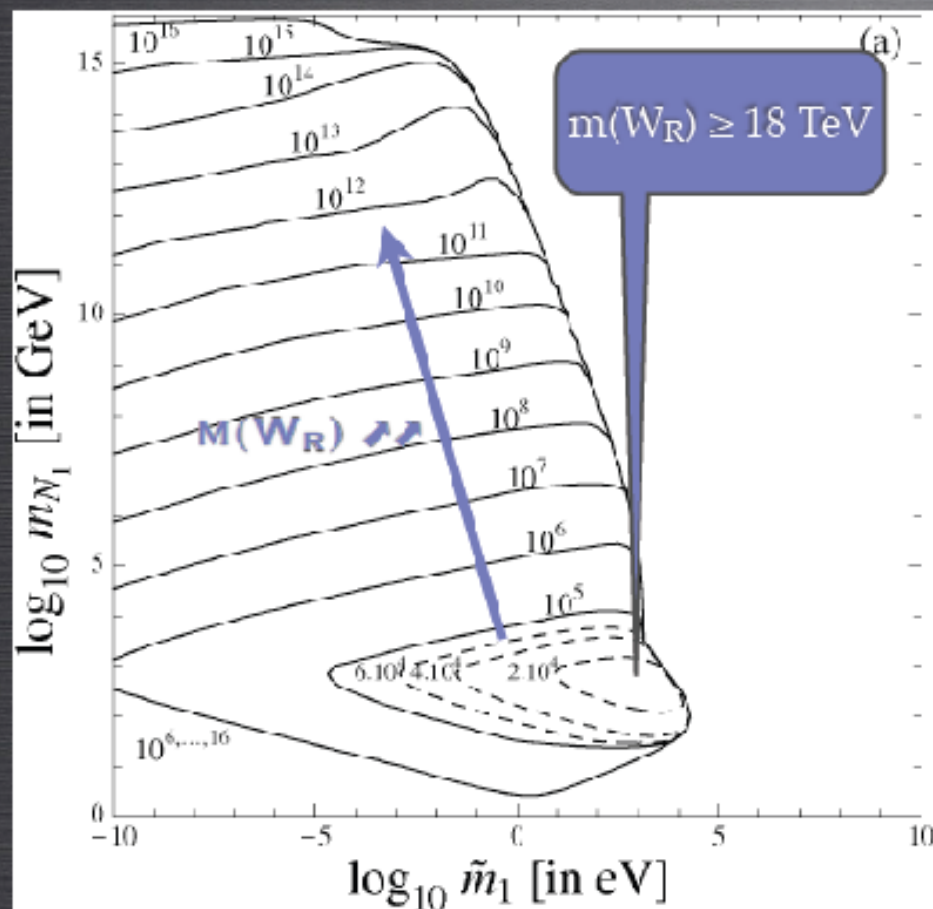


(competing effect : the presence of  $W_R$  allows a faster build-up of the  $N$  population after inflation)

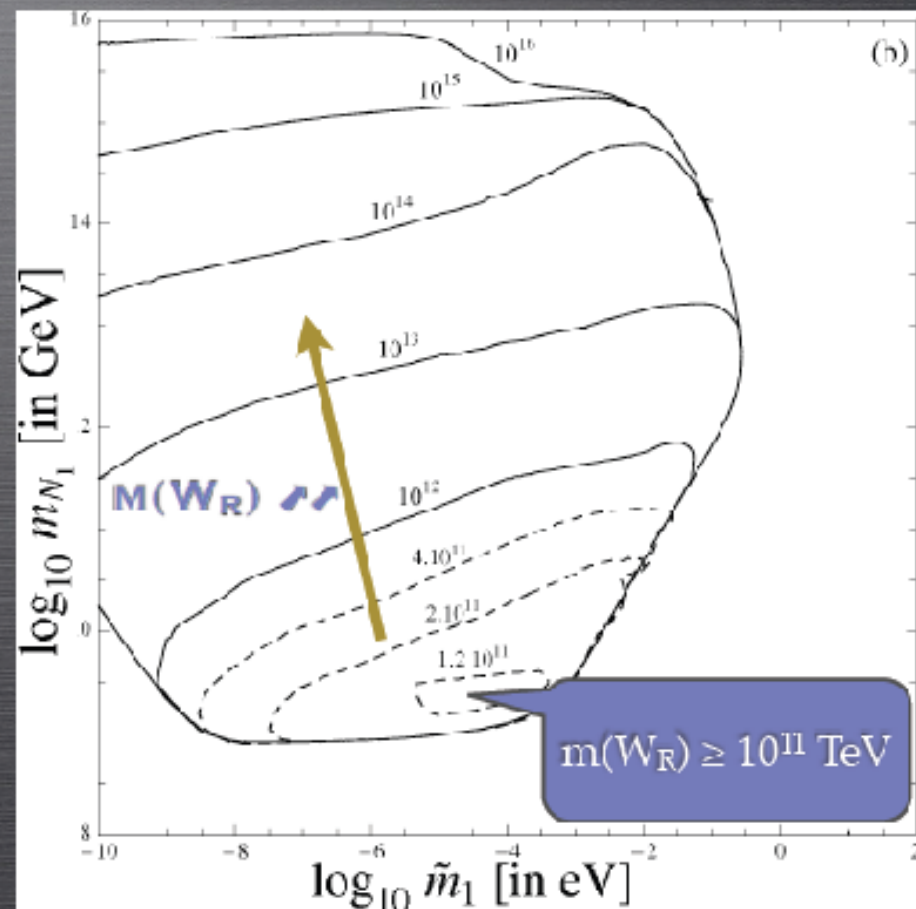
S Carlier, JMF, FS Ling **Phys.Rev. D60 (1999) 096003**  
 JMF, T Hambye, G Vertongen **JHEP 0901 (2009) 051**

# BOUNDS ON $M(W_R)$ & $M(N_R)$

FOR  $\epsilon_{CP} = 1$



FOR  $\epsilon_{CP} = \epsilon_{DI}$



See T Hambye's talk

CAN LHC DISPROVE LEPTOGENESIS ?

