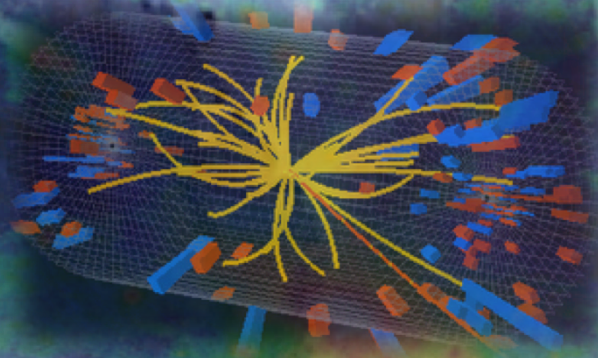


Discovering dark matter

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Niels Bohr Institute, Copenhagen & University of Oxford



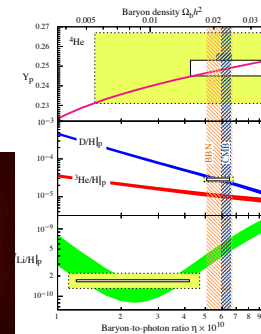
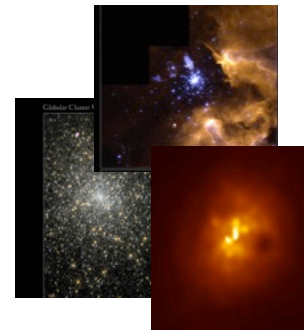
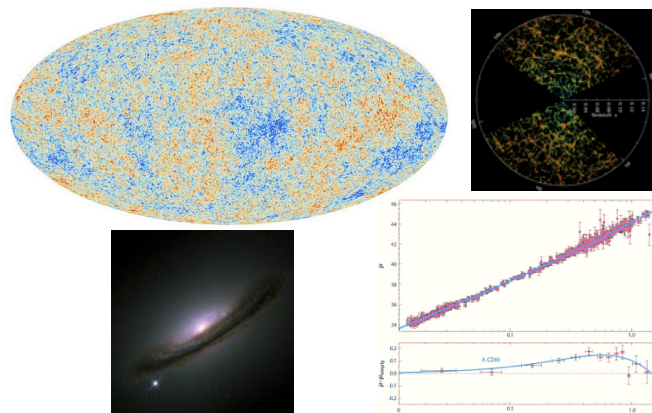
Corfu Summer School 'The Standard Model & Beyond', 4th Sep 2014

What is the world made of?

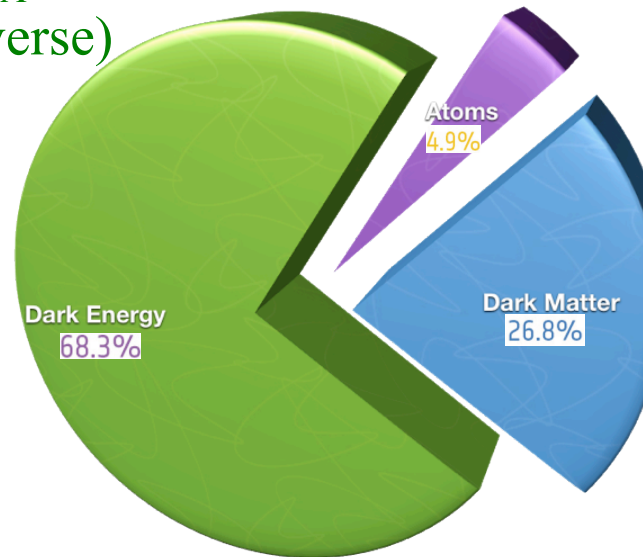
Mainly geometrical evidence:

$$\Lambda \sim O(H_0^2), H_0 \sim 10^{-42} \text{ GeV}$$

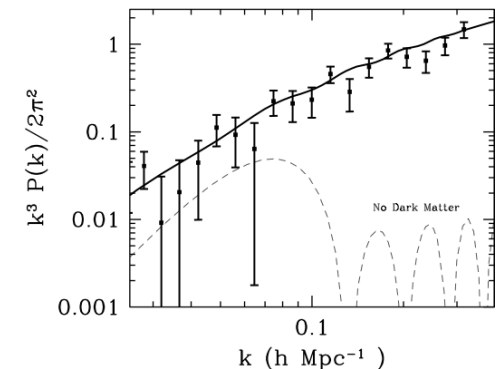
... **dark energy** is *inferred* from the 'cosmic sum rule': $\Omega_m + \Omega_k + \Omega_\Lambda = 1$ (assuming a homogeneous universe)



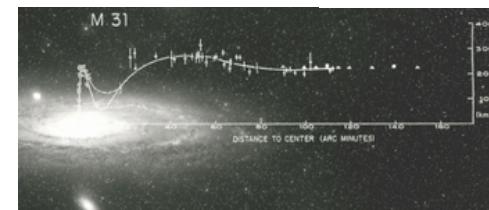
Baryons
(but *no*
anti-baryons)



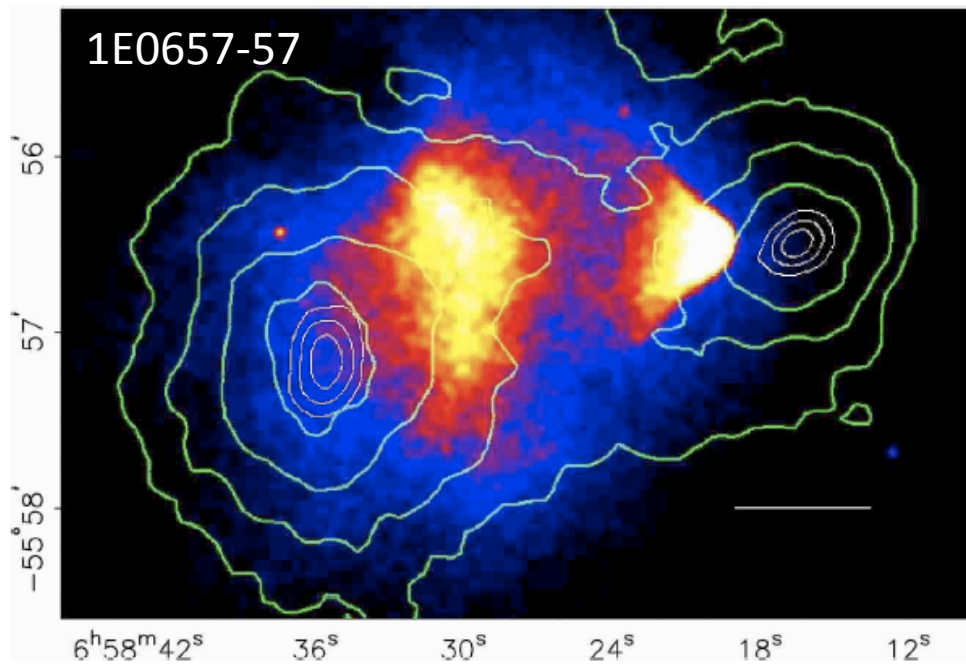
Both geometrical *and* dynamical evidence for **dark matter** (if GR is valid)



Both the baryon asymmetry and dark matter *require* new physics beyond the Standard $SU(3)_c \times SU(2)_L \times U(1)_Y$ Model
... dark energy is even more mysterious (but still lacks compelling dynamical evidence)



What can astrophysics tell us about dark matter interactions?



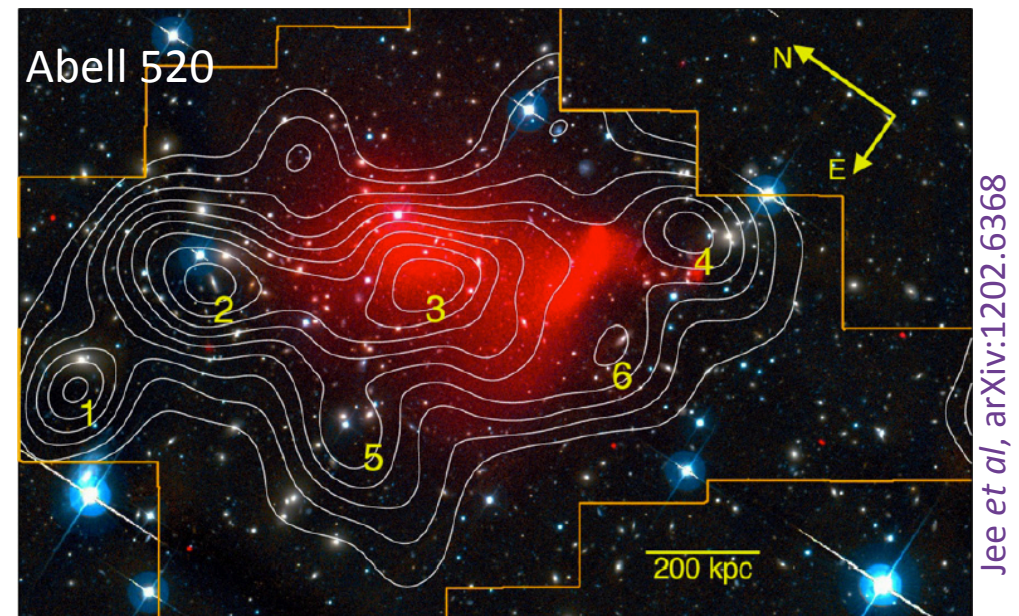
The 'Bullet Cluster' is often cited as evidence that dark matter is *collisionless* ... in actual fact it sets a rather *weak* limit on self-interactions: $\sigma \lesssim 2 \times 10^{-24} \text{ cm}^2/\text{GeV}$

Moreover it poses a *challenge* for Λ CDM cosmology: why is the relative velocity so high (>3000 km/s on a scale of 5 Mpc)?

