

Aspects of Non-Supersymmetric String Phenomenology

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Outline

- Introduction
- Non supersymmetric string models - Coordinate dependent compactifications
- A class of semi-realistic non supersymmetric string vacua
- One loop potential for the moduli fields - Cosmological constant
- Gauge coupling Thresholds - The decompactification problem
- Conclusions

The Standard Model

The Standard Model of particle interactions is a very successful theory.

However, it leaves a number of unanswered questions (Mass origin, flavor puzzle, charge quantization, a number of parameters, dark matter, hierarchy problem, gravity...)

Supersymmetry has been introduced to provide a solution to the gauge hierarchy problem and guarantee stability towards quantum corrections without fine-tuning. The introduction of SUSY at a few TeV leads also to coupling unification.

If SUSY were an exact symmetry of the nature every particle and its superpartner would have degenerate masses. However, this is not verified experimentally so SUSY must be broken.

Non-supersymmetric strings

Space-time supersymmetry is not required for consistency in string theory.

From the early days of the first string revolution it was known that heterotic strings comprise the SUSY $E_8 \times E_8$ and $SO(32)$ models as well as the non-supersymmetric tachyon free $SO(16) \times SO(16)$ theory.

However, non-supersymmetric model building has not received much attention until recently.

S. Abel, K. R. Dienes and E. Mavroudi (2015,2017)

J. R. and I. Florakis (2016,2017)

A. Lukas, Z. Lalak and E. E. Svanes (2015)

Stefan Groot Nibbelink, Orestis Loukas, Andreas Mütter, Erik Parr, Patrick K. S. Vaudrevange (2017)

SUSY breaking in String Theory

Any scenario of supersymmetry breaking in the context of string theory has to address some important issues, as

- Resolve M_W/M_P hierarchy
- Compatibility with gauge coupling evolution (unification) and weak string coupling constant
- Account for the smallness of the cosmological constant
- Resolve possible instabilities (tachyons)
- Moduli field stabilisation

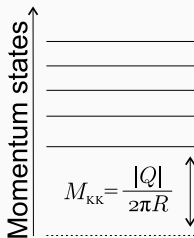
Coordinate dependent compactifications

A stringy Scherk–Schwartz mechanism involves an extra dimension X^5 and a conserved charge Q .
Upon compactification

$$\Phi(X^5 + 2\pi R) = e^{iQ} \Phi(X^5)$$

we obtain a shifted tower of Kaluza–Klein states for charged fields, starting at $M_{KK} = \frac{|Q|}{2\pi R}$

$$\Phi(X^5) = e^{\frac{iQX^5}{2\pi R}} \sum_{n \in \mathbb{Z}} \Phi_n e^{inX^5/R}$$



$Q = \text{Fermion number} \Rightarrow$ leads to different masses for fermions-bosons (lying in the same supermultiplet) and thus to spontaneous breaking of supersymmetry.

SUSY breaking related to the compactification radius $M \sim \frac{1}{R}$

Coordinate dependent compactifications

J. Scherk and J. H. Schwarz (1978,1979)

R. Rohm (1984)

C. Kounnas and M. Porrati (1988)

S. Ferrara, C. Kounnas, M. Porrati and F. Zwirner,(1989)

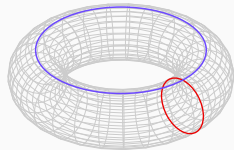
C. Kounnas and B. Rostand, (1990)

Gravitino mass

We compactify the six internal dimensions in three separate two-tori parametrised by the $T^{(i)}, U^{(i)}, i = 1, 2, 3$ moduli. For simplicity, we will consider realising the Scherk–Schwarz mechanism utilising the $T^{(1)}, U^{(1)}$ torus.

At tree level the gravitino receives a mass

$$m_{3/2} = \frac{|U^{(1)}|}{\sqrt{T_2^{(1)} U_2^{(1)}}} = \frac{1}{R_1}$$



for a square torus: $T = \imath R_1 R_2, U = \imath R_2 / R_1$

All $T^{(i)}, U^{(i)}$ moduli remain massless.

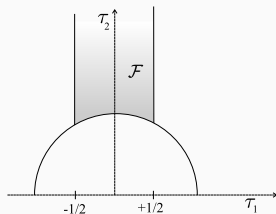
At $R_1 \rightarrow \infty$ we have $m_{3/2} = 0$ and the supersymmetry is restored.

