

Search for new physics in rare charm processes

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Outline

➤ Rare charm decays \longrightarrow experimental results

f_{D_s} puzzle: lattice – experiment in $D_s \rightarrow l\nu_l$

Are there any correlations between NP in $D_s \rightarrow l\nu_l$ and
 $D \rightarrow \mu^+ \mu^-$?

➤ Leptoquarks mediated tree level processes

➤ general approach , GUT SU(5) and proton decay

• SM allowed (charged current)

• SM forbidden at tree level \longrightarrow FCNCs

➤ LFV

➤ Summary

Rare charm decays: experimental results

$$D \rightarrow X\gamma$$

Belle and BABAR $D \rightarrow \phi\gamma$ $(2.73 \pm 0.30 \pm 0.36) \times 10^{-5}$
In 2008 BABAR $D \rightarrow K^*\gamma$ $(3.22 \pm 0.20 \pm 0.27) \times 10^{-4}$

can be understood within
SM -long distance contributions

Dilepton rare charm decays

D0 $D \rightarrow \pi\mu\mu < 3.9 \times 10^{-6}$
CLEO-c $D \rightarrow \pi ee < 4.7 \times 10^{-6}$

CDF result (2008)

$$BR(D \rightarrow \mu^+ \mu^-) < 4.3 \times 10^{-7}$$

EPS (2009), Belle col. improvement!

$$BR(D \rightarrow \mu^+ \mu^-) < 1.4 \times 10^{-7}$$

Lepton flavor violating processes

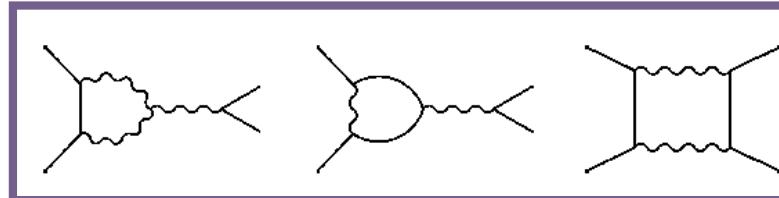
$$D \rightarrow e^+ \mu^- < 8.1 \times 10^{-7} \quad D^+ \rightarrow K^+ e^- \mu^+ < 3.7 \times 10^{-6}$$

$$D_s^+ \rightarrow K^+ e^- \mu^+ < 3.6 \times 10^{-6} \quad \Lambda_c^+ \rightarrow p e^- \mu^+ < 7.5 \times 10^{-6}$$

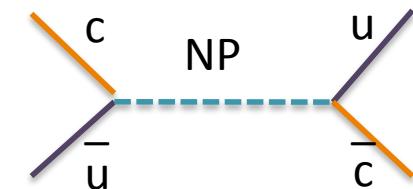
$$D \rightarrow \mu^+ \mu^-$$

possibility for new physics

SM



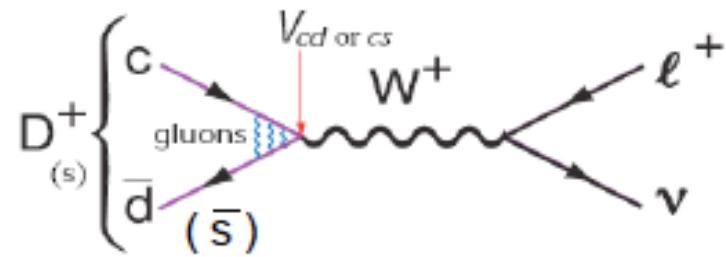
Model	$\mathcal{B}_{D^0 \rightarrow \mu^+ \mu^-}$
Standard Model (SD)	$\sim 10^{-18}$
Standard Model (LD)	$\sim \text{several} \times 10^{-13}$
$Q = +2/3$ Vectorlike Singlet	4.3×10^{-11}
$Q = -1/3$ Vectorlike Singlet	$1 \times 10^{-11} (m_S/500 \text{ GeV})^2$
$Q = -1/3$ Fourth Family	$1 \times 10^{-11} (m_S/500 \text{ GeV})^2$
Z' Standard Model (LD)	$2.4 \times 10^{-12} / (M_{Z'}(\text{TeV}))^2$
Family Symmetry	$0.7 \cdot 10^{-18}$ (Case A)
RPV-SUSY	$1.7 \times 10^{-9} (500 \text{ GeV}/m_{\tilde{d}_k})^2$



Petrov ,
CHARM 2009

Puzzle

$$D_s \rightarrow l\nu_l$$



disagreement between experimental and lattice result

$$D \rightarrow l\nu_l$$

lattice and experiment are in agreement

Are there any correlations between NP in $D \rightarrow l\nu_l$ and

$$D \rightarrow \mu^+ \mu^-$$
 ?

$D_s^+ \rightarrow \mu^+\nu$ and two $D_s^+ \rightarrow \tau^+\nu$ measurements statistically independent: combine

Average:

$$f_{D_s} = 259.5 \pm 6.6 \pm 3.1 \text{ MeV}$$

Lattice: $241 \pm 3 \text{ MeV}$

Puzzle!

Recall

$$f_D = 205.8 \pm 8.5 \pm 2.5 \text{ MeV}$$

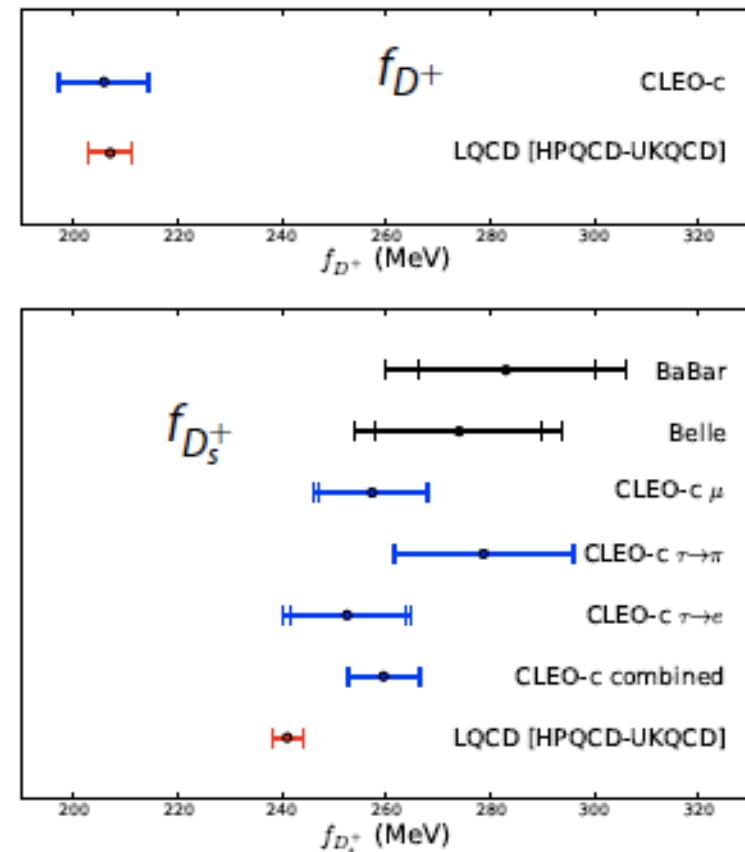
Lattice: $207 \pm 4 \text{ MeV}$

So

$$f_{D_s}/f_D = 1.26 \pm 0.06 \pm 0.02$$

Lattice: 1.162 ± 0.009

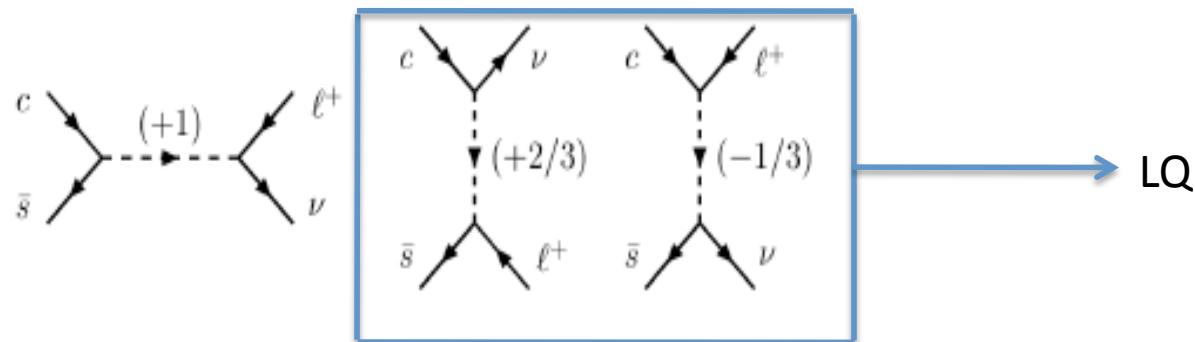
PRD 79, 052001 (2009)



from P. Onysi, CHARM (2009)

The f_{D_s} puzzle introduced new possibility: NP effects in charged charm meson leptonic decays.

