

# Two-Higgs Doublet Models with Scalar Singlet Dark Matter

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## Outline:

- 2HDM Model
- Motivations
- Strategy
- Resulting Constraints on the parameter space
- Direct DM detection constraints
- New Higgs physics at the LHC?
- Summary

2HDM: B. Dumont, J. Gunion, S. Kraml, Y. Jiang, arXiv:1405.3584

2HDMS: A. Drozd, B. Grzadkowski, J. F. Gunion and Y. Jiang, "Extending two-Higgs-doublet models by a singlet scalar field - the Case for Dark Matter", arXiv:1408.2106.

# 2HDM<sub>S</sub> model

## 2HDM<sub>S</sub> - Yukawa Interactions

- Type I (only  $H_2$  couples to fermions)
- Type II ( $H_2$  couples to up-type fermions,  $H_1$  other)

Symmetry:  $Z_2 : H_1 \rightarrow -H_1$ , other scalar fields  $Z_2$ -even

$Z'_2 : S \rightarrow -S$ , other fields  $Z'_2$ -even

$$\begin{aligned} \mathcal{V} = & m_{11}^2 H_1^\dagger H_1 + m_{22}^2 H_2^\dagger H_2 - [m_{12}^2 H_1^\dagger H_2 + \text{h.c.}] + \frac{\lambda_1}{2} (H_1^\dagger H_1)^2 + \frac{\lambda_2}{2} (H_2^\dagger H_2)^2 \\ & + \lambda_3 (H_1^\dagger H_1) (H_2^\dagger H_2) + \lambda_4 (H_1^\dagger H_2) (H_2^\dagger H_1) + \left\{ \frac{\lambda_5}{2} (H_1^\dagger H_2)^2 + \text{h.c.} \right\} \\ & + \frac{m_0^2}{2} S^2 + \frac{\lambda_S}{4!} S^4 + \kappa_1 S^2 (H_1^\dagger H_1) + \kappa_2 S^2 (H_2^\dagger H_2) \end{aligned}$$

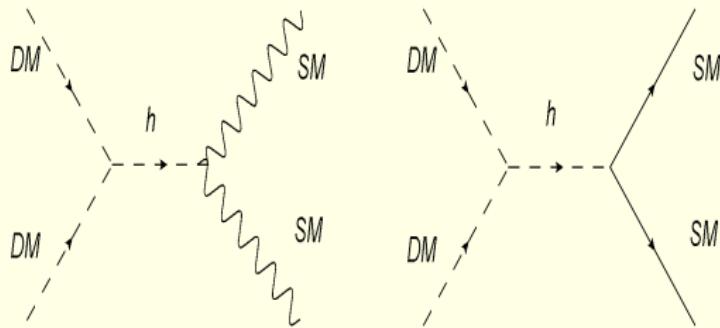
EWSB:  $Z'_2$  unbroken  $\rightarrow$  NO VEV FOR S

$$H_{1,2} = \begin{pmatrix} \varphi_{1,2}^+ \\ (\nu_{1,2} + \rho_{1,2} + i\eta_{1,2})/\sqrt{2} \end{pmatrix} \quad \tan \beta \equiv \frac{\nu_2}{\nu_1}, \quad \nu_1^2 + \nu_2^2 = (246 \text{ GeV})^2$$

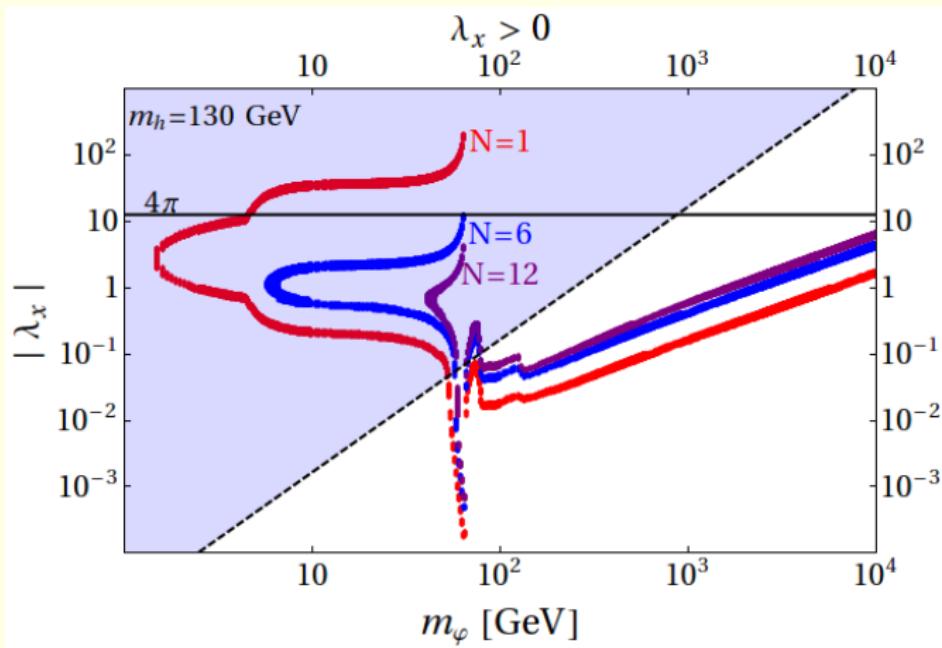
# Motivations

## 2HDM<sub>S</sub>

- An attempt to provide both extra CP violation *and* DM candidate - 2HDM<sub>S</sub> minimal model,
- 2HDM provides an interesting "low-mass" new physics accessible at the LHC,
- To have a chance for  $M_{DM} < m_h/2$



# Motivations



$$BR(h \rightarrow \varphi\varphi) \propto \lambda_x^2 \quad \text{for} \quad V(H, \varphi) = \dots + \lambda_x H^\dagger H \varphi^2$$

5 mass eigenstates:  $h, H, A, H^\pm, S$

- 10 parameters in the potential, various basis possible

## General Basis:

- $\lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5$
- $m_{12}^2, \tan \beta$
- $m_S, \kappa_1, \kappa_2$

