

# The Quest for Primordial Tensor Modes

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# Useful Axions

Axions can play a role for

- the strong CP problem in QCD (Peccei, Quinn, 1977)
- the mechanism of inflation (Freese, Frieman, Olinto, 1990)
- the source of quintessence (Frieman, Hill, Stebbins, Waga, 1995)
- the relaxion (Graham, Kaplan, Rajendran, 2015)

Axions are abundant in string theory constructions

- there is an opportunity for multi-axion systems
- that seems to be helpful for the consistency of axionic models

**Vielfalt statt Einfalt: Diversity beats Simplicity**

# The Role of Axions

Concentrate here on (aligned) inflation

(Kim, Nilles, Peloso, 2005)

- axionic inflation
- Planck satellite and BICEP2 data
- high scale inflation and trans-Planckian excursions
- **the alignment of axions and its stability**

Other application of multi-axion systems

- axionic domain walls for QCD axion (Choi, Kim, 1985)
- alignment of quintessential axions (Kaloper, Sorbo, 2006)
- the relaxion mechanism (Choi, Im, 2015)

# Window of Opportunity

Measurement of sizeable tensor modes could give precious information on the physics at highest energies.

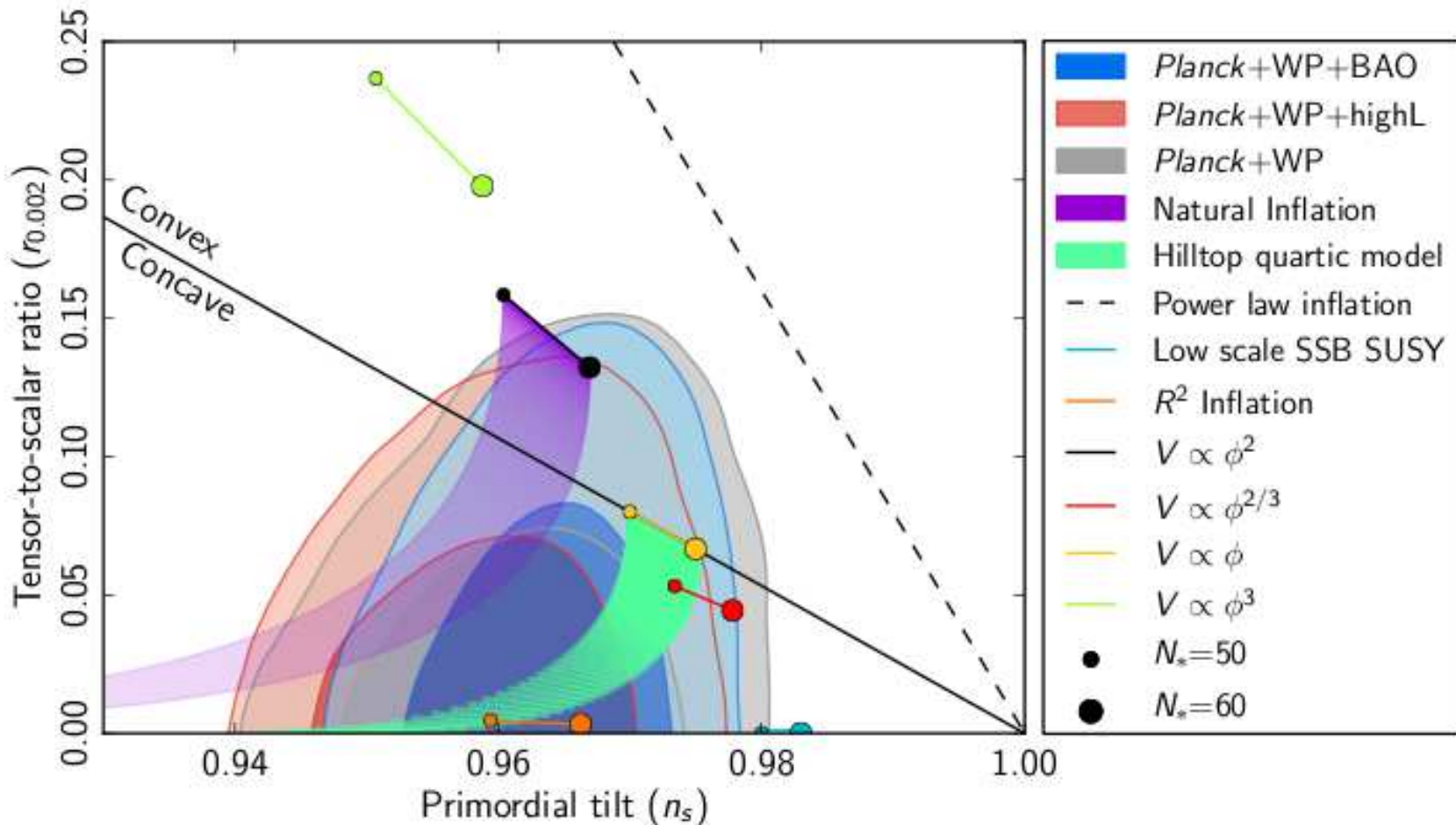
- we might explore physics close to the Planck scale
- get new insight on properties of (quantum) gravity

A theoretical treatment of these sizeable tensor modes could therefore be problematic

- question of trans-Planckian excursions (Lyth bound)
- the question of UV-completion (e.g. string theory)
- the weak gravity conjecture (and variants thereof)

Let us hope that sizeable tensor modes will be found.

# Planck results (Spring 2013)



# How to get Large Tensor Modes

We consider here **two specific cases** for large tensor modes

- the mechanism of axionic (natural) inflation

(Freese, Frieman, Olinto, 1990)

- enhanced tensor modes from extra dimensions

(Giudice, Kolb, Lesgourgues, Riotto, 2002)

On the way we shall be confronted with some obstacles

- the "problem" of trans-Planckian decay constants
- duality symmetries in string theory
- upper limits on Hubble scale during inflation

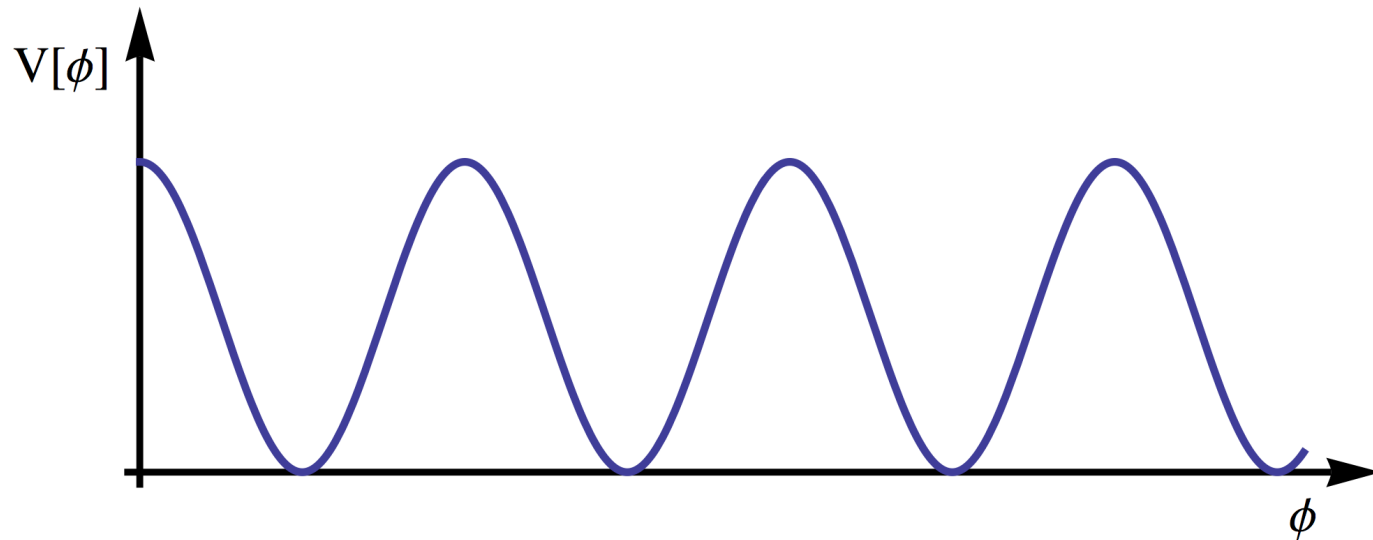
Based on work by

(Kappl, Nilles, Winkler, 2015; Im, Nilles, Trautner, 2017)

# Axionic Inflation

The axion exhibits a shift symmetry  $\phi \rightarrow \phi + c$

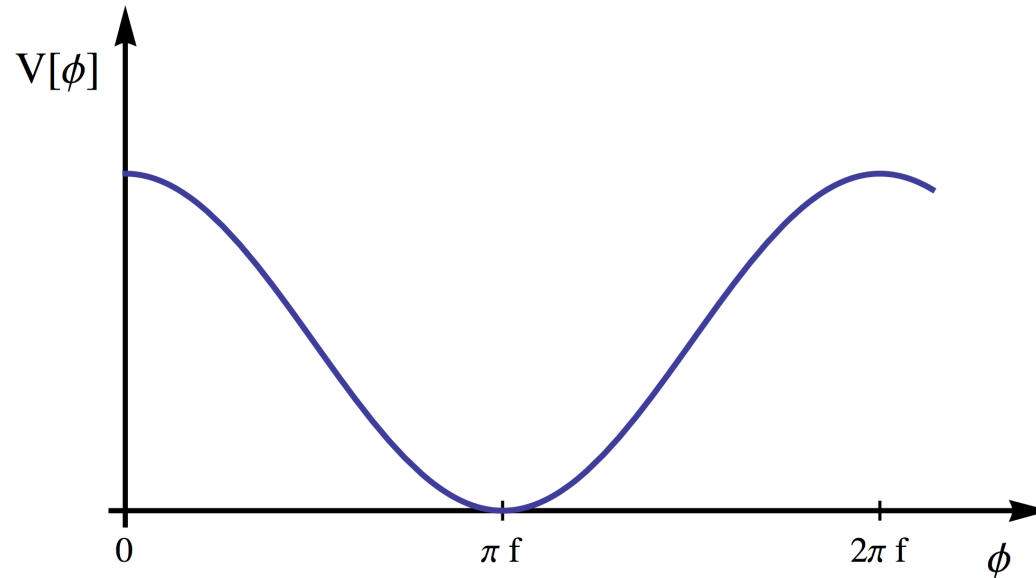
Nonperturbative effects break this symmetry to a remnant **discrete shift symmetry**



