

Axions, Majorana Neutrino Masses and implications for the dark sector of the Universe

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and Beyond
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European Institute for Sciences and Their Applications



OUTLINE

- **PART I: Mechanism (beyond seesaw) for right-handed neutrino mass generation through Axion-Right-handed Neutrino Interactions**

NEM & Pilaftsis
Phys.Rev. D86
(2012) 124038

- **PART II – Astrophysical Implications: Λ CDM fits very well**
Astrophysical Data for **Universe** at **Large scales**
- **BUT: @ GALACTIC SCALES, DWARF GALAXIES) – DISCREPANCY between Λ CDM-based simulations and observations – “small scale Cosmology crisis” – problems** (i) Core-cusp problem, (ii) The missing satellites problem
(iii) Too-Big-to-fail problem
- **Self-Interacting Dark matter (SIDM)** as a solution (on top of astrophysical ones) ?
- **PART III: Right-Handed (50 keV mass) neutrinos with massive vector self-interactions as a concrete SIDM model & consequences for galactic structure**

Arguelles, NEM, Rueda, Ruffini
JCAP 1604 (2016) no.04, 038

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Anomalies, Kalb-Ramond Axions and Gravity
Basic String-Inspired Effective Field theory

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Will argue that:

(i) resolution of **Galactic core-halo structure** problems of Λ CDM simulations vs observations + core-cusp and other problems of small-scale cosmology

“crisis” can be provided by **self-interacting Right-handed (Majorana) neutrinos with masses, m , at least 47 keV**

(ii) From a particle physics perspective of ν MSM, **with Higgs portal communication to standard model sector**, **cosmological constraints imply masses of lightest of RH neutrinos, m , at most 50 keV**

So combination of these (diverse) constraints imply narrow window

$$47 \text{ keV } c^{-2} \leq m \leq 50 \text{ keV } c^{-2}$$



PART III: Right-Handed (50 keV mass) neutrinos with massive vector self-interactions as a concrete SIDM model & consequences for galactic structure

PART I

Right-Handed Neutrino
Majorana Mass generation
(beyond seesaw)
& the role of Axions...

ANOMALOUS GENERATION
OF RIGHT-HANDED MAJORANA
NEUTRINO MASSES THROUGH
TORSIONFUL QUANTUM GRAVITY
UV complete string models ?

NEM & Pilaftsis 2012
PRD 86, 124038
arXiv:1209.6387



String Theories with Antisymmetric Tensor Backgrounds

Massless Gravitational multiplet of (closed) strings: **spin 0 scalar (dilaton)**
spin 2 traceless symmetric rank 2 tensor (graviton)
spin 1 antisymmetric rank 2 tensor

KALB-RAMOND FIELD $B_{\mu\nu} = -B_{\nu\mu}$

Effective field theories (low energy scale $E \ll M_s$) "gauge" invariant

$$B_{\mu\nu} \rightarrow B_{\mu\nu} + \partial_{[\mu}\theta(x)_{\nu]}$$

Depend only on field strength : $H_{\mu\nu\rho} = \partial_{[\mu}B_{\nu\rho]}$

Bianchi identity :

$$\partial_{[\sigma}H_{\mu\nu\rho]} = 0 \rightarrow d \star \mathbf{H} = 0$$

ROLE OF H-FIELD AS TORSION

EFFECTIVE GRAVITATIONAL ACTION IN STRING LOW-ENERGY LIMIT

4-DIM
PART

$$\begin{aligned} S^{(4)} &= \int d^4x \sqrt{-g} \left(\frac{1}{2\kappa^2} R - \frac{1}{6} H_{\mu\nu\rho} H^{\mu\nu\rho} \right) \\ &= \int d^4x \sqrt{-g} \left(\frac{1}{2\kappa^2} \bar{R} \right) \end{aligned}$$

$$\bar{\Gamma}_{\nu\rho}^{\mu} = \Gamma_{\nu\rho}^{\mu} + \frac{\kappa}{\sqrt{3}} H_{\nu\rho}^{\mu} \neq \bar{\Gamma}_{\rho\nu}^{\mu}$$

Contorsion

ROLE OF H-FIELD AS TORSION – AXION FIELD

EFFECTIVE GRAVITATIONAL ACTION IN STRING LOW-ENERGY LIMIT

$$\sim \frac{1}{2} \partial^\mu b \partial_\mu b$$

4-DIM
PART

$$S^{(4)} = \int d^4x \sqrt{-g} \left(\frac{1}{2\kappa^2} R - \frac{1}{6} H_{\mu\nu\rho} H^{\mu\nu\rho} \right)$$

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$$\bar{\Gamma}_{\nu\rho}^\mu = \Gamma_{\nu\rho}^\mu + \frac{\kappa}{\sqrt{3}} H_{\nu\rho}^\mu \neq \bar{\Gamma}_{\rho\nu}^\mu$$

IN 4-DIM DEFINE DUAL OF H AS :

$$-3 \sqrt{2} \partial_\sigma b = \sqrt{-g} \epsilon_{\mu\nu\rho\sigma} H^{\mu\nu\rho}$$

$b(x)$ = Pseudoscalar
(Kalb-Ramond (KR) axion)

FERMIONS COUPLE TO H-TORSION VIA GRAVITATIONAL COVARIANT DERIVATIVE

$$S_\psi = \frac{i}{2} \int d^4x \sqrt{-g} \left(\bar{\psi} \gamma^\mu \bar{\mathcal{D}}_\mu \psi - (\bar{\mathcal{D}}_\mu \bar{\psi}) \gamma^\mu \psi \right)$$

TORSIONFUL CONNECTION, FIRST-ORDER FORMALISM

$$\bar{\mathcal{D}}_a = \partial_a - \frac{i}{4} \bar{\omega}_{bca} \sigma^{bc}$$

$$\bar{\omega}_{ab\mu} = \omega_{ab\mu} + K_{ab\mu}$$

contorsion

$$K_{abc} = \frac{1}{2} \left(T_{cab} - T_{abc} - T_{bca} \right)$$

$$H_{cab}$$

Non-trivial contributions to B^μ

$$B^d = \epsilon^{abcd} e_{b\lambda} \left(\partial_a e_c^\lambda + \Gamma_{\alpha\mu}^\lambda e_c^\alpha e_a^\mu \right)$$

$$\bar{\Gamma}_{\nu\rho}^\mu = \Gamma_{\nu\rho}^\mu + \frac{\kappa}{\sqrt{3}} H_{\nu\rho}^\mu \neq \bar{\Gamma}_{\rho\nu}^\mu$$

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Fermionic Field Theories with H-Torsion

EFFECTIVE ACTION AFTER INTEGRATING OUT QUANTUM TORSION FLUCTUATIONS

Fermions: $S_\psi \ni -\frac{3}{4} \int d^4 \sqrt{-g} S_\mu \bar{\psi} \gamma^\mu \gamma^5 \psi = -\frac{3}{4} \int S \wedge *J^5$

+ standard Dirac terms without torsion

$$S = *T$$

$$S_d = \frac{1}{3!} \epsilon^{abcd} T_{abc}$$

$$T_{abc} \rightarrow H_{cab} = \epsilon_{cabd} \partial^d b$$

Bianchi identity

$$d *S = 0$$

classical

conserved
"torsion" charge

$$Q = \int *S$$

Postulate conservation at quantum level by adding counterterms

Implement $d *S = 0$ via $\delta(d *S)$ constraint
 \rightarrow Lagrange multiplier in Path integral \rightarrow b-field

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$$\begin{aligned}
& \int DS Db \exp \left[i \int \frac{3}{4\kappa^2} \mathbf{S} \wedge \star \mathbf{S} - \frac{3}{4} \mathbf{S} \wedge \star \mathbf{J}^5 + \left(\frac{3}{2\kappa^2} \right)^{1/2} b d\star \mathbf{S} \right] \\
&= \int Db \exp \left[-i \int \frac{1}{2} db \wedge \star db + \frac{1}{f_b} db \wedge \star \mathbf{J}^5 + \frac{1}{2f_b^2} \mathbf{J}^5 \wedge \star \mathbf{J}^5 \right]
\end{aligned}$$

multiplier field $\Phi(x) \equiv (3/\kappa^2)^{1/2} b(x)$.

$$f_b = (3\kappa^2/8)^{-1/2} = \frac{M_P}{\sqrt{3\pi}}$$

$$\begin{aligned}
& \int D\mathbf{S} D\mathbf{b} \exp \left[i \int \frac{3}{4\kappa^2} \mathbf{S} \wedge \star \mathbf{S} - \frac{3}{4} \mathbf{S} \wedge \star \mathbf{J}^5 + \left(\frac{3}{2\kappa^2} \right)^{1/2} b d\star \mathbf{S} \right] \\
&= \int D\mathbf{b} \exp \left[-i \int \frac{1}{2} d\mathbf{b} \wedge \star d\mathbf{b} + \frac{1}{f_b} d\mathbf{b} \wedge \star \mathbf{J}^5 + \frac{1}{2f_b^2} \mathbf{J}^5 \wedge \star \mathbf{J}^5 \right]
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partial integrate

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partial integrate

Use chiral anomaly equation (one-loop) in curved space-time:

$$\nabla_\mu J^{5\mu} = \frac{e^2}{8\pi^2} F^{\mu\nu} \tilde{F}_{\mu\nu} - \frac{1}{192\pi^2} R^{\mu\nu\rho\sigma} \tilde{R}_{\mu\nu\rho\sigma}$$

$$\equiv G(\mathbf{A}, \omega).$$

Hence, effective action of torsion-full QED

$$\int Db \exp \left[-i \int \frac{1}{2} db \wedge \star db - \frac{1}{f_b} b G(\mathbf{A}, \omega) + \frac{1}{2f_b^2} \mathbf{J}^5 \wedge \star \mathbf{J}^5 \right]$$

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$$bR\tilde{R} - bF\tilde{F}$$

coupling

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Fermionic Field Theories with H-Torsion
EFFECTIVE ACTION AFTER INTEGRATING OUT
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$$\mathcal{S} = \int d^4x \sqrt{-g} \left[\frac{1}{2} (\partial_\mu b)^2 + \frac{b(x)}{192\pi^2 f_b} R^{\mu\nu\rho\sigma} \tilde{R}_{\mu\nu\rho\sigma} \right. \\ \left. + \frac{1}{2f_b^2} J_\mu^5 J^{5\mu} \right] +$$

+ Standard Model terms for fermions

SHIFT SYMMETRY $b(x) \rightarrow b(x) + c$

$c R^{\mu\nu\rho\sigma} \tilde{R}_{\mu\nu\rho\sigma}$ and $c F^{\mu\nu} \tilde{F}_{\mu\nu}$ total derivatives

ANOMALOUS MAJORANA NEUTRINO MASS TERMS from QUANTUM TORSION

OUR SCENARIO *Break* such *shift symmetry* by coupling first $b(x)$ to another pseudoscalar field such as QCD axion $a(x)$ (or e.g. other string axions)

$$\mathcal{S} = \int d^4x \sqrt{-g} \left[\frac{1}{2} (\partial_\mu b)^2 + \frac{b(x)}{192\pi^2 f_b} R^{\mu\nu\rho\sigma} \tilde{R}_{\mu\nu\rho\sigma} \right. \\ \left. + \frac{1}{2f_b^2} J_\mu^5 J^{5\mu} + \gamma (\partial_\mu b) (\partial^\mu a) + \frac{1}{2} (\partial_\mu a)^2 \right. \\ \left. - y_a i a \left(\bar{\psi}_R^C \psi_R - \bar{\psi}_R \psi_R^C \right) \right],$$

