



- Hierarchy problem
  - in Composite Higgs models: Higgs mass generated dynamically through loops of SM fermions and gauge bosons
  - Higgs mass is naturally light
- Higgs pair production:
  - Measurement of triple Higgs coupling → reconstruction of Higgs potential

- Higgs boson is a bound state from a strongly-interacting sector [Kaplan, Georgi, Galison, Dugan; Dimopoulos, Preskill; Banks]
- Higgs boson emerges as a pseudo-Nambu-Goldstone boson from a global symmetry

$$G \xrightarrow{f} H \supset H_0 = SU(2)_L \times U(1)_Y$$

- $G$  is explicitly broken by couplings of SM fields to strong sector  
→ loops of SM fermions and gauge bosons generate Higgs potential
- Higgs boson is naturally separated by a mass gap from the other usual resonances
- In an effective low-energy description only the Higgs couplings to the SM fields are modified and depend on  $\xi = \frac{v^2}{f^2}$  with  $\xi \in [0, 1]$   
[Giudice, Grojean, Pomarol, Rattazzi]

- Realized as 5D theory on AdS spacetime  $\rightarrow$  holographic interpretation in terms of 4D strongly coupled field theories
- Global symmetry  $G = SO(5) \times U(1)_X$  broken down to
  - $SO(4) \times U(1)_X$  on IR-brane
  - $SU(2)_L \times U(1)_Y$  on UV-brane
- Higgs-fermion and Higgs self-couplings depend on the representation of the fermions:
  - spinorial representation:  $MCHM_4$
  - fundamental representation:  $MCHM_5$

|             | MCHM <sub>4</sub> | MCHM <sub>5</sub>             |
|-------------|-------------------|-------------------------------|
| $HVV$       | $\sqrt{1-\xi}$    | $\sqrt{1-\xi}$                |
| $HHVV$      | $1-2\xi$          | $1-2\xi$                      |
| $HHH$       | $\sqrt{1-\xi}$    | $\frac{1-2\xi}{\sqrt{1-\xi}}$ |
| $Hf\bar{f}$ | $\sqrt{1-\xi}$    | $\frac{1-2\xi}{\sqrt{1-\xi}}$ |

New coupling:

$$g_{HHf\bar{f}} = \frac{m_f}{v^2} \xi \quad \text{in MCHM}_4$$

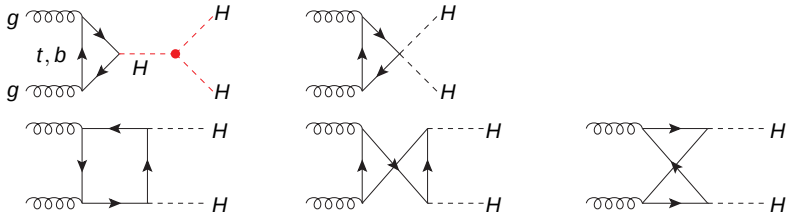
and

$$g_{HHf\bar{f}} = \frac{m_f}{v^2} 4\xi \quad \text{in MCHM}_5$$

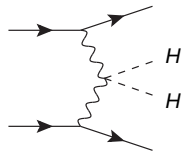
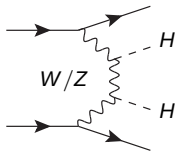
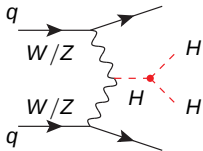
In SM limit  $\xi \rightarrow 0$  the new coupling vanishes.