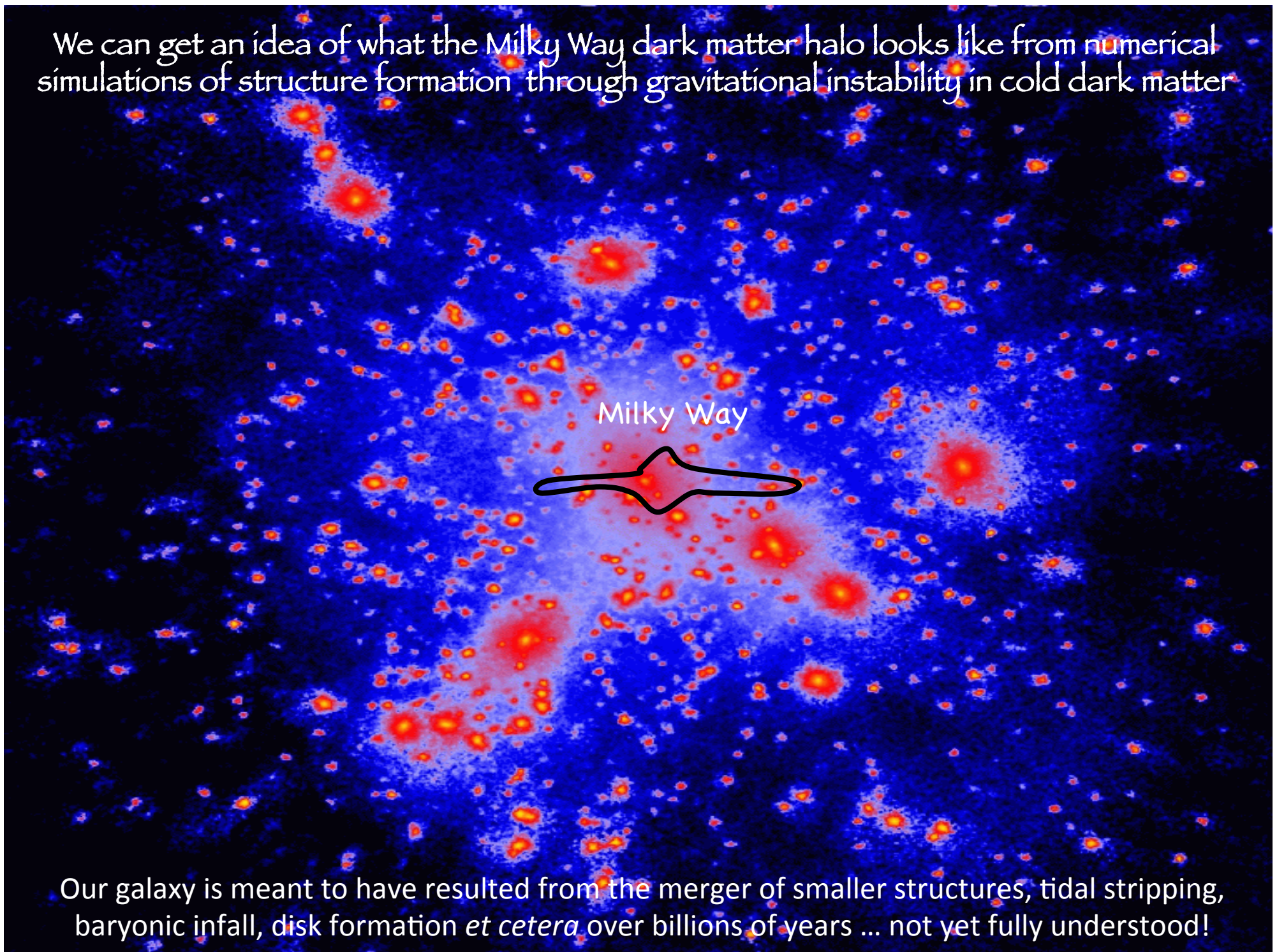
Nine other colliding clusters have been found ... the odds are *tiny* in a Gaussian density field!

But in Abell 520, the DM concentration is partly *coincident* with the X-ray emitting gas implying that DM is *self-interacting* with: $\sigma \approx 2 \times 10^{-24} \text{ cm}^2/\text{GeV}$ (Jee et al, 1401.3356)

This result is contested ... in any case the separation between DM and galaxies will be *time-dependent* and sensitive to whether the self-interactions are contact or long-range (Frandsen et al, 1308.3419) ... so data from gravitational lensing can in principle discriminate between DM particle candidates



We can get an idea of what the Milky Way dark matter halo looks like from numerical simulations of structure formation through gravitational instability in cold dark matter

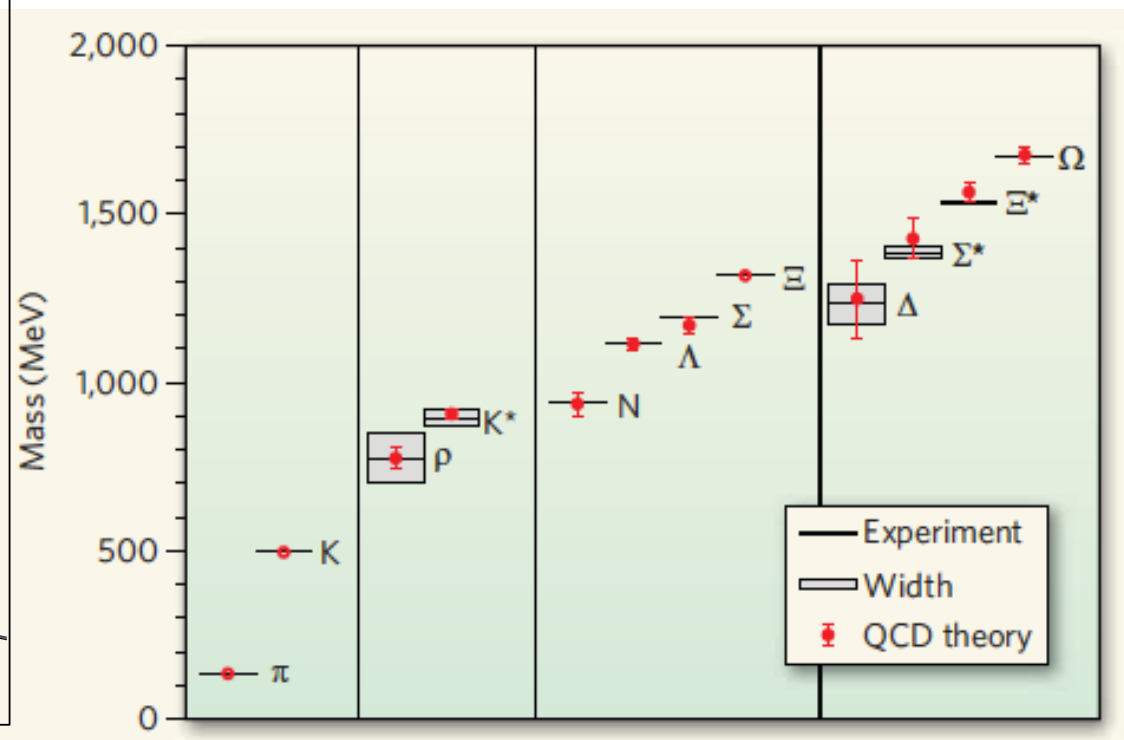
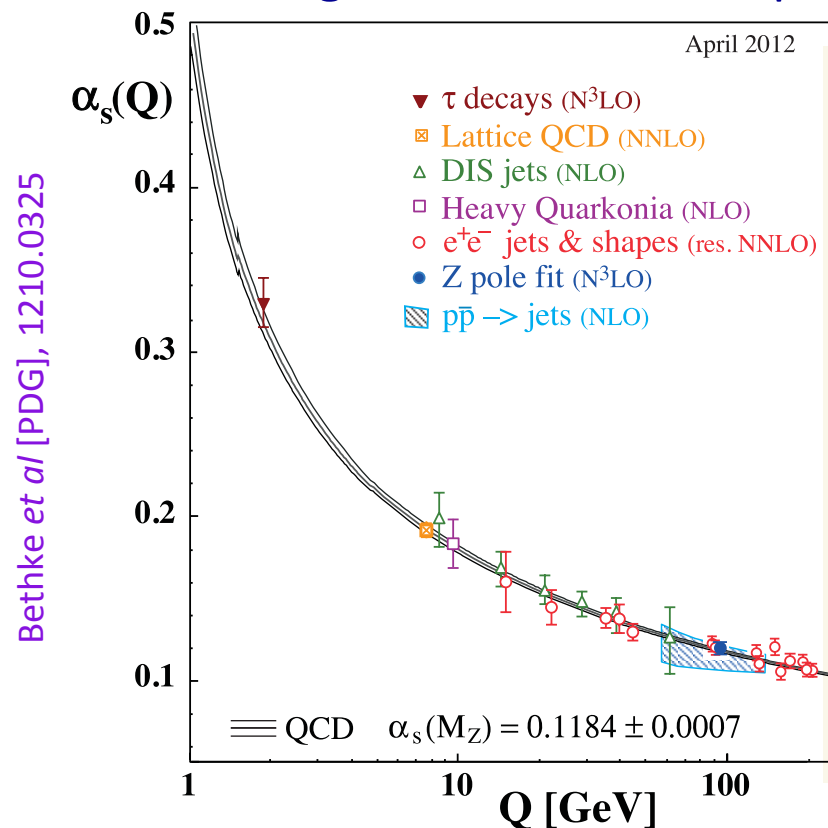


Our galaxy is meant to have resulted from the merger of smaller structures, tidal stripping, baryonic infall, disk formation *et cetera* over billions of years ... not yet fully understood!

What should the world be made of?

Mass scale	Particle	Symmetry/ Quantum #	Stability	Production	Abundance
Λ_{QCD}	Nucleons	Baryon number	$\tau > 10^{33}$ yr	'freeze-out' from thermal equilibrium	$\Omega_B \sim 10^{-10}$ <i>cf.</i> observed $\Omega_B \sim 0.05$

We have a good theoretical explanation for why baryons are massive and stable



Durr et al, Science 322:2224, 2008

We understand the dynamics of QCD ... and can calculate the mass spectrum

Nevertheless we get the cosmology of baryons *badly* wrong!

$$\dot{n} + 3Hn = -\langle\sigma v\rangle(n^2 - n_{\text{T}}^2)$$

Chemical equilibrium is maintained as long as the annihilation rate exceeds the Hubble expansion rate