ANOMALOUS MAJORANA NEUTRINO MASS TERMS from QUANTUM TORSION

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Yukawa

right-handed neutrino fields

Field redefinition

$$b(x) \rightarrow b'(x) \equiv b(x) + \gamma a(x)$$

so, effective action becomes

$$\begin{aligned} \mathcal{S} = \int d^4x \sqrt{-g} & \left[\frac{1}{2} (\partial_\mu b')^2 + \frac{1}{2} (1 - \gamma^2) (\partial_\mu a)^2 \right. \\ & + \frac{1}{2f_b^2} J_\mu^5 J^{5\mu} + \frac{b'(x) - \gamma a(x)}{192\pi^2 f_b} R^{\mu\nu\rho\sigma} \tilde{R}_{\mu\nu\rho\sigma} \\ & \left. - y_a i a \left(\bar{\psi}_R^C \psi_R - \bar{\psi}_R \psi_R^C \right) \right]. \end{aligned} \quad ($$

must have

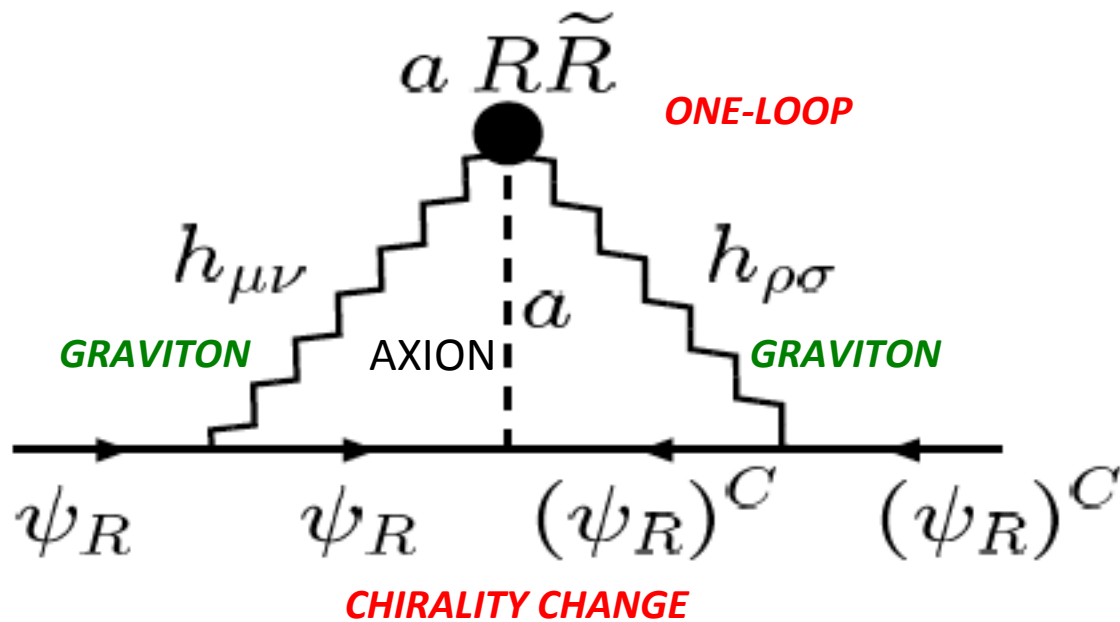
$$|\gamma| < 1$$

otherwise axion field $a(x)$ appears as a ghost \rightarrow canonically normalised kinetic terms

$$\begin{aligned} \mathcal{S}_a = \int d^4x \sqrt{-g} & \left[\frac{1}{2} (\partial_\mu a)^2 - \frac{\gamma a(x)}{192\pi^2 f_b \sqrt{1 - \gamma^2}} R^{\mu\nu\rho\sigma} \tilde{R}_{\mu\nu\rho\sigma} \right. \\ & \left. - \frac{i y_a}{\sqrt{1 - \gamma^2}} a \left(\bar{\psi}_R^C \psi_R - \bar{\psi}_R \psi_R^C \right) + \frac{1}{2f_b^2} J_\mu^5 J^{5\mu} \right]. \end{aligned}$$

CHIRALITY CHANGE

THREE-LOOP ANOMALOUS FERMION MASS TERMS



$\Lambda = \text{UV cutoff}$

$$M_R \sim \frac{1}{(16\pi^2)^2} \frac{y_a \gamma \kappa^4 \Lambda^6}{192\pi^2 f_b (1 - \gamma^2)} = \frac{\sqrt{3} y_a \gamma \kappa^5 \Lambda^6}{49152\sqrt{8} \pi^4 (1 - \gamma^2)}$$

SOME NUMBERS

$$\Lambda = 10^{17} \text{ GeV}$$

$$\gamma = 0.1$$

M_R is at the TeV

for $y_a = 10^{-3}$

$$\Lambda = 10^{16} \text{ GeV}$$

$M_R \sim 16 \text{ keV}$,

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**INTERESTING
WARM DARK MATTER
REGIME**

Appropriate Hierarchy for the other two massive Right-handed neutrinos for Leptogenesis-Baryogenesis & Dark matter constraints can be arranged by choosing Yukawa couplings

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$M_R \sim 16 \text{ keV}$,

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May be (discrete) **symmetry** reasons
(*cf* **Leontaris-Vlachos approach**)
force **two** of the heavier **RH neutrinos**
to be **degenerate** \rightarrow dictate patterns
for the axion-RH-neutrino
Yukawa couplings y_a

**INTERESTING
WARM DARK MATTER
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Appropriate Hierarchy for the other two massive
Right-handed neutrinos for Leptogenesis-Baryogenesis
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by choosing Yukawa couplings

FINITENESS OF THE MASS

Arvanitaki, Dimopoulos *et al.*

MULTI-AXION SCENARIOS (e.g. string axiverse)

$$\mathcal{S}_a^{\text{kin}} = \int d^4x \sqrt{-g} \left[\frac{1}{2} \sum_{i=1}^n \left((\partial_\mu a_i)^2 - M_i^2 \right) + \gamma (\partial_\mu b) (\partial^\mu a_1) - \frac{1}{2} \sum_{i=1}^{n-1} \delta M_{i,i+1}^2 a_i a_{i+1} \right];$$

$$\delta M_{i,i+1}^2 < M_i M_{i+1} \quad \text{positive mass spectrum for all axions}$$

simplifying all mixing equals

$$M_R \sim \frac{\sqrt{3} y_a \gamma \kappa^5 \Lambda^{6-2n} (\delta M_a^2)^n}{49152 \sqrt{8} \pi^4 (1 - \gamma^2)} \quad n \leq 3$$

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FINITENESS OF THE MASS

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M_R : UV finite for $n=3$ @ 2-loop independent of axion mass

FINITENESS OF THE MASS

MULTI-AXION SCENARIOS (e.g. string axiverse)

$$S_a^{\text{kin}} = \int d^4x \sqrt{-g} \left[\frac{1}{2} \sum_{a=1}^n (\partial_\mu a_a)^2 - \frac{1}{2} M^2 \right] + \gamma (\partial_\mu b) (\partial^\mu a_1)$$

Three RH neutrinos
Three axions
Three generations

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$$M_R \sim \frac{\sqrt{3} y_a \gamma \kappa^5 \Lambda^{6-2n} (\delta M_a^2)^n}{49152 \sqrt{8} \pi^4 (1 - \gamma^2)} \quad n \leq 3$$

$$M_R \sim \frac{\sqrt{3} y_a \gamma \kappa^5 (\delta M_a^2)^3}{49152 \sqrt{8} \pi^4 (1 - \gamma^2)} \frac{(\delta M_a^2)^{n-3}}{(M_a^2)^{n-3}} \quad n > 3$$

M_R : UV finite for $n=3$ @ 2-loop independent of axion mass

PART II

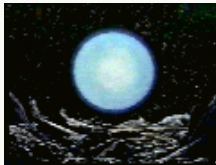
Implications for the Dark Sector-
Astro/Cosmological
Phenomenology

THE DARK SECTOR OF THE UNIVERSE

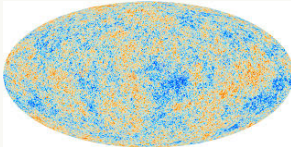
<http://www.cosmos.esa.int/web/planck/publications#Planck2015>

Observations from:

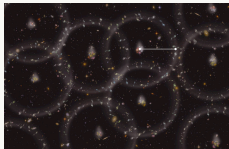
Supernovae Ia



CMB



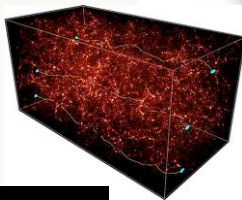
Baryon Acoustic Oscillations



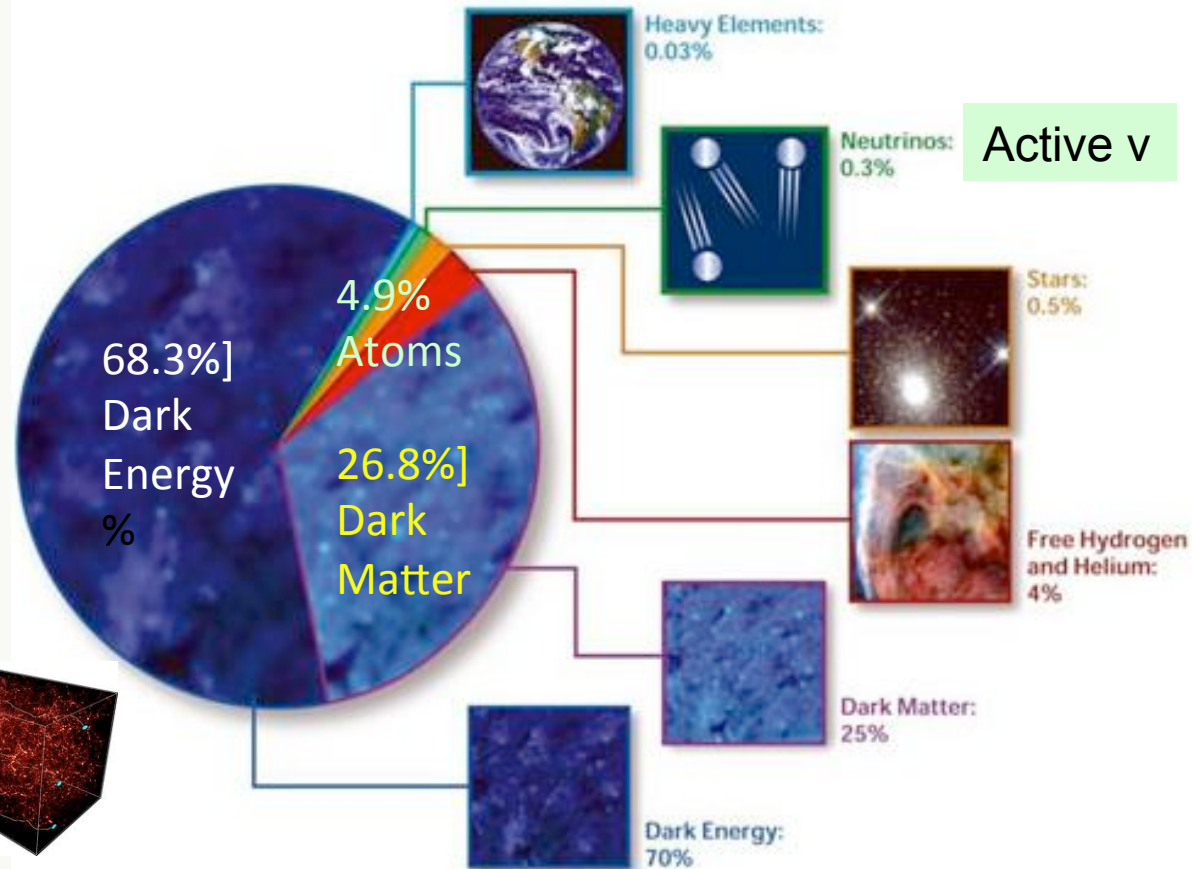
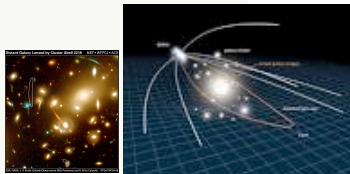
Galaxy Surveys