$$V(\phi) = \Lambda^4 \left[ 1 + \cos \left( \frac{\phi}{f} \right) \right]$$

# The Axion Potential

Discrete shift symmetry identifies  $\phi = \phi + 2\pi n f$

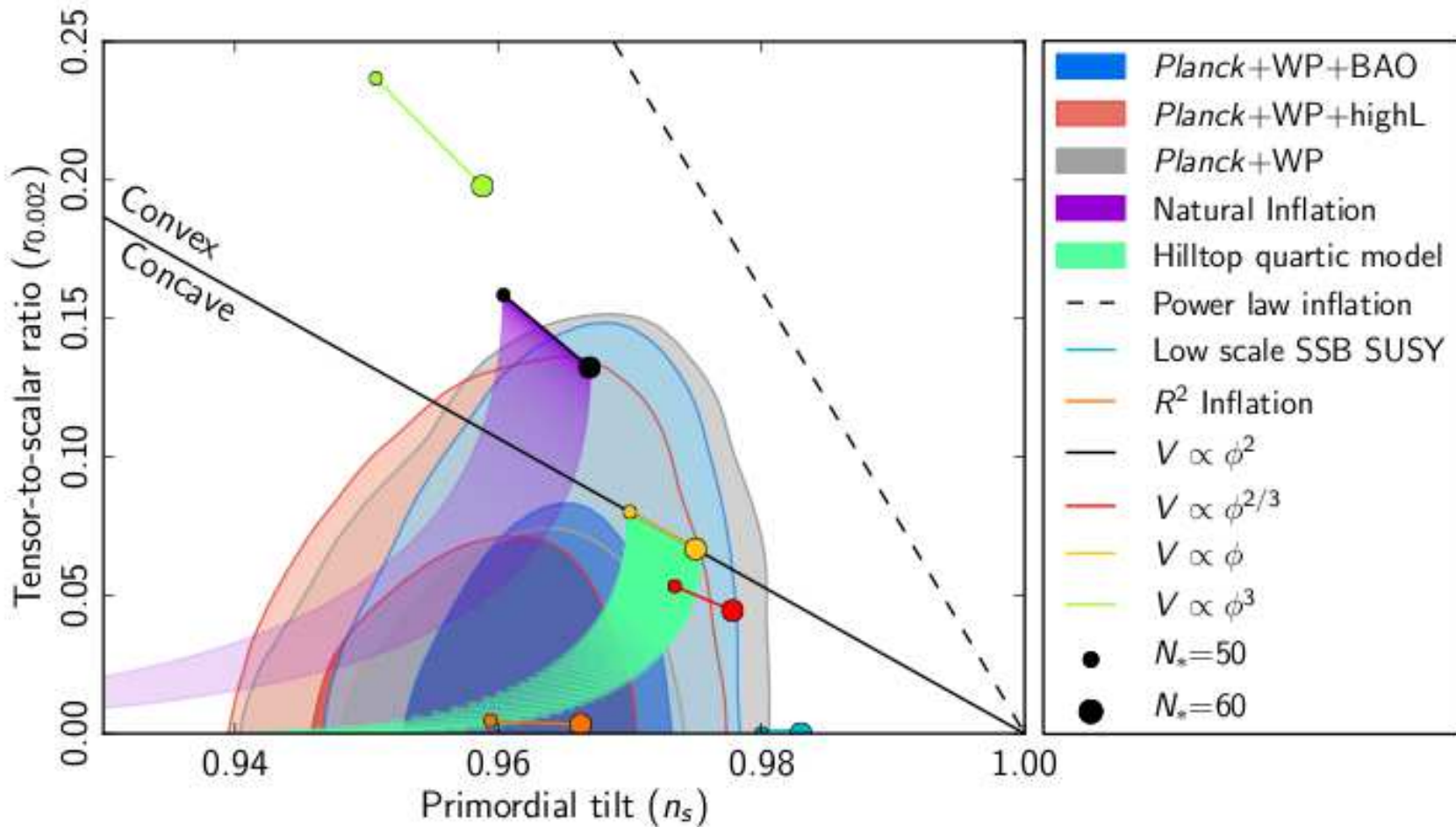


$$V(\phi) = \Lambda^4 \left[ 1 + \cos \left( \frac{\phi}{f} \right) \right]$$

$\phi$  confined to one fundamental domain



# Planck results (Spring 2013)



# The question of tensor modes

Sizeable tensor modes are of particular interest:

- they might lead us to scales of physics close to the Planck scale and the so-called “Lyth bound”
- potential  $V(\phi)$  of order of GUT scale
- trans-Planckian excursions of the inflaton field
- For a quadratic potential  $V(\phi) \sim m^2 \phi^2$  it implies  $\Delta\phi \sim 15M_{\text{P}}$  to obtain 60 e-folds of inflation

Axionic inflation, on the other hand, seems to require the decay constant to be limited:  $f \leq M_{\text{P}}$

So this might be problematic, in particular for a UV-completion in string theory

(Banks, Dine, Fox, Gorbatov, 2003)

# Aligned axions

A way out is the consideration of two (or more) fields.

(Kim, Nilles, Peloso, 2004)

- still we require  $f \leq M_{\text{P}}$  for the individual axions
- aligned axion has effective decay constant beyond the Planck scale
- string favours a multi-axion picture

The alignment prolongs the fundamental domain of the aligned axion to super-Planckian values, as the axionic inflaton spirals down in the potential of the second axion

This avoids the restrictions of the single axion model.

# The KNP set-up

We consider two axions

$$\mathcal{L}(\theta, \rho) = (\partial\theta)^2 + (\partial\rho)^2 - V(\rho, \theta)$$

with potential

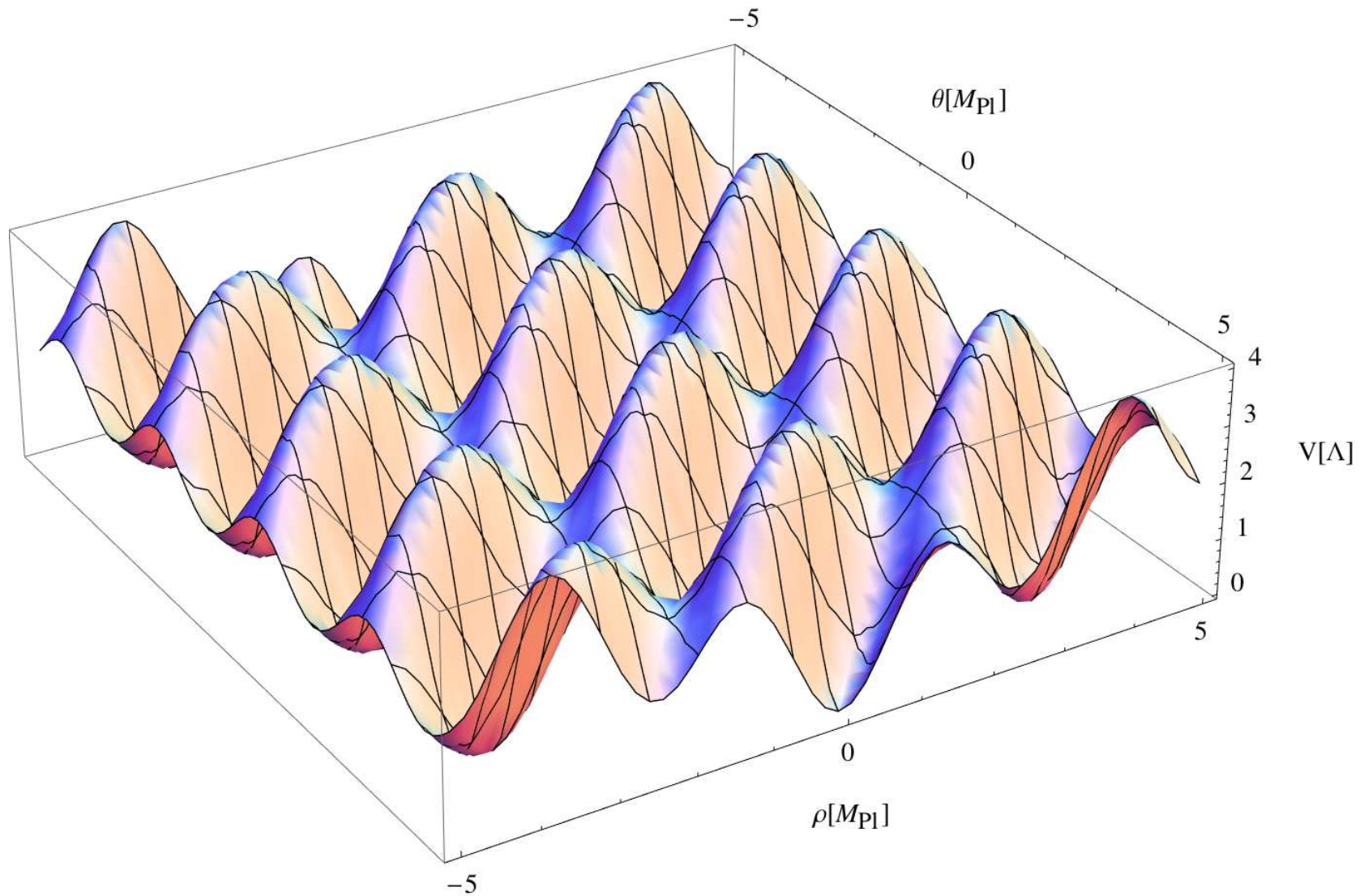
$$V(\theta, \rho) = \Lambda^4 \left( 2 - \cos \left( \frac{\theta}{f_1} + \frac{\rho}{g_1} \right) - \cos \left( \frac{\theta}{f_2} + \frac{\rho}{g_2} \right) \right)$$

