

Large N Graviton Scattering and Black Hole Formation

DIETER LÜST (LMU-München, MPI)



Workshop on Particles and Cosmology (TR33_meeting), Corfu, 14th. Sept. 2015

Sonntag, 13. September 15



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Work in collaboration with Gia Dvali, Cesar Gomez, Reinke Isermann and Stephan Stieberger, arXiv: 1409.7405

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Outline:

I) Unitarity in graviton scattering and black hole production

II) Large N graviton scattering amplitudes at high energies in field and string theory

III) Summary

Quantum mechanics:

- Complementary picture:
 - Wave \Leftrightarrow N particles

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Semiclassical limit: $\hbar = \text{const.}, \quad N \to \infty$ Distances can be still arbitrarily short and energies can be arbitrarily high.

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In quantum gravity and in string theory some of these statements have to be refined.

In particular two questions and puzzles:

• What is the quantum nature of Black Holes ?

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⇒ Classicalization & the black hole N-portrait

What is the high energy behavior of graviton scattering amplitudes ?

Unitarity at tree level ?

Classicalization & the black hole N-portrait:

[G. Dvali, C. Gomez,]

• Are described by IR physics,

.. where there is no need to modify gravity in the IR

Quantization of gravity in IR \leftrightarrow semiclassical regime.

Classicalization & the black hole N-portrait:

[G. Dvali, C. Gomez,]

• Are described by IR physics,

where there is no need to modify gravity in the IR
 Quantization of gravity in IR ↔ semiclassical regime.
 However there remain still some UV problems:

• Precise coefficient coefficient in black hole entropy:

$$\mathcal{S} = egin{array}{ccc} rac{1}{4} & rac{A}{L_P^2} \end{array}$$

• Renormalization, UV finiteness of loop amplitudes

New UV degrees of freedom String theory !

Graviton scattering:



It is known that tree level graviton scattering amplitudes grow like s (center of mass energy). \Rightarrow Violation of unitarity at $s = M_P^2$

One possible solution: Wilsonian approach:

Amplitude is unitarized by integrating in new weakly coupled degrees of freedom of shorter and shorter wave lengths (at higher and higher energies). However it is expected that black holes will be produced in particle scattering processes with high energies of the order

$$\sqrt{s} > R_s^{-1} \equiv (\sqrt{s}L_P^2)^{-1}$$

[´t Hooft (1987);Antoniadis,Arakani-Hamed,Dimopoulos, Dvali (1998); Banks, Fischler (1999); Dimopoulos, Landsberg (2001);Yoshino, Nambu (2002); Giddings,Thomas (2002); Eardley, Giddings (2002); Giddings, Rychkov (2004); ...]

Classicalization: Amplitudes get unitarized by classical black hole formation.

[G. Dvali, C. Gomez (2010); G. Dvali, G. Giudice, C. Gomez, A. Kehagias (2010)]

(Gravity protects itself at high energies by black hole formation.)

So we need a better understanding of how black holes are formed in graviton scattering amplitudes.

Black hole corpuscular N-portrait:

Quantum black hole = Bound state of N gravitons

(Bose-Einstein condensate)

[G. Dvali, C. Gomez (2011 - 2014); G. Dvali, C. Gomez, D.L. (2012)]

Black hole corpuscular N-portrait:

Quantum black hole = Bound state of N gravitons (Bose-Einstein condensate)

Relevant properties: [G. Dvali, C. Gomez (2011 - 2014); G. Dvali, C. Gomez, D.L. (2012)]

- N is large and the gravitons are soft.
- Interaction strength among individual gravitons is small: $\alpha = \frac{L_P^2}{R^2} << 1 \qquad (R \ ... \ graviton \ wave \ length)$
- Collective (`t Hooft like) coupling: $\lambda = lpha N$
- Black holes are formed at the quantum critical point:

$$\lambda = 1$$

Black hole bound state (at $\lambda = 1$):

- Mass and size: $M_{BH} = \sqrt{N}M_P$, $R_{BH} = \sqrt{N}L_P$
- Exponential degeneracy, entropy: $\mathcal{S} \sim N$
- Semiclassical behavior: $N \to \infty$



Black hole bound state (at $\lambda = 1$):

- Mass and size: $M_{BH} = \sqrt{NM_P}$, $R_{BH} = \sqrt{NL_P}$
- Exponential degeneracy, entropy: $\mathcal{S} \sim N$
- Semiclassical behavior: $N \to \infty$



Can we reconcile this picture in graviton scattering processes (expressed in terms of N and λ)?

Is there a signal of non-perturbative black hole physics in perturbative graviton amplitudes?

So far: computation of graviton N-point amplitudes with small N (N=4).