Structure Formation data



Strong & Weak lensing

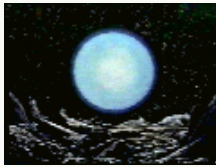


THE DARK SECTOR OF THE UNIVERSE

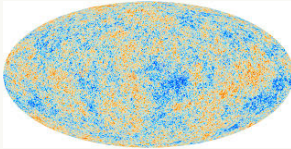
<http://www.cosmos.esa.int/web/planck/publications#Planck15>

Observations from:

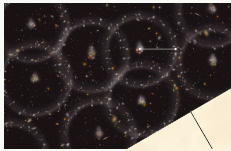
Supernovae Ia



CMB



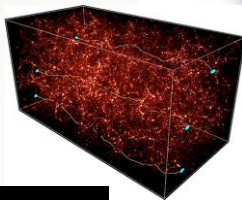
Baryon Acoustic Oscillations



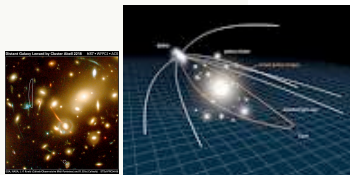
Galaxy Surveys



Structure formation data



Strong & Weak lensing



Λ CDM fits them all at Cosmological Distances





But....there are still open
issues with
the Λ CDM framework
@ small (galactic) scales

What are they?
and what do
sterile neutrinos have to do with them???

PART IIB

Small-scale Cosmology "crisis"

Collisionless Λ CDM - based N-body simulations

\neq

galactic scale observations
especially Dwarf Galaxy structure

The 3-Problems of Galactic-Scale-Cosmology (GSC)

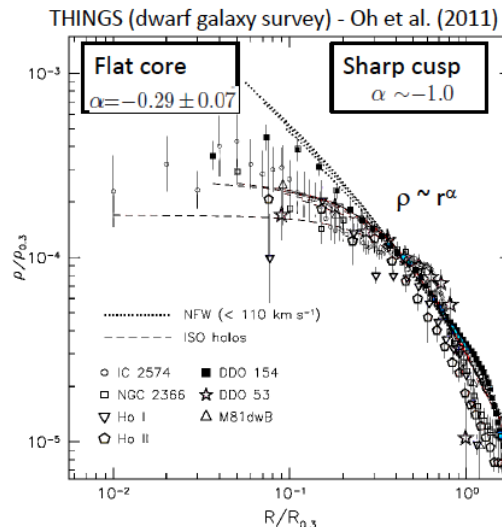
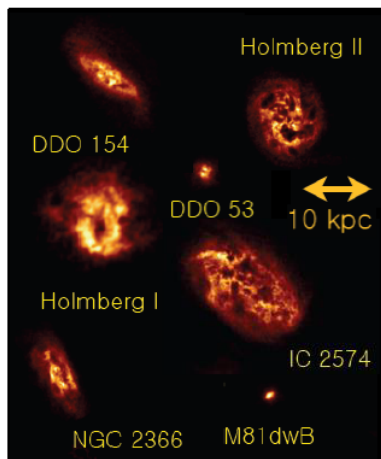
(i) The Core-Cusp problem (or cuspy-halo problem):

Nearly all **simulations** form dark matter halos which have *cuspy dark matter* distributions, with the density increasing steeply at small radii; on the contrary, *the rotation curves* of most of the observed *dwarf galaxies* indicate flat central density profiles ("*cores*").

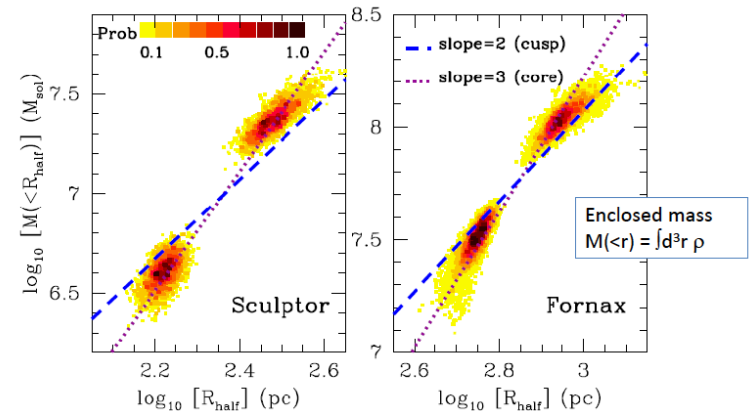
B. Moore (1994)
J.G. de Blok [arXiv:0910.3538]
Se-Heon Oh *et al.*,
Astrophys. J. 149 (6), 96 (2015).

1. Cores in dwarfs outside MW halo

Moore (1994), Flores & Primack (1994), ...



1. Cores in MW dwarf spheroidals



Stellar subpopulations (metal-rich & metal-poor) as "test masses" in gravitational potential

Walker & Penarrubia (2011)

The 3-Problems of Galactic-Scale-Cosmology (GSC)

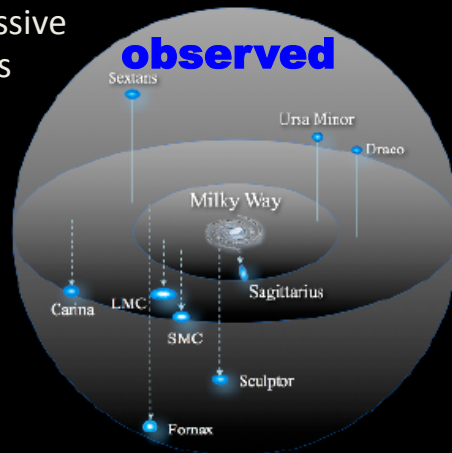
(ii) The missing satellite problem (or, dwarf galaxy problem)

Although there seem to be **enough observed normal-sized galaxies** to account for such a distribution, **the number of dwarf galaxies** is orders of magnitude **lower than** that expected from the **simulations**.

E.g. there were observed to be around 38 dwarf galaxies in the Local Group, and only around 11 orbiting the Milky Way, yet one **dark matter simulation** predicted around **500 Milky Way dwarf satellites**

simulated

Most massive subhaloes

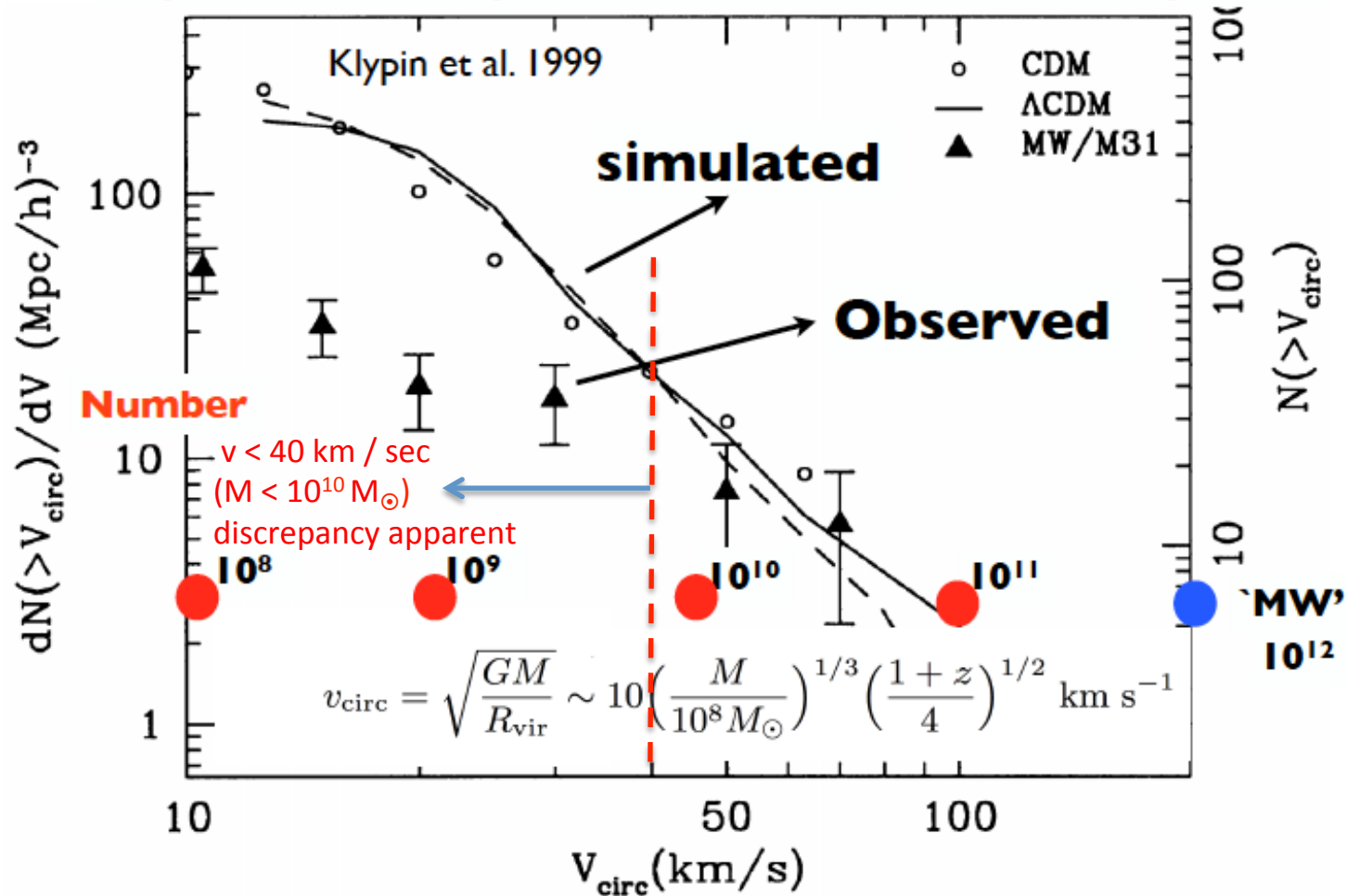


B. Moore *et al.*, *Astrophys. J.* 524 , L19 (1999)
A. Klypin, *et al.*, *Astrophys. J.* 522, 82 (1999)
E. Polisensky and M. Ricotti, PR D83, 043506 (2011)

(ii) The missing satellite (dwarves) problem

Missing Satellite Problem (MSP)

A quantitative comparison of # satellites at $r < 400$ kpc.