This potential has a flat direction if  $\frac{f_1}{g_1} = \frac{f_2}{g_2}$

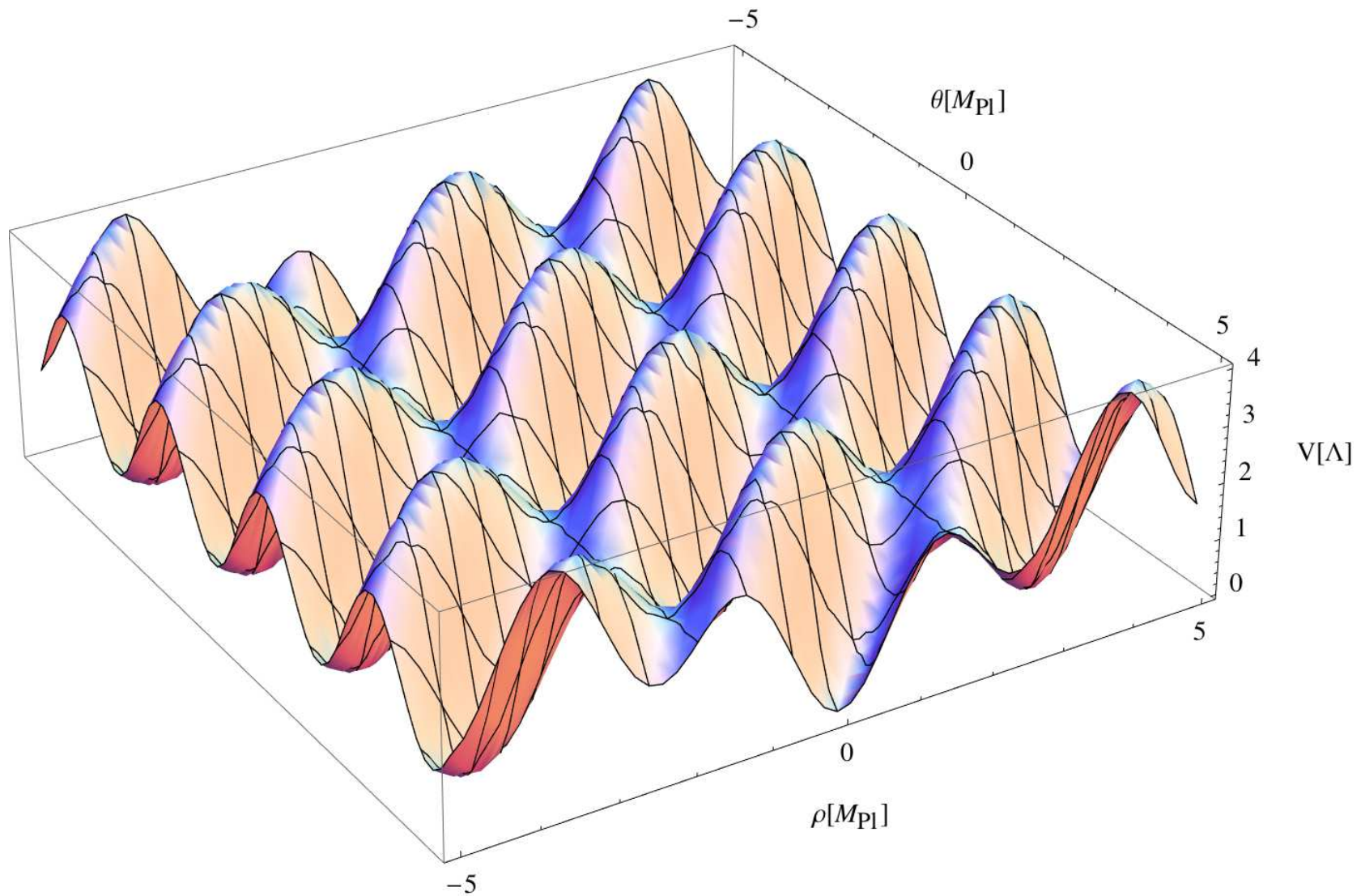
Alignment parameter defined through  $\alpha = g_2 - \frac{f_2}{f_1} g_1$

For  $\alpha = 0$  we have a massless field  $\xi$ .