Dobrescu and Kronfeld (2008) have suggested that charged Higgs or scalar leptoquarks can explain the lattice-experiment discrepancy.



(I. Doršner , S.F., J. F. Kamenik and N. Košnik ; **0906.5585**)

We consider all possible renormalizable leptoquark interactions with SM matter fields.

Leptoquarks

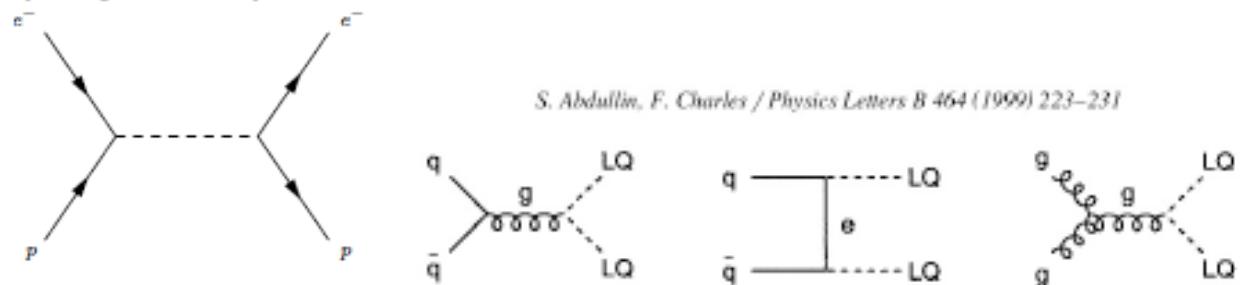
- Singlets
 - Doublets
 - Triplets
- } $SU(2)_L$

Leptoquarks

★ arise naturally in unification theories, Pati-Salam, R -parity violating SUSY (squarks), extended technicolor, compositeness models

★ Experimentally they have been searched directly:

Single production at $e^\pm p \rightarrow e^\pm p$ experiments (HERA, ZEUS)
⇒ Constraints in the coupling-mass plane



★ Pair production in hadron colliders

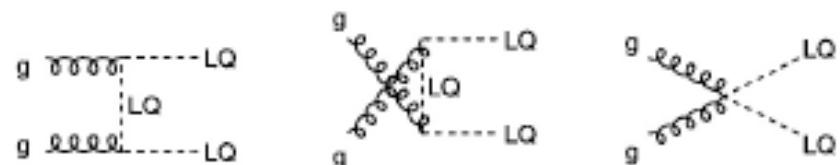
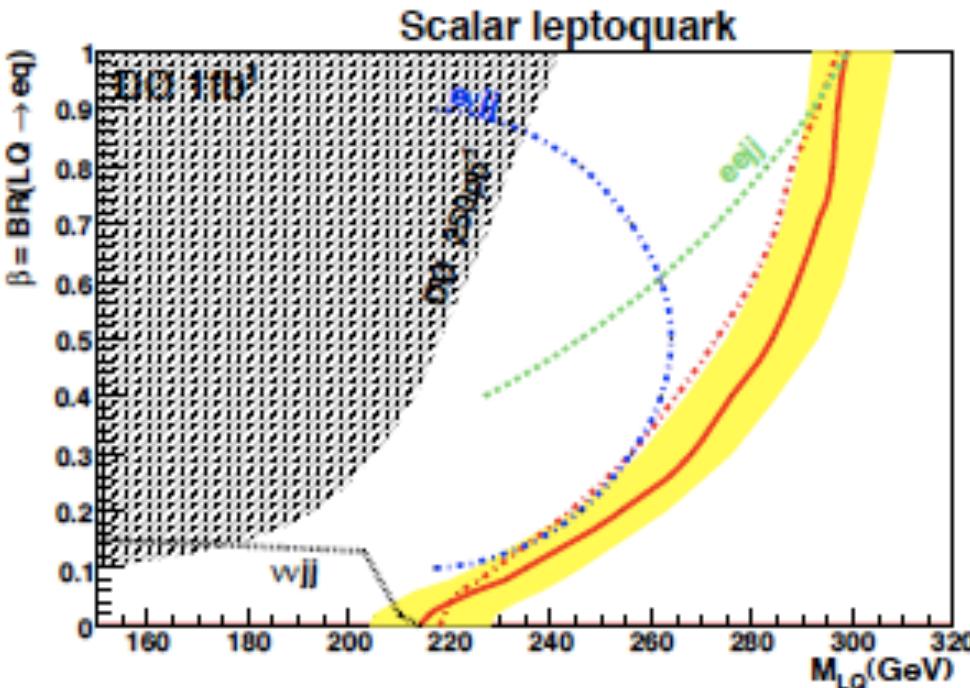


Fig. 1. Leptoquark pair production diagrams.

★ False indication for on-shell production in HERA ep scattering (1997)

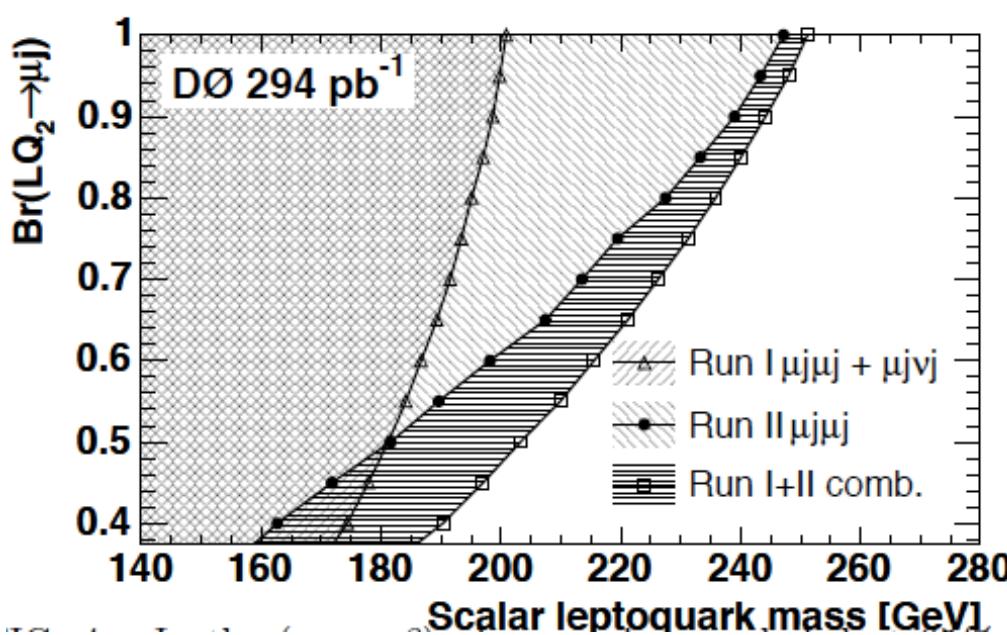
★ Lower bound on mass from D0,CDF $\sim 230 - 250$ GeV for leptoquarks coupled to 1st or 2nd generation



DØ Collaboration

arXiv: 0907.1048

(first generation)



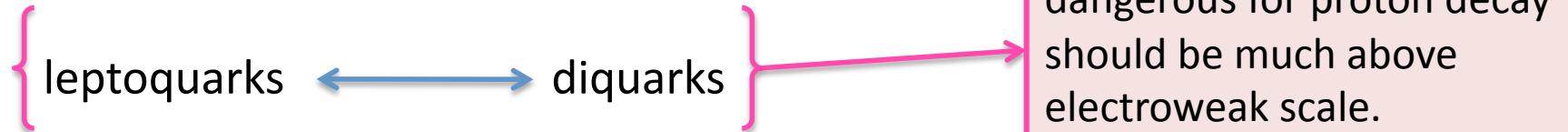
hep-ex/0601047

(second generation)

➤ leptoquarks and proton decay

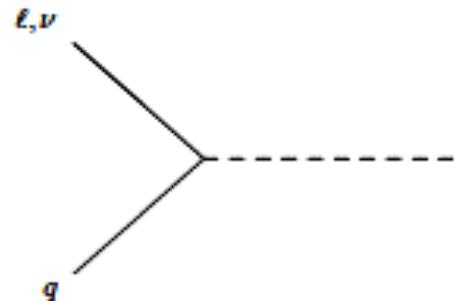


➤ leptoquarks in low energy physics



“genuine” leptoquark: couples to quark and lepton

If one requires that leptoquarks contribute only at tree level , then one can talk about:



$SU(3)_c \times SU(2)_L \times U(1)_Y$ gauge groups:
 $(\mathbf{3}, \mathbf{3}, -1/3)$, $(\bar{\mathbf{3}}, \mathbf{2}, -7/6)$ and $(\mathbf{3}, \mathbf{1}, -1/3)$

only doublet is “genuine” leptoquark

SU(5) embedding

Matter fields :

$$\mathbf{10}_i (= (\mathbf{1}, \mathbf{1}, \mathbf{1})_i \oplus (\overline{\mathbf{3}}, \mathbf{1}, -\mathbf{2}/\mathbf{3})_i \oplus (\mathbf{3}, \mathbf{2}, \mathbf{1}/\mathbf{6})_i = (\mathbf{e}_i^C, \mathbf{u}_i^C, \mathbf{Q}_i))$$

$$\overline{\mathbf{5}}_i (= (\mathbf{1}, \mathbf{2}, -\mathbf{1}/\mathbf{2})_i \oplus (\overline{\mathbf{3}}, \mathbf{1}, \mathbf{1}/\mathbf{3})_i = (\mathbf{L}_i, \mathbf{d}_i^C))$$

$$\text{where } Q_i = (u_i \quad d_i)^T \text{ and } L_i = (\nu_i \quad e_i)^T.$$

up quark (down quark and charged lepton) masses originate from the contraction of

$\mathbf{10}_i$ and $\mathbf{10}_j$ ($\overline{\mathbf{5}}_j$) with 5- and/or 45-dimensional Higgs representation.
 $\mathbf{10} \times \mathbf{10} = \overline{\mathbf{5}} \oplus \overline{\mathbf{45}} \oplus \overline{\mathbf{50}}$ and $\mathbf{10} \times \overline{\mathbf{5}} = \mathbf{5} \oplus \mathbf{45}$.

Most general renormalizable set of Yukawa coupling contractions with $\mathbf{5}_H$ and $\mathbf{45}_H$ is

$$\begin{aligned} V = & Y_{5^*}^{ij} \mathbf{10}_i^{\alpha\beta} \overline{\mathbf{5}}_{\alpha j} \mathbf{5}_{H\beta}^* + Y_5^{ij} \epsilon_{\alpha\beta\gamma\delta\epsilon} \mathbf{10}_i^{\alpha\beta} \mathbf{10}_j^{\gamma\delta} \mathbf{5}_H^\epsilon \\ & + Y_{45^*}^{ij} \mathbf{10}_i^{\alpha\beta} \overline{\mathbf{5}}_{\delta j} \mathbf{45}_{H\alpha\beta}^{*\delta} + Y_{45}^{ij} \epsilon_{\alpha\beta\gamma\delta\epsilon} \mathbf{10}_i^{\alpha\beta} \mathbf{10}_j^{\zeta\gamma} \mathbf{45}_{H\zeta}^{\delta\epsilon}, \end{aligned}$$

mass matrices

$$\begin{aligned}
 M_D &= (Y_{5^*}^T v_5^* + 2Y_{45^*}^T v_{45}^*) / \sqrt{2}, \\
 M_E &= (Y_{5^*} v_5^* - 6Y_{45^*} v_{45}^*) / \sqrt{2}, \\
 M_U &= [4(Y_5^T + Y_5)v_5 - 8(Y_{45}^T - Y_{45})v_{45}] / \sqrt{2},
 \end{aligned}$$

where $\langle \mathbf{5}_H^5 \rangle = v_5 / \sqrt{2}$, $\langle \mathbf{45}_{H1}^{15} \rangle = \langle \mathbf{45}_{H2}^{25} \rangle = \langle \mathbf{45}_{H3}^{35} \rangle = v_{45} / \sqrt{2}$ and $|v_5|^2 + |v_{45}|^2 = v^2$ ($v = 247 \text{ GeV}$). Y_{5^*} , Y_{45^*} , Y_5 and Y_{45} are arbitrary 3×3 Yukawa matrices.

Higgs in 5 $M_E^T = M_D$

one Higgs (only) in 5, at GUT scale
 $m_\tau/m_b = m_\mu/m_s = m_e/m_d$

Higgs in 45 $M_E^T = -3M_D$

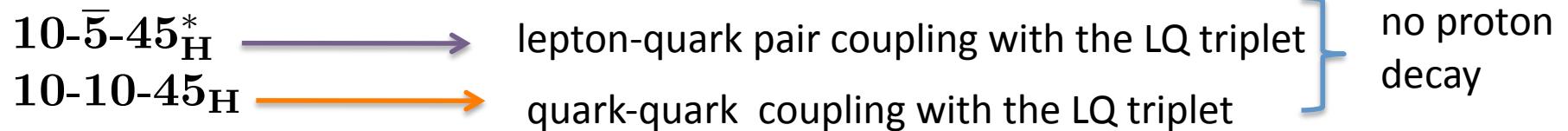
In this approach
both are needed $\mathbf{5}_H$ and $\mathbf{45}_H$

Leptoquarks

$$\begin{aligned}
 \mathbf{45}_H &= (\Delta_1, \Delta_2, \Delta_3, \Delta_4, \Delta_5, \Delta_6, \Delta_7) = \\
 &= (8, 2, 1/2) \oplus (\bar{6}, 1, -1/3) \oplus (3, 3, -1/3) \oplus (\bar{3}, 2, -7/6) \oplus (3, 1, -1/3) \oplus (\bar{3}, 1, 4/3) \oplus \\
 &\quad (1, 2, 1/2)
 \end{aligned}$$

Proton decay and triplet, doublet and singlet of LQ

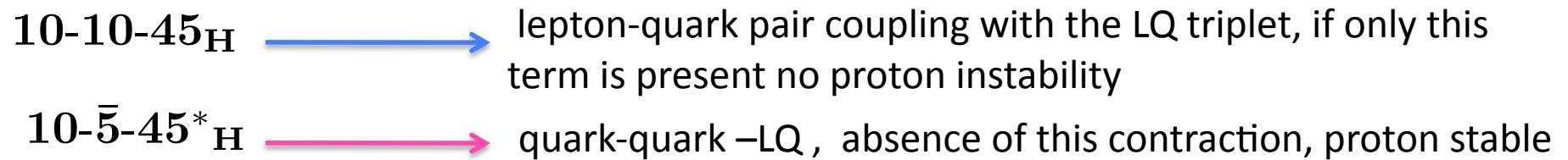
triplet $\Delta_3 = (3, 3, -1/3)$



doublet $\Delta_4 = (3, 2, -7/6)$

It cannot couple to quark – quark pair even via mixing with Higgs doublet and other Higgs states.

singlet $\Delta_5 = (3, 1, -1/3)$



Contraction of 10, 10 and 45 can lead to proton decay, but SUSY SU(5) GUT sufficiently suppresses proton decay.

Fermion weak doublets

weak \longleftrightarrow mass – eigen basis

$$\begin{bmatrix} f_1 \\ f_2 \end{bmatrix}$$


(Blum, Grossman, Nir and Perez 0903.2118)
 CKM and PMNS matrix $K - \bar{K}, D - \bar{D}$

$$\overline{Q_q^w} X^{q\ell} = (\overline{u}_q^w \quad \overline{d}_q^w) X^{q\ell} = (\overline{u}_q \quad \overline{d}'_q) (U^\dagger X)^{q\ell},$$

$$X'^{q\ell} L_\ell^w = X'^{q\ell} (\nu_\ell^w \quad e_\ell^w)^T = (X' E)^{q\ell} (\nu'_\ell \quad e_\ell)^T,$$

3 x 3 Yukawa matrix in the weak basis

rotations are assigned to down-type
 quarks and neutrions

$$Y_{LQ} \equiv U^\dagger X \quad (V_{CKM} = U^\dagger D)$$

$$d' = V_{CKM} d \quad \nu' = V_{PMNS} \nu. \quad Y'_{LQ} \equiv X' E \quad (V_{PMNS} = E^\dagger N)$$

quark-mass eigen states:

$$(Q_1, Q_2, Q_3) = \begin{pmatrix} u & c & t \\ d' & s' & b' \end{pmatrix}, \quad (d' \ s' \ b') = (d \ s \ b) V_{CKM}^T$$

We use parameterization

$$Y_{LQ}^{q\ell} = y_{LQ}^\ell (\sin \phi, \cos \phi)$$

$$d' = \cos \theta_c d + \sin \theta_c s, s' = -\sin \theta_c d + \cos \theta_c s$$

$$V_{us} = -V_{cd} = \sin \theta_c = 0.225$$

(good approximation – to neglect effects of the third generation)

If the Y_{LQ} matrix had all rows, except for the q -th one, set to zero, which would correspond to leptoquark coupling *only* to u_q , one would still get non-zero couplings to all three left-handed down-quarks.

antineutrino in a process the factor

(neutrino)

$$\sum_j Y_{LQ}^{\prime qj} V_{PMNS}^{ji} \xrightarrow{} V_{PMNS}^{li}$$

Neutrinos are not tagged in present experiment

The sum over all neutrino species gives

$$\sum_{i=1,2,3} |\mathcal{A}_i|^2 \sim \sum_{i=1,2,3} V_{PMNS}^{ji} V_{PMNS}^{li*} = \delta^{jl}$$

(equivalent to the absence of neutrino mixing!)