## Physical Basis:

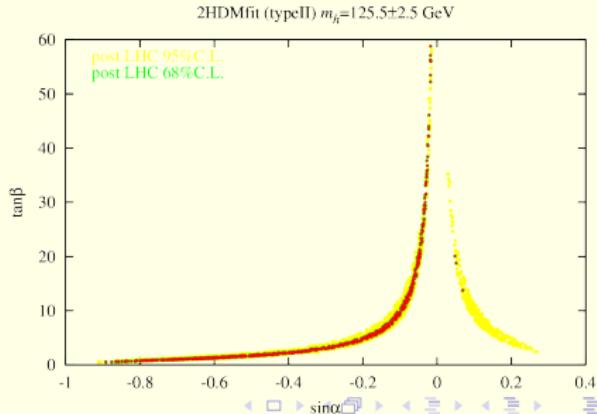
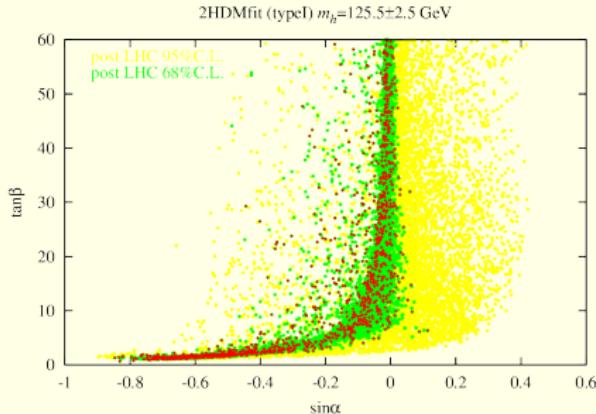
- $m_h, m_H, m_A, m_{H^\pm}, \sin \alpha$
- $m_{12}^2, \tan \beta$
- $m_S, \lambda_h, \lambda_H$

- 2 types of Yukawa interaction

# Strategy

## 2HDM: Dumont, Gunion, Jiang, Kraml

- theoretical constraints  
(perturbativity, vacuum stability, perturbative unitarity)
- experimental constraints
  - B/LEP limits  $H^+$
  - STU
  - heavy Higgs search
  - LHC fit at 68% CL



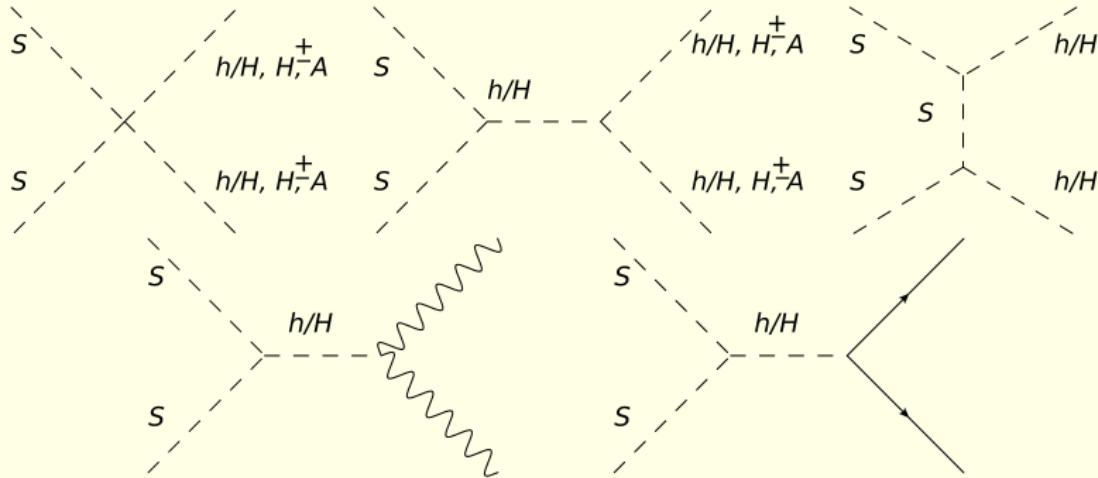
## 2HDM

Take good 2HDM points

Scalar Singlet parameter scan:

- $m_S \in [1 \text{ GeV}, 1 \text{ TeV}]$
- $\lambda_h, \lambda_H \in [-4\pi, 4\pi]$
- theoretical constraints (perturbativity, vacuum stability, perturbative unitarity, EWSB)
- with  $BR(h \rightarrow DM, DM) < 10\%$
- WMAP/Planck
- direct DM detection

# Strategy

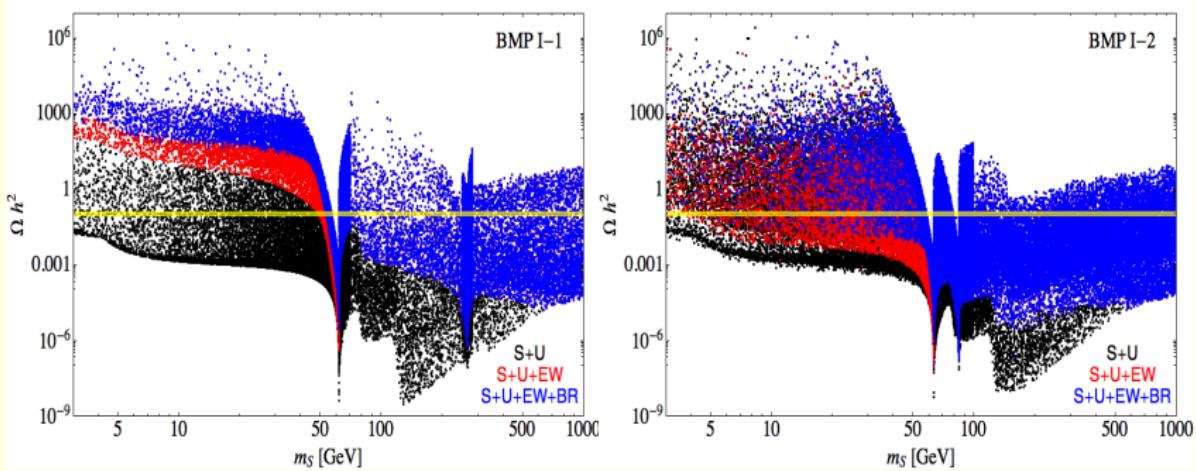


Calculation of DM relic abundance  $\Omega$ :