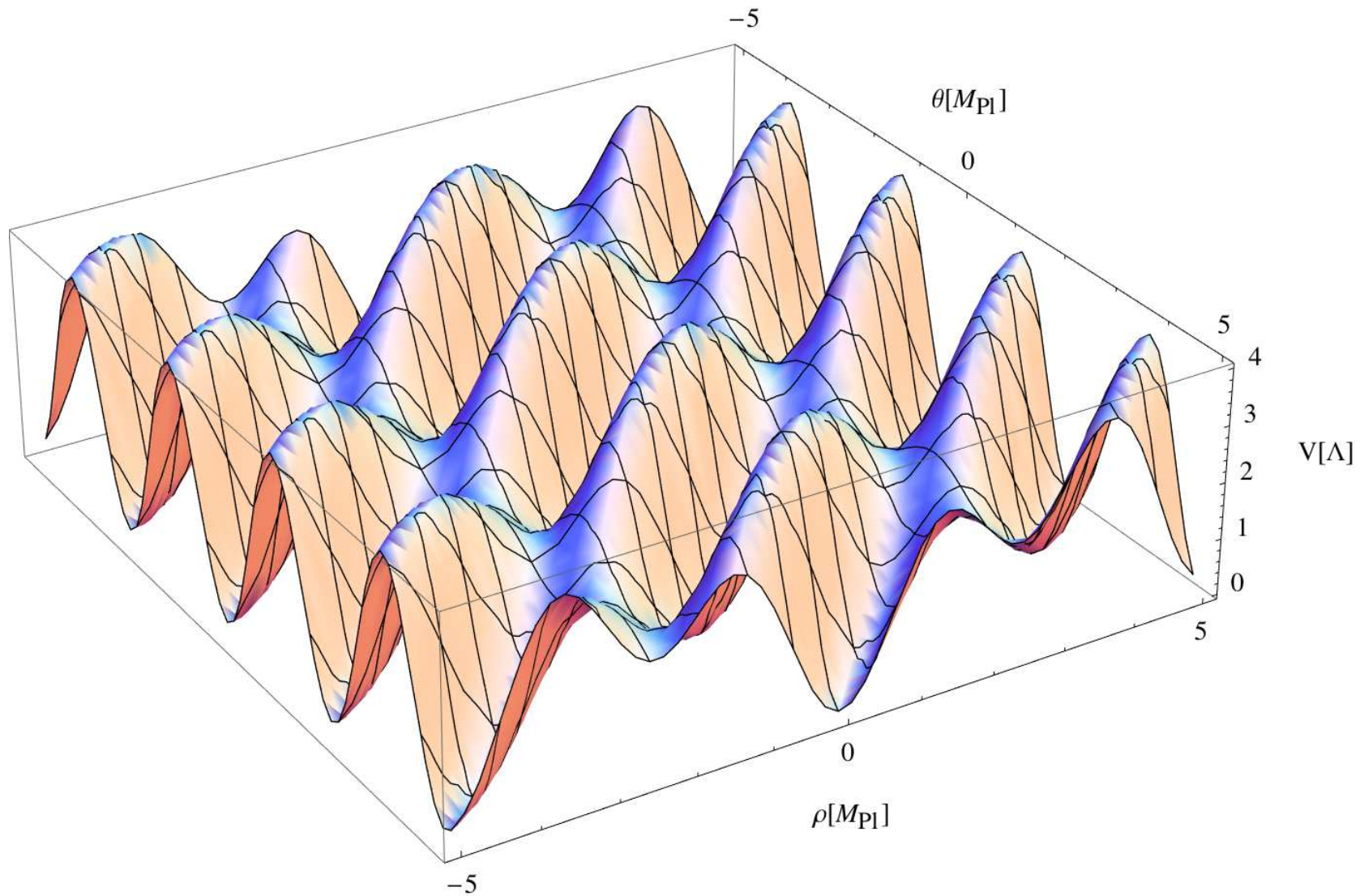
# Potential for $\alpha = 1.0$



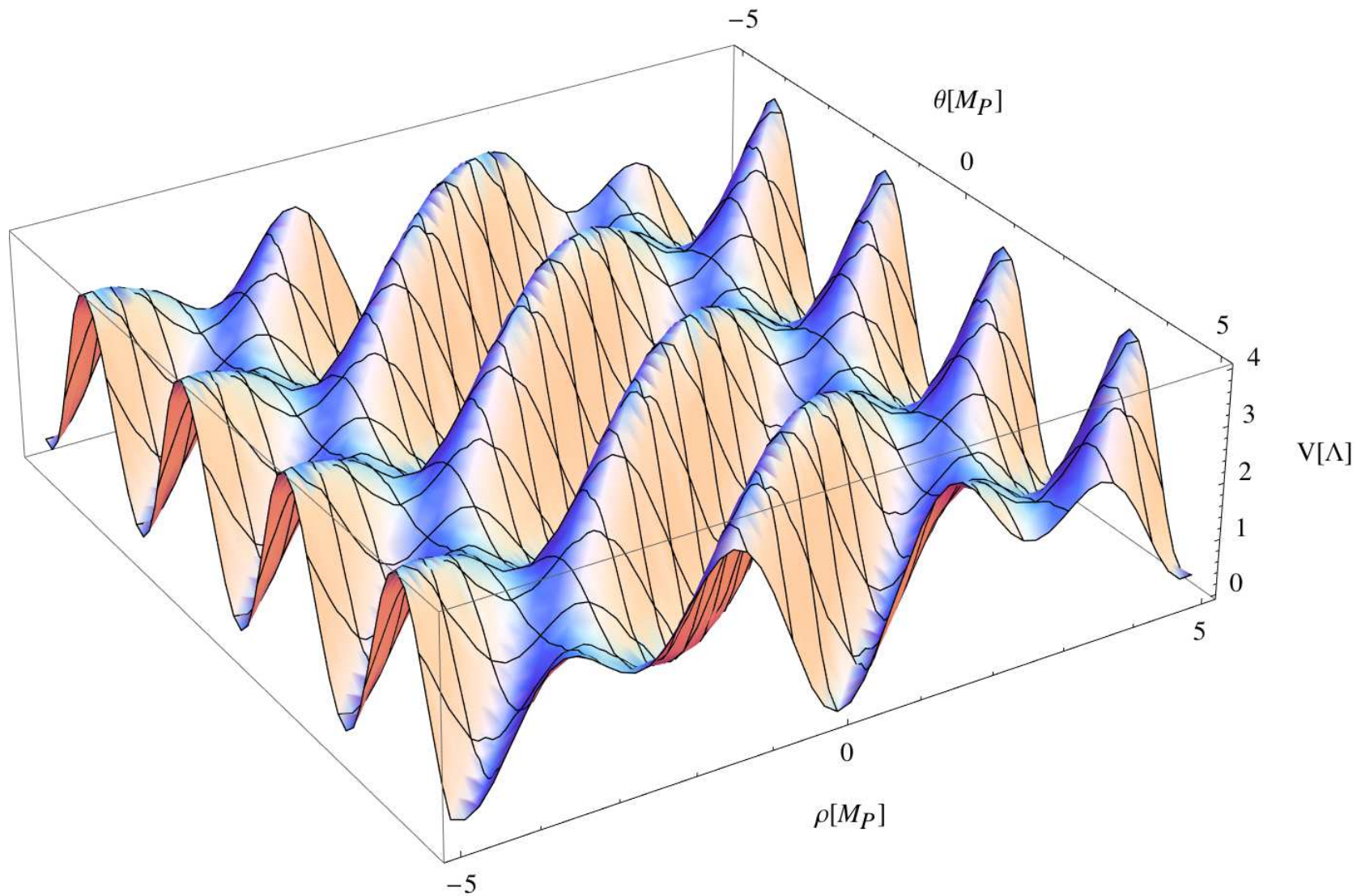
# Potential for $\alpha = 0.8$



# Potential for $\alpha = 0.5$

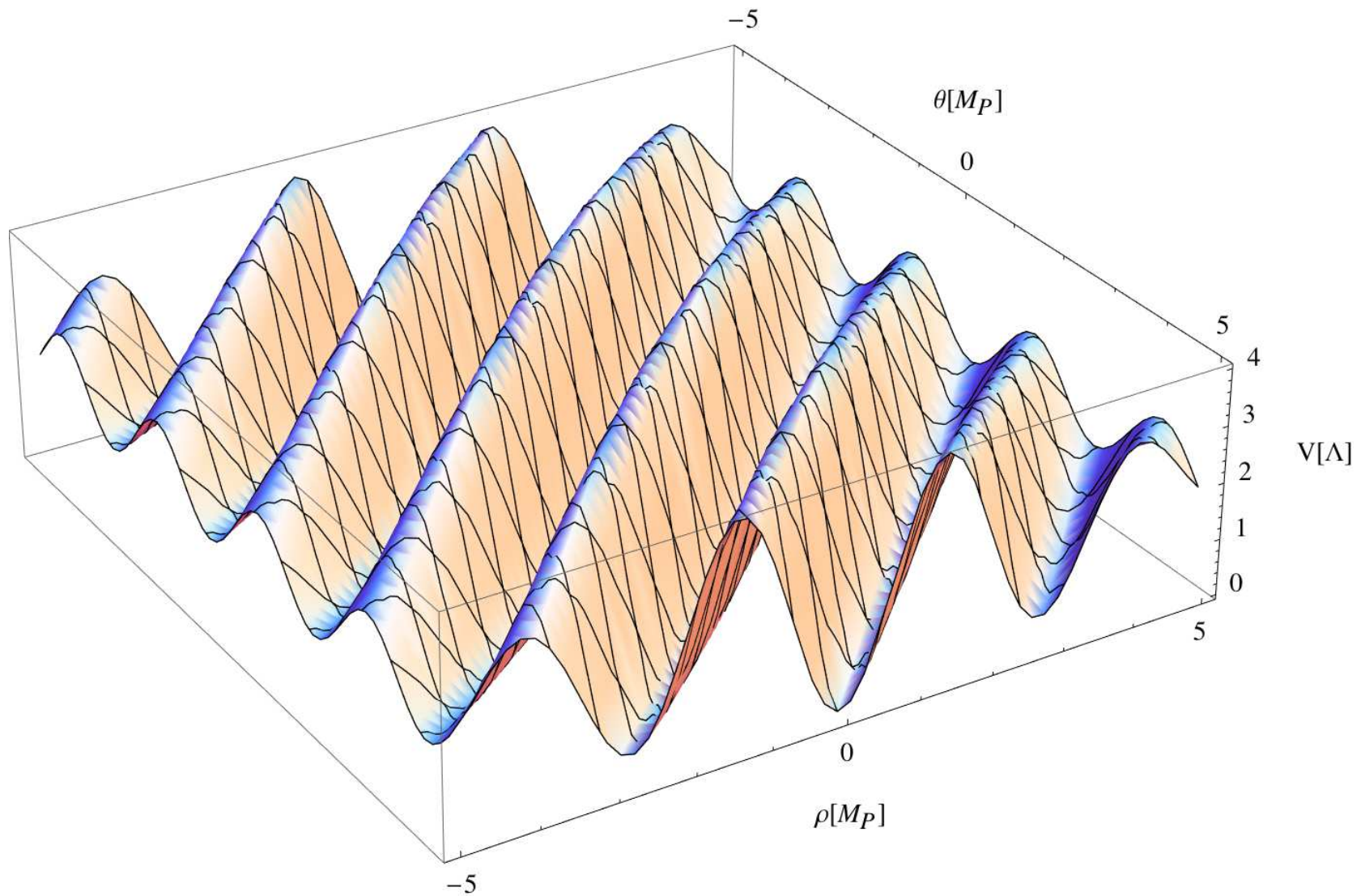


# Potential for $\alpha = 0.3$

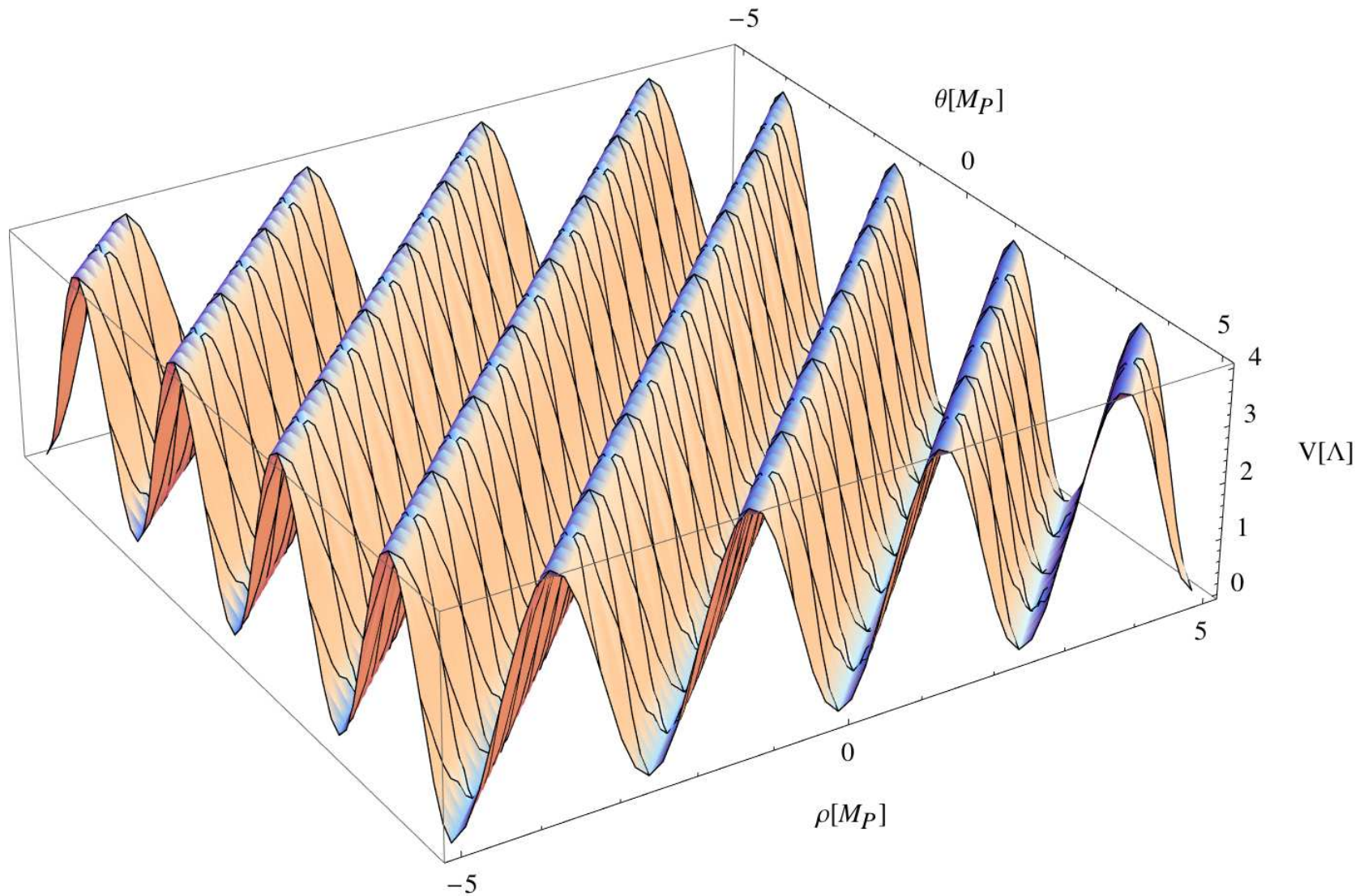




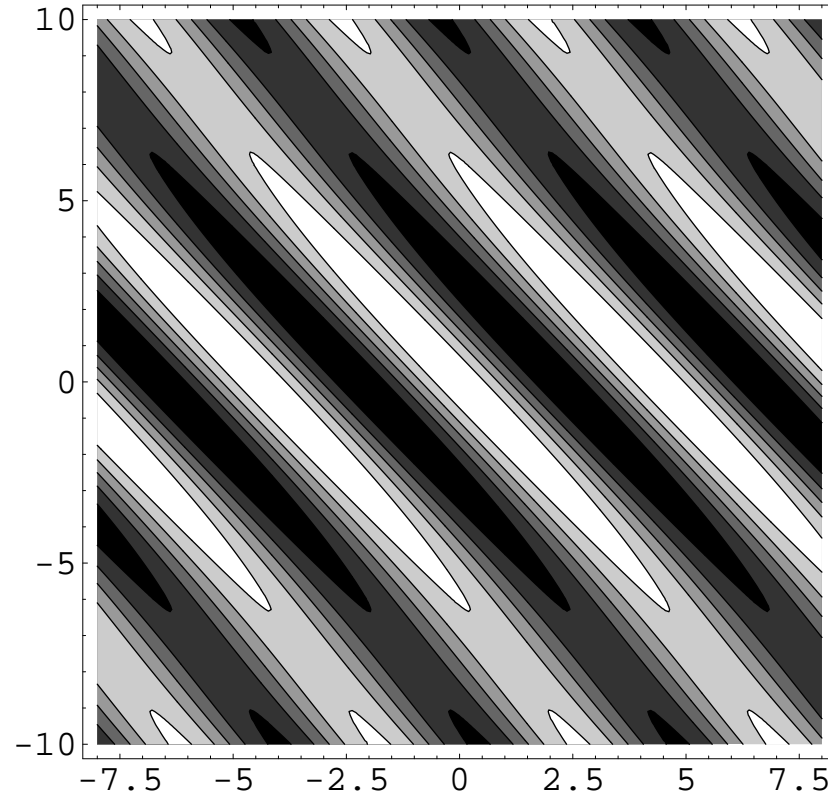
# Potential for $\alpha = 0.1$



# Potential for $\alpha = 0$



# The aligned Axion Landscape



The field  $\xi$  rolls within the valley of  $\psi$ . The motion of  $\xi$  corresponds to a motion of  $\theta$  and  $\rho$  over **many cycles**. The system is still controlled by discrete symmetries.

# UV-Stability

We have a very flat direction and within the effective QFT we are at the “edge of control”

- is inflation perturbed by other effects?
- is there an upper limit on  $f_{\text{eff}}$ ?

Remember that in case of a single axion we had the limit

- $f \leq M_{\text{string}}$  (Banks, Dine, Fox, Gorbatov, 2003)
- derived from dualities in string theory (e.g. T-duality)

In the multi-axion case these arguments are not directly applicable, but we still have to worry about these questions, also in view of the “weak gravity conjecture”.

(Arkani-Hamed, Motl, Nicolis, Vafa, 2006)

# $T$ –Duality

String dualities give important constraints on the axion decay constants, especially  $T$ –duality  $SL(2, Z)$ :

$$T \rightarrow \frac{aT - ib}{icT + d}$$

generated by an inversion and a shift