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Our paper: new look at graviton scattering at trans-Planckian energy

 Explicit calculation of field theory and string amplitudes in a new kinematical large N regime, relevant for black hole production:

 $2 \longrightarrow N$ with $N \rightarrow \infty$

• We will argue that the perturbative $2 \longrightarrow N$ amplitude indeed contains relevant non-perturbative information supporting the picture of black hole production and classicalization.

Crossing the UV barrier:

The 2 \rightarrow N string amplitude exhibits an interesting transition property:

- Soft final gravitons: Unitarization by black holes.
- Hard final gravitons: Unitarization by string Regge states.

New trans-Planckian cross-over energy scale:

$$E_{\rm IR/UV} = NM_{\rm string}$$

II) Large N Graviton Scattering Amplitudes

 $2 \longrightarrow N$ graviton amplitude with high center of mass s:

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 $2 \longrightarrow N$ graviton amplitude with high center of mass s:



(i) Field theory

To compute the graviton scattering amplitudes one can try on-shell methods and KLT techniques. [Kawai, Lewellen, Tye (1986)],

<u>Problem:</u> KLT uses a double sum over (N-3)! squares of Yang-Mills amplitudes => in practice very hard to perform $N \to \infty$ limit

Instead we use CHY formula for N-graviton amplitude

Compact formula for tree-level gravitational S-matrix $\,M_N\,$ in arbitrary dimensions

$$M_N = \int \frac{d^N \sigma}{\operatorname{Vol} SL(2, \mathbf{C})} \prod_{a=1}^N \delta \left(\sum_{b \neq a} \frac{s_{ab}}{\sigma_a - \sigma_b} \right) E_N^2(\{k, \xi, \sigma\})$$

integral over delta-function support certain determinant (Pfaffi N-punctered sphere on solutions of encoding external momen scattering equations and polarizations *E*

Sonntag, 13. September 15

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Scattering equations:

$$\sum_{b \neq a} \frac{s_{ab}}{\sigma_a - \sigma_b} = 0$$

$$(N-3)!$$
 solutions

relate space of kinematic invariants of N gravitons to that of the positions of N points on a sphere [cfr. with twistor approach by E.Witten (2003)]

Problem: for N > 5 the scattering equations are very hard to

solve for generic momenta. [See L. Dolan and P. Goddard (2013/2014), C. Baadsgaard, N. Bjerrum-Bohr, J. Bourjaily, P. Damgaard, arXiv:1506.06137]

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- Fortunately in the classicalization limit, i.e. the limit we are interested in scattering equations can be solved explicitly

assid
p classicalization limit can be
parameterized as:
(in units of s/(N-2)^2)
$$s_{1,N} = \frac{1}{2} (N-3) (N-a-b)$$
,
 $s_{N-1,N} = -\frac{1}{2} (N-3) (2-b)$, $s_{1,N-1} = -\frac{1}{2} (N-3) (2-a)$,
 $s_{1,i} = -\frac{1}{2} (N-2-b)$, $s_{i,N} = -\frac{1}{2} (N-2-a)$,
 $s_{N-1,i} = \frac{1}{2} (4-a-b)$, $s_{ij} = 1$, $i, j \in \{2, ..., N-2\}$,

th this gives rise to a two-parameter a,b solution, which is (N-3)!-fold degenerate

This parametrization can be mapped to a problem Kalousios (2013) has already studied:

Solutions of scattering equations are identified with the zeros of Jacobi polynomials.

$$M_{N}(1,...,N) = -\kappa^{N-2} 2^{8-N} \frac{s}{(N-2)^{2}} \left[(N-3)!! \right]^{2} \frac{\Gamma\left(\frac{a}{2}\right) \Gamma\left(\frac{3}{2} + \frac{b-N}{2}\right) \Gamma\left(\frac{1-N+a+b}{2}\right)}{\Gamma\left(1 + \frac{a-N}{2}\right) \Gamma\left(\frac{b-1}{2}\right) \Gamma\left(\frac{a+b-3}{2}\right)} \\ \times \frac{\Gamma\left(\frac{3}{2} + \frac{a-N}{2}\right) \Gamma\left(\frac{b}{2}\right) \Gamma\left(\frac{a+b-2}{2}\right)}{\Gamma\left(1 + \frac{b-N}{2}\right) \Gamma\left(\frac{a-1}{2}\right) \Gamma\left(\frac{a+b-N}{2}\right)} H_{N}(a,b)^{2}$$

Exact in any real a,b and N

$$\stackrel{N \to \infty}{\longrightarrow} \kappa^N \; \frac{s}{N^2} \; N!$$

This parametrization can be mapped to a problem Kalousios (2013) has already studied:

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Note: Incidentally the solutions to the scattering equations describe the saddle point contributions in the high-energy limit of open and closed string amplitudes (Gross, Mende) \rightarrow see next part of the talk. To obtain the physical probability, i.e. the S-matrix element, we have to consider phase space integral:

$$d|\langle 2|S|N-2\rangle|^{2} = \frac{1}{(N-2)!} \prod_{i=2}^{N-1} dp_{i}^{4} |M_{N}|^{2} \delta^{4}(P_{total})$$

$$(p_{in} \sim \sqrt{s}, p_{out} \sim \frac{\sqrt{s}}{N-2})$$

Physical $2 \rightarrow N-2$ perturbative, scattering probability in classicalization regime:

$$|\langle 2|S|N-2\rangle|^2 = \left(\frac{L_P^2 s}{N^2}\right)^N N! = \left(\frac{\lambda}{N}\right)^N N! \sim e^{-N}\lambda^N$$

Collective coupling $\lambda \equiv \alpha N = s/M_P^2 N$

This perturbative scattering probability possesses a maximum at the following critical value for N:

$$N_{crit} = sL_P^2 \quad \Leftrightarrow \quad \lambda_{crit} = 1$$

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Remark: similar calculations can be done for scalar field theories, like $~\lambda\phi^4~$.

In this case the amplitudes show a different large N behavior:



The perturbative amplitude is suppressed by e^{-N} .

This is just the inverse of the degeneracy of states of a black hole with entropy $\mathcal{S}\sim N$.

Therefore this suppression factor is compensated at the critical point $\lambda = 1$ by e^N from the degeneracy of black hole states:

 $A_{BH} \sim \sum_{j} |\langle 2|S|N \rangle|_p^2 |\langle N|BH \rangle_j|_{np}^2 \sim \lambda^N e^{-N}|_p \times e^N|_{np}$

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So, black hole is exactly dominating at $\lambda = 1$.

In summary:

• Perturbative $2 \longrightarrow N$ graviton amplitude:

$$|M_N^{pert.}|^2 \simeq \lambda^N e^{-N}, \quad \lambda = s/(M_P^2 N)$$

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- Perturbative $2 \longrightarrow N$ graviton amplitude:

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• Non-perturbative enhancement at $\lambda = 1$ due to black hole entropy factor : e^N

$$|M_N^{n.p.}|^2 \simeq \lambda^N$$

(fully saturated at $\lambda = 1$)









For large s unitarization occurs if N increases appropriately:

This bound implies that $N \gtrsim N_{crit} = sL_P^2$

This is the core of the idea of classicalization!

N should be larger than the corresponding entropy of a black hole with mass equal to the center of mass energy.



However there remain still some UV problems:

What is happening in the regime where $~~\lambda>1~~?$ $N~<~N_{crit}=sL_P^2$



[Veneziano (1968); Amati, Ciafaloni, Veneziano (1987); Gross, Mende (1987), Gross, Manes (1989]

$$\mathcal{M}_4 \sim K \frac{\Gamma(-\frac{\alpha'}{4}s)\Gamma(-\frac{\alpha'}{4}t)\Gamma(-\frac{\alpha'}{4}u)}{\Gamma(\frac{\alpha'}{4}s)\Gamma(\frac{\alpha'}{4}t)\Gamma(\frac{\alpha'}{4}u)}$$
$$\longrightarrow_{\alpha'\to\infty} \kappa^2 |A_4|^2 \times 4\pi\alpha' \frac{st}{u} \exp\left\{\frac{\alpha'}{2}(s\ln|s|+t\ln|t|+u\ln|u|)\right\}$$

[Veneziano (1968); Amati, Ciafaloni, Veneziano (1987); Gross, Mende (1987), Gross, Manes (1989]

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$$\longrightarrow_{\alpha'\to\infty} \kappa^{2}|A_{4}|^{2} \times 4\pi\alpha' \frac{st}{u} \exp\left\{\frac{\alpha'}{2}(s\ln|s|+t\ln|t|+u\ln|u|)\right\}$$

Square of
YM-amplitude

[Veneziano (1968); Amati, Ciafaloni, Veneziano (1987); Gross, Mende (1987), Gross, Manes (1989]



[Veneziano (1968); Amati, Ciafaloni, Veneziano (1987); Gross, Mende (1987), Gross, Manes (1989]



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Example: 4-point graviton amplitude



(Note: this was basically the state of the art before our paper.)