One loop potential

The effective potential at one loop as a function moduli $t_l = \tau^{(i)}, U^{(i)}$ is obtained by integrating the string partition function $Z(\tau_1, \tau_2; t_l)$ over the worldsheet torus Σ_1

$$V_{\text{one-loop}}(t_l) = -\frac{1}{2(2\pi)^4} \int_{\mathcal{F}} \frac{d^2\tau}{\tau_2^3} Z(\tau, \bar{\tau}; t_l),$$

where $\tau = \tau_1 + i\tau_2$ and $\mathcal{F} = \text{SL}(2; \mathbb{Z}) \backslash \mathbb{H}^+$ is a fundamental domain.

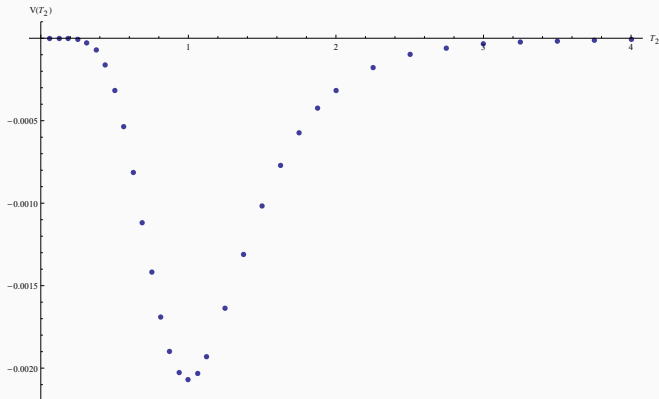


For given values of the moduli

$$Z = \sum_{\substack{n \in \mathbb{Z}/2 \\ n \geq -1/2}} \sum_{m \in \mathbb{Z}} Z_{n,m} q_r^n q_i^m = \sum_{\substack{n \in \mathbb{Z}/2 \\ n \geq -1/2}} \left[\sum_{m=-[n]-1}^{[n]+2} Z_{n,m} q_i^m \right] q_r^n.$$

where $q_r = e^{-2\pi\tau_2}$ and $q_i = e^{2\pi i\tau_1}$

One loop moduli potentials



Typical one-loop potential versus the modulus T_2 .

Undesirable features: SUSY breaking at the string scale, huge cosmological constant, region of tachyon instabilities

One loop potential: Analytic results

$$\begin{aligned}
 Z = & \frac{1}{2^8} \frac{1}{\eta^{12} \bar{\eta}^{24}} \sum_{H_1, G_1=0,1} \Gamma_{2,2}^{\text{shift}} \begin{bmatrix} H_1 \\ G_1 \end{bmatrix} \left(T^{(1)}, U^{(1)} \right) \\
 & \times \sum_{\substack{h_2, H=0,1 \\ g_2, G=0,1}} \sum_{\substack{k, \rho, \gamma_2, \gamma_3=0,1 \\ \ell, \sigma, \delta_3, \delta_4=0,1}} (-1)^{\hat{\Phi}'} \times \vartheta \begin{bmatrix} 1 + H_1 + h_2 \\ 1 + G_1 + g_2 \end{bmatrix}^2 \vartheta \begin{bmatrix} 1 + H_1 \\ 1 + G_1 \end{bmatrix}^2 \\
 & \times \bar{\vartheta} \begin{bmatrix} k \\ \ell \end{bmatrix}^6 \bar{\vartheta} \begin{bmatrix} k + h_2 \\ \ell + g_2 \end{bmatrix}^2 \bar{\vartheta} \begin{bmatrix} \rho \\ \sigma \end{bmatrix}^4 \bar{\vartheta} \begin{bmatrix} \rho + H \\ \sigma + G \end{bmatrix}^4 \vartheta \begin{bmatrix} \gamma_2 \\ \delta_2 \end{bmatrix} \vartheta \begin{bmatrix} \gamma_2 + h_2 \\ \delta_2 + g_2 \end{bmatrix} \\
 & \times \bar{\vartheta} \begin{bmatrix} \gamma_2 \\ \delta_2 \end{bmatrix} \bar{\vartheta} \begin{bmatrix} \gamma_2 + h_2 \\ \delta_2 + g_2 \end{bmatrix} \vartheta \begin{bmatrix} \gamma_3 \\ \delta_3 \end{bmatrix} \vartheta \begin{bmatrix} \gamma_3 - h_3 \\ \delta_3 - g_3 \end{bmatrix} \bar{\vartheta} \begin{bmatrix} \gamma_3 \\ \delta_3 \end{bmatrix} \bar{\vartheta} \begin{bmatrix} \gamma_3 - h_3 \\ \delta_3 - g_3 \end{bmatrix}
 \end{aligned}$$