The 3-Problems of Galactic-Scale-Cosmology (GSC)

(iii) The Too-Big-to-Fail Problem

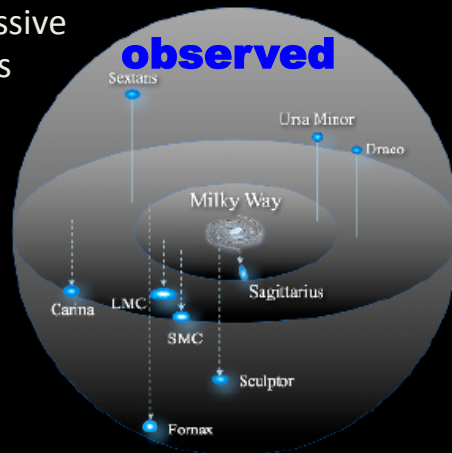
Λ CDM simulations predict that the most massive subhaloes of the Milky Way are too dense to host any of its brightest satellites, with luminosity higher than 10^5 the luminosity of the Sun.

(Models that are based on simulations predict much larger rotational velocities than the observed ones)

Rotational velocities \rightarrow measure of enclosed mass \rightarrow Λ CDM predicted **satellites are too massive** (too big).)

simulated

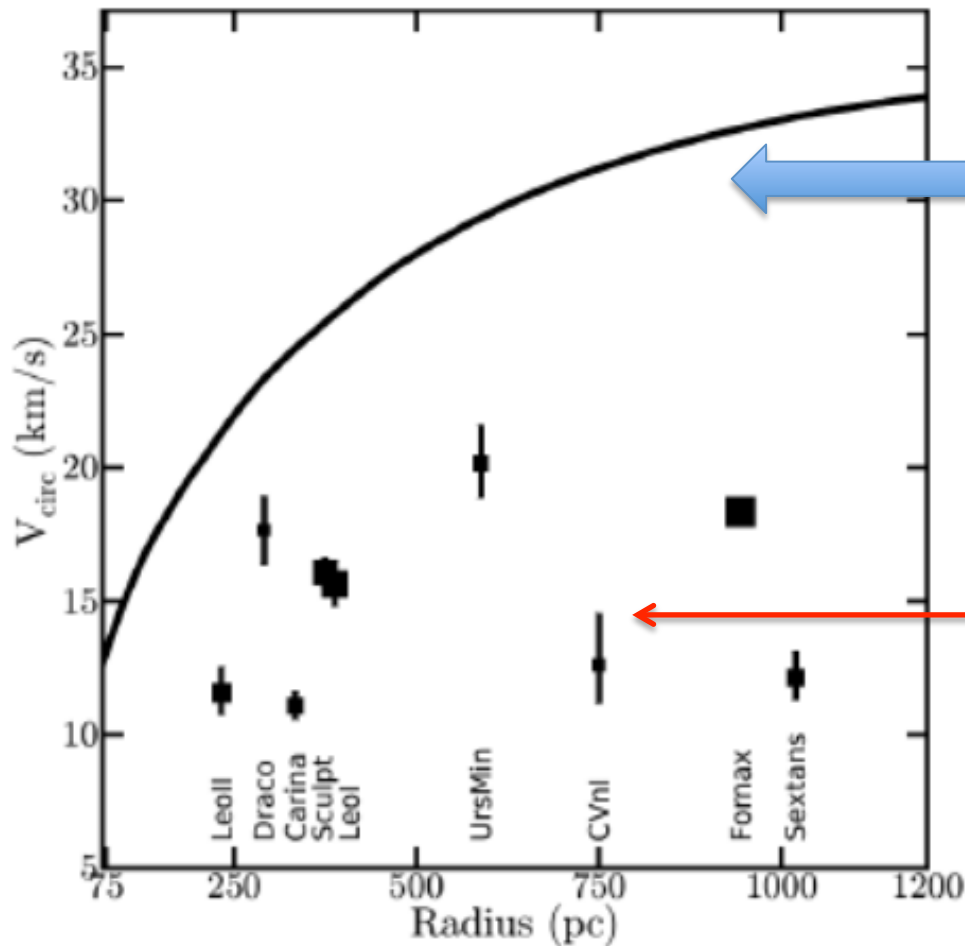
Most massive subhaloes



M. Boylan-Kolchin, J.S. Bullock & M. Kaplinghat,
MNRAS 415, L11 (2011);
ibid. 422, 1203 (2012)

Central density of most massive subhaloes (left) **too high** to host dwarf galaxies of MW (right)

(iii) The too-big-to-fail Problem



Continuous curve: **rotation curve** of typical largest sub-halo of the Milky Way as **simulated by collisionless Λ CDM**

Data points pertain to **observed circular velocities** of the largest subhaloes of the Milky Way at their half-light radii

$$v_{\text{rot}}^2(r) = r \left| \frac{\partial \Phi(r)}{\partial r} \right| = \frac{GM(< r)}{r}$$

M. Boylan-Kolchin, J.S. Bullock & M. Kaplinghat, MNRAS 415, L11 (2011); *ibid.* 422, 1203 (2012)

Towards a Solution of the 3-Problems of Galactic-Scale-Cosmology (GSC)

Astrophysical explanations

The missing satellite problem:

(i) Smaller halos do exist but only a few of them end up becoming visible (have not been able to attract enough baryonic matter to create a visible dwarf) (cf **Keck observations (2007) of eight newly discovered ultrafaint Milky Way dwarf satellites** showed that six were almost exclusively composed of DM, around 99.9% (with a mass-to-light ratio of about 1000)) – Such ultra-faint dwarfs substantially alleviate the discrepancy, but there are still discrepancies by a factor of about four too few dwarves over a significant range of masses.

(ii) **Galaxy formation** in low-mass dark matter halos is **strongly suppressed after re-ionization** → simulated circular velocity function of CDM subhalos in approximate agreement with the observed circular velocity function of Milky Way satellite galaxies.

(iii) **Dwarves** tend to **be merged into or tidally stripped apart by larger galaxies** due to complex interactions. This tidal stripping has been part of the problem in identifying dwarf galaxies in first place, which is difficult due to their low surface brightness and high diffusion so that they **are virtually unnoticeable**.

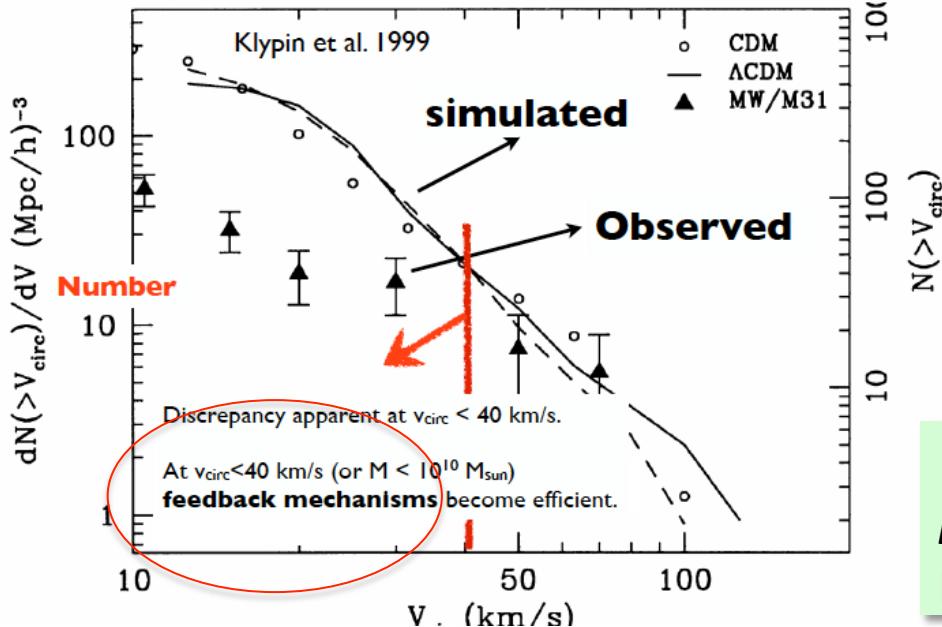
Towards a Solution of the 3-Problems of Galactic-Scale-Cosmology (GSC)

Astrophysical explanations

(iv) (Baryonic) Feedback plays an important role: complex processes by means of which star formation and matter accretion onto black holes deposit energy in the surrounding environments of galaxies

Missing Satellite Problem (MSP)

A quantitative comparison of # satellites at $r < 400$ kpc.



Various types of feedback:

Radiative: photoionization, radiation pressure (*stellar*, or from accretion disk of a supermassive BH (**AGN**))

Mechanical: supernovae explosions, cosmic ray exerted pressure

Possible to explain **Missing satellite problem** with **Baryonic (not well understood) physics feedback**

Towards a Solution of the 3-Problems of Galactic-Scale-Cosmology (GSC)

Microscopic Physics explanations needed?

All of the above problems seem that **cannot be entirely solved** by **conventional Astrophysics** explanations

- **discrepancies still remain moreover: case by case studies**

Towards a Solution of the 3-Problems of Galactic-Scale-Cosmology (GSC)

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CHANGE THE Λ CDM \rightarrow



Towards a Solution of the 3-Problems of Galactic-Scale-Cosmology (GSC)

Microscopic Physics explanations

All of the above problems seem that **cannot be entirely solved** by **conventional Astrophysics** explanations

- **discrepancies still remain moreover: case by case studies**

CHANGE THE Λ CDM \rightarrow

(i) Exotic mechanisms of Early Universe imply suppressed density fluctuations at subgalactic scales (e.g. **models with broken scale invariance during inflation**, but **somewhat lacking clear microscopic motivation from particle physics**)

Kamionkowski, Liddle astro-ph/9911103; Yokohama, astro-ph/0009127;
Zentner, Bullock, astro-ph/0205216; Ashoorioon, Krause, hep-th/0607001;
Kobayashi, Takahashi, arXiv:1011.3988, ...