MicrOmegas by G. Belanger, F. Boudjema, A. Pukhov, A. Semenov,  
arXiv:0803.2360

$$\Omega^{WMAP/Planck} = 0.1187 \pm 0.0017$$

# Resulting Constraints on the parameter space

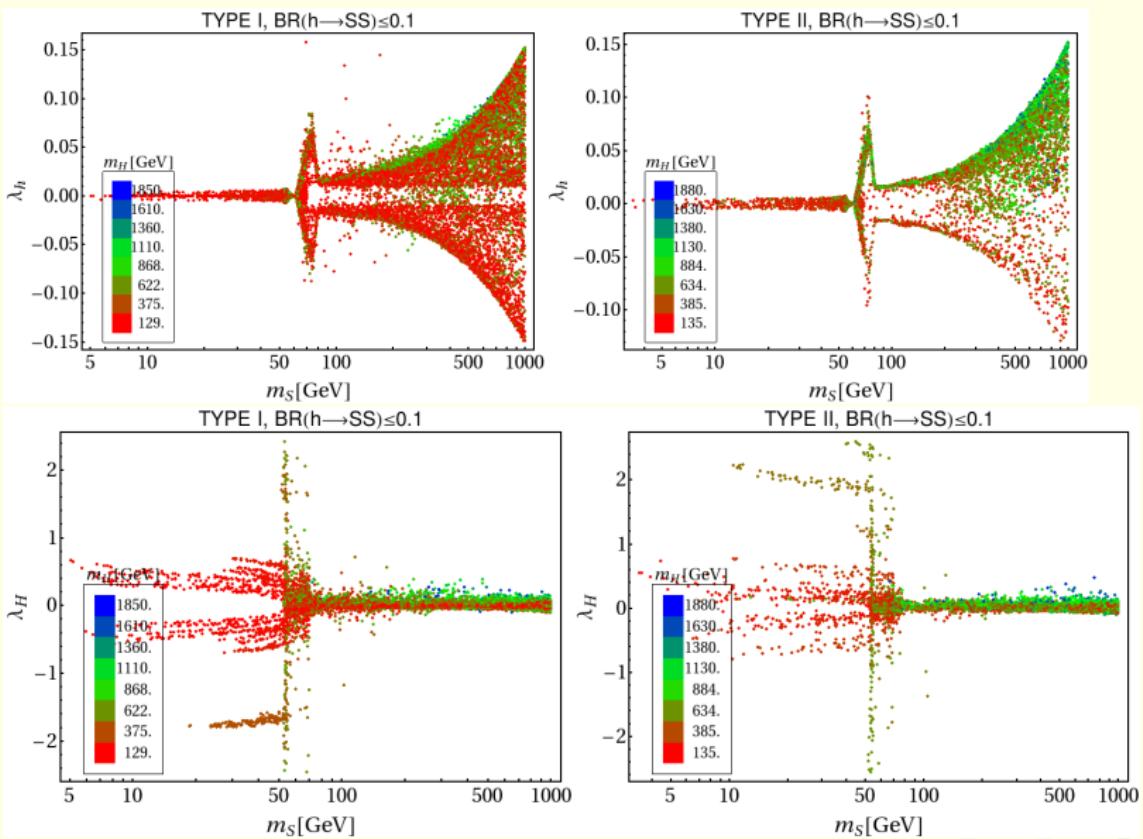


#	$\tan \beta$	$\sin \alpha$	$m_{12}^2$	$m_h$	$m_H$	$m_A$	$m_{H^\pm}$
I-1	1.586	-0.587	+5621	123.71	534.25	645.13	549.25
I-2	1.346	-0.663	-2236	126.49	168.01	560.92	556.94

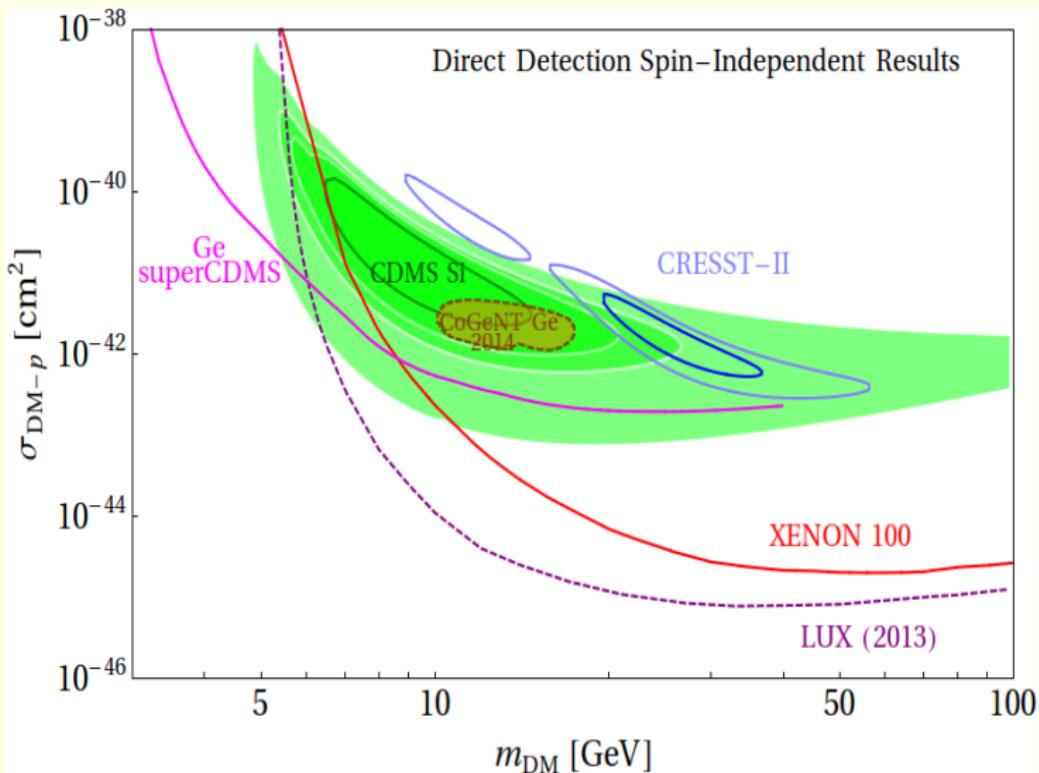
$$BR(h \rightarrow SS) = ???$$

- $\Omega_{DM}$  requires sufficiently strong SM - DM coupling
- search  $\lambda_h, \lambda_H$  give appropriate  $BR(h \rightarrow SS)$  i  $\Omega_{DM}$
- H responsible for DM production!