‘Freeze-out’ occurs when annihilation rate:

$$\Gamma = n\sigma v \sim m_N^{3/2} T^{3/2} e^{-m_N/T} \frac{1}{m_\pi^2}$$

becomes comparable to the expansion rate

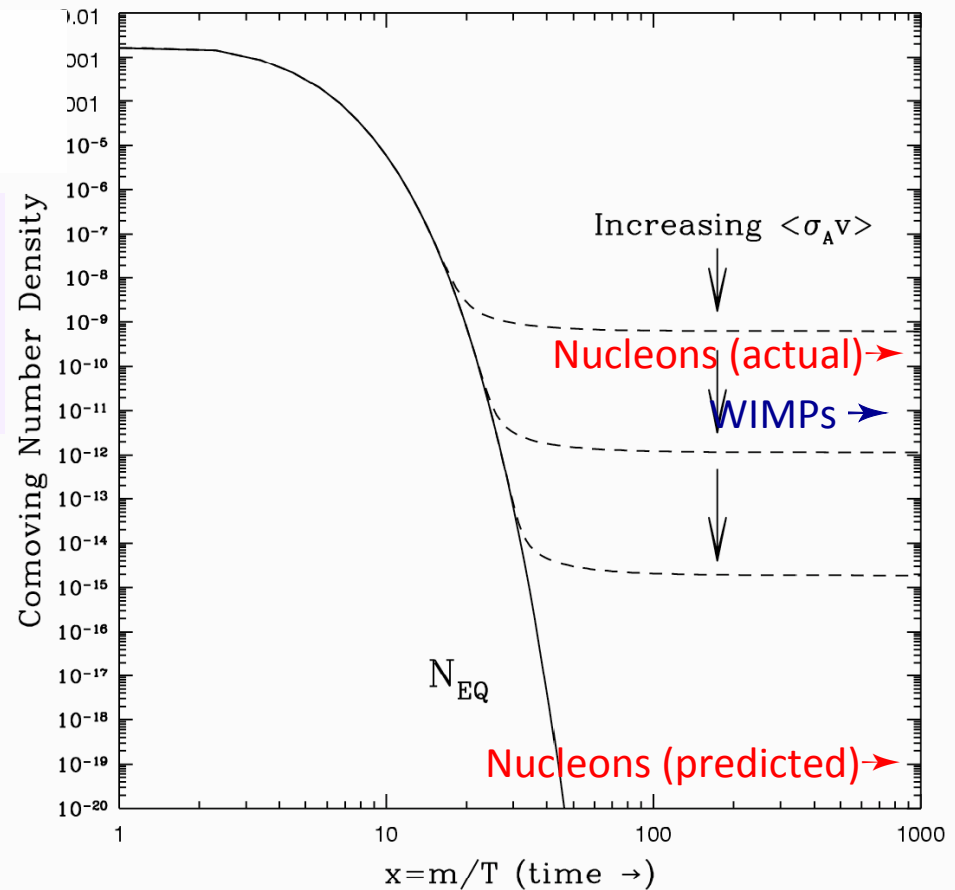
$$H \sim \frac{\sqrt{g}T^2}{M_{\text{P}}}$$

where $g \sim \#$ relativistic species

i.e. ‘freeze-out’ occurs at $T \sim m_N/45$, with: $\frac{n_N}{n_\gamma} = \frac{n_{\bar{N}}}{n_\gamma} \sim 10^{-19}$

However the observed ratio is **6×10^9 times bigger for baryons**, and there seem to be **no antibaryons**, so we must invoke an initial baryon asymmetry: $\frac{n_B - n_{\bar{B}}}{n_B + n_{\bar{B}}} \sim 10^{-9}$

Why do we not call this the ‘baryon disaster’? (cf. ‘WIMP miracle’!)



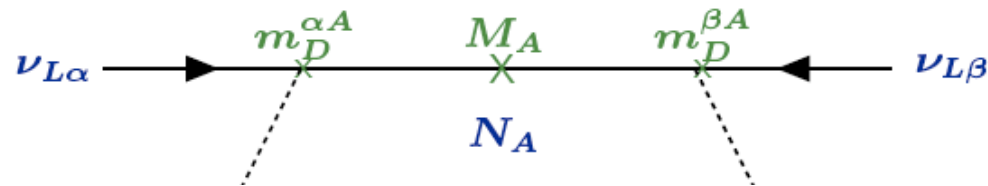
To make the baryon asymmetry requires a lot of new physics:

- B -number violation
- CP violation
- Departure for thermal equilibrium

The SM does allow B -number violation (through non-perturbative - sphaleron-mediated – processes) ... but CP -violation is *too weak* and $SU(2)_L \times U(1)_Y$ breaking is a ‘cross-over’ (*not out-of-equilibrium*)

Hence the generation of the observed matter-antimatter asymmetry *requires* new BSM physics (could be related to neutrino mass **if this arises from violation of lepton number** → **leptogenesis**)

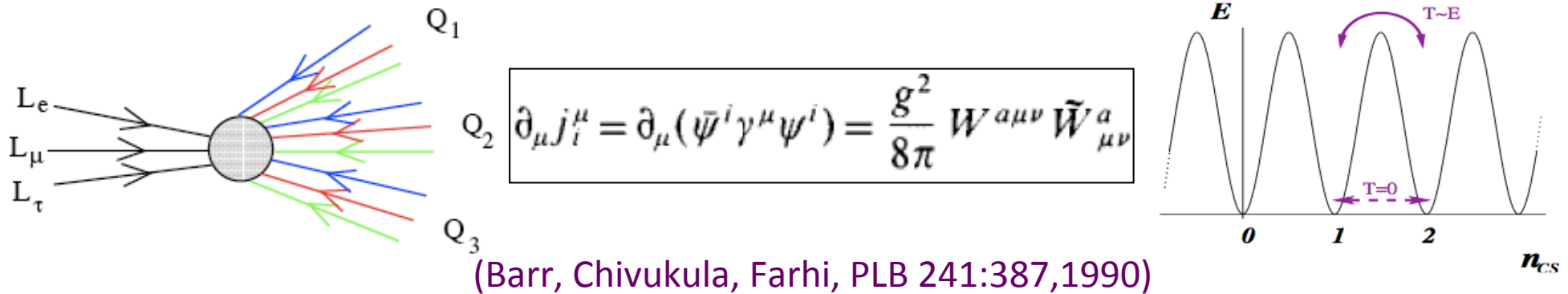
‘See-saw’: $\mathcal{L} = \mathcal{L}_{SM} + \lambda_{\alpha J}^* \bar{\ell}_{\alpha} \cdot H N_J - \frac{1}{2} \bar{N}_J M_J N_J^c \quad \lambda M^{-1} \lambda^T \langle H^0 \rangle^2 = [m_{\nu}]$



$$\Delta m_{atm}^2 = m_3^2 - m_2^2 \simeq 2.6 \times 10^{-3} \text{eV}^2$$

$$\Delta m_{\odot}^2 = m_2^2 - m_1^2 \simeq 7.9 \times 10^{-5} \text{eV}^2$$

Asymmetric baryonic matter

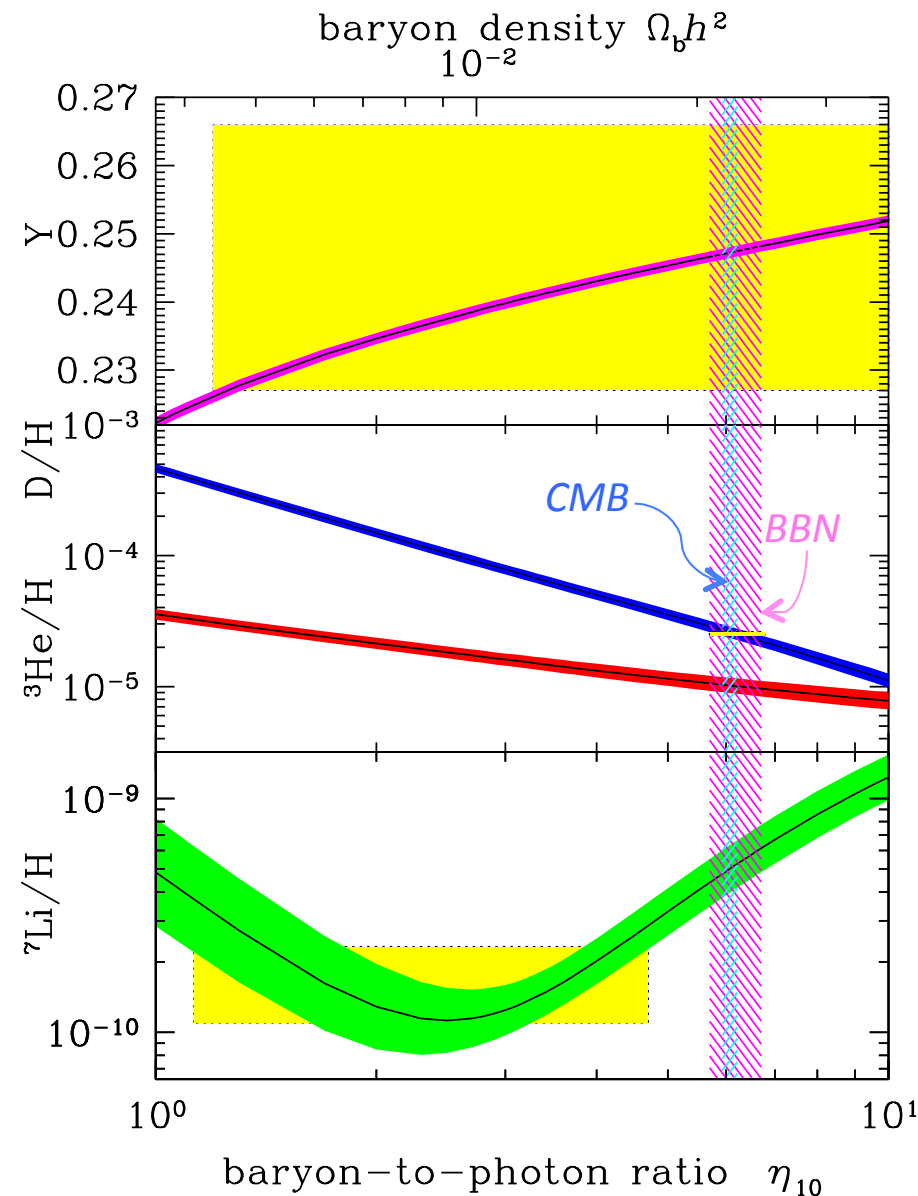


Any primordial lepton asymmetry (e.g. from *out-of-equilibrium* decays of the right-handed N) would be redistributed by $B+L$ violating processes in the SM (which *conserve* $B-L$) amongst *all* fermions – in particular **baryons** - which couple to the electroweak anomaly

Although **leptogenesis** may never be directly testable, evidence for a *Majorana* neutrino mass from observation of neutrinoless $\beta\beta$ -decay would provide powerful support for the idea

... in any case we accept that the only kind of matter which we are certain *exists*, originated ***non-thermally*** in the early universe

Although vastly overabundant compared to the natural expectation, baryons *cannot* close the universe (BBN + CMB concordance)



Fields, Molaro & Sarkar (Particle Data Group), 2014

... the dark matter *must* therefore be mainly *non-baryonic*

The Standard $SU(3)_c \times SU(2)_L \times U(1)_Y$ Model (viewed as an effective field theory up to some high energy cut-off scale M) accurately describes all microphysics

$$+M^4 + \underbrace{M^2 \Phi^2}_{\text{hierarchy problem}} \quad m_H^2 \simeq \frac{h_t^2}{16\pi^2} \int_0^{M^2} dk^2 = \frac{h_t^2}{16\pi^2} M^2 \quad \text{super-renormalisable}$$

$$\mathcal{L}_{\text{eff}} = F^2 + \bar{\Psi} \not{D} \Psi + \bar{\Psi} \Psi \Phi + (D\Phi)^2 + \Phi^2 \quad \text{renormalisable}$$

$$+ \underbrace{\frac{\bar{\Psi} \Psi \Phi \Phi}{M}}_{\text{neutrino mass}} + \underbrace{\frac{\bar{\Psi} \Psi \bar{\Psi} \Psi}{M^2}}_{\text{proton decay}} + \dots \quad \text{non-renormalisable}$$