Towards a Solution of the 3-Problems of Galactic-Scale-Cosmology (GSC)

Microscopic Physics explanations

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- **discrepancies still remain moreover: case by case studies**

CHANGE THE Λ CDM \rightarrow

(ii) modify gravity models (no DM except neutrinos) **Milgrom, Bekenstein (TeVeS)**

$$f \left(\frac{|\vec{a}|}{a_0} \right) \vec{a} = -\vec{\nabla} \Phi_N$$

$$a_0 \approx 1.2 \times 10^{-10} \text{ m s}^{-2}$$

simplest models

$$f(x) = \frac{2x}{1 + (2 - \alpha)x + \sqrt{(1 - x)^2 + 4x}};$$

Modified Gravitational acceleration @ galactic scales

Towards a Solution of the 3-Problems of Galactic-Scale-Cosmology (GSC)

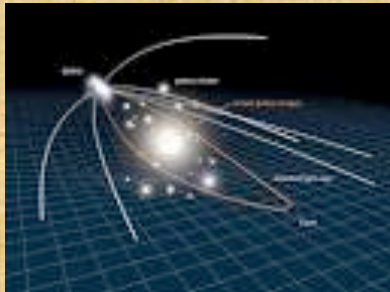
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CHANGE THE Λ CDM \rightarrow

(ii) ~~modify gravity models (no DM except neutrinos)~~
 ~~\rightarrow lensing problematic (bullet cluster or other merging galaxies, offer observational support for DM)~~ **for our talk**

(iii) **CHANGE** the DM properties \rightarrow **include self interactions**
or assume more than one dominant species
... with non-trivial role in galactic structure



Self-Interacting Dark Matter (SIDM) & small-scale Cosmology

Early pioneering works in implementing SIDM in N-body simulations

D. N. Spergel and P. J. Steinhardt, PRL 84 , 3760 (2000)

Figure of merit: (total) cross section per unit DM particle mass

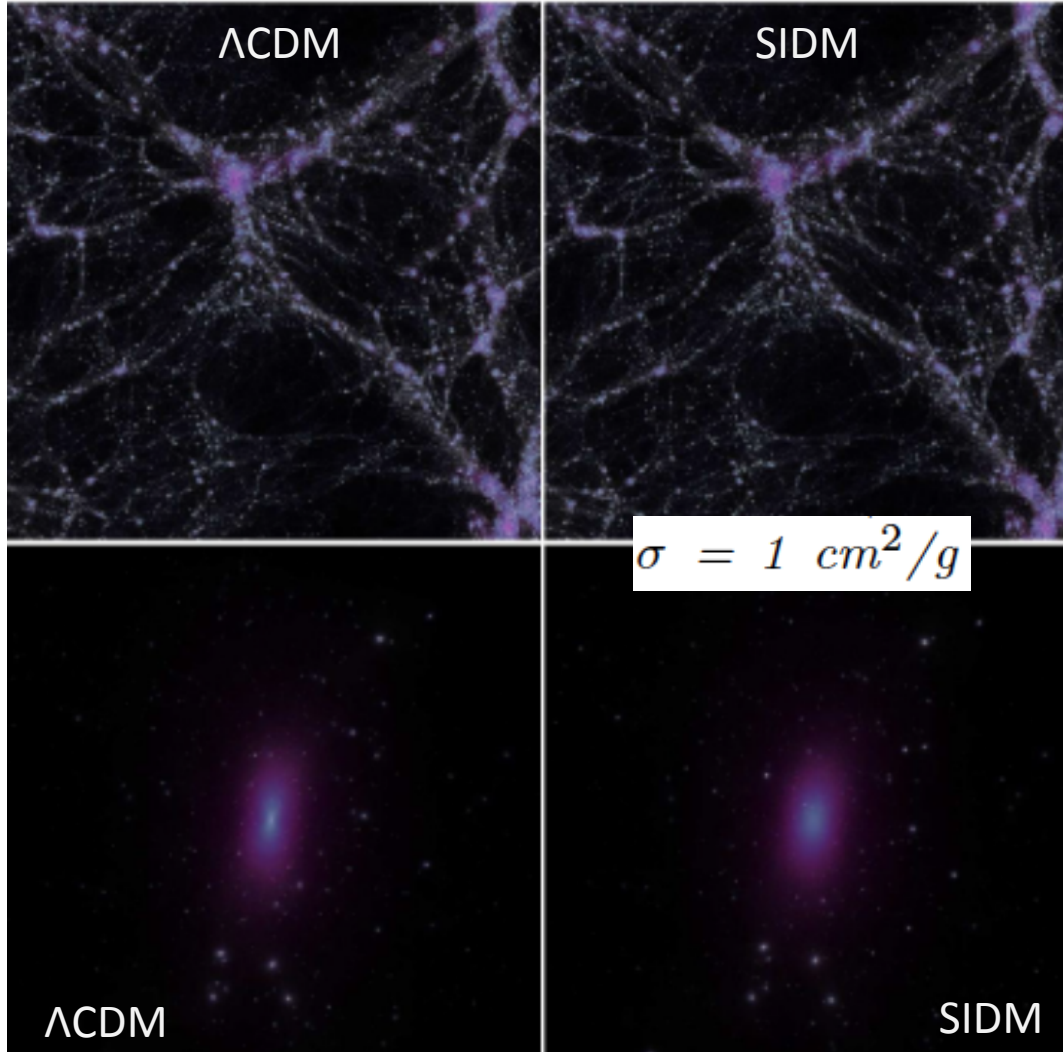
$$\sigma/m$$

Early days: $10 \text{ GeV } c^{-2} \geq m \geq 1 \text{ MeV } c^{-2}$
in DM haloes with densities $10^{-2} M_{\odot}/\text{pc}^3$

$$\sigma/m \sim 0.1 - 100 \text{ cm}^2/\text{g}$$

would imply observational effects in the inner haloes

Self-Interacting Dark Matter (SIDM) & small-scale Cosmology



**Large Scale Structure:
roughly the same**

**Individual galaxies:
more cored & spherical
in SIDM models**

Self-Interacting Dark Matter (SIDM) & small-scale Cosmology

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$$\sigma/m \sim 0.1 - 100 \text{ cm}^2/\text{g}$$

=1 barn/GeV
consistent with
all current
constraints of
GSC

would imply observational effects in the inner haloes

CONSTRAINTS ARE LIMITED

Solves cosmology's

"small scale crisis"