$$T \rightarrow 1/T, \quad T \rightarrow T + i.$$

$$G = K + \log |W|^2$$

must be invariant under  $T$ -duality.

# $T$ –Duality

$K$  and  $W$  might transform nontrivially. Consider e.g.

$$K = -3 \log (T + \bar{T}).$$

This Kähler potential transforms under  $SL(2, Z)$  as

$$K \rightarrow K + \log |icT + d|^6$$

and has to be compensated by a superpotential transforming as a modular form (of weight  $-3$ ):

$$W \rightarrow (icT + d)^{-3}W .$$

# Not just a Cosine

In string theory we do not just get cosine potentials, but obtain modular functions (e.g. Dedekind-functions) from

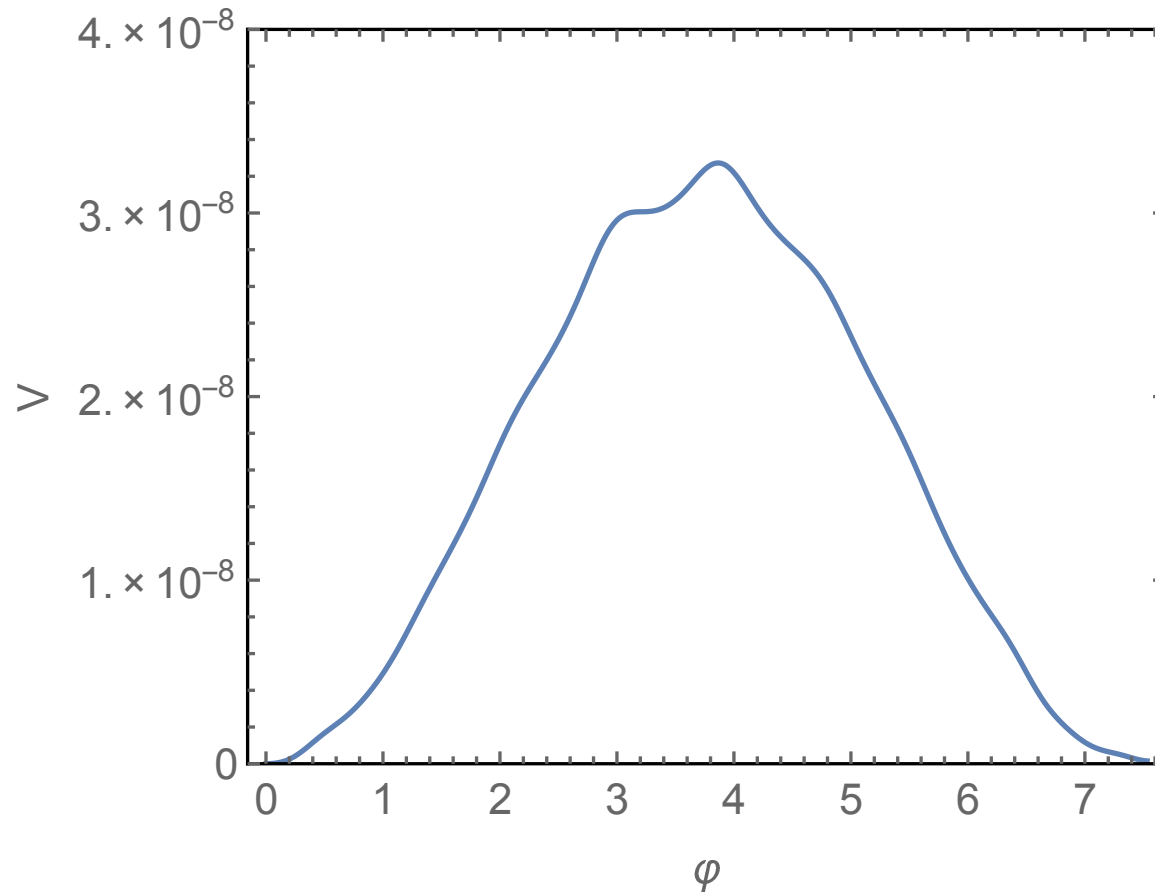
- world sheet instanton effects,
- gauge kinetic functions and gaugino condensates.

So we might consider instead a modular function

$$\eta(T) = e^{-\pi T/12} \times \prod_k (1 - e^{-2k\pi T})$$

The higher harmonics give wiggles in the potential that perturb the flat direction and might stop inflation. In the case of a single axion this prevents a trans-Planckian  $f$ .

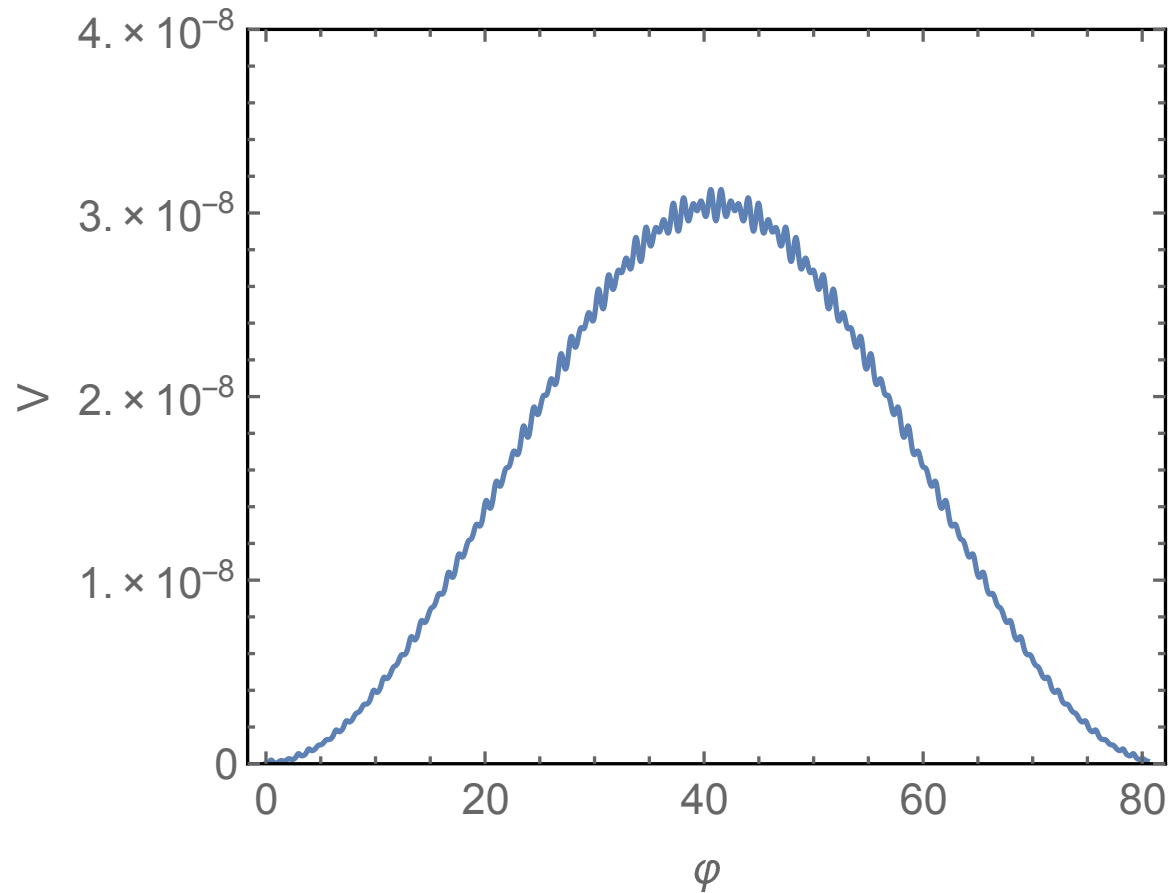
# Wiggles in the aligned potential



The wiggles in the case of weak alignment (small  $f$ )



# Wiggles in the aligned potential



Strong alignment (leading to superPlanckian  $f$ )

# Modulated natural Inflation

It seems plausible that under some circumstances the wiggles become important and

- spoil the flat direction,
- provide an upper limit on decay constant  $f_{\text{eff}}$ .