New physics beyond the SM \Rightarrow **non-renormalisable operators** suppressed by M^n which 'decouple' as $M \rightarrow M_p$ (... so **neutrino mass** is small, **proton decay** is slow etc)

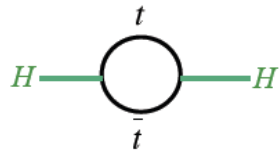
But as M is raised, the effects of the **super-renormalisable operators** are *exacerbated*
One solution for Higgs mass divergence \rightarrow 'softly broken' supersymmetry at $M \sim 1$ TeV

This provides new possibilities for **baryogenesis** as well as a good candidate for **dark matter** – the **lightest supersymmetric particle** (typically the neutralino χ), *if* it is cosmologically *stable* because of a conserved quantum number (R -parity)

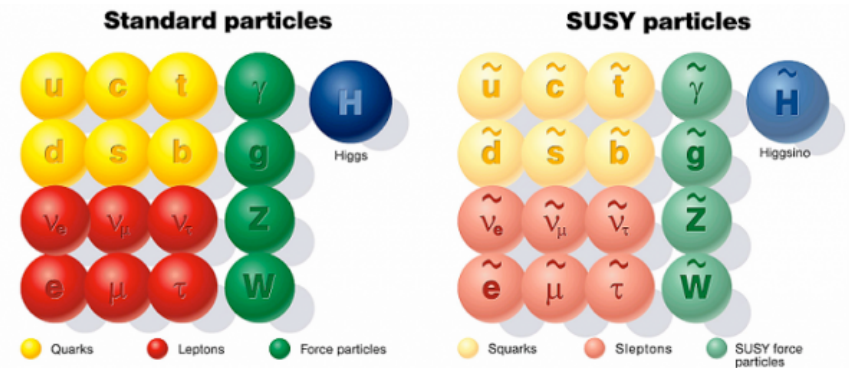
This has been the target of *most* dark matter searches, whether using nuclear recoil detectors or looking for cosmic annihilation products, or missing E_T signals at colliders

What should the world be made of?

Mass scale	Particle	Symmetry/ Quantum #	Stability	Production	Abundance
Λ_{QCD}	Nucleons	Baryon number	$\tau > 10^{33} \text{ yr}$	'freeze-out' from thermal equilibrium Asymmetric baryogenesis	$\Omega_B \sim 10^{-10}$ <i>cf. observed</i> $\Omega_B \sim 0.05$
$\Lambda_{\text{Fermi}} \sim G_F^{-1/2}$	Neutralino?	R -parity?	Violated? (matter parity <i>adequate</i> to ensure p stability)	'freeze-out' from thermal equilibrium	$\Omega_{\text{LSP}} \sim 0.3$



$$\mathcal{L}_{\text{eff}} \supset M_A A_\mu A^\mu + m_f \bar{f}_L f_R + m_H^2 |H|^2$$



For (softly broken) **supersymmetry** we have the ‘WIMP miracle’:

$$\Omega_\chi h^2 \simeq \frac{3 \times 10^{-27} \text{ cm}^{-3} \text{ s}^{-1}}{\langle \sigma_{\text{ann}} v \rangle_{T=T_f}} \simeq 0.1 \quad , \quad \text{since } \langle \sigma_{\text{ann}} v \rangle \sim \frac{g_\chi^4}{16\pi^2 m_\chi^2} \approx 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

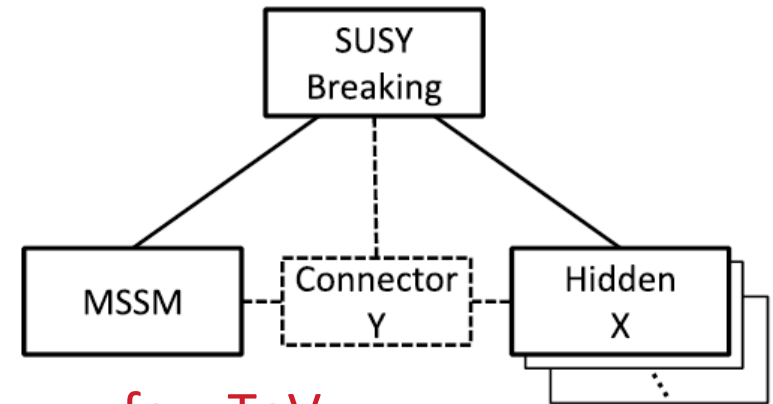
But why should a *thermal* relic have an abundance comparable to non thermal relic baryons?

What should the world be made of?

Mass scale	Particle	Symmetry/ Quantum #	Stability	Production	Abundance
Λ_{QCD}	Nucleons	Baryon number	$\tau > 10^{33} \text{ yr}$	'freeze-out' from thermal equilibrium <i>Asymmetric baryogenesis</i>	$\Omega_{\text{B}} \sim 10^{-10}$ <i>cf. observed $\Omega_{\text{B}} \sim 0.05$</i>
$\Lambda_{\text{Fermi}} \sim G_{\text{F}}^{-1/2}$	Neutralino?	R -parity?	Violated? (<i>matter parity adequate for p stability</i>)	'freeze-out' from thermal equilibrium	$\Omega_{\text{LSP}} \sim 0.3$

(GMSB) Hidden sector matter also provides the
'*WIMPless miracle*' (Feng & Kumar, 0803.4196)

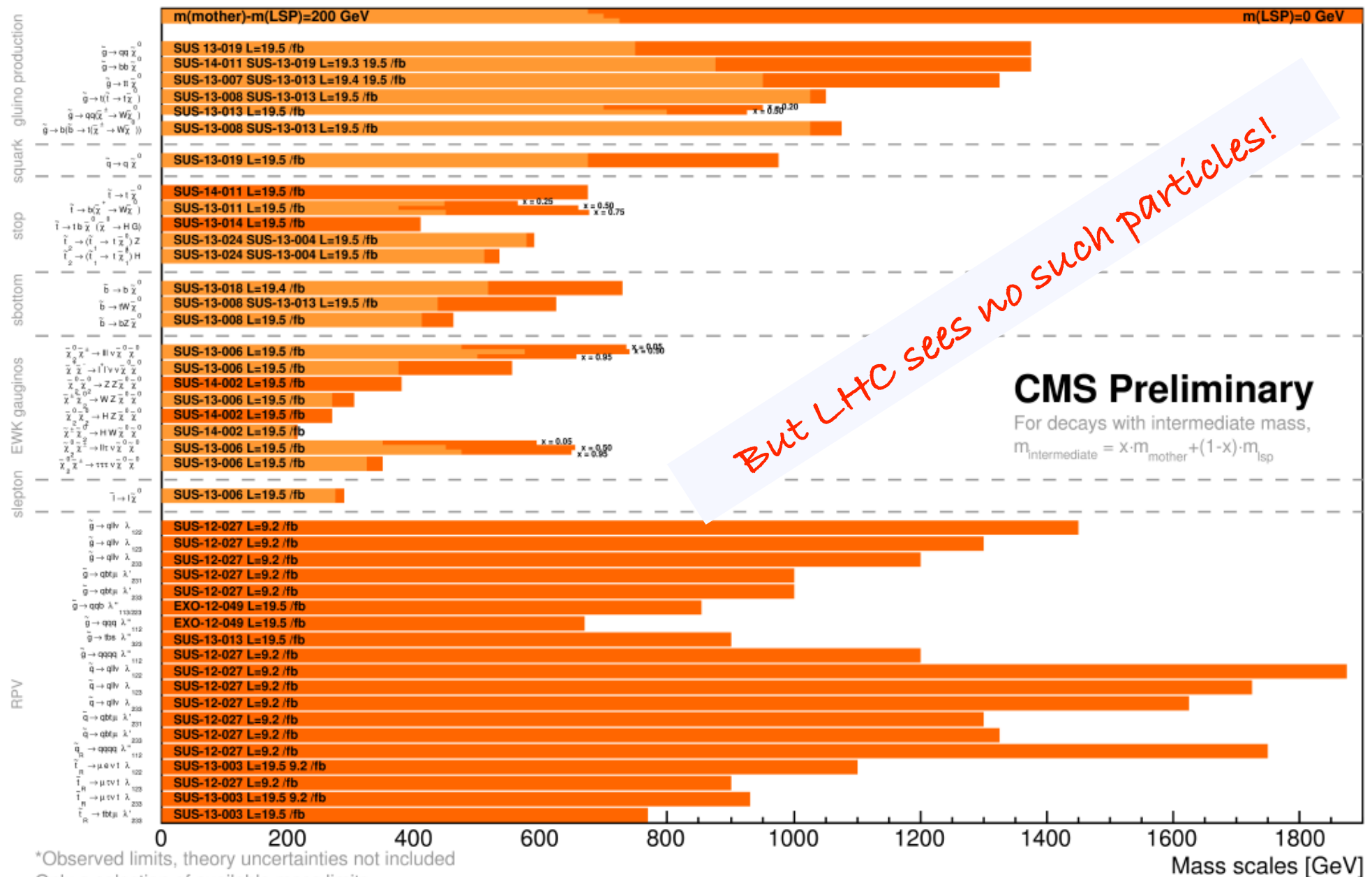
... because: $g_{\text{h}}^2/m_{\text{h}} \sim g_{\chi}^2/m_{\chi} \sim F/16\pi^2 M$



Such dark matter can have *any* mass: $\sim 0.1 \text{ GeV} \rightarrow \sim \text{few TeV}$

$$\Omega_{\chi} h^2 \simeq \frac{3 \times 10^{-27} \text{ cm}^{-3} \text{ s}^{-1}}{\langle \sigma_{\text{ann}} v \rangle_{T=T_{\text{f}}}} \simeq 0.1, \text{ since } \langle \sigma_{\text{ann}} v \rangle \sim \frac{g_{\chi}^4}{16\pi^2 m_{\chi}^2} \approx 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

But why should a *thermal* relic have an abundance comparable to non-thermal relic baryons?

ICHEP 2014

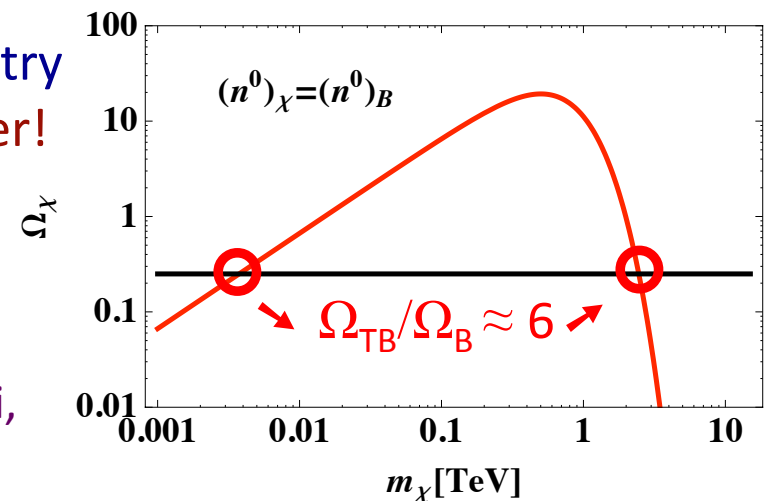
*Observed limits, theory uncertainties not included
Only a selection of available mass limits
Probe *up to* the quoted mass limit

What should the world be made of?