Triplet leptoquarks

$$\mathcal{L}_3 = Y_3^{ij} \overline{Q_i^c} i\tau_2 \boldsymbol{\tau} \cdot \Delta_3^* L_j + \text{h.c.}$$

arbitrary 3x3 matrix

Leptoquark triplet

$$\left\{ \begin{array}{l} \Delta_3^{-4/3} \\ \Delta_3^{-1/3} \\ \Delta_3^{2/3} \end{array} \right\}$$

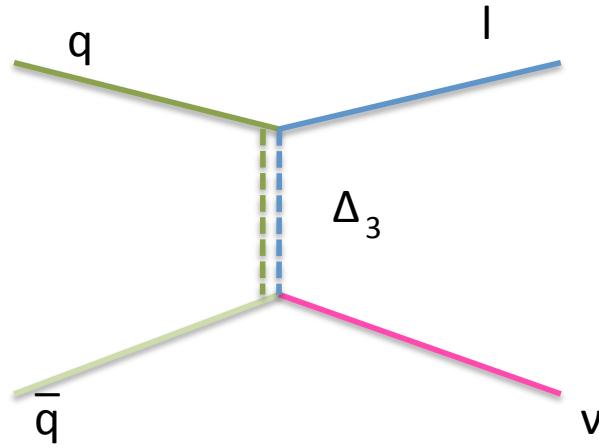
$$\tilde{Y}_3^{q\ell} \equiv \begin{cases} Y_3^{q\ell} & ; q = u, c, t, \\ (V_{CKM}^T Y_3)^{q\ell} & ; q = d, s, b. \end{cases}$$

$\tilde{Y}_3^{s\tau} \tilde{Y}_3^{s\mu*}$, $\tilde{Y}_3^{d\tau} \tilde{Y}_3^{d\mu*}$ and

$$Y_3^{u\tau} Y_3^{u\mu*} = (\cos \theta_c \tilde{Y}_3^{d\tau} + \sin \theta_c \tilde{Y}_3^{s\tau})(\cos \theta_c \tilde{Y}_3^{d\mu*} + \sin \theta_c \tilde{Y}_3^{s\mu*})$$

these couplings are not independent

We consider contributions to following processes:



$$\begin{aligned} D_s &\rightarrow \mu\nu_\mu \\ D_s &\rightarrow \tau\nu_\tau \\ \tau &\rightarrow \eta\mu \\ \tau &\rightarrow \pi\mu \\ \tau &\rightarrow K\mu \\ K &\rightarrow \mu\nu_\mu \\ K^+ &\rightarrow \pi^+\nu\bar{\nu} \\ K_L &\rightarrow \mu^+\mu^- \end{aligned}$$

$$\pi_{\mu/\tau} \equiv Br(\tau \rightarrow \pi\nu)/Br(\pi \rightarrow \mu\nu)$$

(also for K)

$$\begin{array}{c}
 \tau \rightarrow \eta\mu \\
 \text{constraints} \\
 \left. \begin{array}{l} \tilde{Y}_3^{s\tau}\tilde{Y}_3^{s\mu*}, \quad \tilde{Y}_3^{d\tau}\tilde{Y}_3^{d\mu*} \\ Y_3^{u\tau}Y_3^{u\mu*} = (\cos\theta_c \tilde{Y}_3^{d\tau} + \sin\theta_c \tilde{Y}_3^{s\tau})(\cos\theta_c \tilde{Y}_3^{d\mu*} + \sin\theta_c \tilde{Y}_3^{s\mu*}) \end{array} \right\} \\
 \pi_{\mu/\tau}
 \end{array}$$

In triplet LQ scenario one needs one of the measured decay widths $D_s \rightarrow \ell\nu$

$$\begin{array}{c}
 \text{to reproduce } Br(D_s \rightarrow \tau\nu) = 0.0561(44) \\
 \text{and using lattice result } f_{D_s} = 241(3) \text{ MeV}
 \end{array} \left. \right\} \sqrt{\delta_3^\tau} \approx 0.002 \text{ GeV}^{-1}$$

$$\delta_3^\tau \equiv \frac{Y_3^{e\tau*}\tilde{Y}_3^{s\tau}}{V_{es}m_{\Delta_3}^2} \rightarrow (y_3^\tau)^2 \sin\phi \cos\phi (-\tan\theta_c + \tan\phi)/m_{\Delta_3}^2$$

SM correction

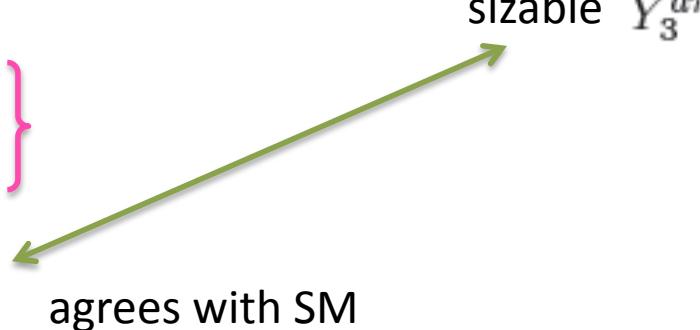
two solutions

to satisfy $D \rightarrow \tau\nu_\tau$ and $\pi_{\mu,\tau}$ one needs either:

1. leptoquarks couple only to s but not to d quark $\tan \phi \approx \tan \theta_c$ ($\tilde{Y}_3^{d\tau} \approx 0$)
and sizable $\tilde{Y}_3^{u\tau} \xrightarrow{\text{pink}} K_{\mu,\tau}$
2. leptoquarks couple only to c but not to u quark $\sin \phi \approx 0$ ($\tilde{Y}_3^{u\tau} = 0$)
sizable $\tilde{Y}_3^{d\tau}$

$$\left\{ \begin{array}{l} K^+ \rightarrow \pi^+ \nu \bar{\nu} \\ Br(\tau \rightarrow K \nu) / Br(K \rightarrow \mu \nu) \end{array} \right\}$$

$$Br(D \rightarrow \mu \nu) = 3.8(4) \times 10^{-4}$$



If $\tilde{Y}_3^{s\tau}$ sizable, then $\tilde{Y}_3^{s\mu} \sim 0$ from $\tau \rightarrow \eta \mu$ decay width