One loop potential: Asymptotic limit

The asymptotic behaviour of the potential is dominated by the contribution of the orbit

$$I_{\text{deg}}^{[0]} = \frac{2c^{[0]}_1(0,0)}{\pi^3 T_2^2} \sum_{m_1, m_2 \in \mathbb{Z}} \frac{U_2^3}{\left|m_1 + \frac{1}{2} + U m_2\right|^6} + \frac{4\sqrt{2}}{\sqrt{T_2}} \sum_{N \geq 1} N^{3/2} c^{[0]}_1(N, 0) \\ \times \sum_{m_1, m_2 \in \mathbb{Z}} \frac{U_2^{3/2}}{\left|m_1 + \frac{1}{2} + U m_2\right|^3} K_3 \left(2\pi \sqrt{\frac{N T_2}{U_2}} \left|m_1 + \frac{1}{2} + U m_2\right|^2 \right)$$

where $K_s(z)$ is the modified Bessel function of the second kind.

$$V_{\text{one-loop}}(R) = -\frac{(n_B - n_F)}{2^4 \pi^7 R^4} \sum_{m_1, m_2 \in \mathbb{Z}} \frac{U_2^3}{\left|m_1 + \frac{1}{2} + U m_2\right|^6} + e^{-\sqrt{2\pi}R} + \dots$$

Super no scale models $n_B = n_F$. Cosmological constant is exponentially small.

C. Kounnas and H. Partouche (2016)

A class of models

Consider a big class of semi-realistic $Z_2 \times Z_2$ heterotic string vacua for explicit realisations of the Scherk–Schwarz scenario. Study chirality, moduli potential and thresholds.

To this end we utilise both the free fermionic formulation and orbifold formulation. In the former we have full control of the spectrum in the latter we have explicit moduli dependence.

in the free fermionic formulation we can utilise the model classification techniques developed in

A. Gregori, C. Kounnas and J. R. (1999)

A. E. Faraggi, C. Kounnas, S. E. M. Nooij and J. R. (2004)

A. E. Faraggi, C. Kounnas and J. R. (2007)

The class of models

We consider the class of four dimensional $N = 1$ heterotic models spontaneously broken to $N = 0$ via the Scherk–Schwarz mechanism.

The $E_8 \times E_8$ gauge symmetry is reduced to

$$SO(10) \times SO(8)^2 \times U(1)^2$$

We select models using the following criteria

- absence of tachyons
- $SO(10)$ chirality
- compatibility with Scherk–Schwarz of $N = 1$ SUSY

Class of models: Basis vectors

The free fermions in the light-cone gauge are:

left: $\psi^\mu, \chi^{1,\dots,6}, y^{1,\dots,6}, \omega^{1,\dots,6}$

right: $\bar{y}^{1,\dots,6}, \bar{\omega}^{1,\dots,6}, \bar{\eta}^{1,2,3}, \bar{\psi}^{1,\dots,5}, \bar{\phi}^{1,\dots,8}$

The class of vacua under consideration is defined by

$$\beta_1 = \mathbf{1} = \{\psi^\mu, \chi^{1,\dots,6}, y^{1,\dots,6}, \omega^{1,\dots,6} | \bar{y}^{1,\dots,6}, \bar{\omega}^{1,\dots,6}, \bar{\eta}^{1,2,3}, \bar{\psi}^{1,\dots,5}, \bar{\phi}^{1,\dots,8}\}$$

$$\beta_2 = S = \{\psi^\mu, \chi^{1,\dots,6}\}$$

$$\beta_3 = T_1 = \{y^{12}, \omega^{12} | \bar{y}^{12}, \bar{\omega}^{12}\}$$

$$\beta_4 = T_2 = \{y^{34}, \omega^{34} | \bar{y}^{34}, \bar{\omega}^{34}\}$$

$$\beta_5 = T_3 = \{y^{56}, \omega^{56} | \bar{y}^{56}, \bar{\omega}^{56}\}$$

$$\beta_6 = b_1 = \{\chi^{34}, \chi^{56}, y^{34}, y^{56} | \bar{y}^{34}, \bar{y}^{56}, \bar{\psi}^{1,\dots,5}, \bar{\eta}^1\}$$

$$\beta_7 = b_2 = \{\chi^{12}, \chi^{56}, y^{12}, y^{56} | \bar{y}^{12}, \bar{y}^{56}, \bar{\psi}^{1,\dots,5}, \bar{\eta}^2\}$$

$$\beta_8 = z_1 = \{\bar{\phi}^{1,\dots,4}\}$$

$$\beta_9 = z_2 = \{\bar{\phi}^{5,\dots,8}\}$$

and a variable set of $2^{9(9-1)/2} + 1 = 2^{36} + 1 \sim 10^{11}$ phases $c[\beta_i]$.