- Higgs self-couplings are necessary to investigate Higgs potential.
- In multi-Higgs-production Higgs self-couplings can be measured.
- Most important processes in SM at the LHC:
  - Gluon fusion
  - Vector boson fusion
  - Double Higgs-strahlung

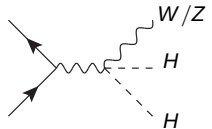
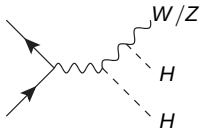
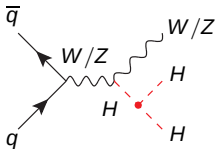
Gluon fusion:

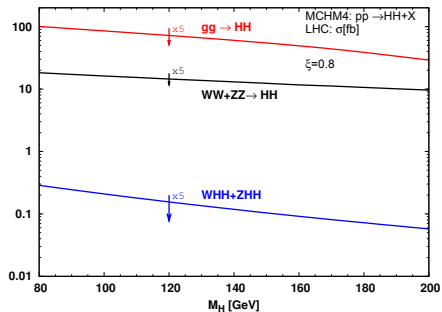
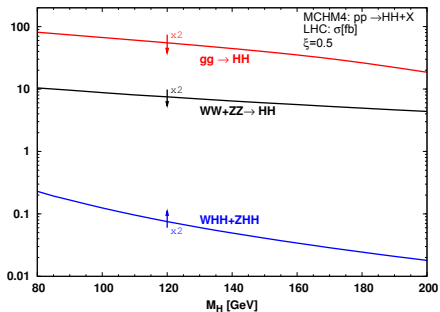
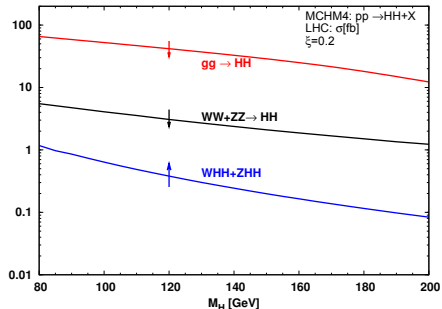
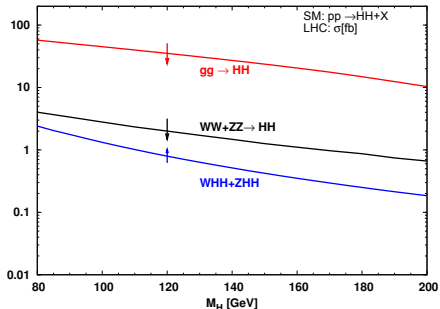


## Vector boson fusion:

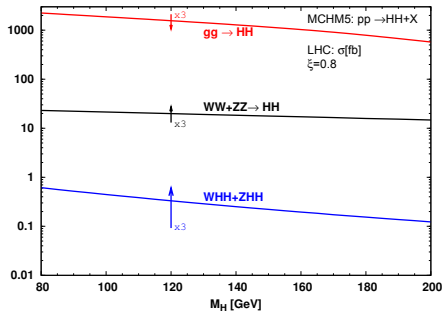
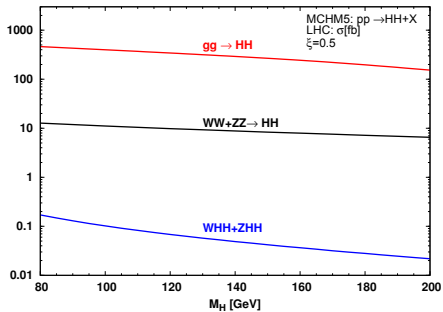
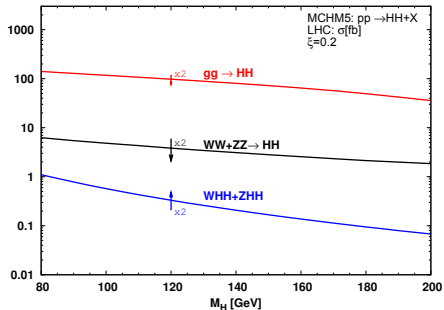
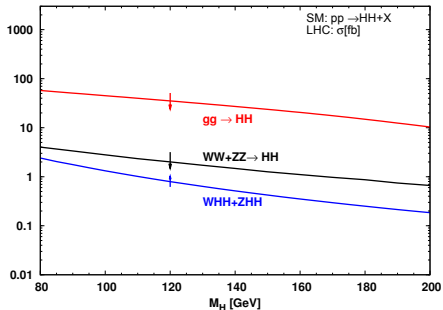