additional constraint comes from $K_L \rightarrow \mu^+ \mu^-$

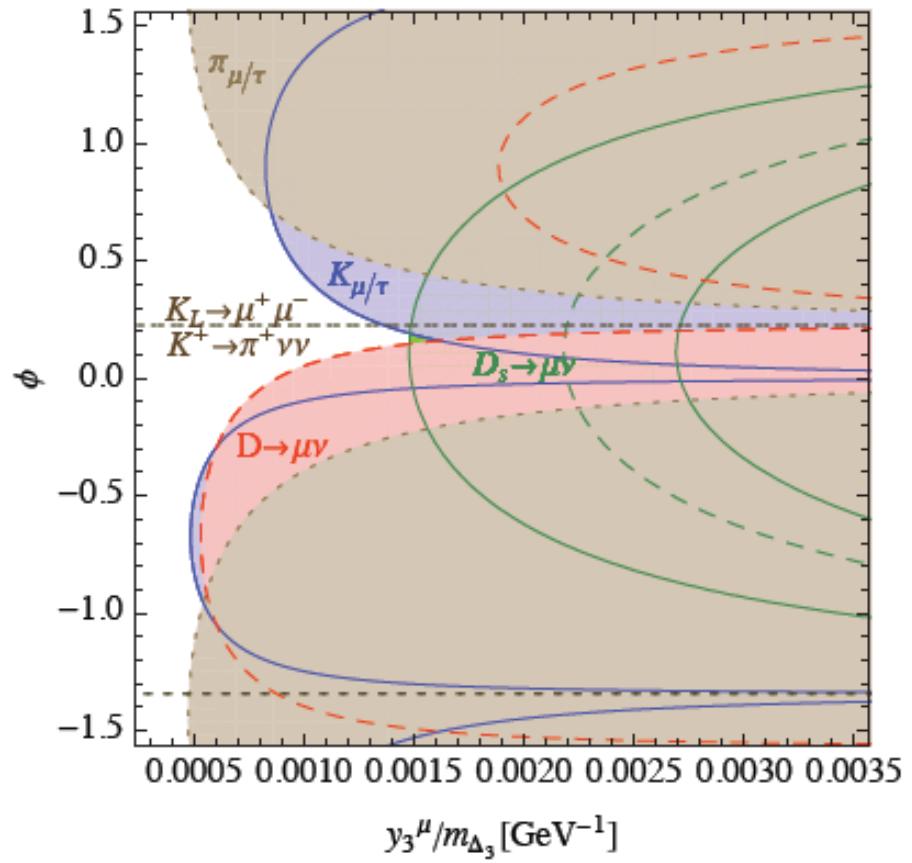
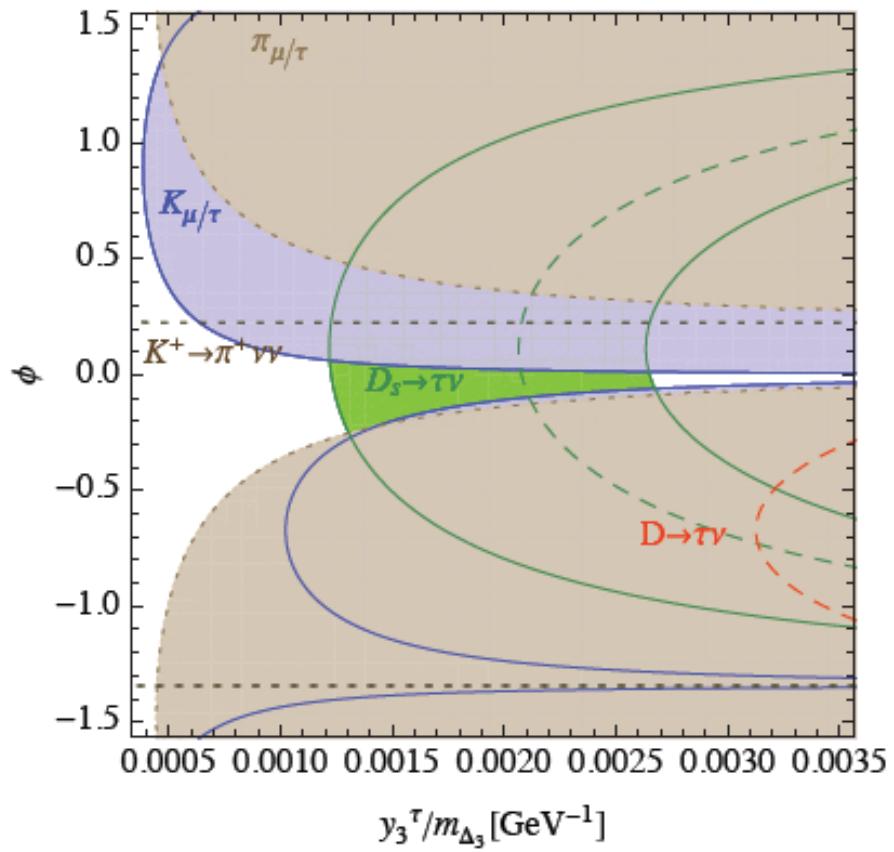
Combining these two constraints a triplet explanation is completely excluded!

Our assumption:

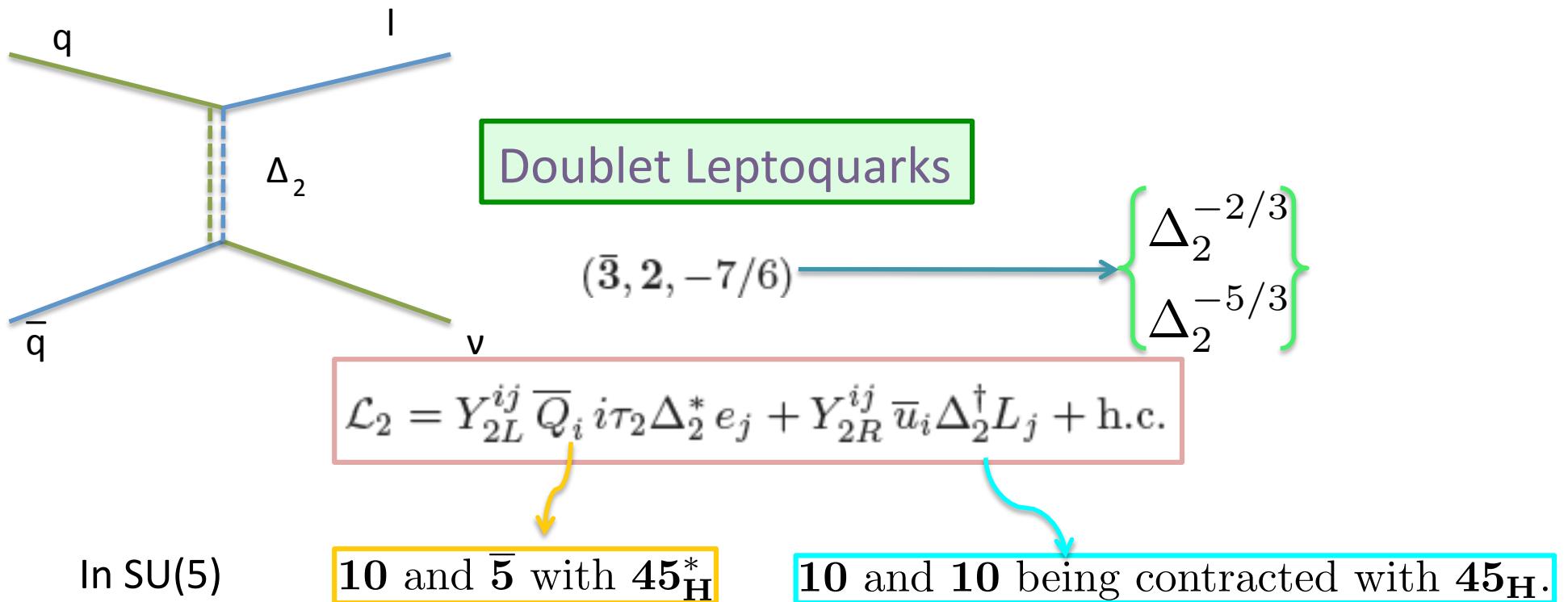
Leptoquark multiplet are nearly degenerate

We require :

- all the measured constraints to be satisfied within one standard deviation
(at 68 %C.L.)
- for the upper we use 90% C.L. limit



Combined bounds on triplet LQ parameters in two-generation case.



We consider constraints
coming from

$$\begin{aligned} D_s &\rightarrow l\nu_l \\ D^0 &\rightarrow \mu^+ \mu^- \\ K_L &\rightarrow \mu^+ \mu^- \end{aligned}$$

and LFV

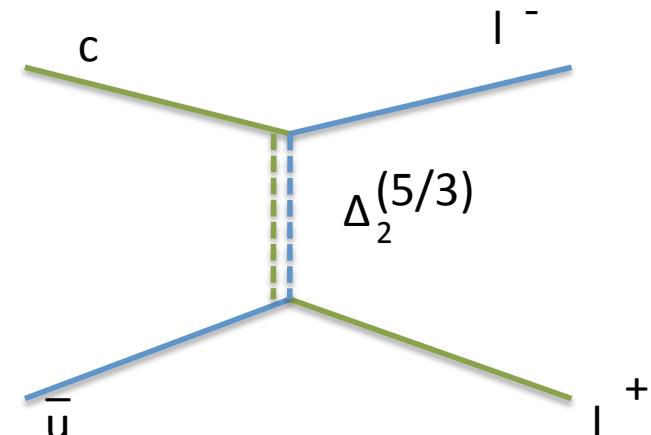
$$\tau \rightarrow \eta \mu$$

the couplings of left-handed down and up type quarks are misaligned

$$\tilde{Y}_{2L}^{q\ell} \equiv (V_{CKM}^\dagger Y_{2L})^{q\ell} \text{ for } q = d, s, b$$

$$D^0 \rightarrow \mu^+ \mu^-$$

$$Y_{2R}^{c\mu} Y_{2L}^{u\mu*} = Y_{2R}^{c\mu} (\cos \theta_c \tilde{Y}_{2L}^{d\mu*} + \sin \theta_c \tilde{Y}_{2L}^{s\mu*})$$



$$Y_{2L}^{c\mu} Y_{2L}^{u\mu*} = (\cos \theta_c \tilde{Y}_{2L}^{s\mu} - \sin \theta_c \tilde{Y}_{2L}^{d\mu})(\cos \theta_c \tilde{Y}_{2L}^{d\mu*} + \sin \theta_c \tilde{Y}_{2L}^{s\mu*})$$

The measurement of $D \rightarrow \mu\nu$ directly constraints $\tilde{Y}_{2L}^{d\mu}$.