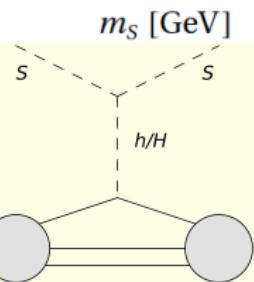
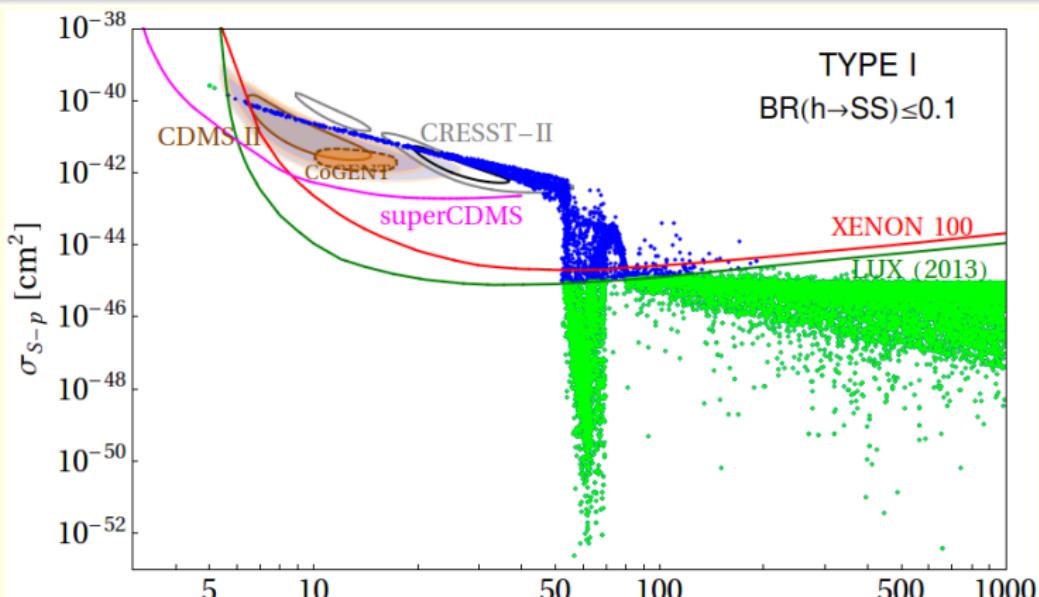
# Resulting Constraints on the parameter space



# Direct DM detection constraints



# Direct DM detection constraints



# Direct DM detection constraints

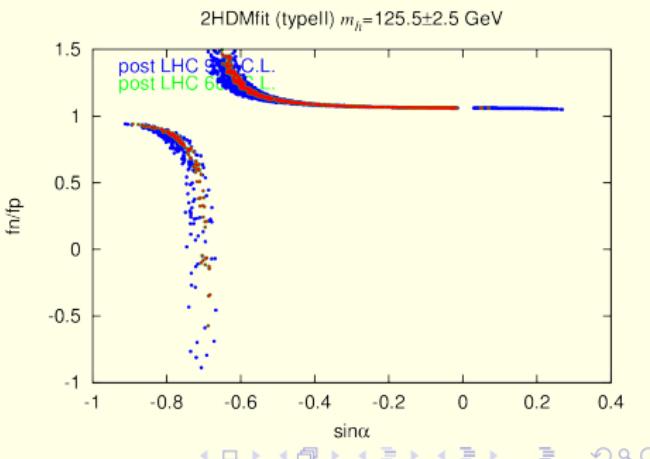
## TYPE II

$$\sigma_{DM-N} = \frac{4\mu_{ZA}^2}{\pi} f_p^2 \left[ Z + \frac{f_n}{f_p} (A - Z) \right]^2$$
$$BR(h \rightarrow SS) \leq 0.1 \Rightarrow \lambda_h < 0.015$$

$$\frac{f_n}{f_p} = \frac{m_n}{m_p} \frac{\sum_q \left[ \left( \frac{\lambda_h}{\lambda_H} \xi_h^q + \left( \frac{m_h}{m_H} \right)^2 \xi_H^q \right) f_n^q \right]}{\sum_q \left[ \left( \frac{\lambda_h}{\lambda_H} \xi_h^q + \left( \frac{m_h}{m_H} \right)^2 \xi_H^q \right) f_p^q \right]} \rightarrow \frac{m_n}{m_p} \frac{\sum_q [(\xi_h^q + \xi_H^q) f_n^q]}{\sum_q [(\xi_h^q + \xi_H^q) f_p^q]} \text{ (S indep.)}$$

**Table:** Yukawa couplings of up and down type quarks to light and heavy Higgs bosons  $h, H$  in Type I/II models. The Yukawa Lagrangian is normalised as follows:  $\mathcal{L}^{\text{Yukawa}} = \frac{m_q}{v} \xi_h^q \bar{q} q h + \frac{m_q}{v} \xi_H^q \bar{q} q H$

	Type I	Type II
$\xi_h^u$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$
$\xi_h^d$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$
$\xi_H^u$	$\sin \alpha / \sin \beta$	$\sin \alpha / \sin \beta$
$\xi_H^d$	$\sin \alpha / \sin \beta$	$\cos \alpha / \cos \beta$



# Direct DM detection constraints

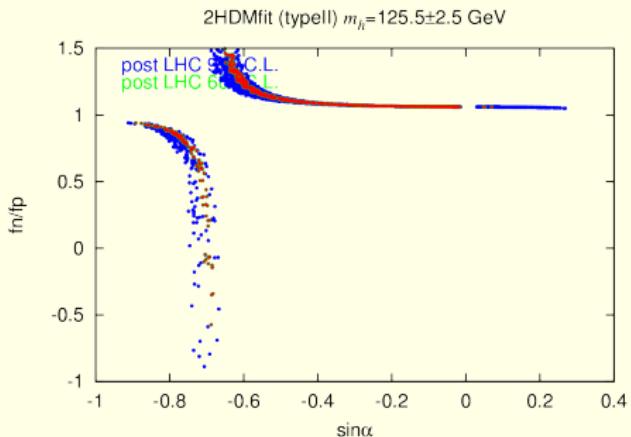
## TYPE II

$$\sigma_{DM-N} = \frac{4\mu^2 Z_A}{\pi} f_p^2 \left[ Z + \frac{f_n}{f_p} (A - Z) \right]^2 \quad \sigma_{DM-p}^{EXP} \geq \sigma_{DM-p}^{THEO} \Theta^{EXP}(f_n, f_p)$$