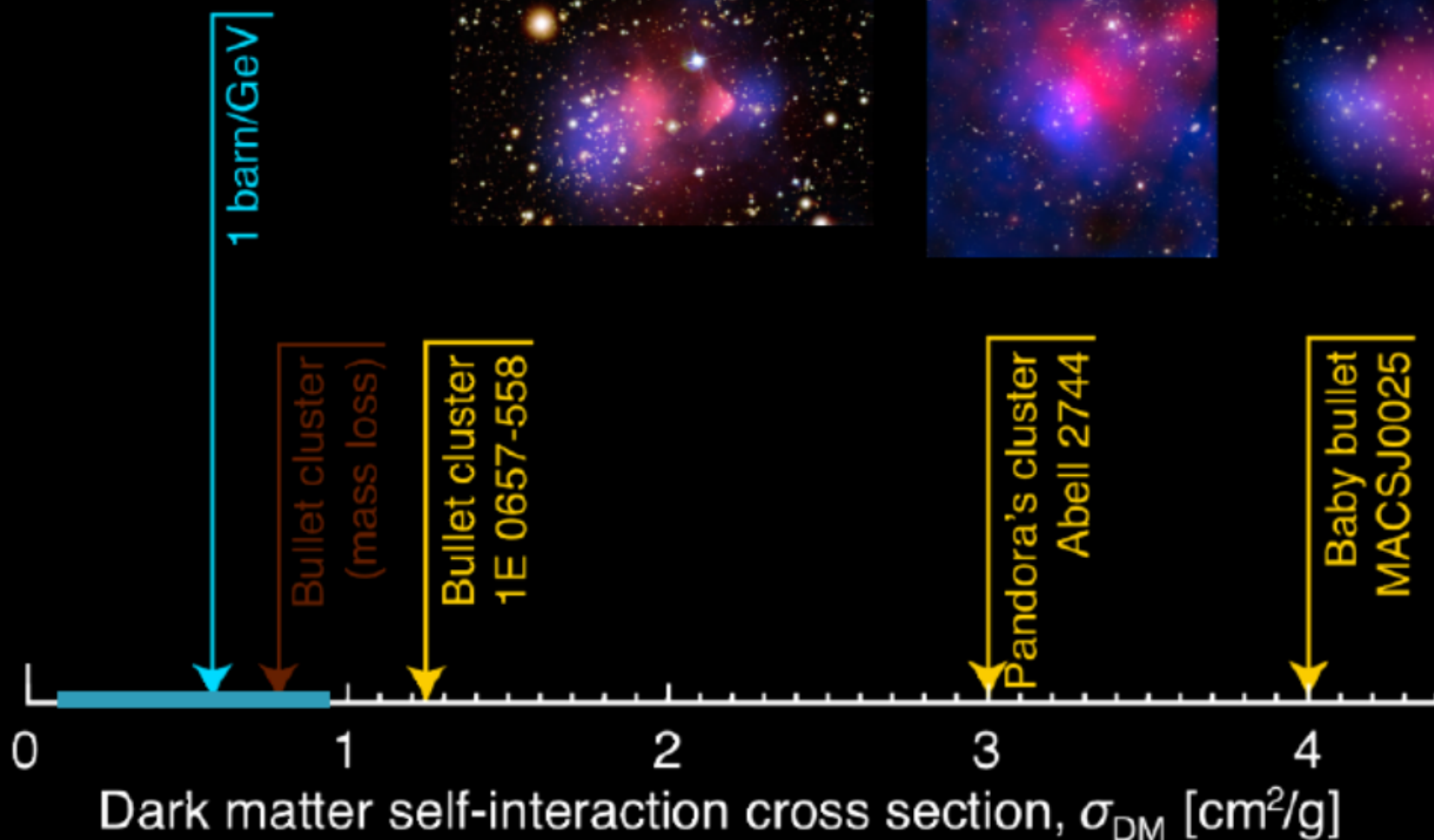
Clowe+ 2004



Mertens+ 2011



Bradac+ 2008



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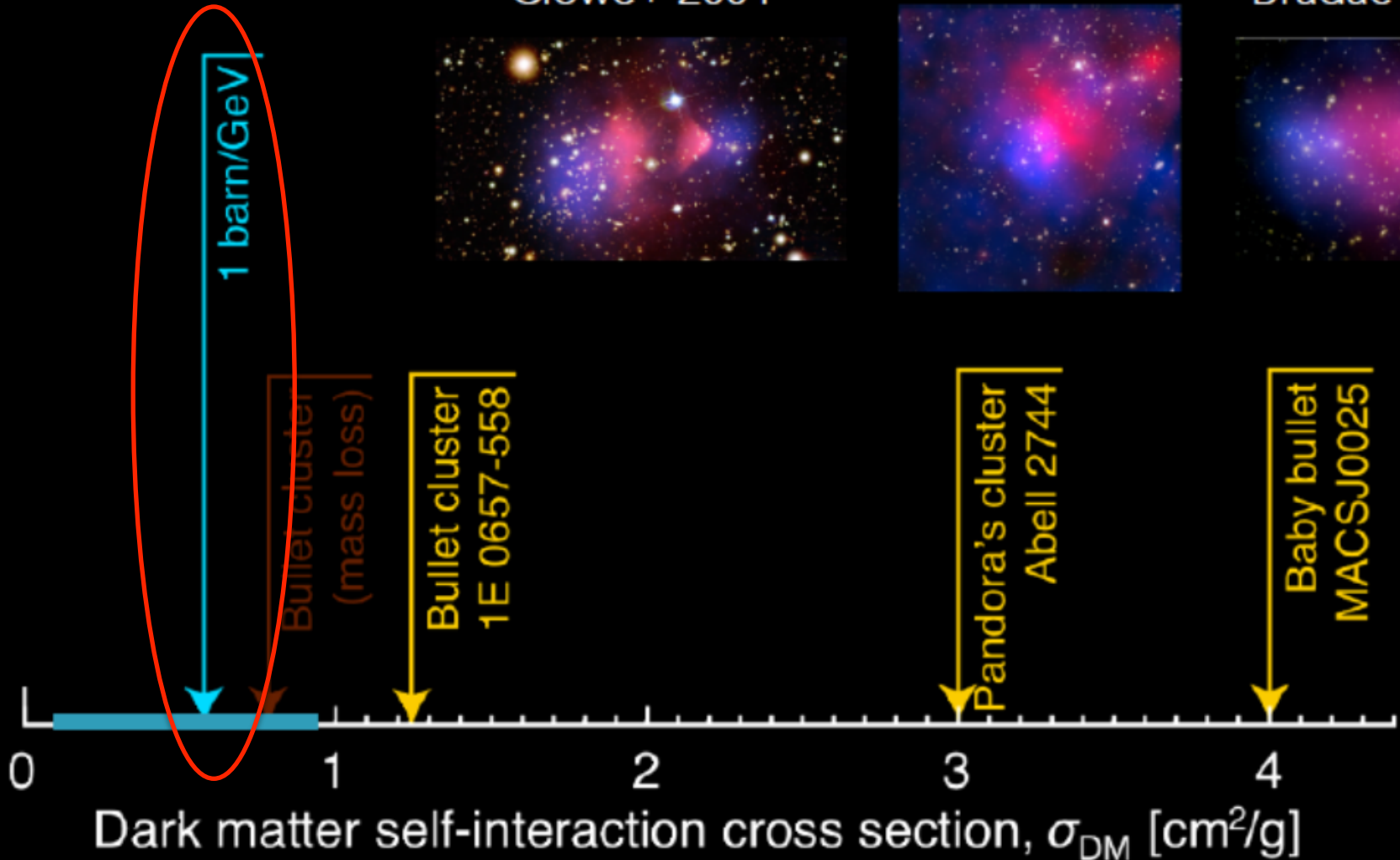
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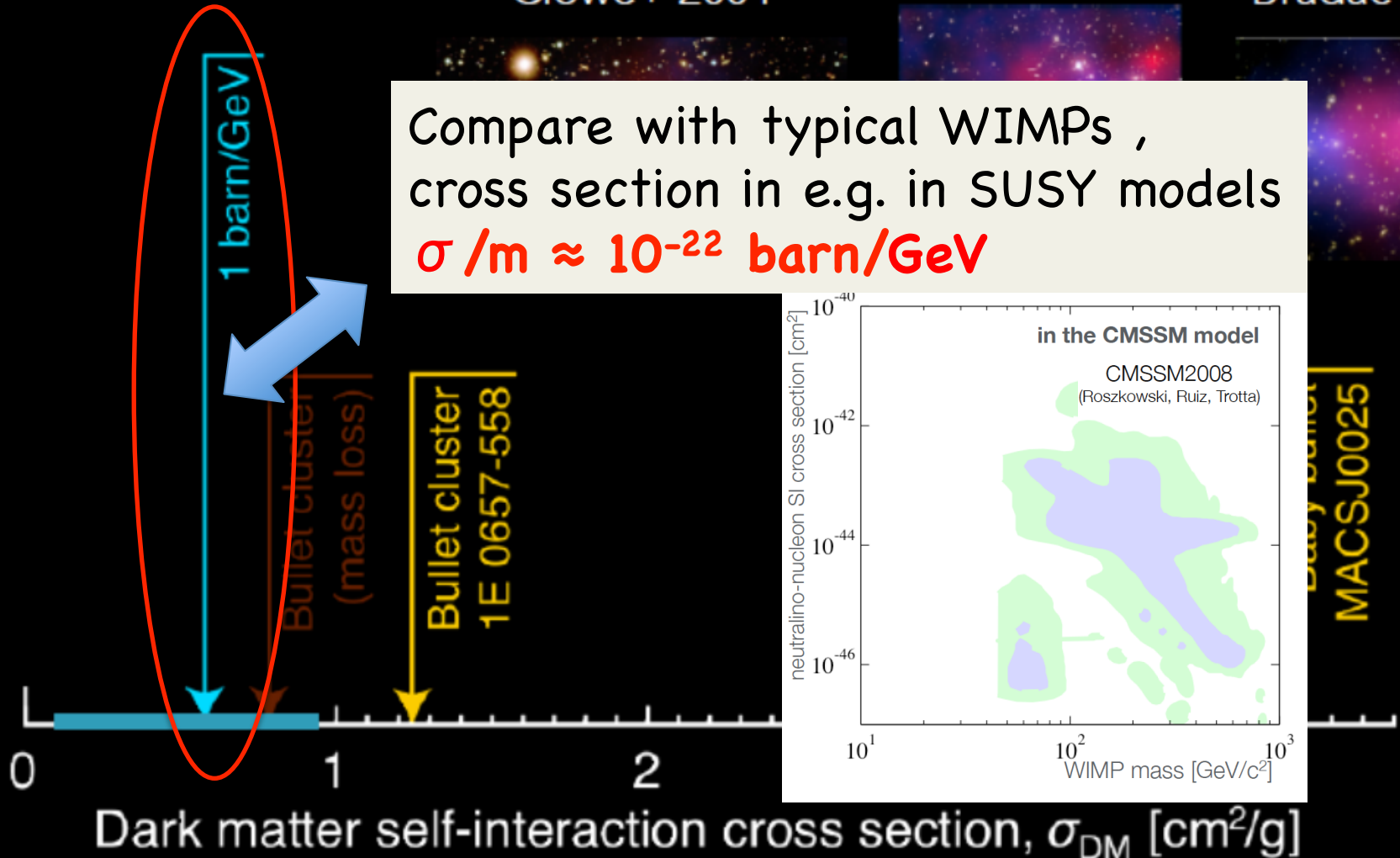
Clowe+ 2004

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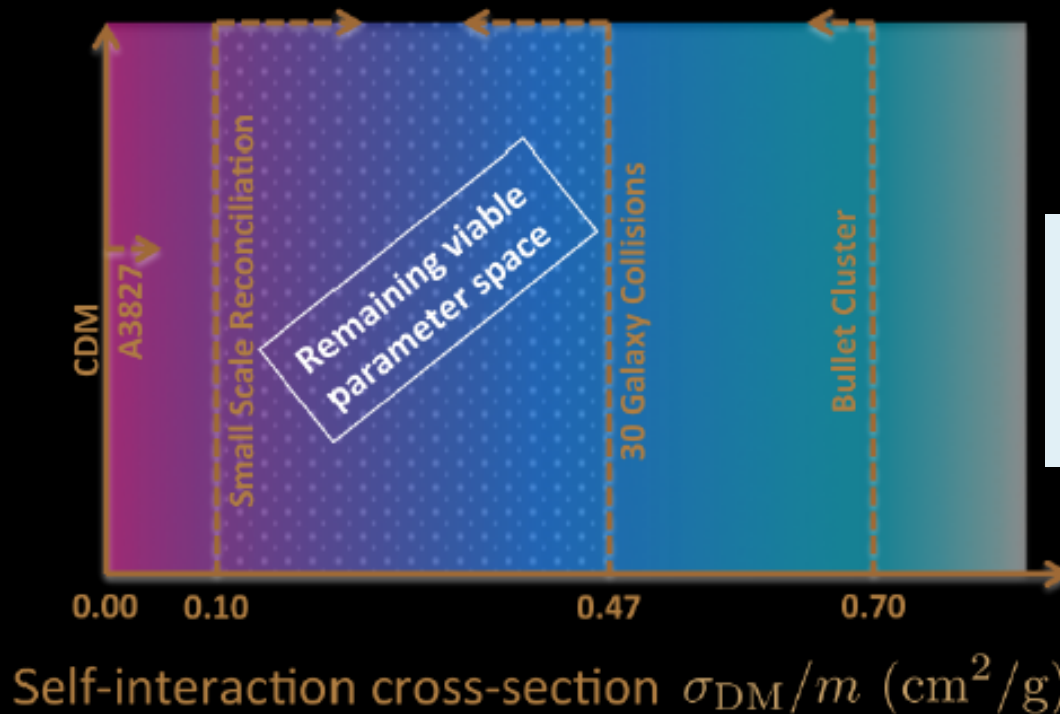
Compare with typical WIMPs ,
cross section in e.g. in SUSY models

$$\sigma / m \approx 10^{-22} \text{ barn/GeV}$$



Self-Interacting Dark Matter (SIDM) & small-scale Cosmology

THE NEW PICTURE OF DARK MATTER

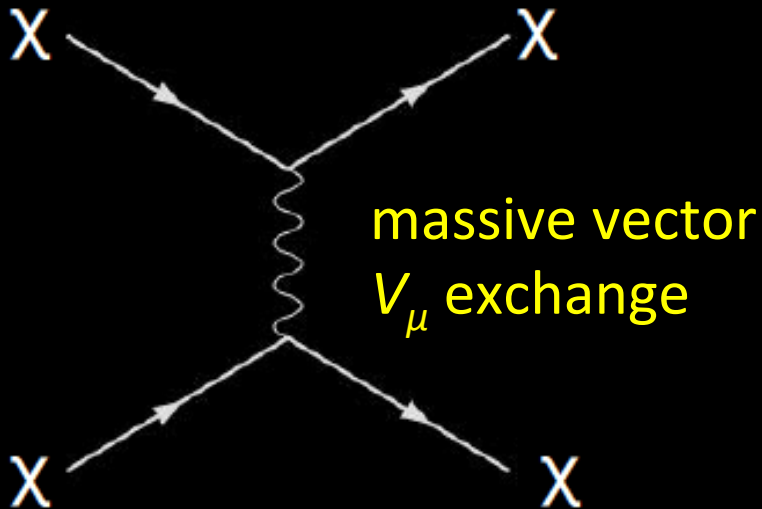


Harvey, Massey,
Kitching, Taylor, Titley
arXiv:1503.07675,
Science

$$0.1 \leq \frac{\sigma_{\text{SIDM}}/m}{\text{cm}^2 \text{g}^{-1}} \leq 0.47$$

OBSERVABLE MANIFESTATION OF SELF-INTERACTIONS IN COLLIDING CLUSTERS

χ = Right-handed neutrino



In **Right-handed neutrino** WDM:

(i) **mass of $O(50)$ keV,**

(ii) **self-interactions stronger than the weak force, $10^8 G_F$**

(iii) **massive $\sim 10^4$ keV exchange vector is OK for core-galaxy structure**

**Arguelles, NEM,
Ruffini, Rueda, JCAP
(2016)**

PART III

Self-Interacting Right-Handed
Neutrino Warm Dark matter
&
galactic core-halo structures

A concrete model for SIDM – Right-handed keV Neutrinos with vector interactions

Arguelles, NEM, Rueda, Ruffini, JCAP 1604, 038 (2016)

- Assume **minimal extension of the Standard Model (non-supersymmetric) with right-handed neutrinos (RHN) self interacting** via massive vector exchange interactions in the dark sector
- Use models of particle physics, e.g. ν MSM (**Shaposhnikov *et al.***) with three RHN, but augment them with these self-interactions
- among the lightest of the RHN (**quasi stable \rightarrow DM**)
- Consistency of the **halo-core profile** of dwarf galaxies in Milky Way or large Elliptical \rightarrow **mass** of lightest RHN in **O(10) keV (WDM)** \leftarrow **Cosmological constraints** of ν MSM

Two different approaches yield similar range for WDM mass!