Chirality

Fermion generations, transforming as $SO(10)$ spinorials, arise from $B_{pq}^l = S + b_{pq}^l$, $l = 1, 2, 3$ where $b_{pq}^1 = b^1 + p T_2 + q T_3$, $b_{pq}^2 = b^2 + p T_1 + q T_2$, $b_{pq}^3 = x + b^1 + b^2 + p T_1 + q T_2$, with $p, q \in \{0, 1\}$, and $x = 1 + S + \sum_{i=1}^3 T_i + \sum_{k=1}^2 z_k$.

Number of generations $N = \sum_{l=1,2,3} \chi^l$ where

$$\chi_{pq}^1 = -4c \left[S + b_2 + (1-q)T_3 \right] p_{pq}^1,$$

$$\chi_{pq}^2 = -4c \left[S + b_1 + (1-q)T_3 \right] p_{pq}^2,$$

$$\chi_{pq}^3 = -4c \left[S + b_1 + (1-q)T_1 \right] p_{pq}^3,$$

and

$$p_{pq}^l = \frac{1}{2^3} \left(1 - c \left[\frac{B_{pq}^l}{T_l} \right] \right) \left(1 - c \left[\frac{B_{pq}^l}{z_1} \right] \right) \left(1 - c \left[\frac{B_{pq}^l}{z_2} \right] \right)$$

Orbifold Partition function

The one-loop partition function at the generic point reads

$$\begin{aligned}
 Z = & \frac{1}{\eta^{12} \bar{\eta}^{24}} \frac{1}{2^3} \sum_{\substack{h_1, h_2, H \\ g_1, g_2, G}} \frac{1}{2^3} \sum_{\substack{a, k, \rho \\ b, \ell, \sigma}} \frac{1}{2^3} \sum_{\substack{H_1, H_2, H_3 \\ G_1, G_2, G_3}} (-1)^{a+b+HG+\Phi} \\
 & \times \vartheta \left[\begin{smallmatrix} a \\ b \end{smallmatrix} \right] \vartheta \left[\begin{smallmatrix} a+h_1 \\ b+g_1 \end{smallmatrix} \right] \vartheta \left[\begin{smallmatrix} a+h_2 \\ b+g_2 \end{smallmatrix} \right] \vartheta \left[\begin{smallmatrix} a-h_1-h_2 \\ b-g_1-g_2 \end{smallmatrix} \right] \\
 & \times \Gamma_{2,2}^{(1)}[H_1|h_1](T^{(1)}, U^{(1)}) \Gamma_{2,2}^{(2)}[H_2|h_2](T^{(2)}, U^{(2)}) \Gamma_{2,2}^{(3)}[H_3|h_1+h_2](T^{(3)}, U^{(3)}) \\
 & \times \bar{\vartheta}[\ell]^k \bar{\vartheta}[\ell+g_1]^{k+h_1} \bar{\vartheta}[\ell+g_2]^{k+h_2} \bar{\vartheta}[\ell-g_1-g_2]^{k-h_1-h_2} \bar{\vartheta}[\sigma]^\rho \bar{\vartheta}[\sigma+G]^\rho
 \end{aligned}$$

Where $T^{(i)} = T_1^{(i)} + iT_2^{(i)}$, $U^{(i)} = U_1^{(i)} + iU_2^{(i)}$ are the moduli of the three two tori, $\eta(\tau)$ is the Dedekind eta function and $\vartheta \left[\begin{smallmatrix} \alpha \\ \beta \end{smallmatrix} \right](\tau)$ stand for the Jacobi theta functions.