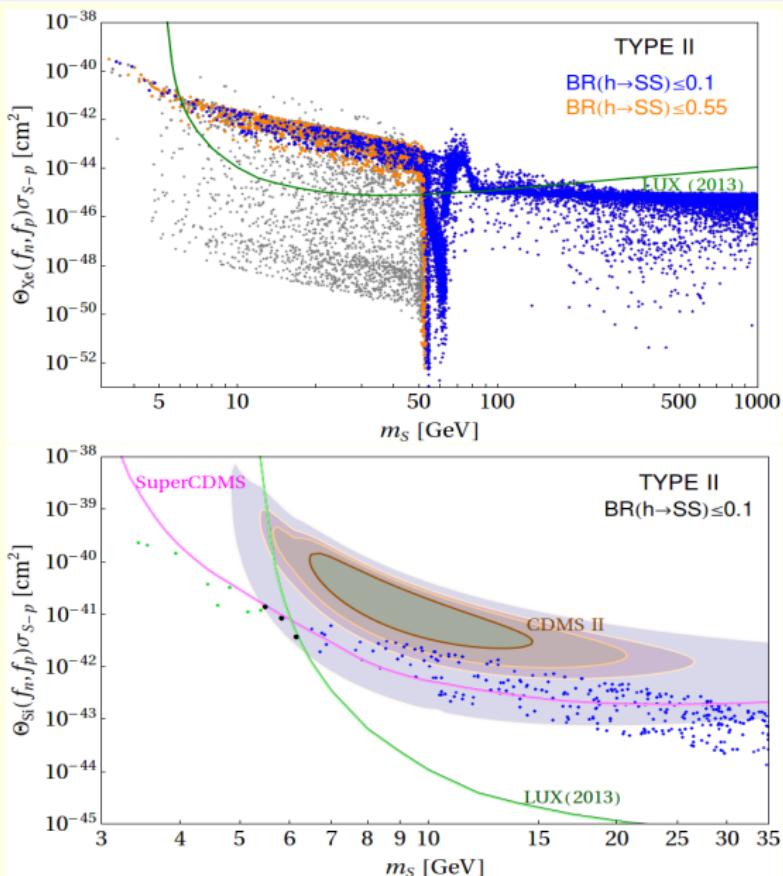
$$\Theta^{EXP}(f_n, f_p) = \sum_I \mu_I \left( \frac{Z_I}{A_I} + \frac{f_n}{f_p} \frac{A_I - Z_I}{A_I} \right)^2$$

**Table:** Yukawa couplings of up and down type quarks to light and heavy Higgs bosons  $h, H$  in Type I/II models. The Yukawa Lagrangian is normalised as follows:  $\mathcal{L}^{Yukawa} = \frac{m_q}{v} \xi_h^q \bar{q} q h + \frac{m_q}{v} \xi_H^q \bar{q} q H$

	Type I	Type II
$\xi_h^u$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$
$\xi_h^d$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$
$\xi_H^u$	$\sin \alpha / \sin \beta$	$\sin \alpha / \sin \beta$
$\xi_H^d$	$\sin \alpha / \sin \beta$	$\cos \alpha / \cos \beta$



# Direct DM detection constraints



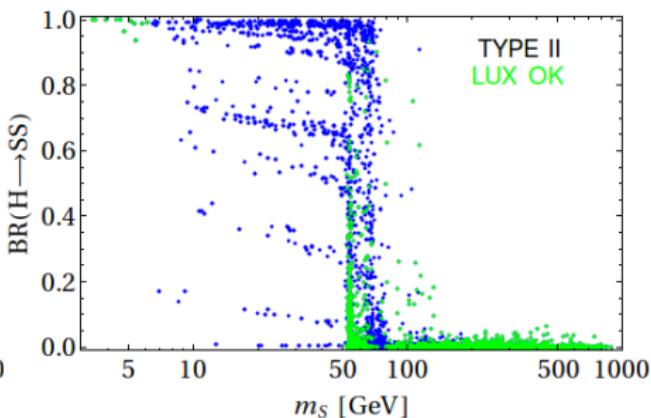
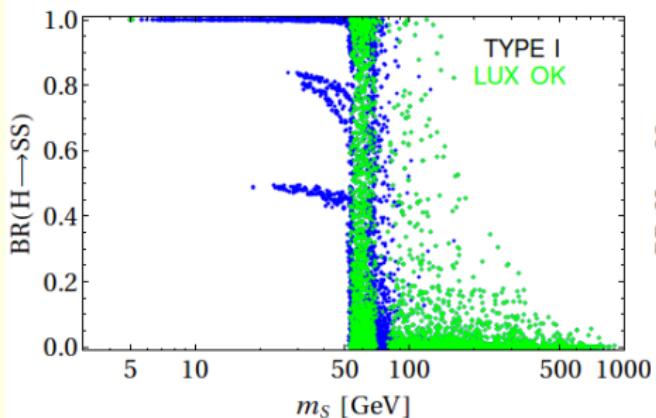
# Direct DM detection constraints

$\tan \beta$	$\sin \alpha$	$m_H$	$m_A$	$m_{H^\pm}$	$m_{12}^2$	$m_S$
2.092	-0.41	138	451	399	-12642	3.44; 3.56; 3.95
3.121	-0.282	187	546	571	8943	4.82; 5.48
2.192	-0.394	209	488	503	7518	5.40
1.728	-0.476	177	318	389	9382	5.16
1.789	-0.461	198	420	430	-6594	4.44; 5.15
1.488	-0.528	157	553	576	-10094	4.61
2.375	-0.363	259	260	339	15899	5.83

**Table:** Summary of the properties of the 2HDM Type II points which make it possible to realize  $m_S < 50$  GeV in agreement with within 99% CL for CDMS II imposing the full set of constraints including the LUX and SuperCDMS bounds and. All masses are given in GeV units.