A concrete model for SIDM – Right-handed keV Neutrinos with vector interactions

Argüelles, NEM, Rueda, *Phys. Rev. D* **94**, 038 (2016)

- Assume **minimal extension** of SM (non-supersymmetric) with **self interacting** vector interactions in the dark sector (RHN)
- Use **minimal** model (e.g. ν MSM) for the RHN, with **vector** self-interactions
- **DM** may consist of **more than one** dominant species!
- Constraints from the **halo-core profile** of dwarf galaxies in Milky Way or large Elliptical \rightarrow **mass** of lightest RHN in **$O(10)$ keV (WDM)** \leftarrow **Cosmological constraints** of ν MSM

Two different approaches yield similar range for WDM mass!

SM Extension with N extra right-handed neutrinos

$$L = L_{SM} + \bar{N}_I i \partial_\mu \gamma^\mu N_I - F_{\alpha I} \bar{L}_\alpha N_I \tilde{\phi} - \frac{M_I}{2} \bar{N}_I^c N_I + \text{h.c.}$$

Minkowski, Fukugita, Yanagida,
Mohapatra, Senjanovic, Lazarides, Shafi, Wetterich,
Sechter, Valle, Paschos, Hill, Luty,
Vergados, de Gouvea..., Liao, Nelson,
Buchmuller, Anisimov, di Bari..., Akhmedov, Rubakov,
Smirnov, Davidson, Giudice, Notari, Raidal,
Riotto, Strumia, Pilaftsis, Underwood,
Asaka, Blanchet, Shaposhnikov, Boyarski, Ruchayskiy...
Hernandez, Giunti...

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Right-handed
Massive **Majorana**
neutrinos

Leptons

$$L_\alpha = \begin{pmatrix} \nu_\alpha \\ \alpha^- \end{pmatrix}, \quad \alpha = e, \mu, \tau$$

SM Extension with N extra right-handed neutrinos

$$L = L_{SM} + \bar{N}_I i \partial_\mu \gamma^\mu N_I - F_{\alpha I} \bar{L}_\alpha N_I \tilde{\phi} - \frac{M_I}{2} \bar{N}_I^c N_I + \text{h.c.}$$



Higgs scalar SU(2)

Dual: $\tilde{\phi}_i = \epsilon_{ij} \phi_j^*$

SM Extension with N extra right-handed neutrinos

ν MSM

Asaka, Blanchet, Boyarski, Ruchayskiy, Shaposhnikov

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Yukawa couplings

Matrix ($l=1,2,3$)

$$F = \tilde{K}_L f_d \tilde{K}_R^\dagger$$

$$f_d = \text{diag}(f_1, f_2, f_3), \quad \tilde{K}_L = K_L P_\alpha, \quad \tilde{K}_R^\dagger = K_R^\dagger P_\beta$$

$$P_\alpha = \text{diag}(e^{i\alpha_1}, e^{i\alpha_2}, 1), \quad P_\beta = \text{diag}(e^{i\beta_1}, e^{i\beta_2}, 1)$$

Majorana phases

Mixing

$$K_L = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{L23} & s_{L23} \\ 0 & -s_{L23} & c_{L23} \end{pmatrix} \begin{pmatrix} c_{L13} & 0 & s_{L13} e^{-i\delta_L} \\ 0 & 1 & 0 \\ -s_{L13} e^{i\delta_L} & 0 & c_{L13} \end{pmatrix} \begin{pmatrix} c_{L12} & s_{L12} & 0 \\ -s_{L12} & c_{L12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$c_{Lij} = \cos(\theta_{Lij}) \text{ and } s_{Lij} = \sin(\theta_{Lij}).$$

SM Extension with N extra right-handed neutrinos

$$L = L_{SM} + \bar{N}_I i \partial_\mu \gamma^\mu N_I - F_{\alpha I} \bar{L}_\alpha N_I \tilde{\phi} - \frac{M_I}{2} \bar{N}_I^c N_I + \text{h.c.}$$

For Constraints
(compiled ν oscillation data)
on (light) sterile neutrinos cf.:
Giunti, Hernandez, ...
N=1 excluded by data

Yukawa couplings
Matrix ($l=1, \dots, N=2$ or 3)

Model with 2 or 3 singlet fermions works well in reproducing Baryon Asymmetry and is consistent with Experimental Data on neutrino oscillations

Model with $N=3$ also works fine, and in fact it allows *one* of the Majorana fermions to almost *decouple* from the rest of the SM fields, thus providing candidates for *light* (keV region of mass) sterile neutrino *Dark Matter*.

SM Extension with N extra right-handed neutrinos

ν MSM

Asaka, Blanchet, Boyarski, Ruchayskiy, Shaposhnikov

$$L = L_{SM} + \bar{N}_I i \partial_\mu \gamma^\mu N_I - F_{\alpha I} \bar{L}_\alpha N_I \tilde{\phi} - \frac{M_I}{2} \bar{N}_I^c N_I + \text{h.c.}$$

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Majorana masses
to (2 or 3) active (light)
neutrinos via *seesaw*

Yukawa couplings
Matrix (N=2 or 3)

Minkowski, Fugujita, Yanagida,
Lazarides, Shafi, Wetterich,
Sechter, Valle, Mohapatra,
Senjanovic, ...

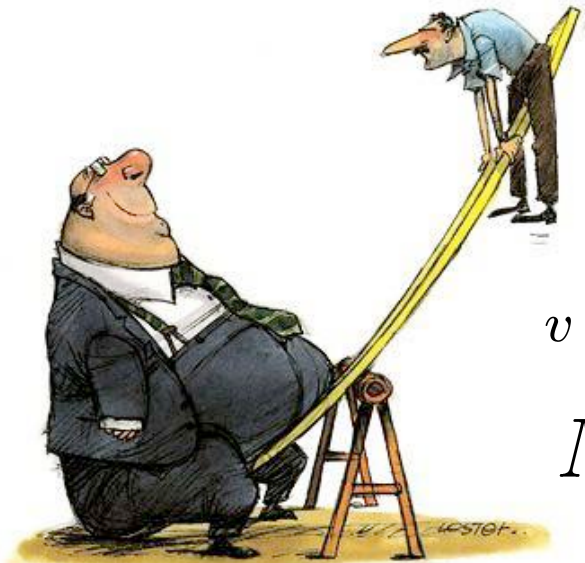
NB: Upon Symmetry Breaking
 $\langle \Phi \rangle = v \neq 0 \rightarrow$ Dirac mass term

$$M_D = F_{\alpha I} v$$

$$v = \langle \phi \rangle \sim 175 \text{ GeV}$$

$$M_D \ll M_I$$

$$m_\nu = -M^D \frac{1}{M_I} [M^D]^T$$





mass of lightest of N_I ,
by agreement
with Cosmological data

$$L = L_{SM} + \bar{N}_I i \partial_\mu \gamma^\mu N_I - F_{\alpha I} \bar{L}_\alpha N_I \tilde{\phi} - \frac{M_I}{2} \bar{N}_I^c N_I + \text{h.c.}$$

Light Neutrino Masses through see saw

$$m_\nu = -M^D \frac{1}{M_I} [M^D]^T$$

$$M_D = F_{\alpha I} v$$

$$v = \langle \phi \rangle \sim 175 \text{ GeV} \quad M_D \ll M_I$$





$N \rightarrow H \nu$

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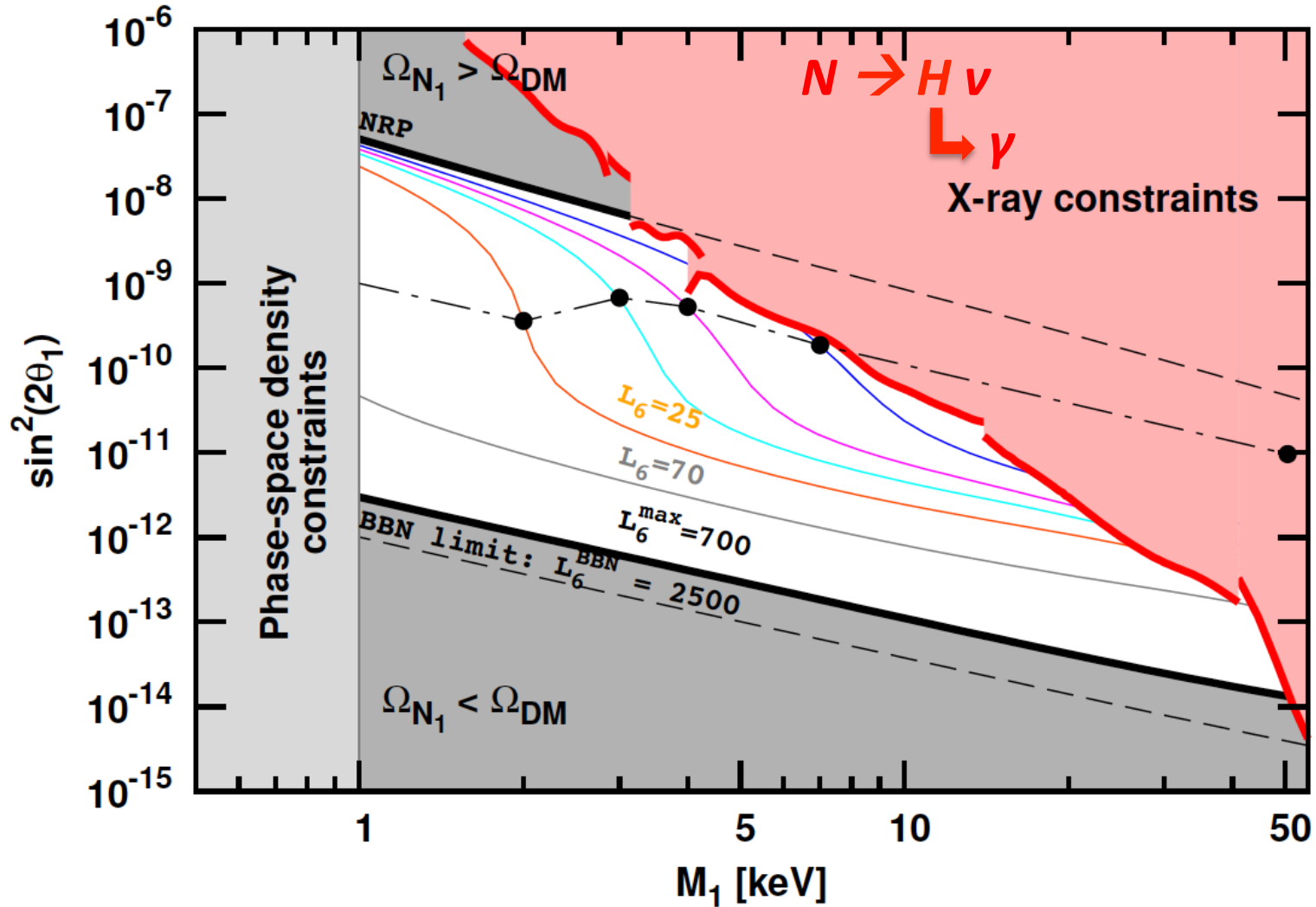
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$$F_{\alpha 1} \approx 10^{-10} \rightarrow m_\nu^2 \approx 10^{-3} \text{ eV}^2$$