## Double Higgs-strahlung:



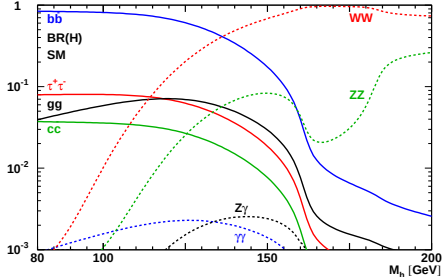






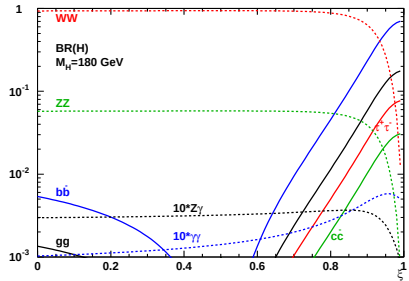
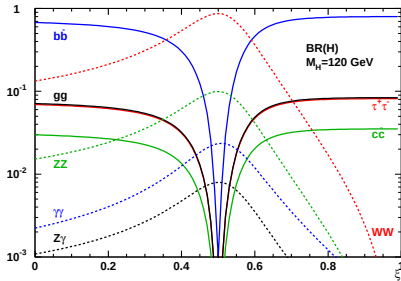
# Branching ratios [Espinosa, Grojean, Mühlleitner]

MCHM<sub>4</sub>:



|             | MCHM <sub>4</sub> | MCHM <sub>5</sub>             |
|-------------|-------------------|-------------------------------|
| $HVV$       | $\sqrt{1-\xi}$    | $\sqrt{1-\xi}$                |
| $Hf\bar{f}$ | $\sqrt{1-\xi}$    | $\frac{1-2\xi}{\sqrt{1-\xi}}$ |

MCHM<sub>5</sub>:



# Sensitivities on $\lambda_{HHH} \neq 0$ in gluon fusion

In the SM the decay channel  $b\bar{b}\gamma\gamma$  for low Higgs masses and  $W^+W^-W^+W^-$  for Higgs masses above the gauge boson threshold have best prospects

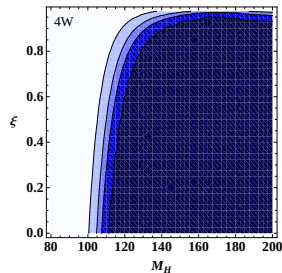
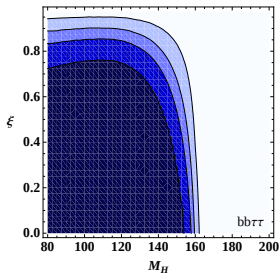
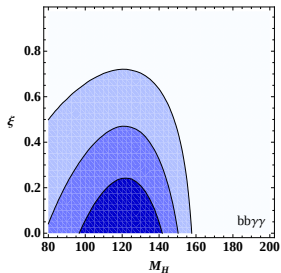
[Baur, Plehn, Rainwater]

Assumption: EWSB is realized in the framework of MCHM ( $\xi$  can be measured with accuracy of  $\sim 20\%$  [Bock, Lafaye, Plehn, Rauch, Zerwas, Zerwas])

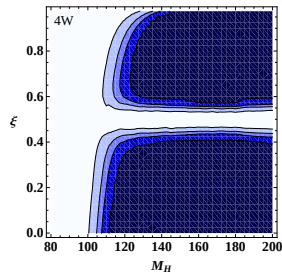
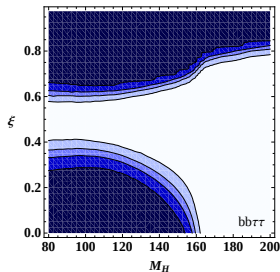
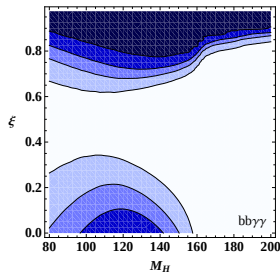
Criterion:

$$S + \beta\sqrt{S} < S_{\lambda_{HHH}=0} \quad \text{or} \quad S - \beta\sqrt{S} > S_{\lambda_{HHH}=0} \quad (\beta = 1, 2, 3, 5)$$

MCHM<sub>4</sub> for  $\int \mathcal{L} = 300 \text{ fb}^{-1}$ :



MCHM<sub>5</sub> for  $\int \mathcal{L} = 300 \text{ fb}^{-1}$ :



Above gauge boson threshold: Prospects of measuring non-vanishing  $\lambda_{HHH}$  are good.