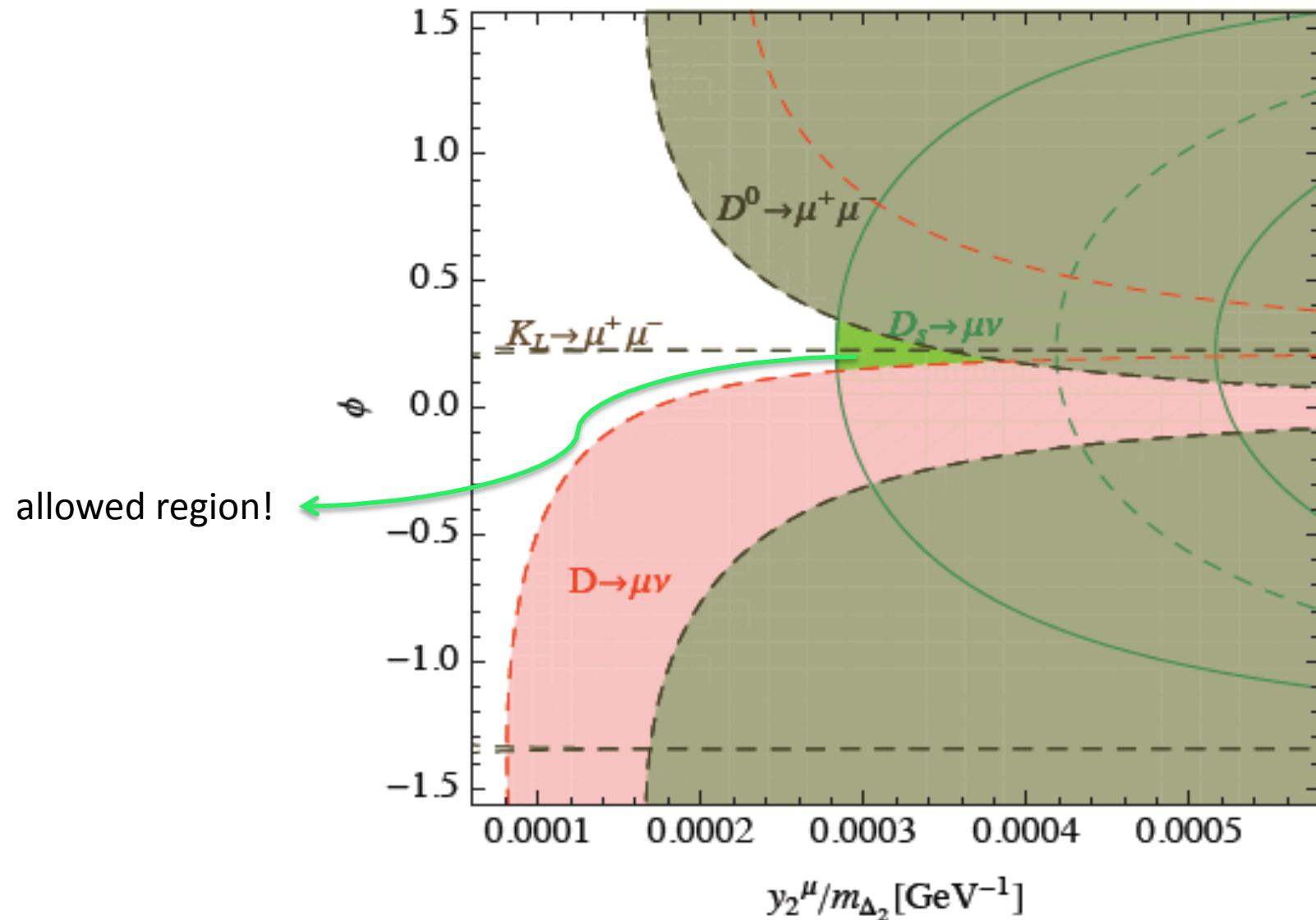
For the numerical analysis we use parameterization:

$$\tilde{Y}_{2L}^{s\mu} = y_{2L}^\mu \cos \phi \quad \tilde{Y}_{2L}^{d\mu} = y_{2L}^\mu \sin \phi$$

chosen $Y_{2R}^{u\mu} = 0 \quad Y_{2R}^{c\mu} = y_{2R}^\mu$

we vary y_{2L}^μ and y_{2R}^μ keeping fixed $y_2^\mu = \sqrt{y_{2L}^\mu y_{2R}^\mu}$

(keep in mind that first generation ($\pi_{\mu/\tau}$) is strongly constrained)



Combined bounds on the doublet LQ.

$$D_s \rightarrow \tau\nu$$

- far from being conclusive in doublet case (D decay mode is not measured)
- no strong experimental bound on FCNC in up sector involving tau (doublet leptoquarks do not contribute to $s \rightarrow d\nu\bar{\nu}$)

$$\delta_2^\ell \equiv \frac{m_{D_s}^2}{m_\ell(m_c + m_s)} \frac{Y_{2R}^{c\ell*}\tilde{Y}_{2L}^{s\ell}}{V_{cs}^* m_{\Delta_2}^2}$$

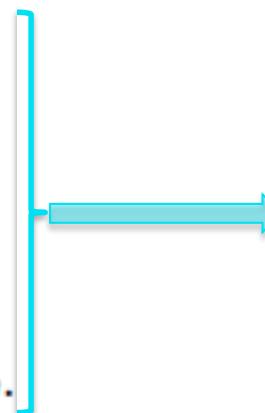
$$\tau \rightarrow \eta^{(\prime)}\mu \sim \left| \tilde{Y}_{2L}^{s\tau} \tilde{Y}_{2L}^{s\mu*} \right|^2$$

$$\delta_2^{LFV} = |Y_{2L}^{s\tau} Y_{2L}^{*s\mu}| / m_{\Delta_2}^2$$

perturbative treatment for couplings

$$|Y_{2L,R}^{ij}| < \sqrt{4\pi}$$

$$m_{\Delta_2} < \sqrt{4\pi \delta_2^{LFV} / |\delta_2^\mu \delta_2^\tau|}$$



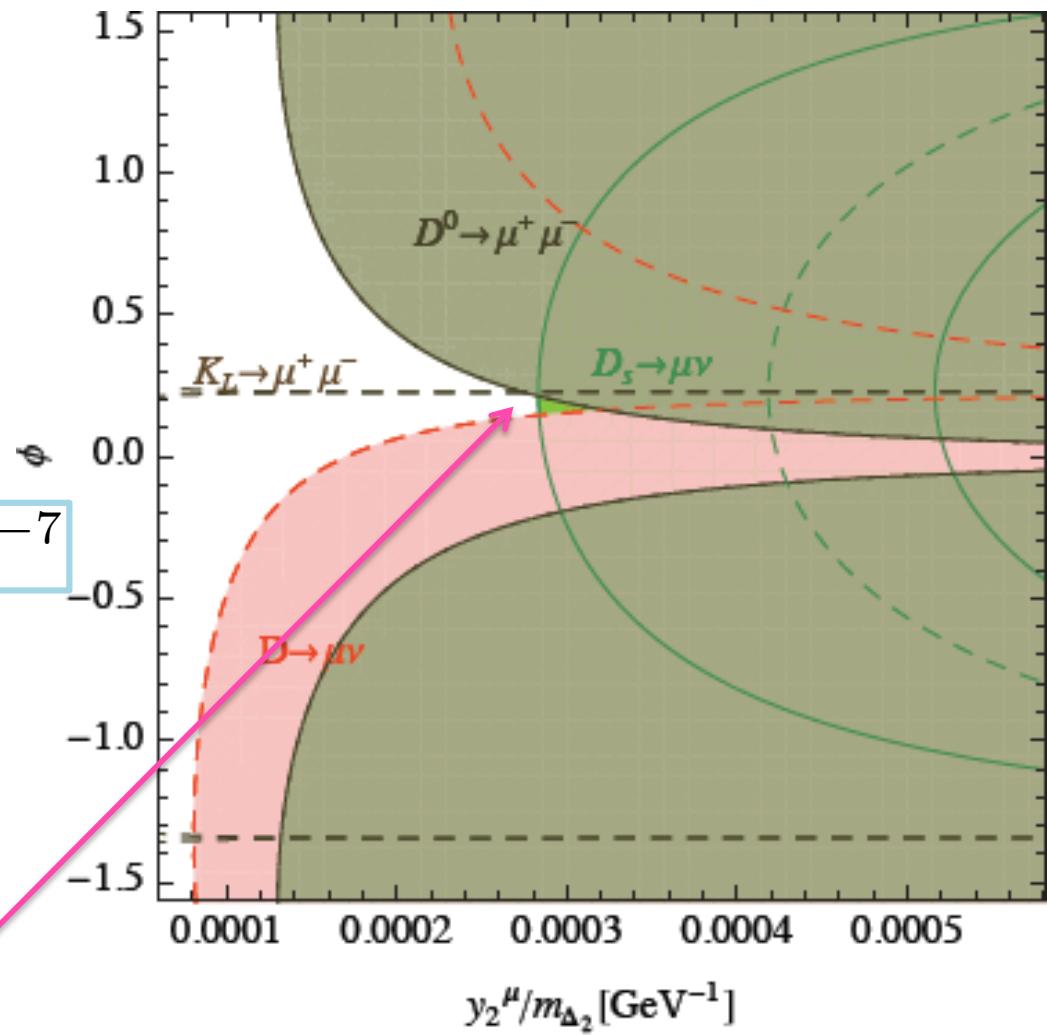
$$m_{\Delta_2} \sim 1.4 \text{ TeV}$$

with present bound

$$Br(\tau \rightarrow \eta\mu) < 6.5 \times 10^{-8} \text{ at 90 \% C.L.}$$

with new improved bound
(Belle EPS, 2009)

$$BR(D \rightarrow \mu^+ \mu^-) < 1.4 \times 10^{-7}$$



Doublet leptoquarks excluded!