Generalization to arbitrary (large) N:

Note: Incidentally the solutions to scattering equations describe saddle point contributions High ienengyeningitmitusepofascattering appluationss, Mende)



Again in the classicalization limit we obtain the explicit result, forvarbitrary N:

$$\mathcal{M}_{N} = \begin{pmatrix} \times \prod_{\substack{n=3\\ \forall n \neq \alpha}}^{N-3} \left(\frac{\nu^{\nu} N^{a-3\nu} (b+\nu)^{b+\nu}}{N^{a-3b} \prod_{\substack{n=3\\ \forall n \neq \alpha}}^{N-3} (\frac{3+\nu)^{a+\nu} (b+\nu)^{b+\nu}}{(\alpha+\beta+\nu)^{a+\nu}} \right)^{\alpha'/4} (\beta_{N}(4,\nu)^{\beta_{N}})^{\nu} + \mathcal{O}(\alpha')^{\frac{\alpha's}{4}}$$

$$\times \prod_{\substack{\nu=1\\ \forall n \neq \alpha}}^{High-energy string} \text{ amplitude for arbitrary } \mathbf{N}$$

$$\times M_{N}^{FT} \text{ or pared (to N)=4 in Veneziano, Gross-Mende}$$

• gives relation between SUGRA and string amplitude at high energies

Generalization to arbitrary (large) N:

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Again in the classicalization limit we obtain the explicit result, for $y^3 N$:

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Two different energy regimes:

(i)
$$\frac{\sqrt{s}}{N} < M_s$$
: $\iff \lambda < Ng_s^2$
,,infrared", field theory regime

Field and ST theory amplitudes agree.

This was already conjectured for the MHV case up to 5 points by [Cheung, O'Connell, Wecht (2010)]

$$F_N = 1 \quad \Rightarrow \quad \mathcal{M}_N = M_N^{FT}$$

(*ii*) $\frac{\sqrt{s}}{N} > M_s : \iff \lambda > Ng_s^2$

"ultraviolet", string theory regime

$$\mathcal{M}_N \sim \kappa^{N-2} \alpha'^{N-3} s e^{-\frac{\alpha'}{2}(N-3)} s \ln(\alpha' s)$$

String states dominate.

Amplitude gets tamed by string states (Regge modes).



Transition occurs at $E_{\rm IR/UV} = NM_{\rm string}$ Gravitons in final state become hard: $E_{final} > M_s$





Sonntag, 13. September 15

What is happening at the point $\lambda = Ng_s^2 = 1$?

Here the F.T. amplitude agrees with the string amplitude at the critical point $\lambda = 1$.

This the point where the string effects match the amplitude from the F.T. black hole formation.

 $g_s = \frac{1}{\sqrt{N}} \Rightarrow$ String - black hole correspondence: black hole can be described by a state of strings.

[Horowitz, Polchinski (1996); Dvali, D.L. (2009); Dvali, Gomez (2010)]

Here the IR is meeting the UV.

What about loop corrections or higher order gravity (UV) corrections?

They should correspond to I/N corrections to what we computed: $(1) \ge q$

$$A_{\rm g-loop} \sim \left(\frac{1}{N}\right)^{s}$$
, $A_{\mathcal{R}^g} \sim \left(\frac{1}{N}\right)^{s}$

What about loop corrections or higher or corrections? They should correspond to I/N corrections? They should correspond to I/N correction $A_{g-loop} \sim \left(\frac{1}{N}\right)^g$, $A_{\mathcal{R}^g} \sim \left(\frac{1}{N}\right)^g$





 propagating, ghostfree spin-2 only on curved backgrounds (de Sitter or anti-De Sitter).

- flat backgrounds: only scalar mode, no gravitational interaction. Non-trivial interplay between UV/IR !

Is there possibly any relation between the limit of large number N of gravitons and the large Nc limit in Yang-Mills gauge theories? Is there possibly any relation between the limit of large number N of gravitons and the large Nc limit in Yang-Mills gauge theories?

- Relation between open and closed string coupling: $g_s = g_{open}^2$
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- Relation between open and closed string coupling: $g_s = g_{open}^2$
- At point of string-bh correspondence: $g_s = 1/\sqrt{N}$
- Planar limit of gauge theory: $g_{open}^2 = 1/N_c$ So naively we get: $N = N_c^2$ What is the interpretation of this relation?

- Summary:
 New computation of N-point gravity (string) amplitudes in trans-planckian large N region in closed form
- We found evidence for classicalization and black hole production (black hole N-portrait).
- We found an interesting trans-Planckian transition between field theory and string theory: string black hole correspondence.

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- Mixed gauge boson (open)/gravity (closed) amplitudes: Bh N-portrait with matter [Dvali, Gomez, D.L. (2013)]

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- Bh N-portrait beyond tree level

First steps in [Kuhnel, Sundborg (2014)]

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- Bh N-portrait beyond tree level First steps in [Kuhnel, Sundborg (2014)]
- There is a very interesting connection between the BMS symmetry of GR and the gravitational scattering [A. Strominger; S. Hawking, arXiv:1509.01147 amplitudes and the b.h. N-portrait Dvali, Gomez, D.L. arXiv: 1509.02114]