Updates : see Dev, Lee, Mohapatra 2014 ..

Leptogenesis is by far the most attractive way to generate the current baryon asymmetry,  
It is extraordinarily sturdy and resilient, and almost hopeless to confirm

BUT

finding a  $W_R$  at a collider near you would kill at least the « type 1 » leptogenesis (= through asymmetrical N decay)

probably the only realistic way to EXCLUDE simple leptogenesis !

Massive Neutrinos as dark matter:

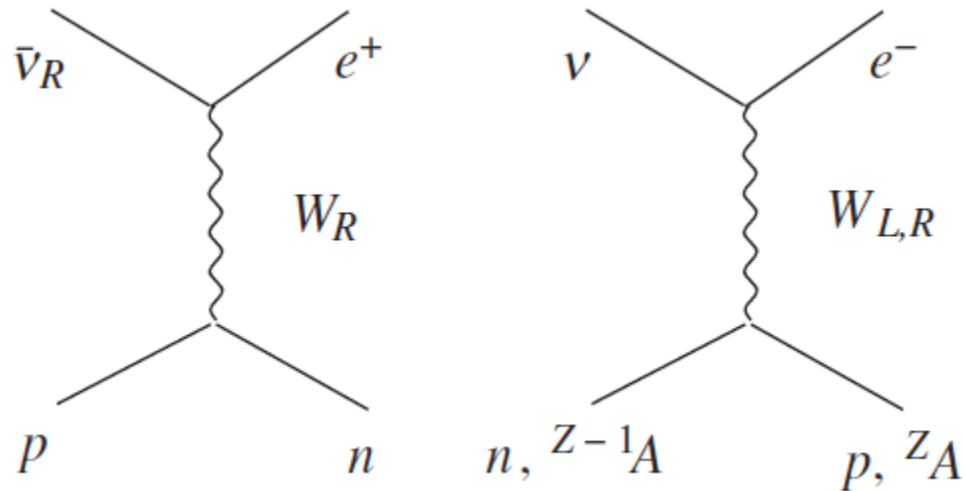
Could be constrained by Solar neutrino experiments ...

DM has little momentum, but the mass of the heavy neutrino triggers the reaction.

If light  $W_R$  present and MeV « heavy neutrino »

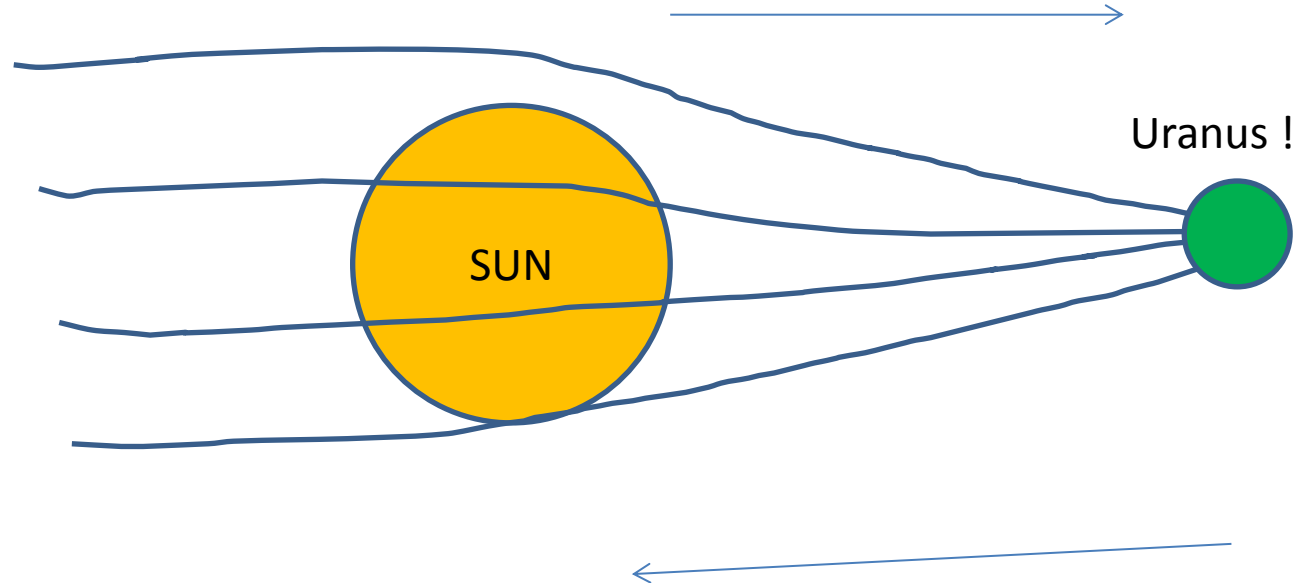
→ Limits .. For  $m_R$  MeV we obtain  $M_R = M_L > 10-20$ ,

JMF, L Lopez-Honorez, E Nezri, S Swillens, G Vertongen, *Phys.Rev. D75 (2007) 085017* [hep-ph/0610240](https://arxiv.org/abs/hep-ph/0610240)



## Just for the fun .. Neutrino lensing...

Stars are Gravitational lenses but bad lenses for light,  
But can be good lenses for neutrinos !



Also binary star as « neutrino  
light house »