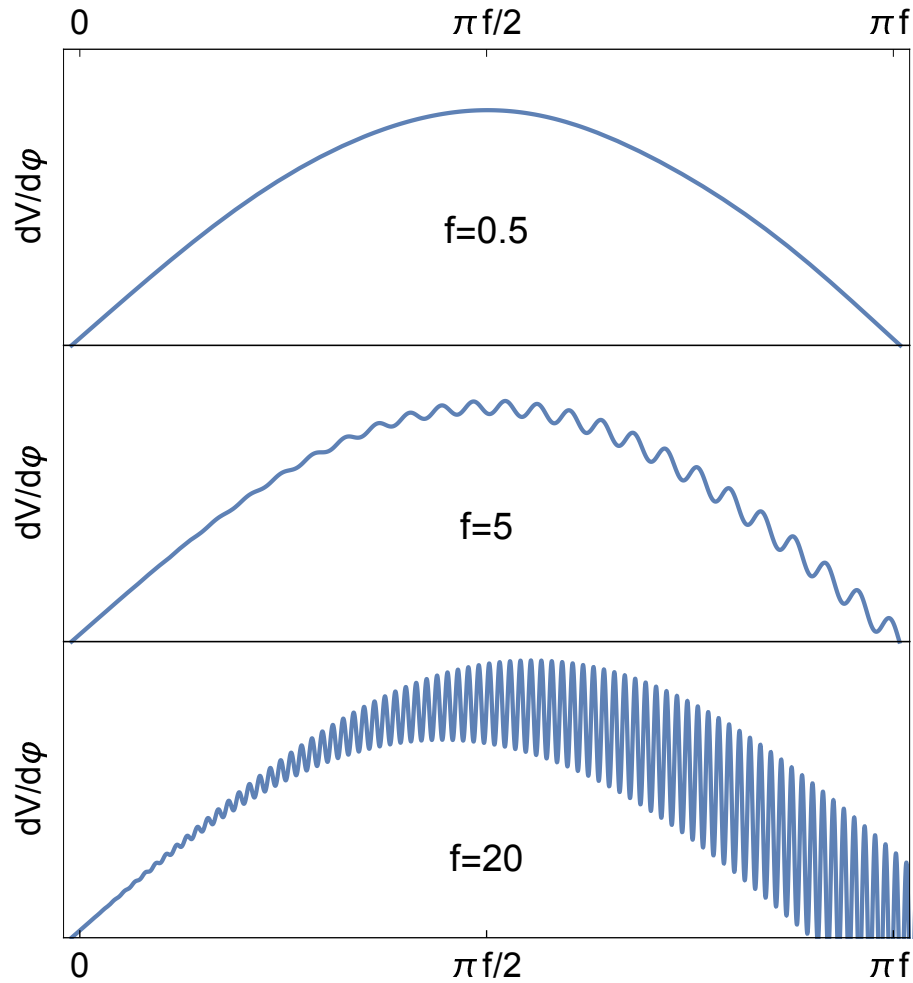
Explicit calculations are necessary to clarify the situation,

- but might be beyond our present capabilities;
- observational confirmation is extremely important.

Restrictions from WGC are satisfied here both in the aligned and non-aligned case.

(Kappl, Nilles, Winkler, 2015; Choi, Kim, 2015; Kobayashi, Nitta, Urakawa, 2016)

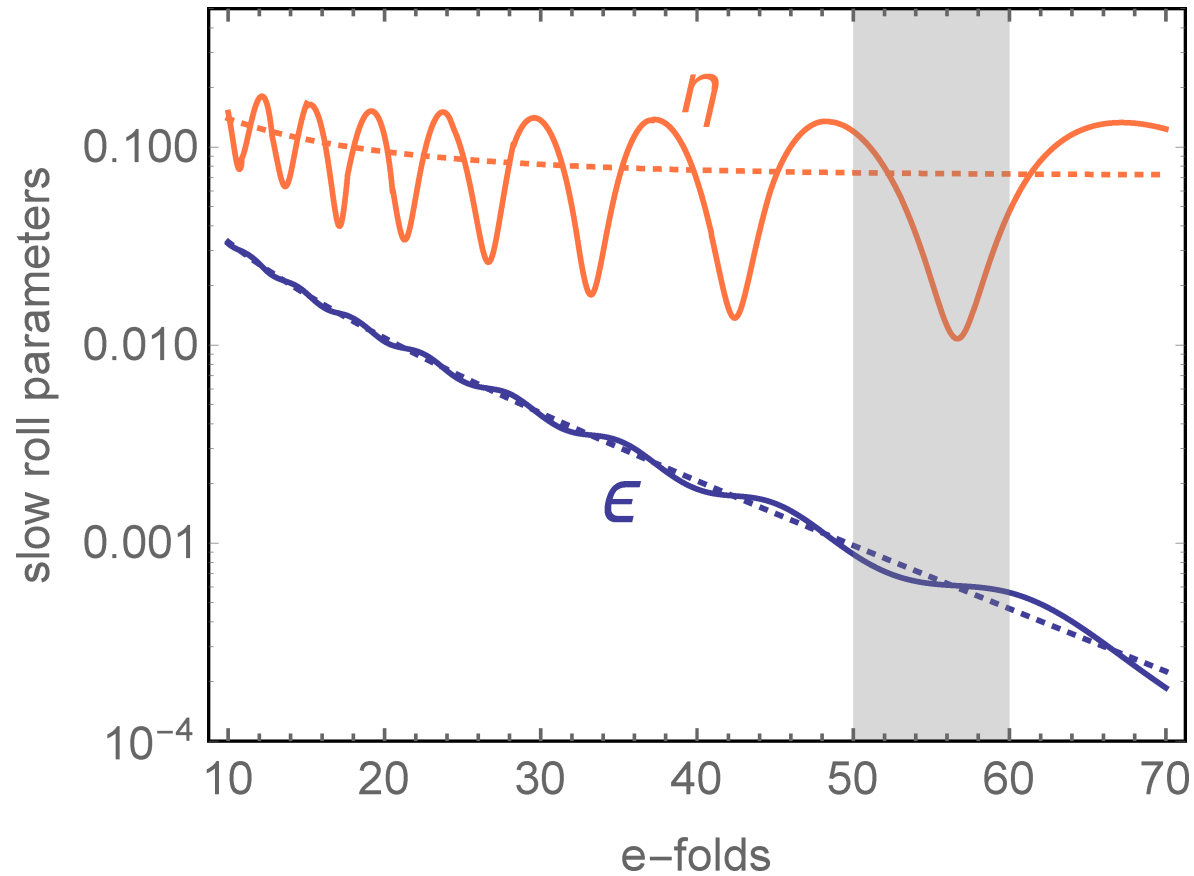
# Slope of Potential



Wiggly structure becomes important

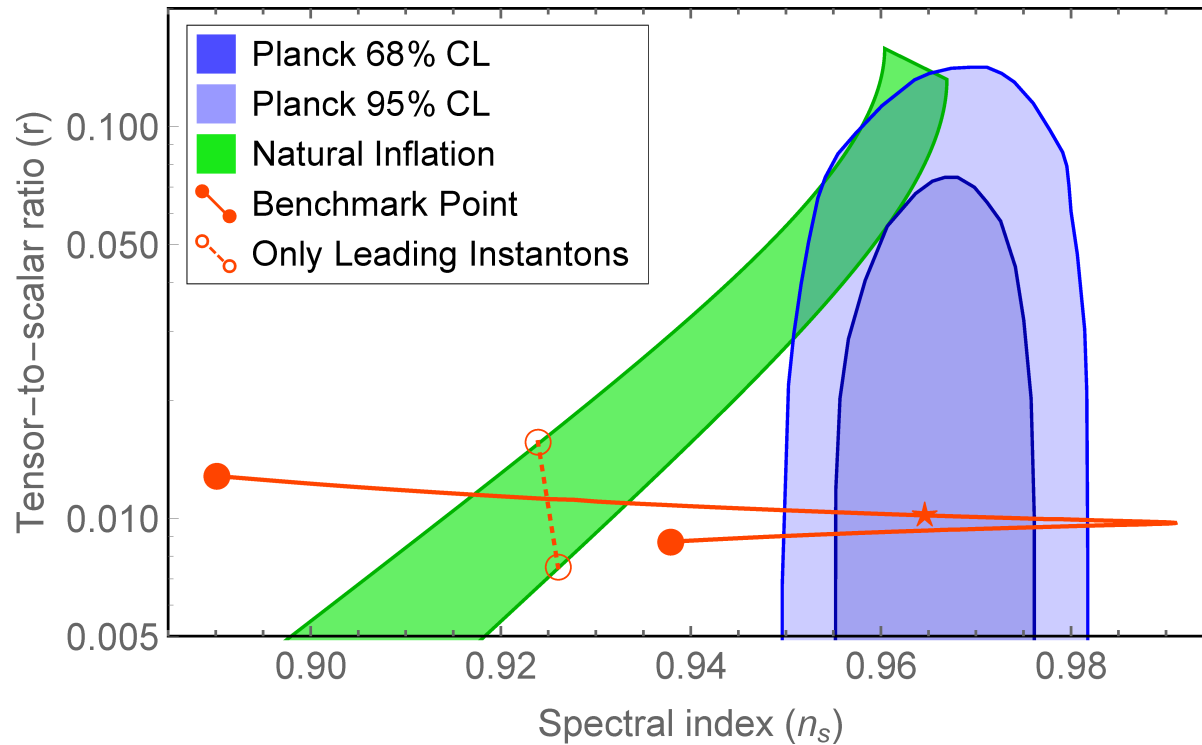
(Abe, Kobayashi, Otsuka, 2015; Kappl, Nilles, Winkler, 2015)