Below gauge boson threshold:  $b\bar{b}\tau^+\tau^-$  might be possible.

- Sensitivity areas present ideal case  $\rightarrow$  for a full analysis: Detector properties and background processes must be investigated
- But e.g. for the  $4W$  final state with  $W^+W^-W^+W^- \rightarrow (jjl^\pm\nu)(jjl^\pm\nu)$ :  
In SM: For  $150 \text{ GeV} \leq M_H \leq 200 \text{ GeV}$  a vanishing triple Higgs coupling can be excluded at 95% C.L. for  $300 \text{ fb}^{-1}$
- Dominating background ( $\mathcal{O}(\alpha_s\alpha^3)$ )
  - $\rightarrow$  no Higgs in intermediate state
  - $\rightarrow$  leading background processes are the same as in SM
- But: Signal cross section is larger as in the SM!

- Composite Higgs models are an interesting alternative to the SM
- Cross sections for Higgs pair production via gluon fusion and vector boson fusion are enhanced compared to the SM for all  $\xi$
- Cross section for Higgs pair production via double Higgs-strahlung is reduced compared to the SM
- Branching ratios in MCHM<sub>5</sub> are changed compared to the SM and depend on  $\xi$ .
- Prospects of measuring non-vanishing  $\lambda_{HHH}$  for large Higgs masses in  $W^+W^-W^+W^-$  decay channel good, for low Higgs masses  $b\bar{b}\tau^+\tau^-$  might be possible
- Measuring  $\lambda_{HHH}$  with higher precision might be possible for higher luminosities.

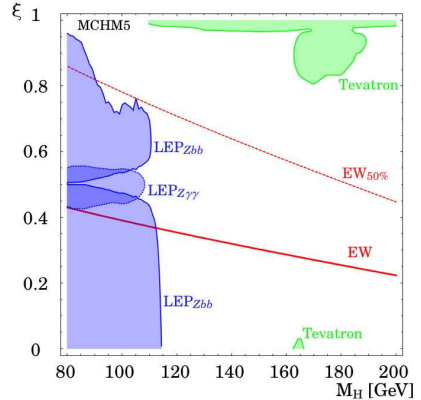
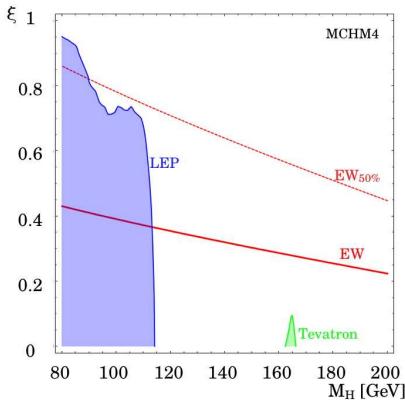
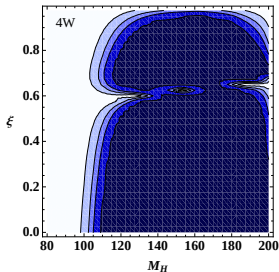
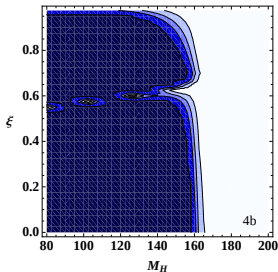


Figure: See [Espinosa, Grojean, Mühlleitner]