Connection with fermionic formulation

Fermionic point $T = \imath$ and $U = (1 + \imath)/2$

Phase $\Phi \left(c \left[\begin{smallmatrix} \beta_i \\ \beta_j \end{smallmatrix} \right] \right)$

Twisted/shifted lattices

$$\Gamma_{2,2}[{}^{H_i}_{G_i}|{}^h_g](T, U) = \begin{cases} \left| \frac{2\eta^3}{\vartheta[1-g]} \right|^2 & , (H_i, G_i) = (0, 0) \text{ or } (H_i, G_i) = (h, g) \\ \Gamma_{2,2}^{\text{shift}}[{}^{H_i}_{G_i}](T, U) & , h = g = 0 \\ 0 & , \text{otherwise} \end{cases}$$

$$\Gamma_{2,2}^{\text{shift}}[{}^{H_i}_{G_i}](T, U) = \sum_{\substack{m_1, m_2 \\ n_1, n_2}} (-1)^{G(m_1+n_2)} q^{\frac{1}{4}|P_L|^2} \bar{q}^{\frac{1}{4}|P_R|^2} ,$$

with

$$P_L = \frac{m_2 + \frac{H_i}{2} - Um_1 + T(n_1 + \frac{H_i}{2} + Un_2)}{\sqrt{T_2 U_2}} ,$$

$$P_R = \frac{m_2 + \frac{H_i}{2} - Um_1 + \bar{T}(n_1 + \frac{H_i}{2} + Un_2)}{\sqrt{T_2 U_2}} .$$

Typical partition functions

Some typical expansions of partition functions (fermionic point)

$$\begin{aligned} Z_{(A)} = & \frac{2q_i}{q_r} - \frac{16q_i}{\sqrt{q_r}} + (-312 + 32q_i + 56q_i^2) \\ & + \left(4064 + \frac{6144}{q_i} + 512q_i - 416q_i^2 \right) \sqrt{q_r} \\ & + \left(12288 + \frac{16384}{q_i^2} + \frac{103680}{q_i} - 12320q_i - 256q_i^2 + 792q_i^3 \right) q_r + \dots \end{aligned}$$

$$\begin{aligned} Z_{(B)} = & \frac{2q_i}{q_r} - \frac{32q_i}{\sqrt{q_r}} + \left(8 + 224q_i + 56q_i^2 \right) + \left(1984 + \frac{2048}{q_i} - 1024q_i - 832q_i^2 \right) \sqrt{q_r} \\ & + \left(30720 + \frac{10240}{q_i^2} + \frac{92160}{q_i} + 1760q_i + 5376q_i^2 + 792q_i^3 \right) q_r + \dots \end{aligned}$$

$$\begin{aligned} Z_{(C)} = & \frac{2q_i}{q_r} - \frac{16q_i}{\sqrt{q_r}} + \left(40 + 64q_i + 56q_i^2 \right) + \left(224 + \frac{6912}{q_i} + 768q_i - 672q_i^2 \right) \sqrt{q_r} \\ & + \left(14336 + \frac{9216}{q_i^2} + \frac{118656}{q_i} - 10144q_i + 3072q_i^2 + 792q_i^3 \right) q_r + \dots \end{aligned}$$

Classification

We expand the partition function in powers of $q_r = e^{-2\pi\tau_2}$

$$Z = \sum_{\substack{n \in \mathbb{Z}/2 \\ n \geq -1/2}} W_n q_r^n$$

The constant term at the fermionic point W_0 or the generic point W_0^G is proportional to $n_B - n_F$.

	$W_0 < 0$	$W_0 = 0$	$W_0 > 0$
$W_0^G < 0$	3560	0	1856
$W_0^G = 0$	96	0	8848
$W_0^G > 0$	0	0	62192
Total	3656	0	72896

Table 1: Number of chiral models for the subclasses of models with W_0^G positive/negative/zero and W_0 positive/negative.

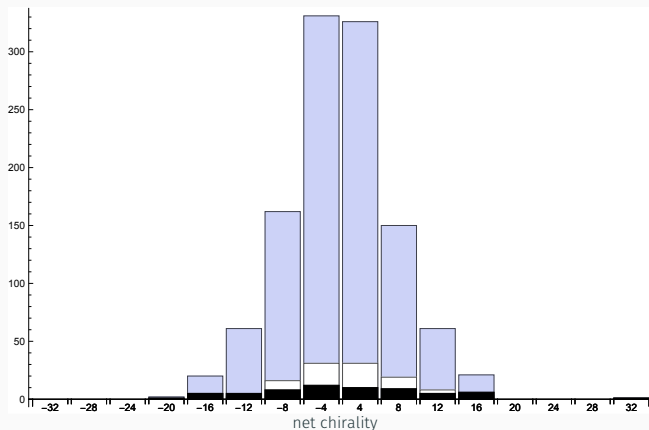
Numerical calculation

n	Model A	Model B
-1	24.4	24.4
$-\frac{1}{2}$	-9.87	-19.7
0	172.	2.11
$\frac{1}{2}$	-29.6	-17.7
1	3.13	-2.73
$\frac{3}{2}$	9.71	8.18
Total	+170.	-5.47