# New Higgs physics at the LHC?

$H \rightarrow SS$  decay - invisible H!  
 $m_H \sim 130 - 200$  GeV



# Conclusions

- 2HDM is allowed by current collider limits, even in the non-decoupling regime
- 2HDM $\textcolor{red}{S}$  provides a viable DM candidate and an opportunity for extra CP-violation
- 2HDM $\textcolor{red}{S}$  is allowed by current collider and  $\Omega$  limits
- LUX requires  $m_S \gtrsim 50 \text{ GeV}$  (TYPE I, II) or together with SuperCDMS  $m_S \lesssim 6 \text{ GeV}$  (TYPE II)
- CDMS II requires  $|\lambda_h| < 0.05$ ,  $|\lambda_H| > 0.1$ , and implies large  $BR(H \rightarrow SS)$  (TYPE I, II)
- A fit of 2HDM $S$  to LUX, superCDMS and CDMS II is only possible within 99% CL for CDMS II, for TYPE II model, then  $m_s \sim 3.4 - 5.8 \text{ GeV}$ . For those points  $BR(H \rightarrow SS) \gtrsim 90\%$



# Theoretical constraints - Vacuum stability

## 2HDM Tree Level Vacuum Stability Constraints

- $\lambda_1, \lambda_2 > 0$
- $\lambda_3 > -\sqrt{\lambda_1 \lambda_2}$
- $\lambda_3 + \lambda_4 - |\lambda_5| > -\sqrt{\lambda_1 \lambda_2}$
- $\lambda_3 > -\sqrt{\lambda_1 \lambda_2}$

## Scalar Singlet Tree Level Vacuum Stability Constraints

- $\lambda_S > 0$
- $\kappa_1 > -\sqrt{\frac{1}{12} \lambda_1 \lambda_S}$
- $\kappa_2 > -\sqrt{\frac{1}{12} \lambda_2 \lambda_S}$
- if  $\kappa_1 < 0$  or  $\kappa_2 < 0$  then
  - $-2\kappa_1\kappa_2 + \frac{1}{6}\lambda_S\lambda_3 > -\sqrt{4(\frac{1}{12}\lambda_1\lambda_S - \kappa_1^2)(\frac{1}{12}\lambda_2\lambda_S - \kappa_2^2)}$
  - $-2\kappa_1\kappa_2 + \frac{1}{6}\lambda_S(\lambda_3 + \lambda_4 - |\lambda_5|) > -\sqrt{4(\frac{1}{12}\lambda_1\lambda_S - \kappa_1^2)(\frac{1}{12}\lambda_2\lambda_S - \kappa_2^2)}$

# Decoupling limit of 2HDM

$$m_h^2 \rightarrow \mathcal{O}(v^2)$$

$$m_{A,H,H^\pm}^2 \rightarrow \mathcal{O}(|m_{12}^2|)$$

$$\cos(\beta - \alpha) \rightarrow \mathcal{O}(v^2/m_{12}^2)$$

$$m_A^2 = \frac{m_{12}^2}{s_\beta c_\beta} - \frac{1}{2}v^2(2\lambda_5 + \lambda_6 t_\beta^{-1} + \lambda_7 t_\beta),$$

$$m_{H^\pm}^2 = m_{A^0}^2 + \frac{1}{2}v^2(\lambda_5 - \lambda_4).$$

$$\mathcal{M}^2 \equiv m_{A^0}^2 \begin{pmatrix} s_\beta^2 & -s_\beta c_\beta \\ -s_\beta c_\beta & c_\beta^2 \end{pmatrix} + \mathcal{B}^2,$$

$$\mathcal{B}^2 \equiv v^2 \begin{pmatrix} \lambda_1 c_\beta^2 + 2\lambda_6 s_\beta c_\beta + \lambda_5 s_\beta^2 & (\lambda_3 + \lambda_4) s_\beta c_\beta + \lambda_6 c_\beta^2 + \lambda_7 s_\beta^2 \\ (\lambda_3 + \lambda_4) s_\beta c_\beta + \lambda_6 c_\beta^2 + \lambda_7 s_\beta^2 & \lambda_2 s_\beta^2 + 2\lambda_7 s_\beta c_\beta + \lambda_5 c_\beta^2 \end{pmatrix}$$