Mass scale	Particle	Symmetry/ Quantum #	Stability	Production	Abundance
Λ_{QCD}	Nucleons	Baryon number	$\tau > 10^{33}$ yr (dim-6 OK)	'Freeze-out' from thermal equilibrium Asymmetric baryogenesis (how?)	$\Omega_B \sim 10^{-10}$ <i>cf.</i> observed $\Omega_B \sim 0.05$
$\Lambda_{\text{QCD}}' \sim 6\Lambda_{\text{QCD}}$	Dark baryon?	$U(1)_{\text{DB}}$	plausible	Asymmetric (like the <i>observed</i> baryons)	$\Omega_{\text{DB}} \sim 0.3$
$\Lambda_{\text{Fermi}} \sim G_F^{-1/2}$	Neutralino? Technibaryon?	R -parity (walking) Technicolour	violated? $\tau \sim 10^{18}$ yr e^+ excess?	'Freeze-out' from thermal equilibrium Asymmetric (like the <i>observed</i> baryons)	$\Omega_{\text{LSP}} \sim 0.3$ $\Omega_{\text{TB}} \sim 0.3$

A new particle can naturally *share* in the B/L asymmetry if it couples to the W ... **linking dark to baryonic matter!**

For example a $O(\text{TeV})$ mass **technibaryon** can be the dark matter (Nussinov 1985) ... another possibility is a ~ 6 GeV mass '**dark baryon**' in a *hidden sector* (Gelmini, Hall & Lin 1986, Kaplan 1992): $\Omega_\chi = (m_\chi \mathcal{N}_\chi / m_B \mathcal{N}_B) \Omega_B$

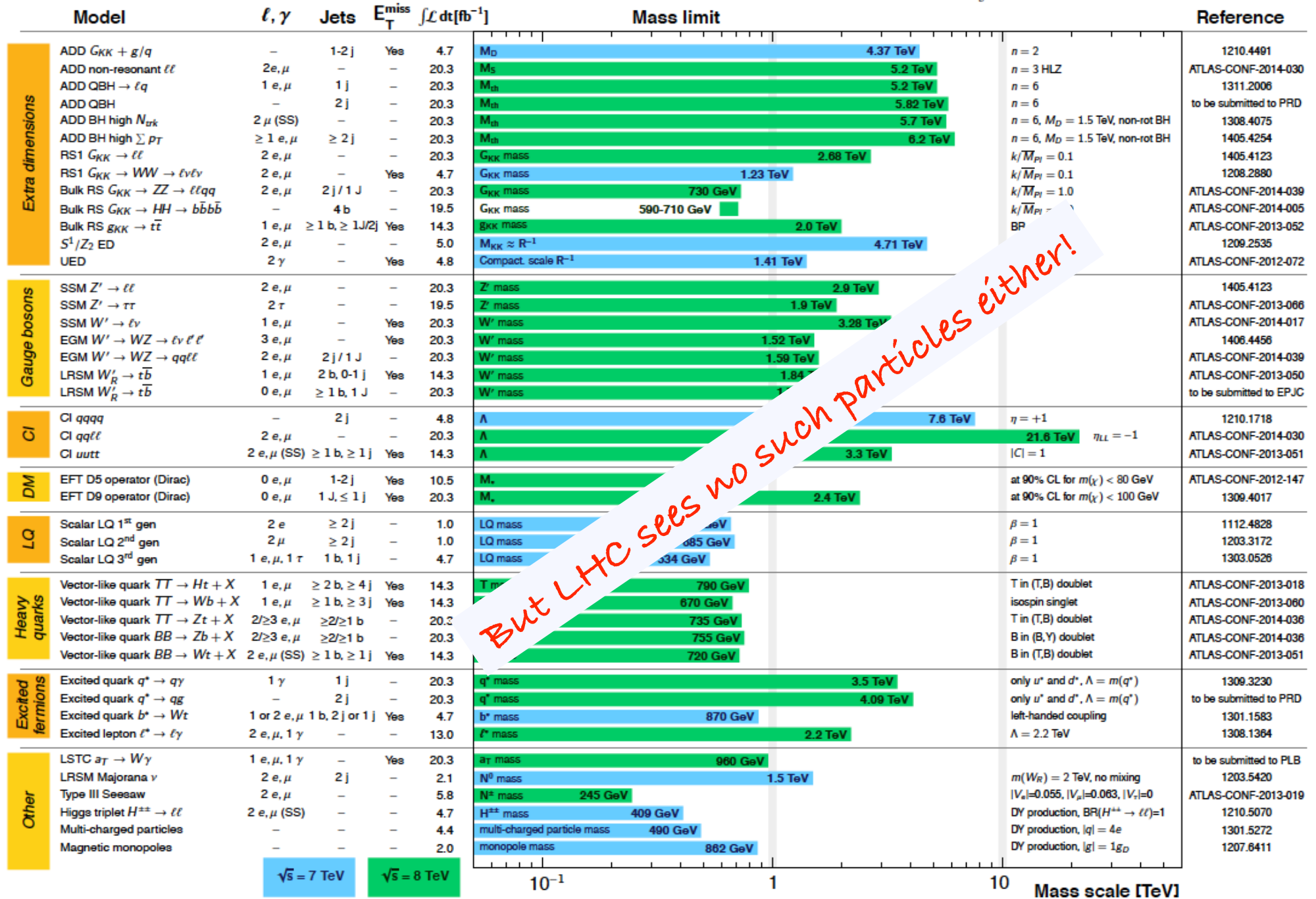


ATLAS Exotics Searches* - 95% CL Exclusion

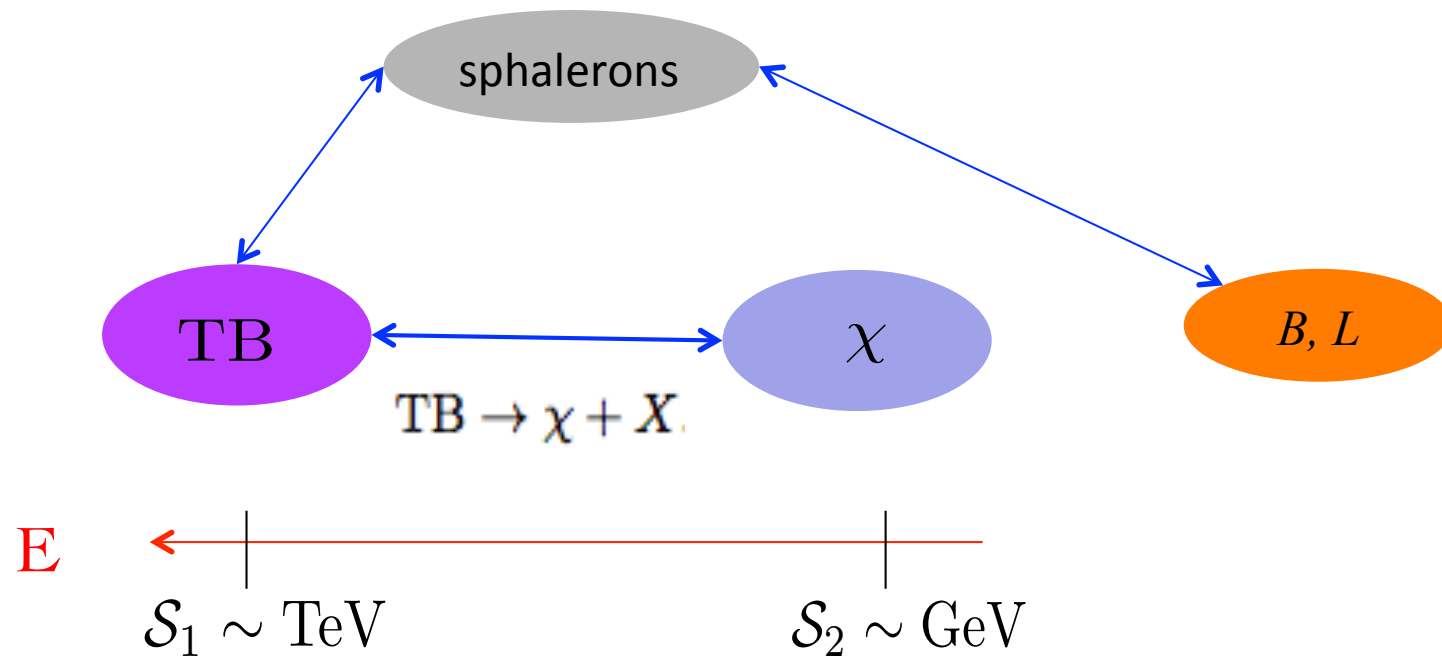
Status: ICHEP 2014

ATLAS Preliminary

$$\int \mathcal{L} dt = (1.0 - 20.3) \text{ fb}^{-1} \quad \sqrt{s} = 7, 8 \text{ TeV}$$



Why may we not have seen these particles yet?



- S_1 States (constituents) carry weak charges and are connected to sphalerons
- S_2 States are SM singlets (in a hidden sector/hidden valley) but directly connected to the S_1 sector (with scale separation – TeV \rightarrow GeV – because of different β -function)

$TB \rightarrow \chi + X$ is in equilibrium until $T \lesssim T_{\text{sph}}$, then χ decouples and becomes DM

The S_1 states *do* couple to the SM (so should show up at LHC14!)