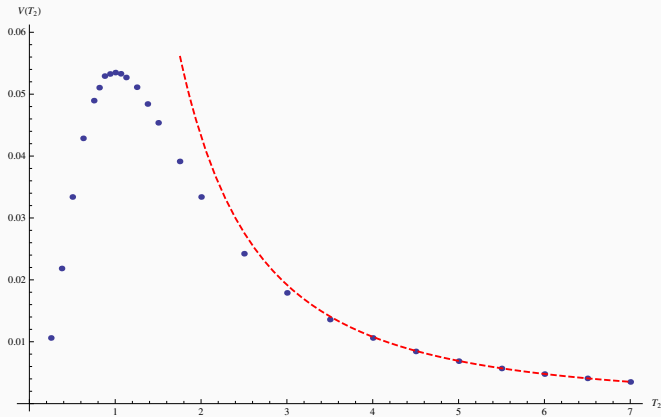
Contributions to the rescaled one-loop potential $2(2\pi)^4 V_{1-\text{loop}}$ arranged according to energy level for models A and B. At each level n , the cumulative contribution of level-matched as well as non level-matched states is displayed.

Chirality

A preliminary scan shows that a number of approximately 7×10^4 models in the class under consideration satisfy all criteria.

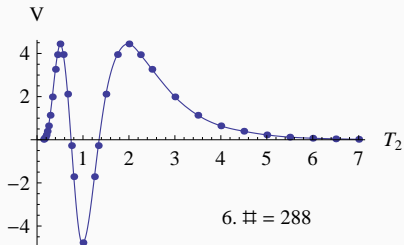
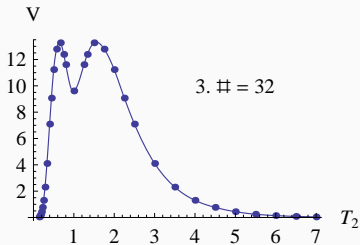
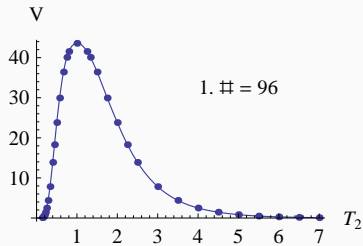
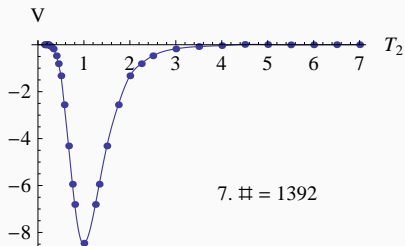


One loop potentials: Numerical results

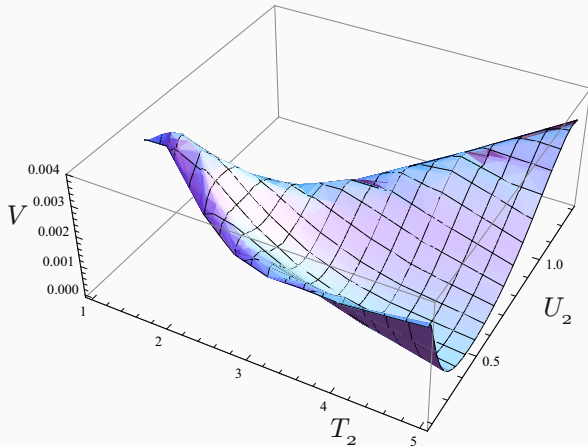


The asymptotic form of the one-loop potential versus the modulus T_2 (dashed line) matched against the direct numerical evaluation of the integral (in dots).