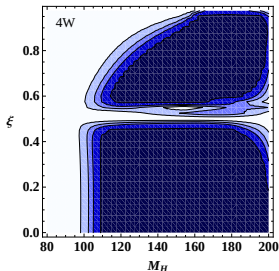
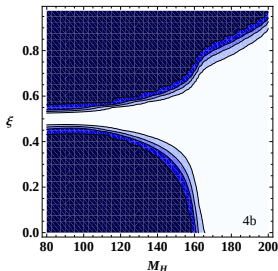
For constraints in model with partially composite top, see [Barbieri, Bellazzini, Rychkov, Varagnolo; Anastasiou, Furlan, Santiago; Gillioz; Lodone]

# Double Higgs-strahlung at the ILC ( $\sqrt{s} = 0.5$ TeV, $\int \mathcal{L} = 500 \text{ fb}^{-1}$ )

MCHM<sub>4</sub>:



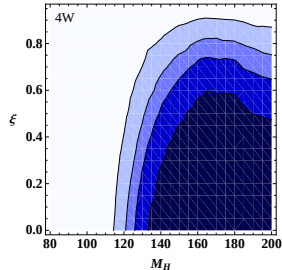
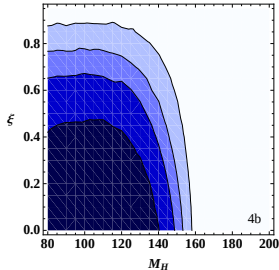
MCHM<sub>5</sub>:



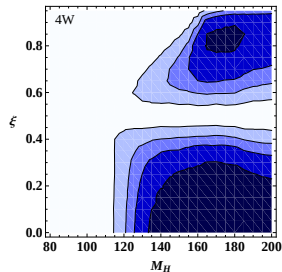
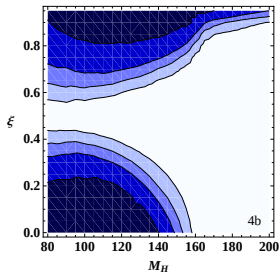


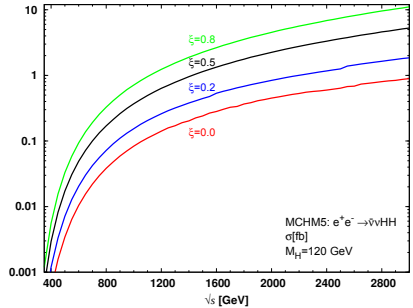
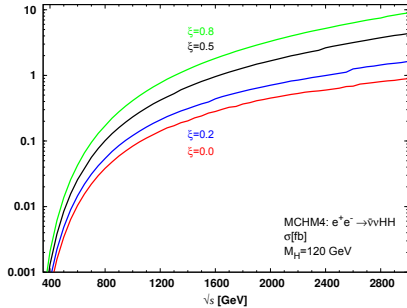
# W boson fusion at the ILC ( $\sqrt{s} = 0.5$ TeV, $\int \mathcal{L} = 500 \text{ fb}^{-1}$ )

MCHM<sub>4</sub>:



MCHM<sub>5</sub>:





$$\mathcal{M} \xrightarrow{s \rightarrow \infty} -\sqrt{2}G_F s \xi$$

New kinetic terms  $\rightarrow$  field redefinition

$$\Phi = \frac{v}{\sqrt{2}} \begin{pmatrix} 0 \\ \frac{1}{v} \left( H - \frac{c_H \xi}{2} \left( H + \frac{H^2}{v} + \frac{H^3}{3v^2} \right) \right) + 1 \end{pmatrix}$$