NB: Such asymmetric dark matter would naturally have strong self-interactions

Axion dark matter

$$\begin{aligned}
 \mathcal{L}_{\text{eff}} = & M^4 + M^2 \Phi^2 && \text{super-renormalisable} \\
 & + (D\Phi)^2 + \bar{\Psi} \not{D} \Psi + F^2 + \bar{\Psi} \Psi \Phi + \Phi^2 && \boxed{+\theta_{\text{QCD}} F \tilde{F}} \text{ renormalisable} \\
 & + \frac{\bar{\Psi} \Psi \Phi \Phi}{M} + \frac{\bar{\Psi} \Psi \bar{\Psi} \Psi}{M^2} + \dots && \text{non-renormalisable}
 \end{aligned}$$

The SM admits a term which would lead to CP violation in strong interactions, hence an (unobserved) electric dipole moment for neutrons \rightarrow requires $\theta_{\text{QCD}} < 10^{-9}$

To achieve this without fine-tuning, θ_{QCD} must be made a dynamical parameter, through the introduction of a new $U(1)_{\text{Peccei-Quinn}}$ symmetry which must be broken ... the resulting (pseudo) Nambu-Goldstone boson is the **axion** which acquires a small mass through its mixing with the pion (the pNGB of QCD): $m_a = m_\pi (f_\pi/f_{\text{PQ}})$

The coherent oscillations of relic axions contain energy density *that behaves like CDM* with $\Omega_a h^2 \sim 10^{11} \text{ GeV}/f_{\text{PQ}} \dots$ however the *natural* P-Q scale is probably $f_{\text{PQ}} \sim 10^{18} \text{ GeV}$

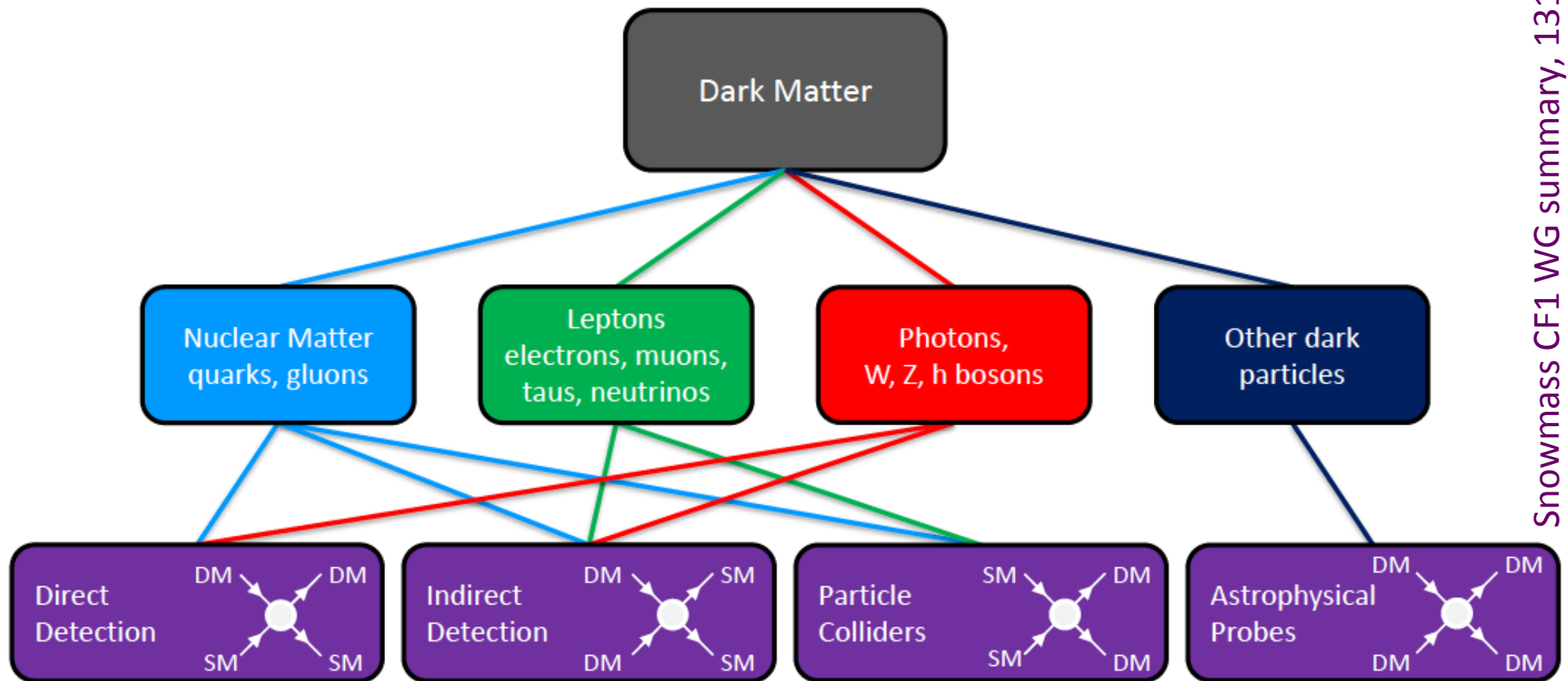
Hence axion dark matter would typically need to be significantly diluted i.e. its relic abundance is *not* predictable (or seek anthropic explanation for why θ_{QCD} is small?)

What should the world be made of?

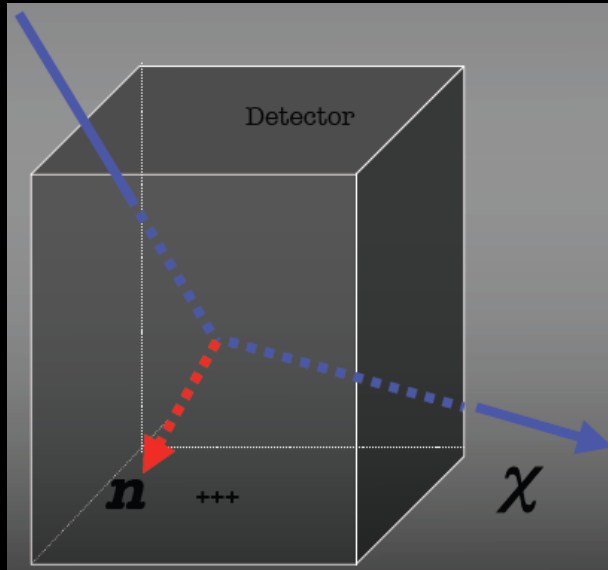
Mass scale	Lightest stable particle	Symmetry/Quantum #	Stability ensured?	Production	Abundance
Λ_{QCD}	Nucleons	Baryon number	$\tau > 10^{33}$ yr	'Freeze-out' from equilibrium Asymmetric baryogenesis	$\Omega_B \sim 10^{-10}$ cf. observed $\Omega_B \sim 0.05$
$\Lambda_{\text{QCD}'} \sim 5\Lambda_{\text{QCD}}$	Dark baryon?	$U(1)_{\text{DB}}$	plausible	Asymmetric (like observed baryons)	$\Omega_{\text{DB}} \sim 0.3$
$\Lambda_{\text{Fermi}} \sim G_F^{-1/2}$	Neutralino? Technibaryon?	R -parity (walking) Technicolour	violated? $\tau \sim 10^{18}$ yr	'freeze-out' from equilibrium Asymmetric (like observed baryons)	$\Omega_{\text{LSP}} \sim 0.3$ $\Omega_{\text{TB}} \sim 0.3$
$\Lambda_{\text{hidden sector}} \sim (\Lambda_F M_P)^{1/2}$ $\Lambda_{\text{see-saw}} \sim \Lambda_{\text{Fermi}}^2 / \Lambda_{\text{B-L}}$	Crypton? hidden valley? Neutrinos	Discrete (very model-dependent) Lepton number	$\tau \geq 10^{18}$ yr Stable	Varying gravitational field during inflation Thermal (abundance \sim CMB photons)	$\Omega_X \sim 0.3?$ $\Omega_\nu > 0.003$
$M_{\text{string}} / M_{\text{Planck}}$	Kaluza-Klein states? Axions	? Peccei-Quinn	? stable	? Field oscillations	? $\Omega_a \gg 1!$

*No definite indication from theory!
must decide by experiment!*

Detecting dark matter particles



The technologies and working environments vary *extremely* widely – from nuclear recoil detectors in shielded underground laboratories, to ground-based + satellite telescopes for detecting annihilation radiation, to searches using collider detectors for missing E_T signals + ‘monojets’, to astronomical gravitational lensing studies of colliding galaxy clusters ...

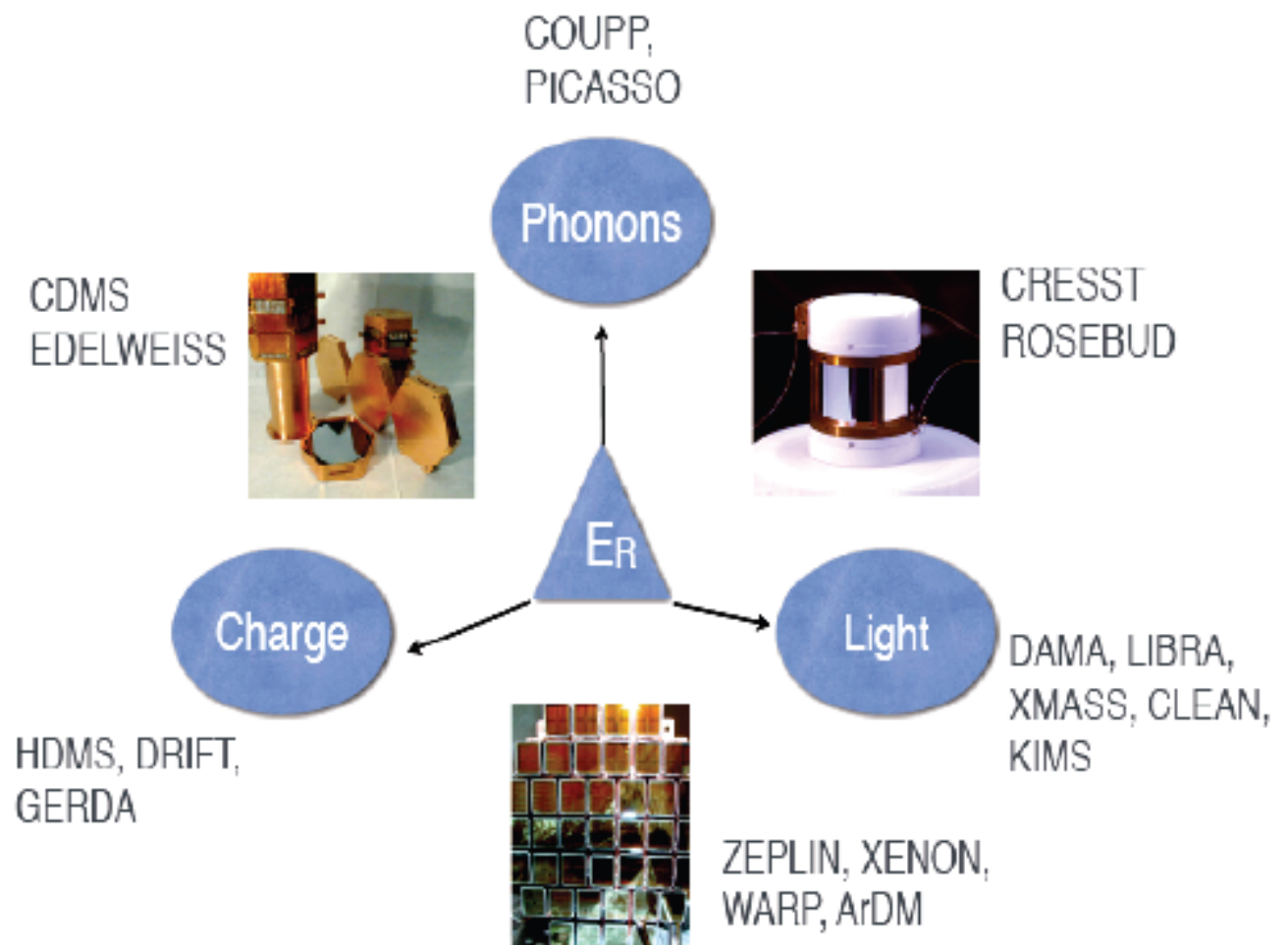


A passing dark matter particle orbiting in the Galaxy (at ~ 300 km/s) can scatter off a nucleus in an underground detector ... the expected rate is *very* low ($\ll 1$ event/kg/yr)