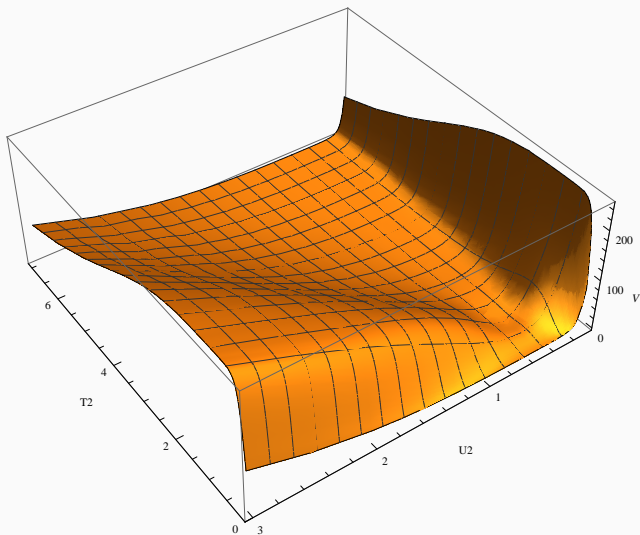
One loop potentials: Super no scale models



One loop potentials: Super no scale models



One loop potentials: Super no scale models



Gauge coupling Running - Thresholds

The gauge coupling running is calculable in the context of string theory. It turns out that they depend on the compactification moduli. At the one loop level

$$\frac{16\pi^2}{g_i^2(\mu)} = k_a \frac{16\pi^2}{g_s^2} + b_a \log \frac{M_s^2}{\mu^2} + \Delta_a$$

where $M_s = g_s M_P$, $M_P = 1/\sqrt{32G_N}$.

$b_a \leftrightarrow$ Massless modes $\Delta_a \leftrightarrow$ Massive modes

$$\Delta_a = \Delta'_a(t_i) + \hat{\Delta}_a$$

L. J. Dixon, V. Kaplunovsky and J. Louis (1991)

C. Angelantonj, I. Florakis and M. Tsulaia (2014)

Florakis (2015)

Decompactification problem

$$\Delta'_a - \Delta'_b = \sum_i \left\{ -\alpha_{ab}^i \log \left[T_2^i U_2^i |\eta(T^i) \eta(U^i)|^4 \right] \right. \\ \left. - \beta_{ab}^i \log \left[T_2^i U_2^i |\vartheta_4(T^i) \vartheta_2(U^i)|^4 \right] \right. \\ \left. - \gamma_{ab}^i \log \left[|\hat{j}_2(T^i/2) - \hat{j}_2(U^i)|^4 |j_2(U^i) - 24|^4 \right] \right\},$$

$\alpha_{ab}^i, \beta_{ab}^i, \gamma_{ab}^i$ model dependent coefficients The dominant growth at $T_2^i \gg 1$

$$\Delta'_a = \alpha_a^i \left(\frac{\pi}{3} T_2^i - \log T_2^i \right) + \dots,$$

Solutions ? : $a_a^i = 0, \dots$

Antoniadis (1990)

E. Kiritsis, C. Kounnas, P.M. Petropoulos, J. R. (1996)

Computation of the thresholds

The dominant moduli dependent contribution is

$$\Delta'_a = -\frac{k_a}{48} Y + \hat{\beta}_a \Delta ,$$

where the universal part Y is defined as

$$Y = \int_{\mathcal{F}} \frac{d^2\tau}{\tau_2} \Gamma_{2,2}(T, U) \left(\frac{\hat{\bar{E}}_2 \bar{E}_4 \bar{E}_6 - \bar{E}_4^3}{\bar{\Delta}} + 1008 \right) ,$$

$$\Delta = \int_{\mathcal{F}} \frac{d^2\tau}{\tau_2} \Gamma_{2,2}(T, U) = -\log \left[T_2 U_2 |\eta(T) \eta(U)|^4 \right] .$$

At the limit $T_2 \gg 1$

$$Y = 48\pi T_2 + \mathcal{O}(T_2^{-1}) , \quad \Delta = \frac{\pi}{3} T_2 - \log T_2 + \mathcal{O}(e^{-2\pi T_2})$$

and finally

$$\Delta_a = \left(\frac{\hat{\beta}_a}{3} - k_a \right) \pi T_2 + \mathcal{O}(\log T_2) .$$

Computation of the thresholds

A comprehensive scan over a class of 7×10^4 models with $SO(10) \times SO(8)^2 \times U(1)^2$ gauge symmetry yields for the non-abelian gauge couplings

Decompactification condition $\hat{\beta}_a = 3k_a$

\hat{b}_{10}	\hat{b}_8	$\hat{b}_{8'}$	# of models	%
3	3	3	29456	38.5
9	-3	-3	15840	20.7
-3	9	9	14000	18.3
.	22.5

In a big class of vacua there is no decompactification problem for the gauge couplings.