SINGLET LEPTOQUARK (3, 1, -1/3)

$$\Delta_1^{-1/3}$$

$$\mathcal{L}_1 = Y_{1L}^{ij} \overline{Q_i^c} i\tau_2 \Delta_1^* L_j + Y_{1R}^{ij} \overline{u_i^c} \Delta_1^* e_j + \text{h.c.}$$

the same term as in MSSM R parity violating

this terms gives modification in
 $D_s \rightarrow \tau \nu_\tau$

we use

$$\left\{ \begin{array}{ll} K^+ \rightarrow \pi^+ \nu \bar{\nu} & \tilde{Y}_{1L}^{d\ell} \approx 0 \\ \frac{\Gamma_{D_s \rightarrow \tau \nu}^{(1)}}{\Gamma_{D_s \rightarrow \tau \nu}^{SM}} & \frac{\Gamma_{\tau \rightarrow K \nu}^{(1)}}{\Gamma_{\tau \rightarrow K \nu}^{SM}} \\ D^0 \rightarrow \mu^+ \mu^- & \end{array} \right.$$

free parameters can be chosen as an overall amplitude δ and two angles: (ϕ, ω)

$$\begin{aligned}\tilde{Y}_{1L}^{s\mu} &= y_1^\mu \sin \omega, \quad Y_{1R}^{c\mu} = y_1^\mu \cos \omega \cos \phi \text{ and} \\ Y_{1R}^{u\mu} &= y_1^\mu \cos \omega \sin \phi\end{aligned}$$

bound from perturbation approach: $y_1^\mu < \sqrt{4\pi}$

numerical fit (y_1^μ, ω, ϕ) to above constraints leads to

➤ exp. result for $Br(D_s \rightarrow \mu\nu)$ cannot be reproduced within one standard deviation without violating any other constraints.

➤ but, due to the lack of exp. information on FCNC in up sector, leaves the verdict on singlet leptoquark in $D_s \rightarrow \tau\nu$ open .

Rare decay $D^+ \rightarrow \pi^+ \mu^+ \mu^-$

Experimentally: $\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-) < 3.9 \times 10^{-6}$

this includes contributions of ρ, ω, ϕ resonances

SM long distance contributions almost saturate this result.

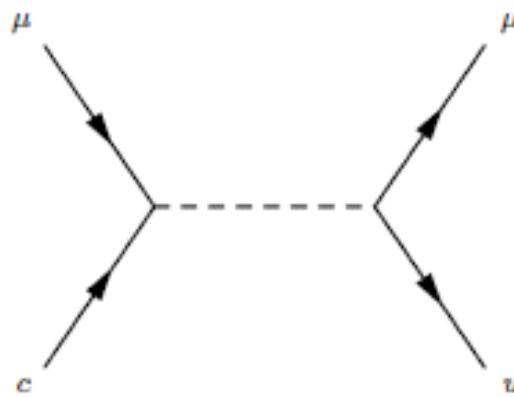
$$\mathcal{A}_V^{\text{LD}} = \frac{a_V}{q^2 - m_V^2 + im_V\Gamma_V} \bar{u}(k_-) \phi v(k_+) \quad \begin{array}{l} \text{Parameters } a_V \text{ fitted to } \mathcal{B} \text{ of resonant mode} \\ D^+ \rightarrow \pi^+ V \rightarrow \pi^+ \mu^+ \mu^- \end{array}$$

Result: resonant branching fraction

$$\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-)_{\text{res}} = (1.8 \pm 0.2) \times 10^{-6}$$

S.F. and N. Kosnik (2009), S.F., N.K. and S. Prelovsek (2007)

$$\mathcal{L}_{LQ} = \tilde{d} \kappa_\ell (\bar{\nu}_\ell P_R s^c - \bar{\ell} P_R c^c) + \tilde{d} \kappa'_\ell \bar{\ell} P_L c^c + \text{H.c.},$$



$$\begin{aligned} \mathcal{L}_{\text{eff}}(c \rightarrow u \ell^+ \ell^-) = & \frac{1}{8M_{\tilde{d}^2}} [C_{\ell c}^{L*} C_{\ell u}^L (\bar{u}c)_{V-A}(\bar{\ell}\ell)_{V-A} + C_{\ell c}^{R*} C_{\ell u}^R (\bar{u}c)_{V+A}(\bar{\ell}\ell)_{V+A} \\ & + C_{\ell c}^{L*} C_{\ell u}^R \left(\frac{1}{2} (\bar{u}\sigma^{\mu\nu}c)(\bar{\ell}\sigma_{\mu\nu}(1-\gamma_5)\ell) - (\bar{u}c)_{S-P}(\bar{\ell}\ell)_{S-P} \right) \\ & + C_{\ell c}^{R*} C_{\ell u}^L \left(\frac{1}{2} (\bar{u}\sigma^{\mu\nu}c)(\bar{\ell}\sigma_{\mu\nu}(1+\gamma_5)\ell) - (\bar{u}c)_{S+P}(\bar{\ell}\ell)_{S+P} \right)] \end{aligned}$$

From $D^+ \rightarrow \pi^+ \mu^+ \mu^-$ we find constraints on the two combinations

$$\frac{|C_{\mu c}^{L(R)} C_{\mu u}^{L(R)}|}{(M_{\tilde{d}}/\text{TeV})^2} < 0.19, \quad \frac{|C_{\mu c}^{L(R)} C_{\mu u}^{R(L)}|}{(M_{\tilde{d}}/\text{TeV})^2} < 0.16,$$

one of which is also present in $D^0 \rightarrow \mu^+ \mu^-$ (helicity-lifted):

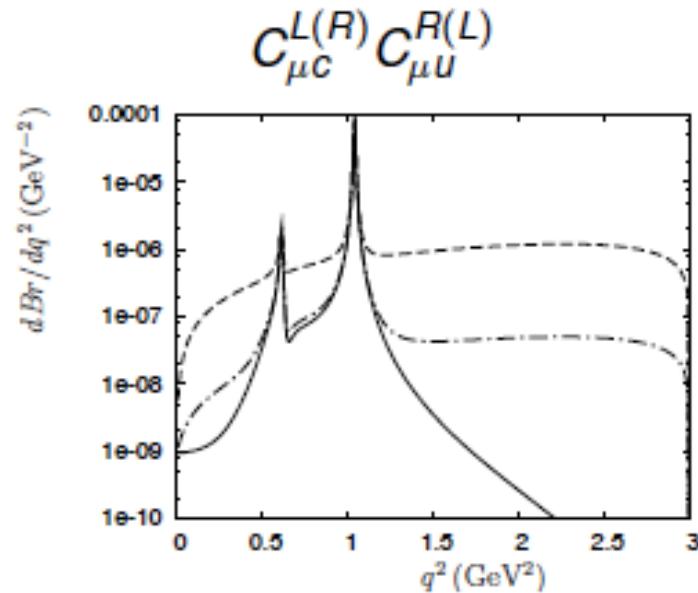
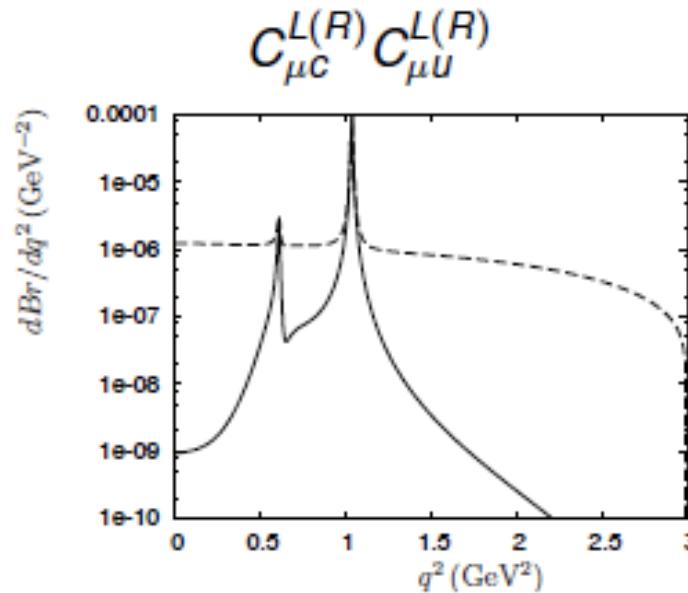
$$\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) = \tau_{D^0} \frac{f_D^2 m_{D_0}^5}{256 \pi m_c^2} \frac{|C_{\mu c}^L C_{\mu u}^R|^2 + |C_{\mu c}^R C_{\mu u}^L|^2}{M_{\tilde{d}}^4}$$

and from $\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-)$ there is much stronger bound

$$\boxed{\frac{|C_{\mu c}^{L(R)} C_{\mu u}^{R(L)}|}{(M_{\tilde{d}}/\text{TeV})^2} < 0.032}$$