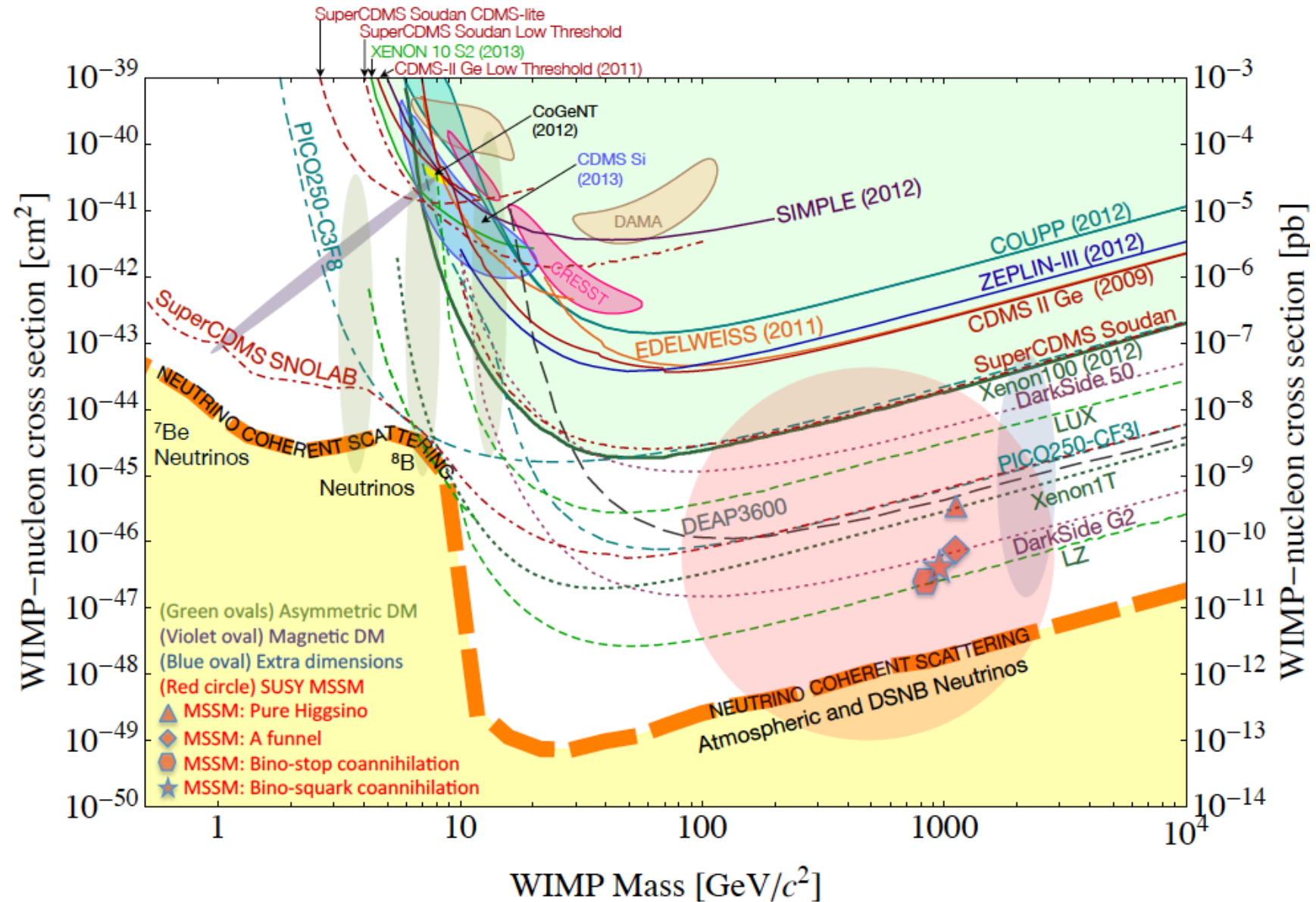
The recoil is detected via the ionization (charge), scintillation (light), and sound (phonons) \rightarrow heat

Experiments usually measure more than one channel to discriminate against the much bigger electron recoil background

(Very different techniques required to detect axions)



For ~ 25 years there has been a world-wide race on to detect dark matter



Snowmass CF1 WG summary, 1310.8327

Several claims for putative signals have apparently been ruled out by more sensitive experiments ... but are we making a fair comparison?

There are many ambiguities in interpreting the measured recoil rate:

$$\frac{dR}{dE_R}(E_R, t) = M_{\text{tar}} \frac{\rho_\chi}{2m_\chi \mu^2} \frac{(f_p Z + f_n(A - Z))^2}{f_n^2} \sigma_n F^2(E_R) \int_{v_{\text{min}}}^{\infty} d^3v \frac{f_{\text{local}}(\vec{v}, t)}{v}$$

Particle physics
Nuclear physics
astrophysics

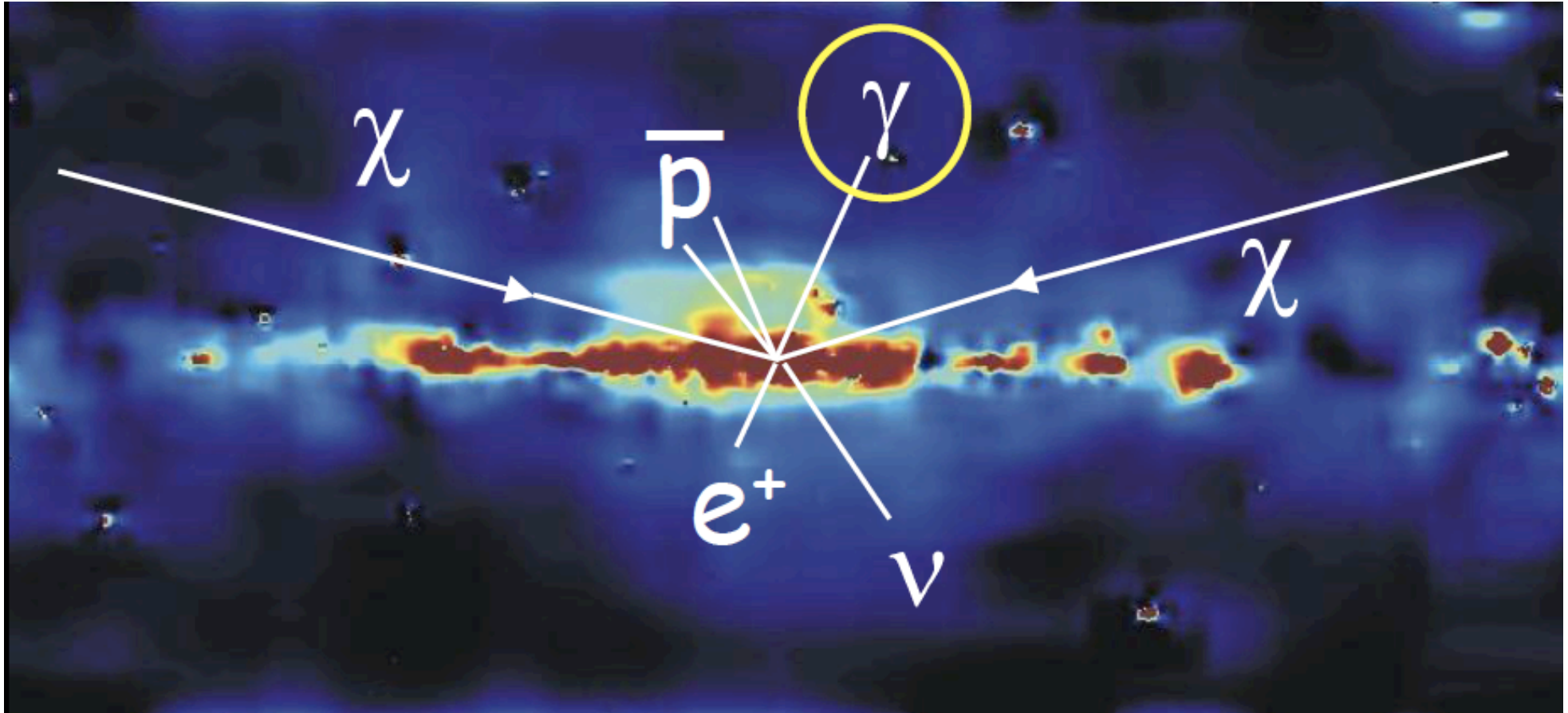
★ Dark matter may interact *differently* with neutrons and protons (Giulani, hep-ph/0504157) if the mediator is a (new) vector boson, so e.g. the events seen by CDMS-Si *can be* quite consistent with the upper limits set by XENON100/LUX.

★ Moreover different experiments are sensitive to *different* regions of the (uncertain) dark matter velocity distribution, hence apparently inconsistent results (e.g. CoGeNT and CRESST) can be reconciled by departing from the *assumed* isotropic Maxwellian form (Fox *et al*, 1011.1915, Frandsen *et al*, 1111.0292, Del Nobile *et al*, 1306.5273).

★ Then there are experimental uncertainties (efficiencies, energy resolution, instrumental backgrounds) ... as well as uncertainties in translating measured energies into recoil energies (channelling, quenching), uncertain nuclear form factors ...

No *single* experiment can either confirm or rule out dark matter
(... also not a good strategy to look just under the supersymmetric lamp post!)