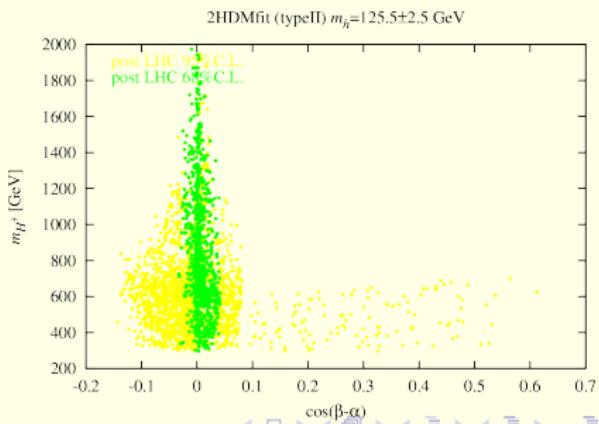
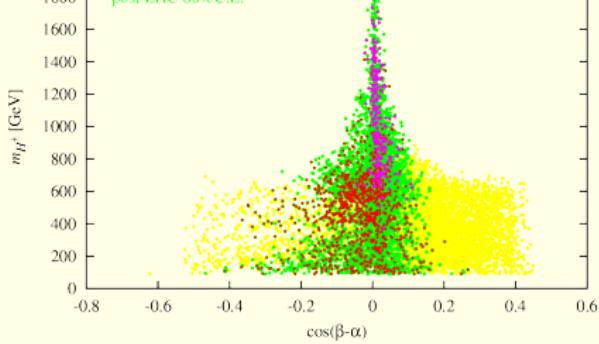
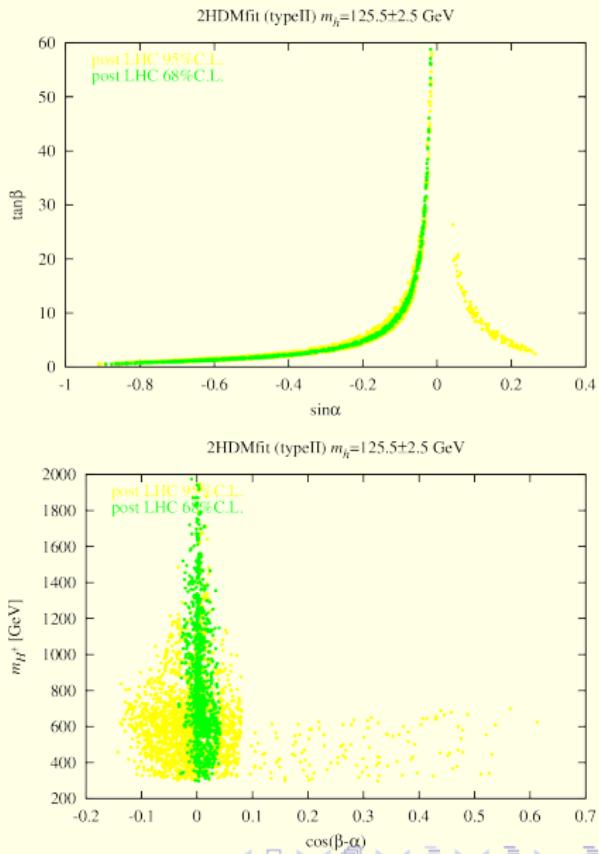
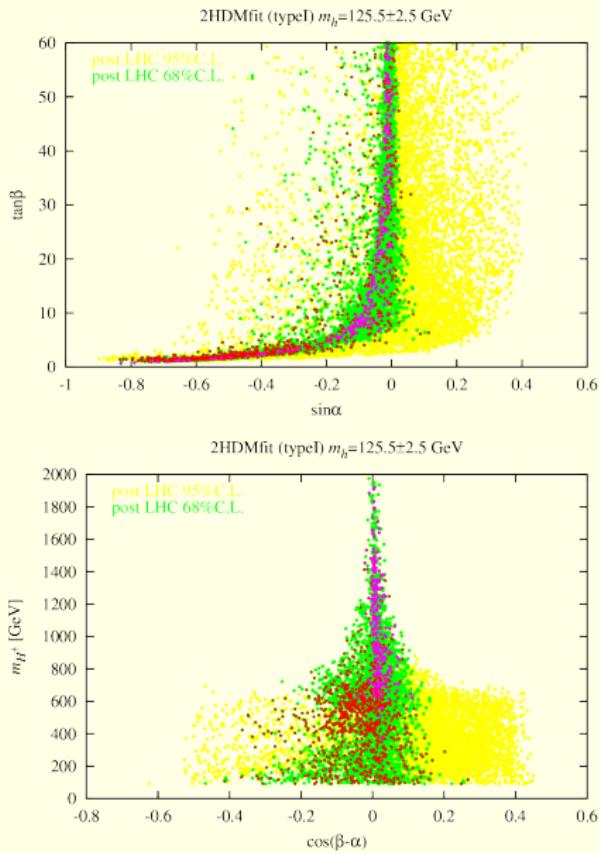
SM-like light Higgs ( $\alpha = \beta - \pi/2$ )

(Yukawa couplings are like in the SM and VVh as well)  
with other scalars heavy

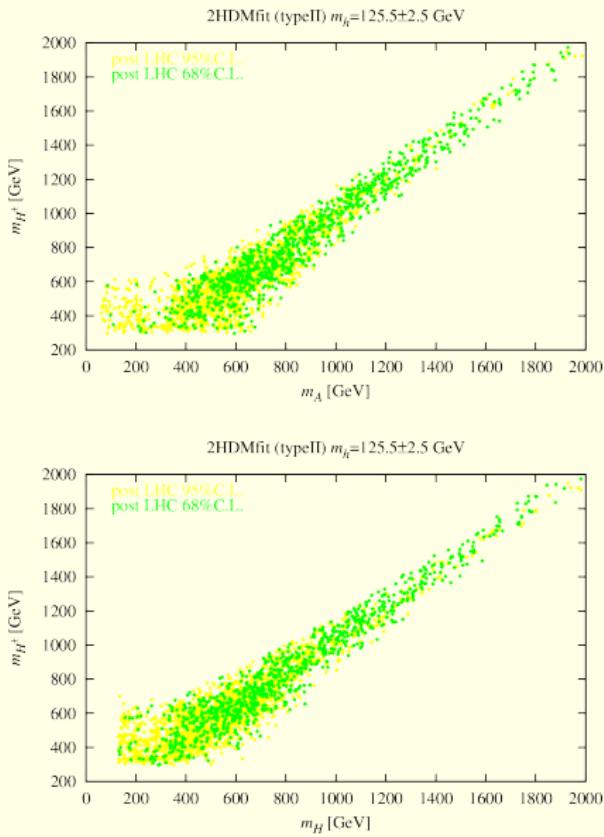
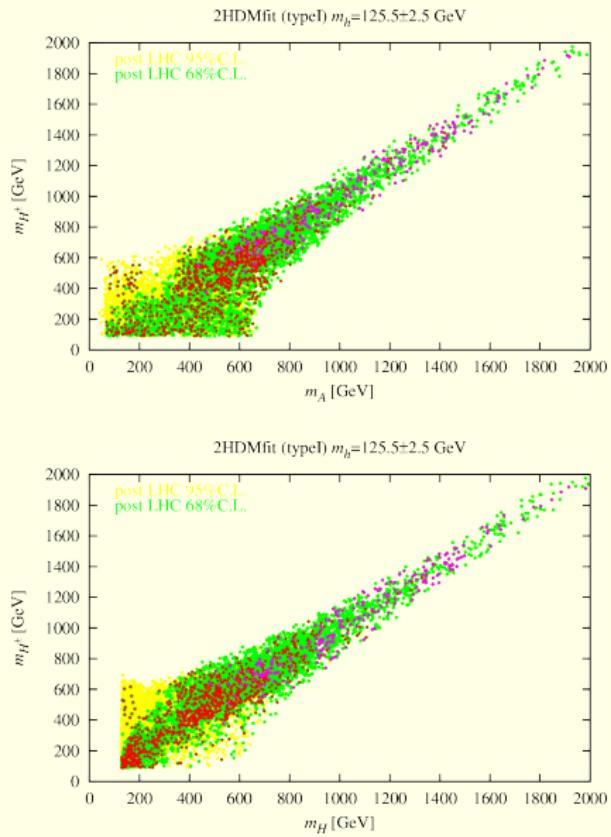
## 2HDM Input:

- Yukawa type I/II
- $m_h \in [123 \text{ GeV}, 128 \text{ GeV}]$
- $m_H \in [128 \text{ GeV}, 2 \text{ TeV}], m_A \in [5 \text{ GeV}, 2 \text{ TeV}]$
- $m_{H^\pm} \in [*, 2 \text{ TeV}]$
- $\sin \alpha \in [-\pi/2, \pi/2], \tan \beta \in [5, 60], m_{12}^2 \in [-(2\text{TeV})^2, (2\text{TeV})^2]$