$\rightarrow$  redefinition of Higgs and fermion masses and vacuum expectation value

$$\frac{v^2}{2} = \frac{\mu^2}{2\lambda} \left( 1 - \frac{3}{4} c_6 \xi \right) = \frac{(246 \text{ GeV})^2}{2} .$$

$$m_f = \frac{1}{\sqrt{2}} y_f v \left( 1 + \frac{\xi}{2} c_y \right) ,$$

$$\frac{M_H^2}{2} = \frac{\left( \sqrt{2\lambda} v \right)^2}{2} \left( 1 - c_H \xi + \frac{3}{4} c_6 \xi \right) .$$

$$g_{HVV} = g_{HVV}^{SM} \left( 1 - \frac{c_H}{2} \xi \right)$$

$$g_{Hff} = g_{Hff}^{SM} \left( 1 - \xi \frac{c_H}{2} + \xi c_y \right)$$

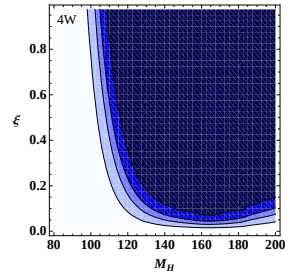
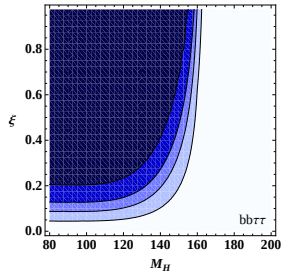
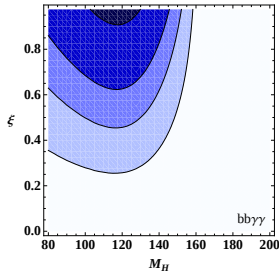
$$g_{HHH} = g_{HHH}^{SM} \left( 1 + \xi c_6 - \xi \frac{3c_H}{2} \right)$$

$$\text{with } g_{HWW}^{SM} = g M_W \text{ and } g_{HZZ}^{SM} = \frac{g M_Z}{2}$$

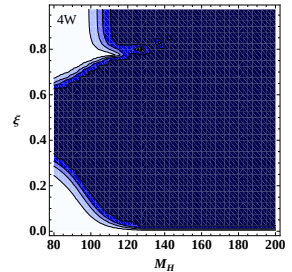
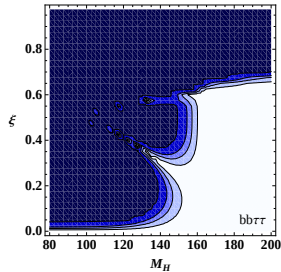
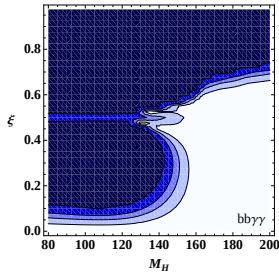
$$\text{with } g_{Hff}^{SM} = \frac{g m_f}{2 M_W}$$

$$\text{with } g_{HHH}^{SM} = \frac{3 g M_H^2}{2 M_W}$$

# Can the MCHM<sub>4</sub> be distinguished from the SM for $\int \mathcal{L} = 300 \text{ fb}^{-1}$ ?

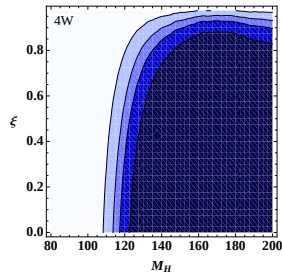
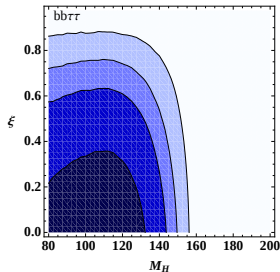
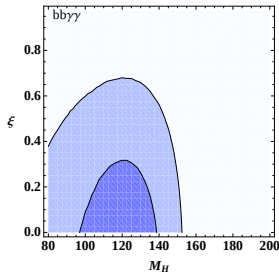


# Can the MCHM<sub>5</sub> be distinguished from the SM for $\int \mathcal{L} = 300 \text{ fb}^{-1}$ ?



# Can $\lambda_{HHH}$ be measured with 30% precision in MCHM<sub>4</sub>?

$\int \mathcal{L} = 3000 \text{ fb}^{-1}$  for  $b\bar{b}\gamma\gamma$ ,  $\int \mathcal{L} = 600 \text{ fb}^{-1}$  for  $b\bar{b}\tau^+\tau^-$  and  $4W$



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