Gauge coupling running

For models satisfying the decompactification condition $\hat{\beta}_a = 3k_a$ the coupling running is

$$\frac{16\pi^2}{g_a^2(\mu)} = k_a \frac{16\pi^2}{g_s^2} + \beta_a \log \frac{M_s^2}{\mu^2} + \beta'_a \log \left(\frac{2e^{1-\gamma}}{3\pi\sqrt{3}} \frac{M_{KK}^2}{M_s^2} \right) + \dots$$

Here, γ is the Euler-Mascheroni constant, $M_{KK} = 1/\sqrt{T_2}$ is the Kaluza-Klein scale. $\beta_a = b_a^{(1)} + b_a^{(2)} + b_a^{(3)}$ and $\beta'_a = b_a^{(1)} + b_a^{(2)}$ with $b_a^{(1)} = \hat{\beta}_a$

A Standard Model scenario

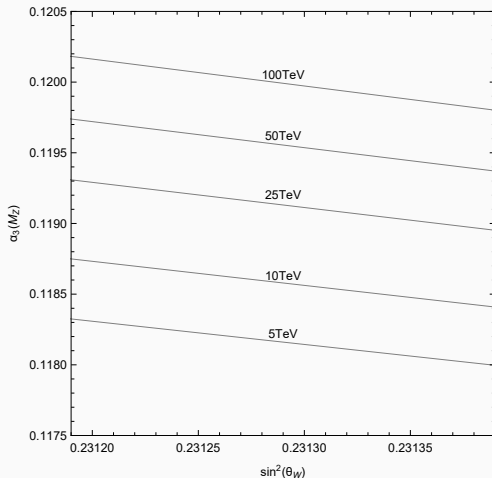
$$\frac{k_2 + k_Y}{\alpha_S} = \frac{1}{\alpha_{\text{em}}} - \frac{\beta_2 + \beta_Y}{4\pi} \log \frac{M_S^2}{M_Z^2} - \frac{\beta'_2 + \beta'_Y}{4\pi} \log \left(\frac{2e^{1-\gamma}}{3\pi\sqrt{3}} \frac{M_{\text{KK}}^2}{M_S^2} \right)$$

$$\sin^2 \theta_W = \frac{k_2}{k_2 + k_Y} + \frac{\alpha_{\text{em}}}{4\pi} \left[\frac{k_Y \beta_2 - k_2 \beta_Y}{k_2 + k_Y} \log \frac{M_S^2}{M_Z^2} + \frac{k_Y \beta'_2 - k_2 \beta'_Y}{k_2 + k_Y} \log \left(\frac{2e^{1-\gamma}}{3\pi\sqrt{3}} \frac{M_{\text{KK}}^2}{M_S^2} \right) \right]$$

$$\frac{1}{\alpha_3(M_Z)} = \frac{k_3}{\alpha_{\text{em}}(k_2 + k_Y)} + \frac{1}{4\pi} \left[\left(\beta_3 - \frac{k_3(\beta_2 + \beta_Y)}{k_2 + k_Y} \right) \log \frac{M_S^2}{M_Z^2} + \left(\beta'_3 - \frac{k_3(\beta'_2 + \beta'_Y)}{k_2 + k_Y} \right) \log \left(\frac{2e^{1-\gamma}}{3\pi\sqrt{3}} \frac{M_{\text{KK}}^2}{M_S^2} \right) \right]$$

A Standard Model scenario

For $(\beta_Y, \beta_2, \beta_3) = (-7, -\frac{19}{6}, \frac{41}{6})$, $(k_Y, k_2, k_3) = (\frac{5}{3}, 1, 1)$ and $(\beta'_Y, \beta'_2, \beta'_3) = (-\frac{15}{2}, -\frac{43}{6}, -\frac{23}{3})$.



Conclusions

We have analysed a class of non supersymmetric heterotic vacua where SUSY is spontaneously broken via the Scherk–Schwartz mechanism. In this context we have constructed semi-realistic models with the following interesting characteristics

- Fermion chirality
- Dynamical determination of supersymmetry breaking scale $M_{\text{SUSY}} \ll M_{\text{Planck}}$
- Exponentially small cosmological constant
- Finite gauge coupling running (no decompactification problem)
- These developments pay the way for non-supersymmetric string phenomenology (consider more realistic models e.g. Pati–Salam)