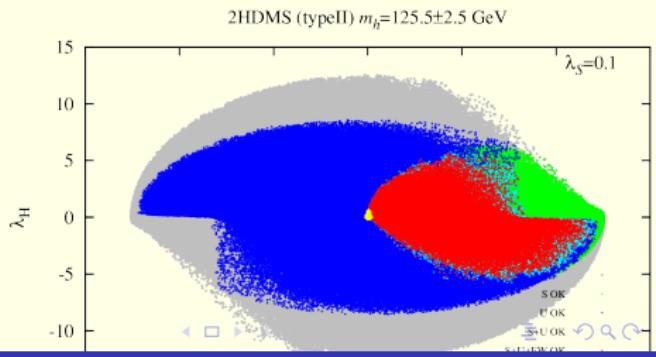
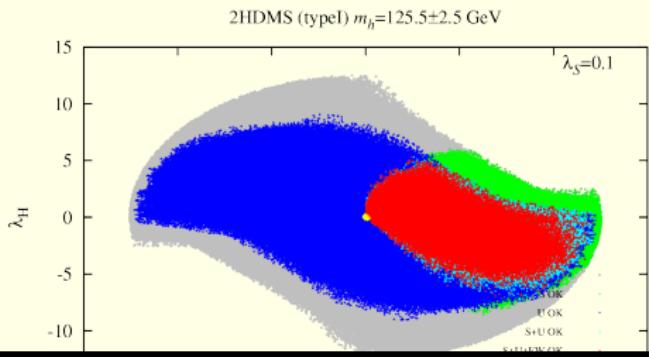
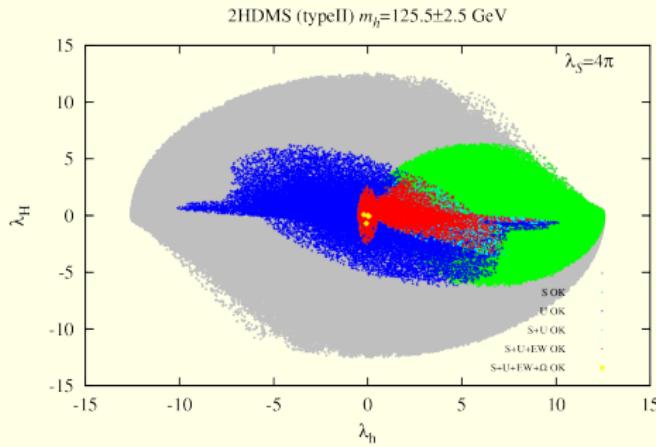
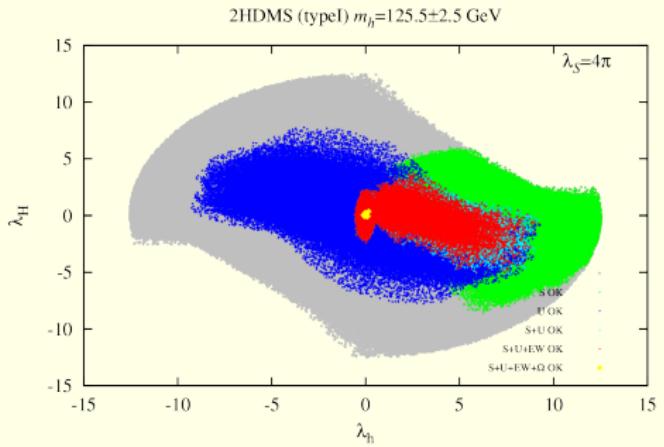
# 2HDM preliminary results Dumont, Gunion, Jiang, Kraml



# 2HDM preliminary results Dumont, Gunion, Jiang, Kraml

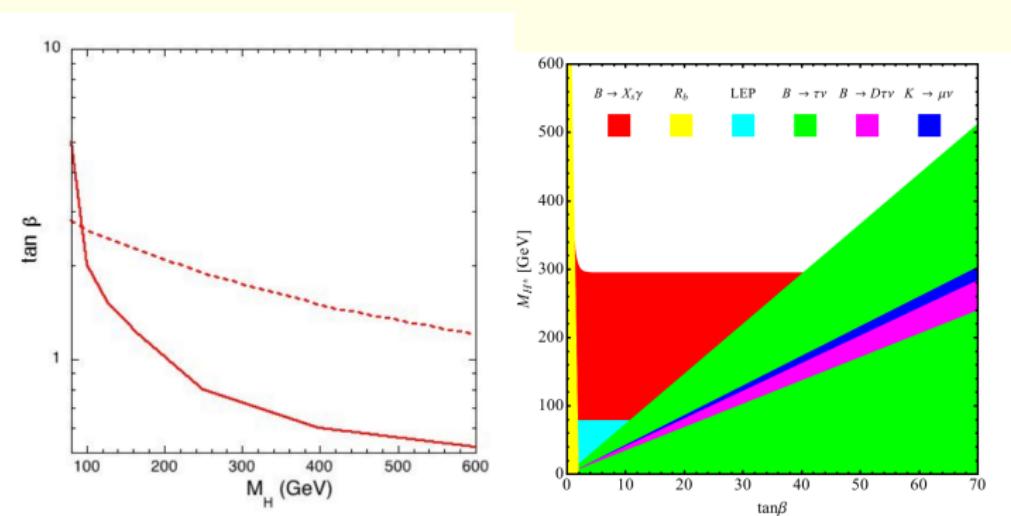


# Theoretical constraints



## Experimental Constraints:

- precision electroweak data: S,T,U constraints
- bounds in the  $(m_{H^\pm}, \tan \beta)$  plane from various B-physics constraints for the type I/II (0805.2141, 1006.0470, 0912.0267)



LEFT: solid line: bounds from  $Z \rightarrow b\bar{b}$ ,  $\epsilon_K$ ,  $\Delta_{B_S}$ ; dashed: bounds from  $B \rightarrow \gamma X_b$

RIGHT: bounds from various B-physics constraints for the type II model

# 2HDM constraints by Dumont, Gunion, Jiang, Kraml

## Search limits on the heavier Higgs bosons