This bound, applied to $\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-)$ results in $9.4 \times 10^{-8} \rightarrow C_{\mu c}^{L(R)} C_{\mu u}^{R(L)}$ cannot be observed in $D^+ \rightarrow \pi^+ \mu^+ \mu^-$

Present experimental bound on the $D^0 \rightarrow \mu^+ \mu^-$ rate leads to the rate $D^+ \rightarrow \pi^+ \mu^+ \mu^-$ two order of magnitude smaller than the SM result.



ruled out

- inclusion of $Q = -1/3$ weak-isosinglet scalar leptoquark leads to tree-level $c \rightarrow u \mu \mu$
- $D^+ \rightarrow \pi^+ \mu^+ \mu^-$ sensitive to both $C_{\mu c}^{L(R)} C_{\mu u}^{L(R)}$, $C_{\mu c}^{L(R)} C_{\mu u}^{R(L)}$
- $D^0 \rightarrow \mu^+ \mu^-$ only to helicity-unsuppressed $C_{\mu c}^{L(R)} C_{\mu u}^{R(L)}$
- Bound from $\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-)$ renders $D^+ \rightarrow \pi^+ \mu^+ \mu^-$ only sensitive to $C_{\mu c}^{L(R)} C_{\mu u}^{L(R)}$

Summary:

- Scalar leptoquarks cannot explain both $D_s \rightarrow l\nu$ decay widths, due to constraints coming from precision kaon, tau and D mesons.
- The triplet leptoquark is excluded from contributing to any of the widths.
- Sizable contributions due to single right-handed down squark exchange in RPV supersymmetric models are also excluded.
- Leptoquark singlet is definitely excluded only from explaining the $D_s \rightarrow \mu\nu$ width.
- The doublet contribution in $D^0 \rightarrow \mu^+ \mu^-$ is excluded with the new Belle bound.

Future perspective

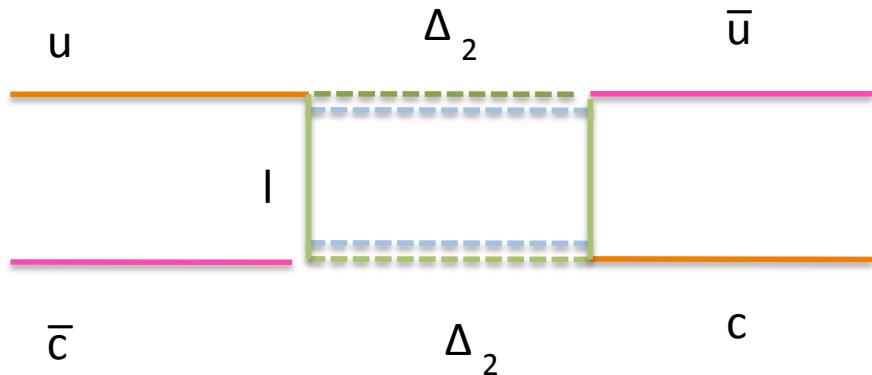
Possible signatures of LQ
in $D_s \rightarrow \tau\nu$

- 
- $Br(J/\psi \rightarrow \tau^+ \tau^-)$ at the level of 10^{-11}
(probably beyond the reach of BESIII)
 - $Br(t \rightarrow c\tau^+ \tau^-)$ at the level of 10^{-5}
(close to the limiting sensitivity of the LHC)

$D^0 - \bar{D}^0$ and $K^0 - \bar{K}^0$ oscillations

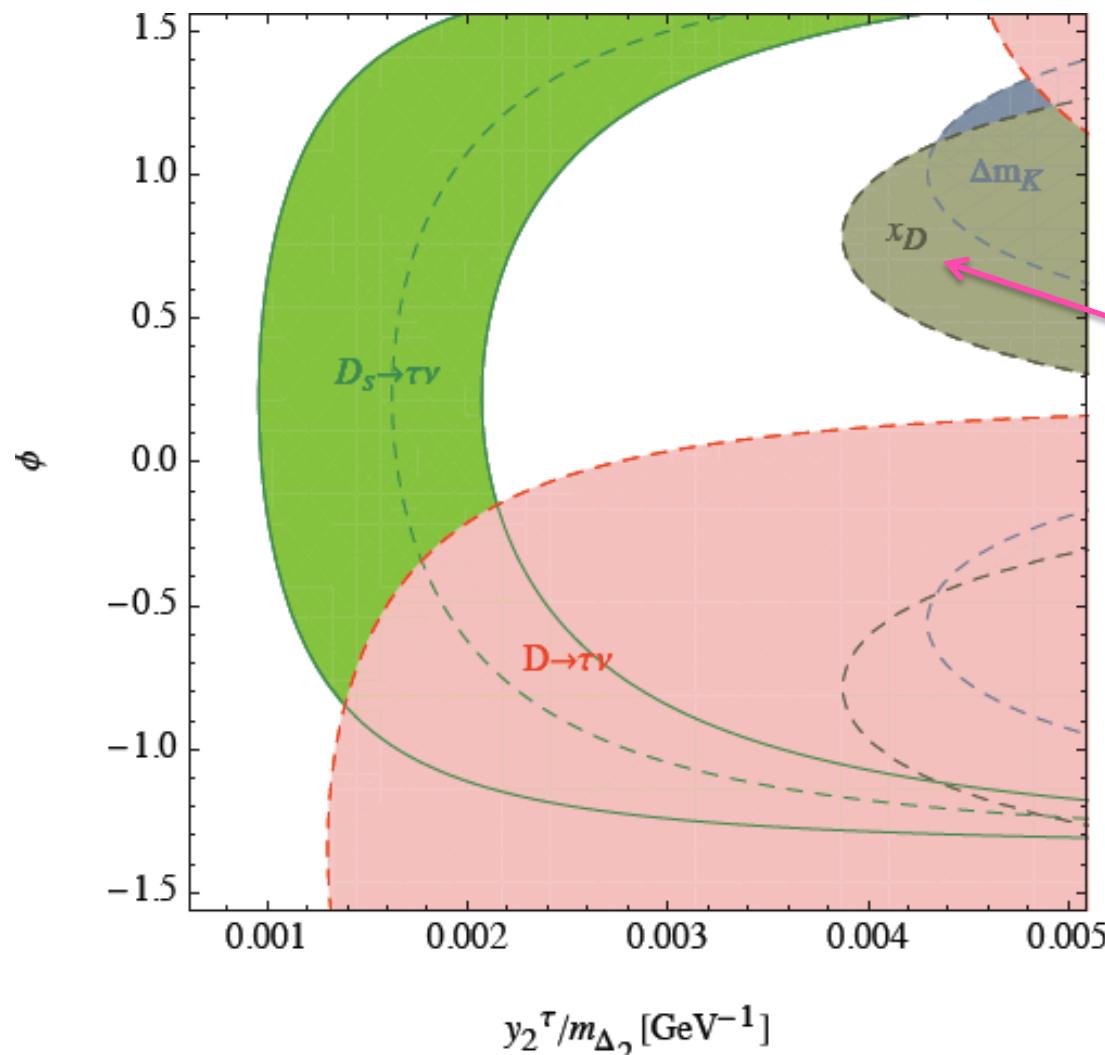
Doublet leptoquarks

$$\mathcal{M}(D^0 \leftrightarrow \bar{D}^0) = \frac{1}{8\pi^2 m_{\Delta_2}^2} \left\{ \Sigma_{l=\mu,\tau} (Y_{2L}^{cl} Y_{2L}^{ul*})^2 (\bar{c}u)_{V-A} (\bar{c}u)_{V-A} + (Y_{2R}^{cl} Y_{2R}^{ul*})^2 (\bar{c}u)_{V+A} (\bar{c}u)_{V+A} \right\}$$



$$\mathcal{M}(K^0 \leftrightarrow \bar{K}^0) = \frac{1}{8\pi^2 m_{\Delta_2}^2} \left\{ \Sigma_{l=\mu,\tau} (\tilde{Y}_{2L}^{dl} \tilde{Y}_{2L}^{sl*})^2 (\bar{s}d)_{V-A} (\bar{s}d)_{V-A} \right\}$$

$$Y_{2L}^{cl} Y_{2L}^{ul*} = (\cos\theta_c \tilde{Y}_{2L}^{sl} - \sin\theta_c \tilde{Y}_{2L}^{dl})(\cos\theta_c \tilde{Y}_{2L}^{dl*} + \sin\theta_c \tilde{Y}_{2L}^{sl*}).$$



Loop processes are not relevant for the bounds coming from the tree level diagrams!