# Slow roll parameters



$\epsilon$  ( $\eta$ ) depend on first (second) derivative

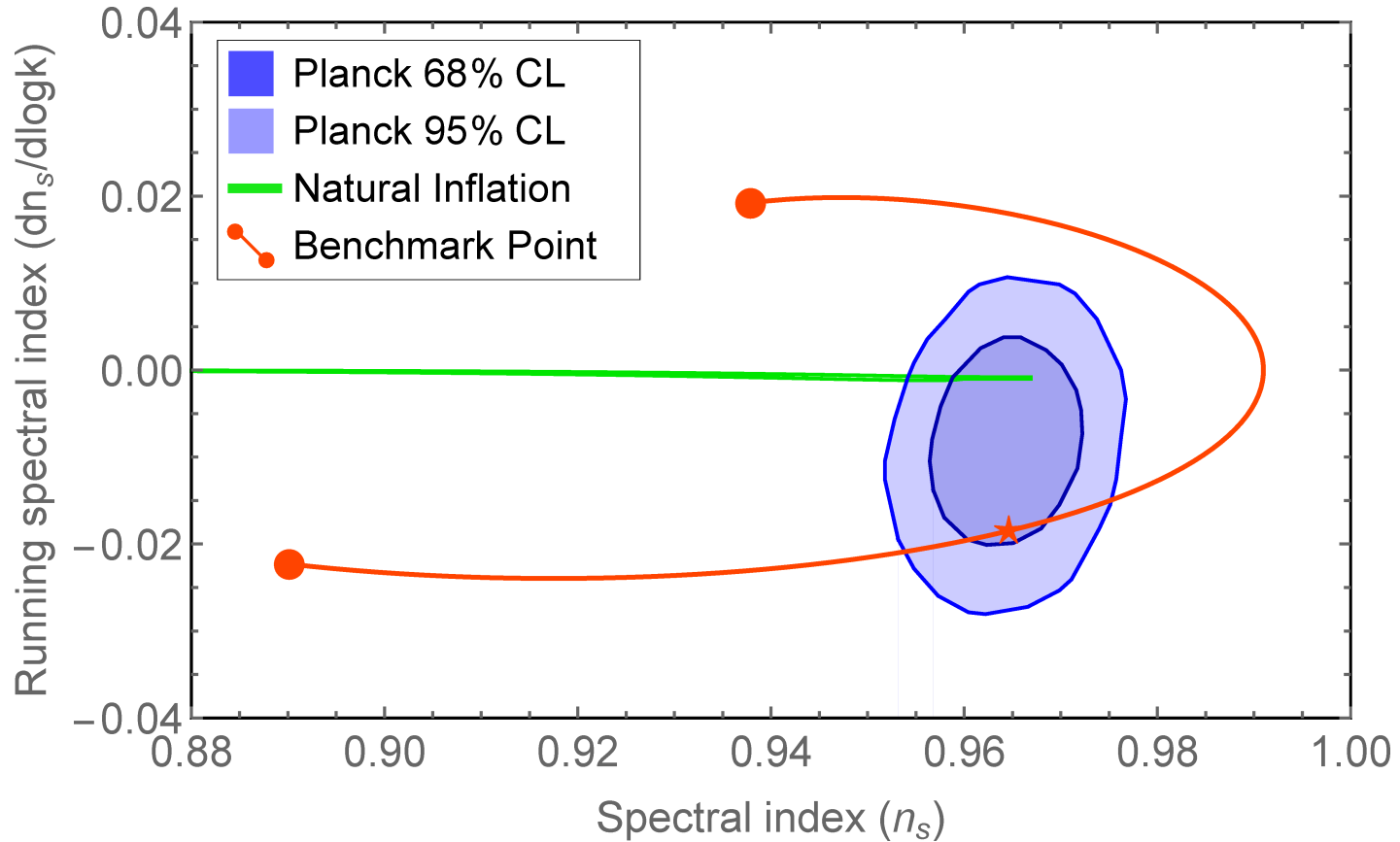
# $n_s - r$ plane



Strong variations of  $n_s$  on the number of e-folds.

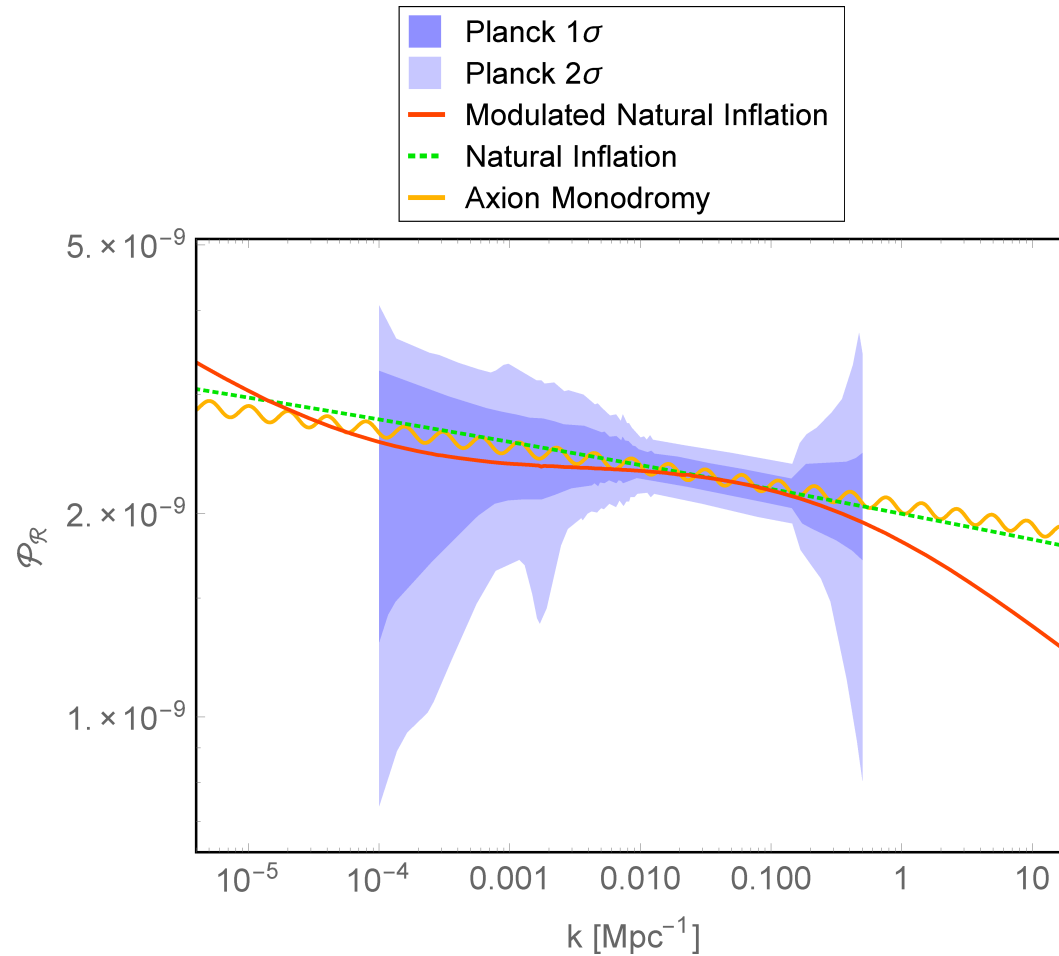
(Kappl, Nilles, Winkler, 2015)

# Running of spectral index



Comparison of spectral index with Planck data

# Scalar power spectrum

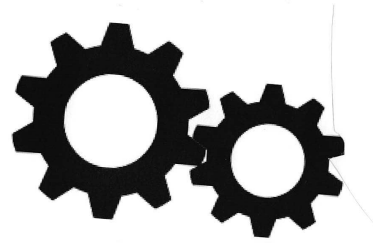


Comparison to Planck reconstructed power spectrum

# More than two axions

The alignment mechanism can be extended to more than two axions and find an interpretation as a "clockwork"

(Choi, Kim, Yun, 2014; Choi, Im, 2015; Kaplan, Rattazzi, 2015; Guidice, McCullough, 2016)



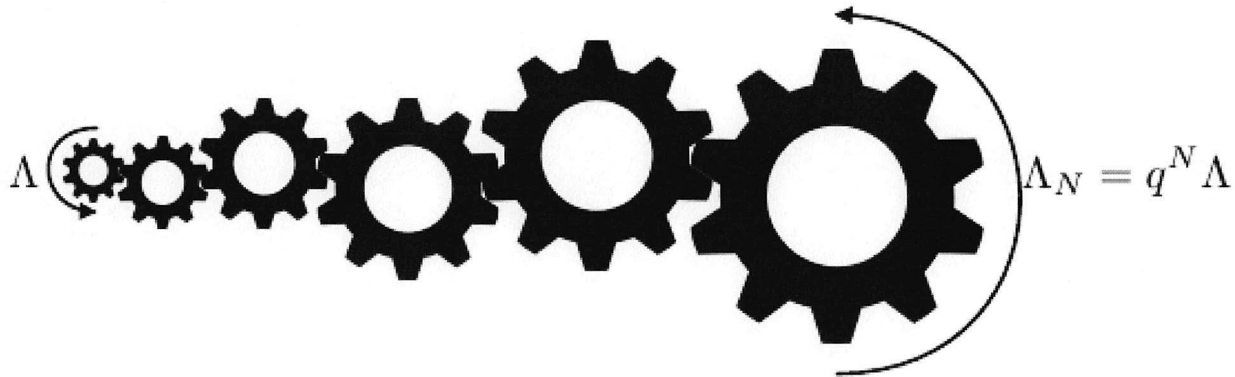
The two-axion alignment as a clockwork with two gears, e.g. "minutes" and "hours"



# The Multi-Axion Clockwork

Alignment with N axions

(Picture from Giudice and McCullough, 2016)



# Intermediate Summary

Sizeable tensor modes are possible,

- but there is most probably an upper limit on  $f_{\text{eff}}$  and  $r$ ,
- we might have "wiggles" and running indices