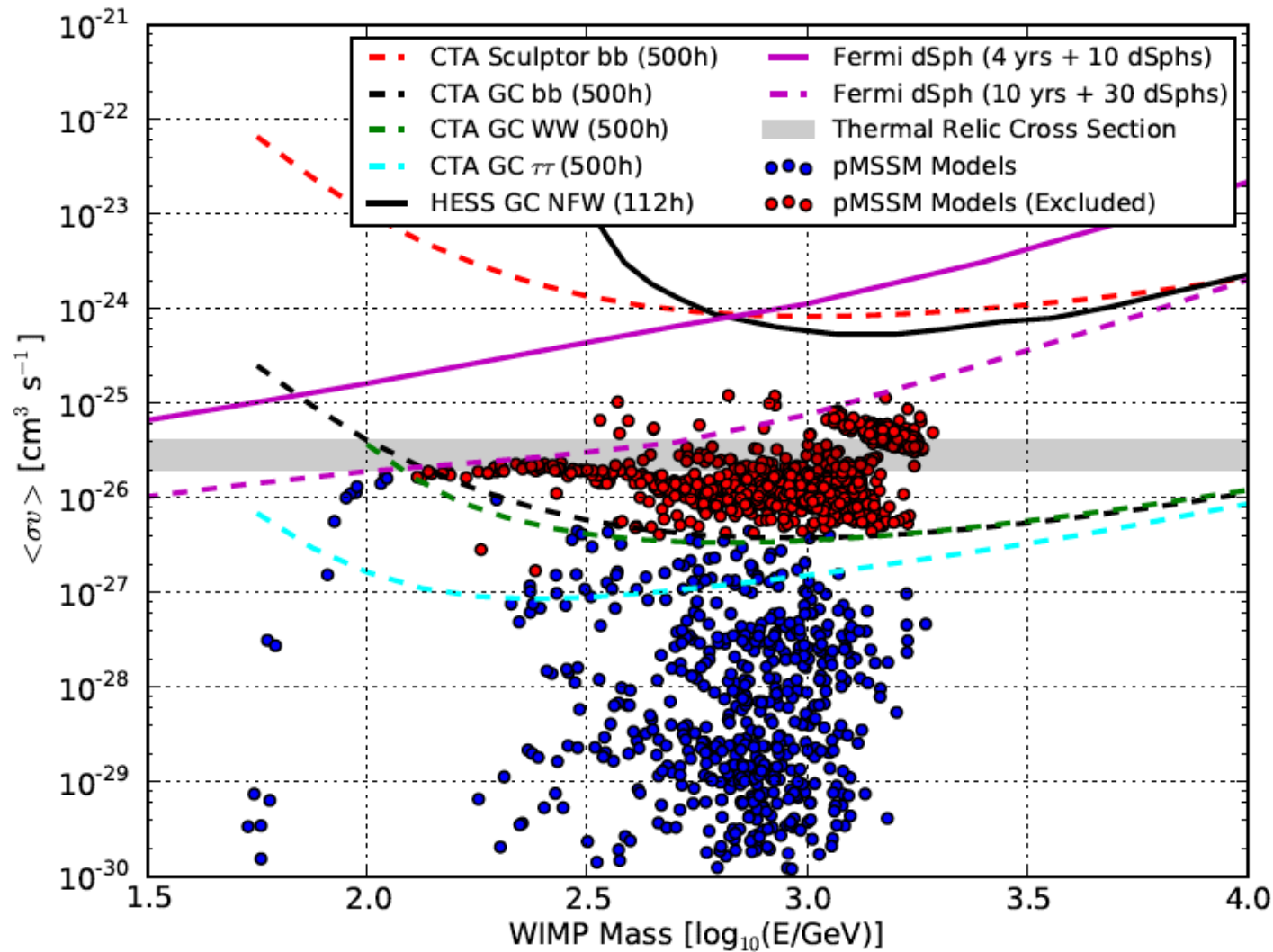
Many techniques for indirect detection ... and many claims!



The *PAMELA/AMS-02* 'excess' (e^+), *WMAP/Planck* 'haze' (radio), *Fermi* 'bubbles' + GC 'excess' + 130 GeV line (all γ -ray) ... have all been ascribed to dark matter annihilations

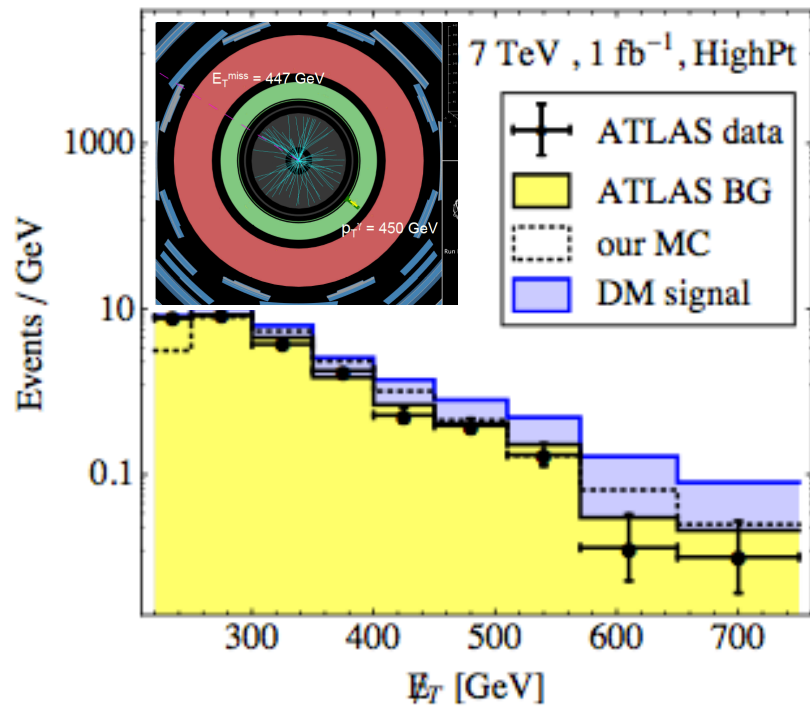
These probe dark matter *elsewhere* in the Galaxy so complement direct detection experiments ... but we are just beginning to understand the astrophysical backgrounds

Prospects are good however for probing down to the expected annihilation signal for a thermal relic with Fermi and CTA



Snowmass CF2 WG Summary, 1310.7040

Moreover low energy extensions of IceCube (*DeepCore*, *PINGU*) will improve the sensitivity for detecting neutrinos from dark matter trapped in the Sun



However these bounds require the scale Λ of the effective operator to exceed ~ 0.7 TeV, while perturbative unitarity requires $g_q, g_\chi < \sqrt{4\pi}$ i.e. $m_R < 2$ TeV ... so for higher energy collisions *cannot* rely on effective operator description (Fox *et al*, 1203.1662)

NB: For scalar-mediated processes, heavy quark loops can significantly enhance the monojet cross-section (Haisch, Kahlhoefer, Unwin, 1208.4605) – very sensitive probe!

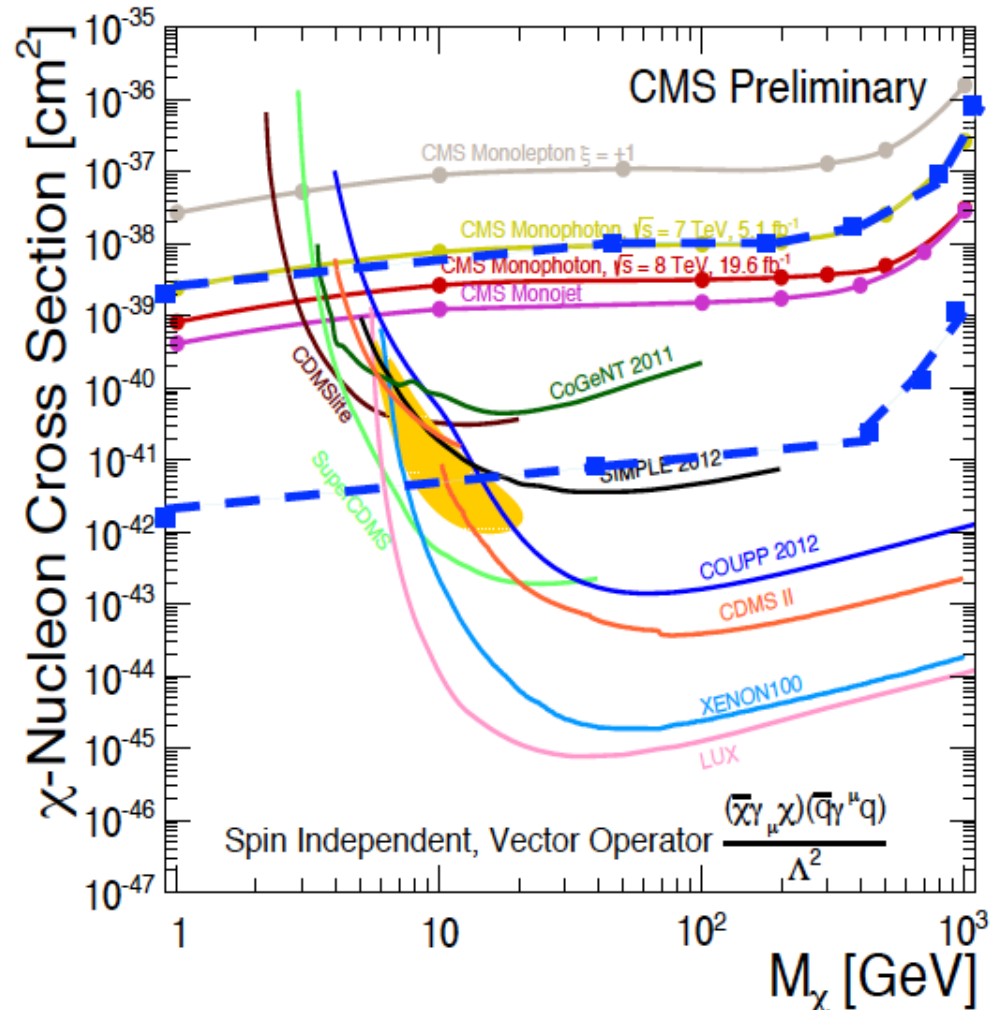
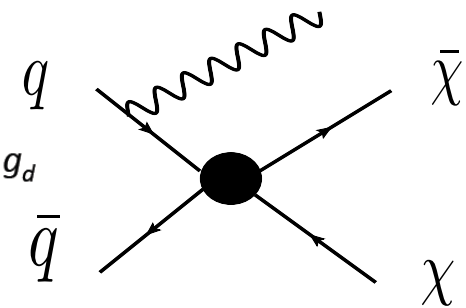
‘Monojet’ events at colliders directly measure the coupling of dark matter to SM particles, e.g.

$$\mathcal{L}_\chi^{\text{eff}} = \frac{1}{\Lambda^2} \bar{\chi} \gamma_\mu \chi \bar{q} \gamma^\mu q$$

$$\rightarrow \sigma_p^{\text{SI}} = \frac{f^2 \mu_{\chi n}^2}{\pi \Lambda^4}, \text{ where } f = 3 \text{ for } g_u = g_d$$

$$\Lambda = m_R / \sqrt{g_q g_\chi}$$

$$\rightarrow \sigma(j + \text{MET}) \sim 1/\Lambda^4 \sim \sigma_p$$



Summary

Experimental situation reminiscent of searches in the '80s
for temperature fluctuations in the CMB

... there were clear theoretical predictions but only upper
limits on detection (causing near crisis for theory)

Finally breakthrough in 1992 that transformed cosmology!

Theoretical expectations for dark matter are not as clear but
there are several *complementary* experimental approaches
and there has been impressive recent progress

There are bound to be false alarms but it is a
reasonable expectation that the nature of dark
matter will soon be determined experimentally