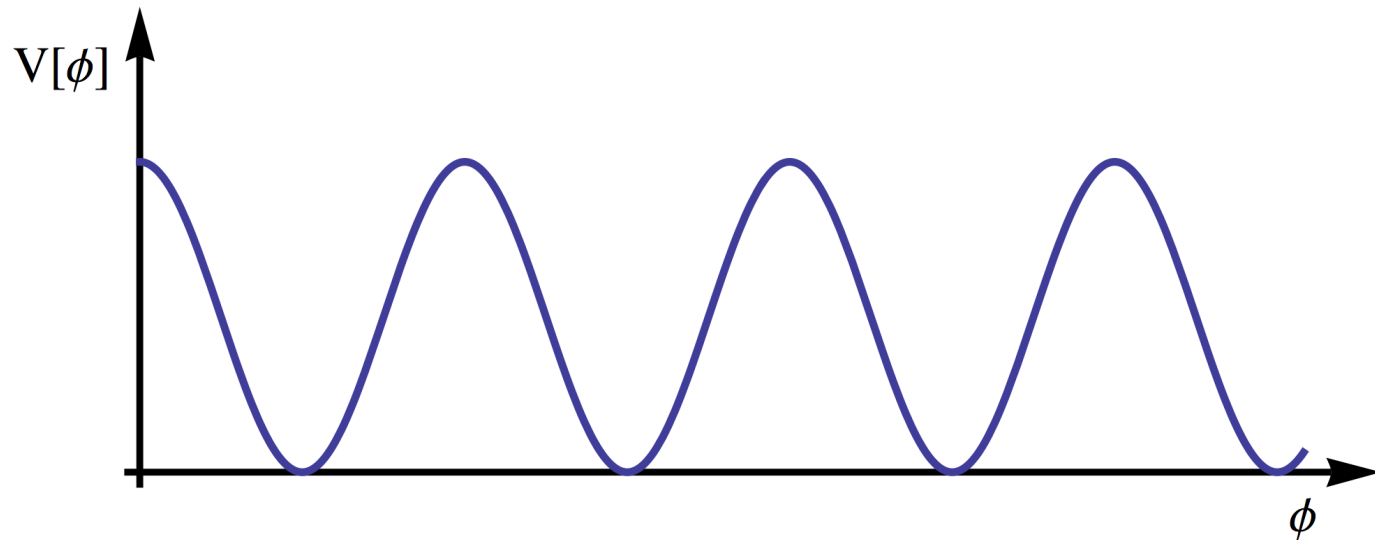
We are in a region where we lose computational control.

- the UV-completion requires higher harmonics
- the "cosine" is no longer just a "cosine"
- multi-axion "clockwork systems" might extend the axionic field range (Choi, Kim, Yun, 2014)

We need experimental observations to clarify the situation and teach us new lessons about gravity.

# QCD axion and axionic domain walls

In general we have  $a = a + 2\pi N f_a$  for  $V \sim \cos(Na/f_a)$ ,



leading to  $N$  nontrivial degenerate vacua separated by maxima of the potential.

During the cosmic evolution this might lead to the production of potentially harmful axionic domain walls.

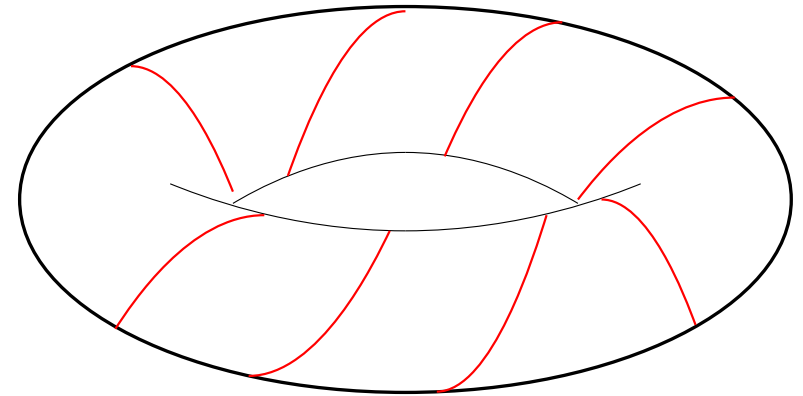
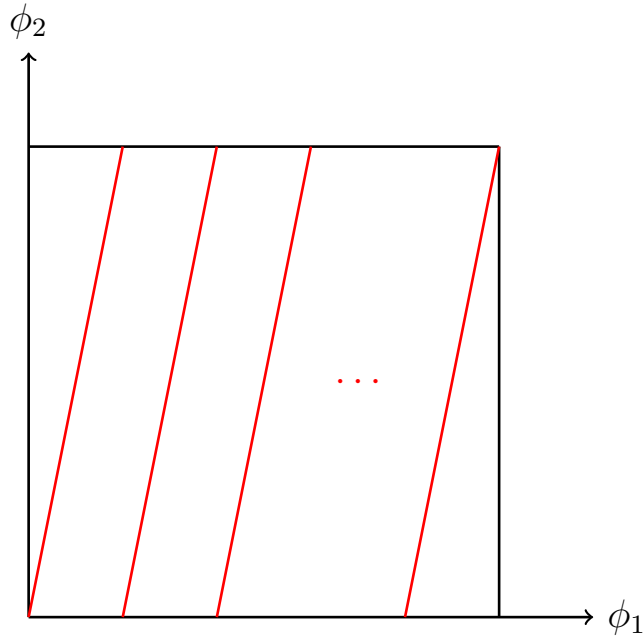
# Multi-Axion-models

Consider a system with two (or more) axions

$$V \sim \Lambda_1^4 \cos \left( \frac{a_1}{f_1} + N \frac{a_2}{f_2} \right) + m \Lambda_2^3 \cos \left( \frac{a_2}{f_2} \right)$$

- For fixed  $a_1$  there are  $N$  nontrivial vacua and potentially  $N_{\text{DW}} = N$  domain walls
- for  $m = 0$  there is a Goldstone direction, **and thus a continuous unique vacuum with  $N_{\text{DW}} = 1$**  (Choi, Kim, 1985)
- aligned axion "clockwork" can enlarge the axion scale from TeV to  $10^{11}$  GeV (Higaki, Jeong, Kitjima, Takahashi, 2015)
- enhancing axion-photon-photon coupling via clockwork (Farina, Pappadopulo, Rompineve, Tesi, 2016)

# The axionic vacuum



(Choi, Kim, Yun, 2014)

- There is continuous unique vacuum with effective domain wall number is  $N_{\text{DW}} = 1$  (Choi, Kim, 1985)
- the Goldstone mode develops an axionic potential in the case  $m \neq 0$

# Quintessential axion alignment

Axions could be the source for dynamical dark energy

- in contrast to scalar quintessence, the axion has only derivative couplings and does not lead to a “fifth force”
- we need a slow roll field with  $\Lambda \sim 0.003 \text{ eV}$
- to act as dark energy today we need  $f_a \geq M_{\text{Planck}}$
- the quintaxion mass is  $m_a \sim \Lambda^2 / M_{\text{Planck}} \sim 10^{-33} \text{ eV}$

Again we need a trans-Planckian decay constant for a consistent description of the present stage of the universe

- the problem can be solved via aligned axions à la KNP

(Kaloper, Sorbo, 2006)

# The relaxion mechanism

Axions could be at the origin of mass hierarchies. This requires

(Graham, Kaplan, Rajendran, 2015)

- a slowly rolling (relaxion) field,
- stopped by nonperturbative effects.
- Large mass hierarchies need a long time evolution of the relaxion field
- and an unconventional cosmological evolution.

Again we need a huge relaxion decay constant for a consistent description of the present stage of the universe:

- the problem can be solved via aligned axions à la KNP (sometimes called clock-work axion).

(Choi, Im, 2015; Kaplan, Rattazzi, 2015)

# Tensor Modes from Extra Dimensions

Extra space dimensions might provide new ingredients:

- strength of gravity could vary in bulk
- weak scale hierarchy problem might be solved via large or warped extra dimensions

This could influence the size of tensor modes. We consider

- large extra dimensions (LED) (Arkani-H., Dimopoulos, Dvali, 1998)
- warped extra dimensions (RS) (Randall, Sundrum, 1999)
- linear dilaton model (LD) (Antoniadis, Dimopoulos, Giveon, 2001)

Matter fields live on visible brane, gravity on hidden brane.  
The inflaton can reside on either of them. (Im, Nilles, Trautner, 2017)



# The mechanism

We start with a warm-up example

- one large extra dimension (LED)
- inflaton field on visible (IR) brane
- we assume that the mechanism of radius stabilisation does not influence the tensor modes

This simplification is called IRB assumption

- scalar modes are essentially  $d=4$  dimensional  
(Giudice, Kolb, Lesgourgues, Riotto, 2002)
- tensor modes are influenced by bulk effects
- **relevance of effective Planck mass during inflation**

# Effective Planck Mass

Effective Planck mass during inflation

$$M_{\text{Pl,eff}}^2 = M^3 2 \pi R \left(1 - \frac{2}{3} \pi^2 R^2 H^2\right)$$

has to be compared to

$$M_{\text{Pl,eff}}^2 \Big|_{H=0}^{\text{LED}} = M^3 2 \pi R .$$

This leads to enhanced tensor modes and

$$\frac{2}{3} \pi^2 R^2 H^2 < 1$$

implies an upper limit on Hubble scale during inflation.

(Im, Nilles, Trautner, 2017)

# Results

## Results are model dependent

(Im, Nilles, Trautner, 2017)

- we obtain **enhanced tensor modes** in LED and RS within IRB-scenario
- surprisingly the IRB assumption is not applicable to the Linear Dilaton (LD) case
- a satisfactory picture requires contributions from the hidden brane ("**remote inflation**")
- "**remote inflation**" is an option in the RS scenario as well
- LD case with dilaton as stabilizer field is consistent with IRB assumption and leads to **reduced tensor modes**

(Nihei, 1999; Kaloper, 1999; Kim, Kim, 1999)

(Kehagias, Riotto, 2016)

# Summary

Sizeable tensor modes are a challenge for model building

- especially for a consistent UV-completion
- restrictions from string theory via dualities
- effective theories (like aligned axions) as one way out
  - extend upper limit on  $f_{\text{eff}}$  via "clockwork"
  - specific signatures of "modulated natural inflation"
- extra dimensions as another way out
  - enhanced tensor modes imply upper limit on  $H$
  - remote inflation as a new option
  - implication of reduced tensor modes?

Sizeable tensor modes: a window of opportunity