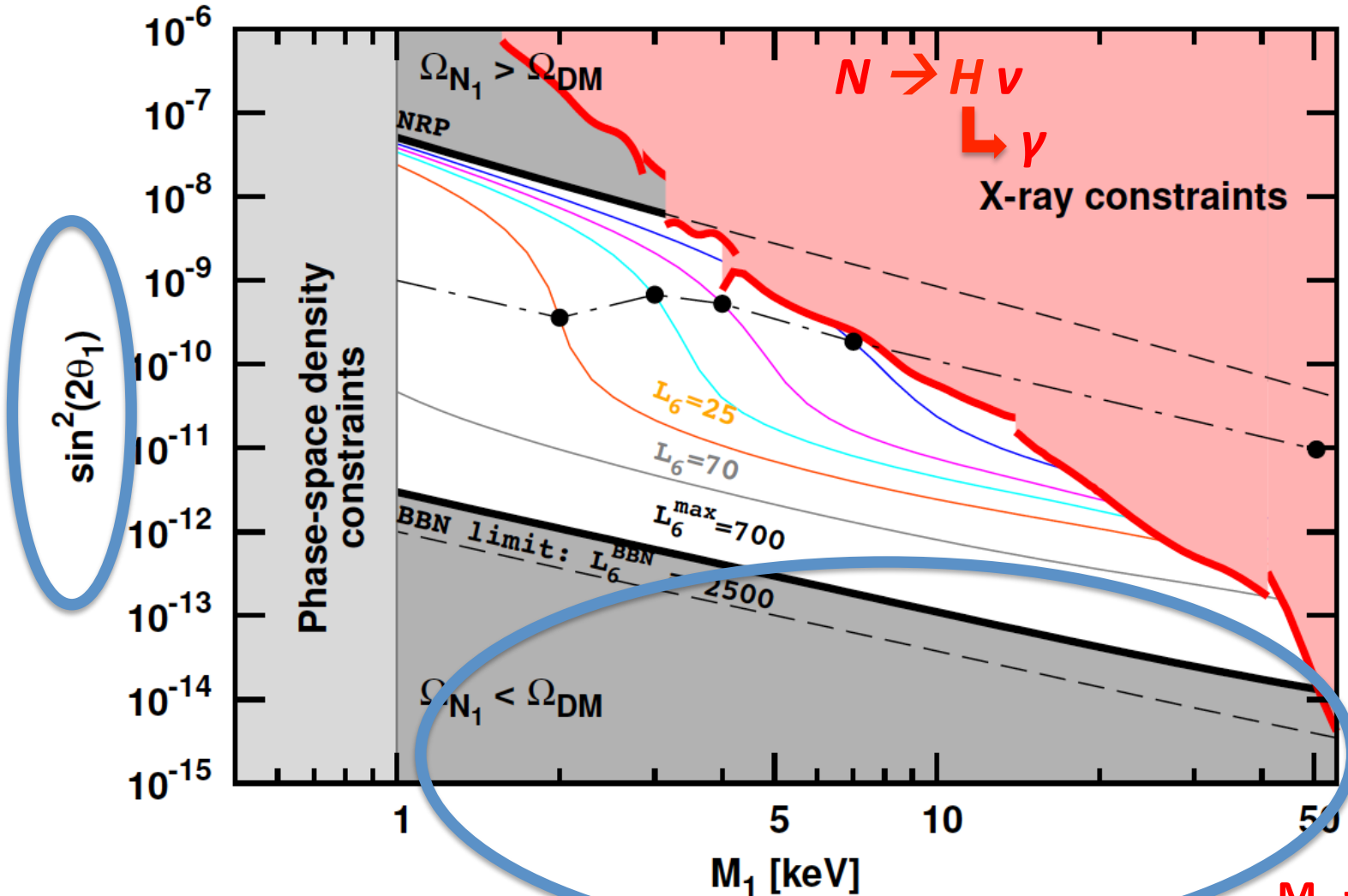
vMSM

MODEL CONSISTENT WITH BBN, STRUCTURE FORMATION DATA IN THE UNIVERSE & ALL OTHER ASTROPHYSICAL CONSTRAINTS



vMSM

MODEL CONSISTENT WITH BBN, STRUCTURE FORMATION DATA IN THE UNIVERSE & ALL OTHER ASTROPHYSICAL CONSTRAINTS

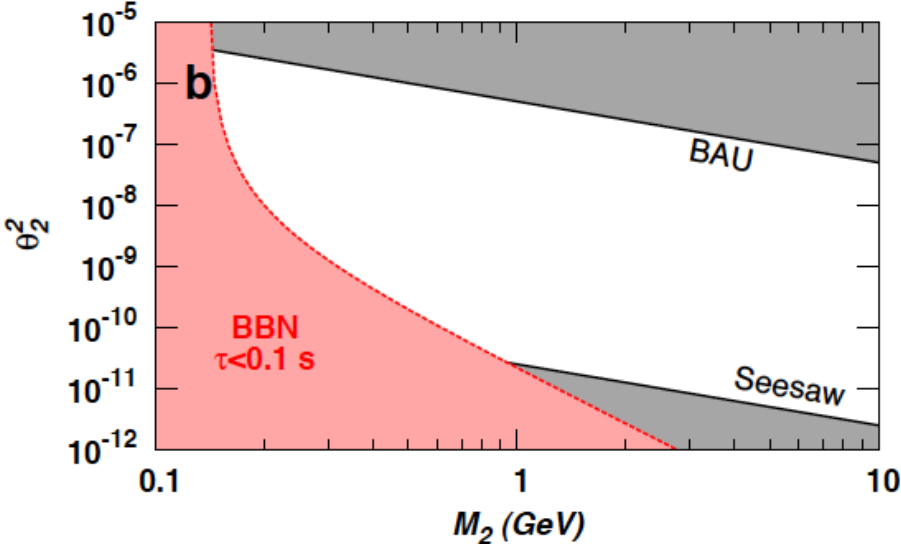
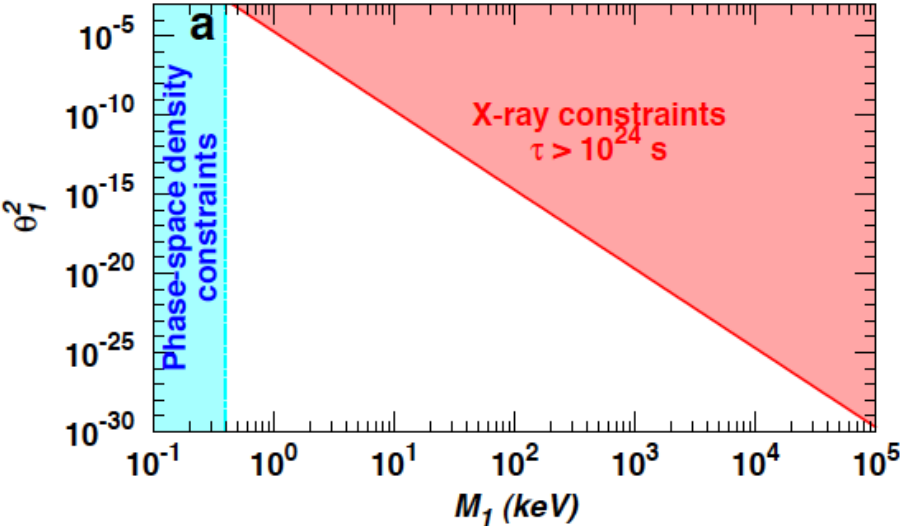


$M_1 = O(10)$ keV

More than one sterile neutrino needed to reproduce Observed oscillations

ν MSM

Boyarski, Ruchayskiy, Shaposhnikov...



Constraints on two heavy degenerate singlet neutrinos

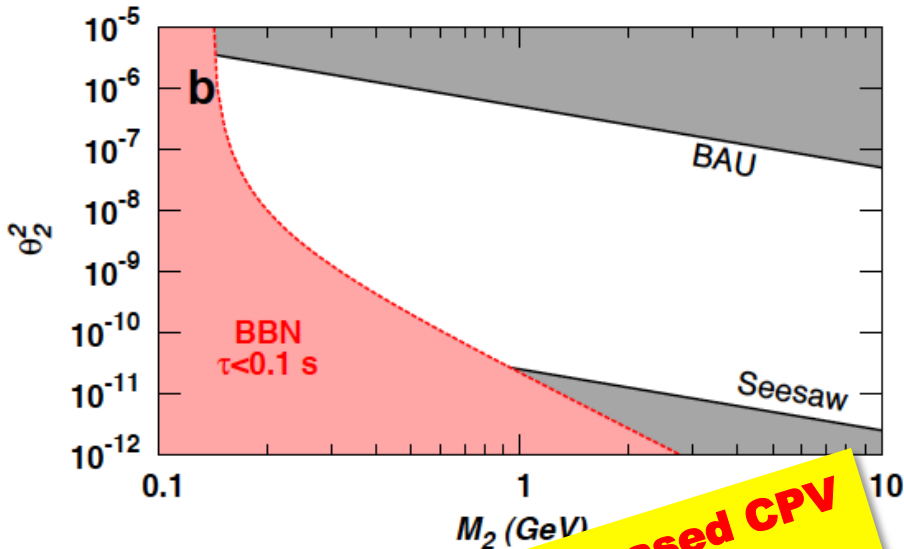
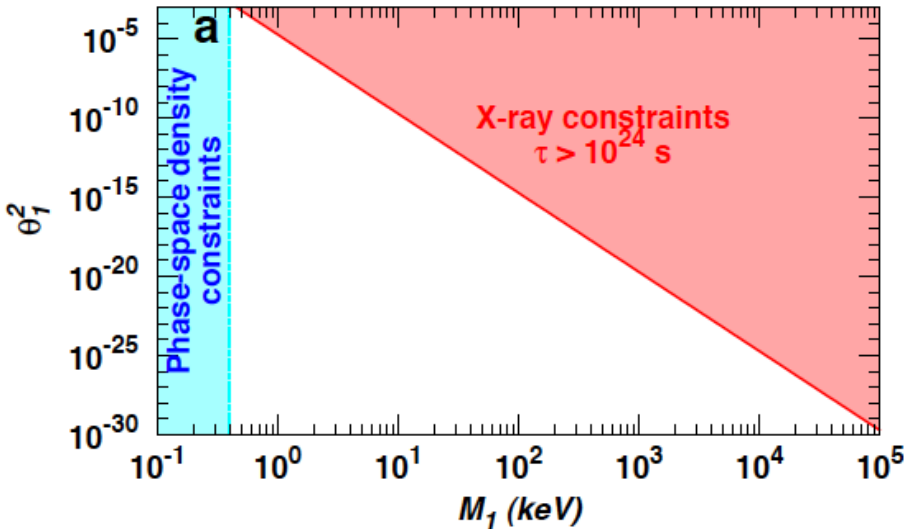
N_1 DM production estimation in Early Universe must take into account its interactions with $N_{2,3}$ heavy neutrinos



More than one sterile neutrino needed to reproduce Observed oscillations

ν MSM

Boyarski, Ruchayskiy, Shaposhnikov...



Increased CPV
Pilaftsis,
Underwood...

Constraints on two heavy degenerate singlet neutrinos

N_1 DM production estimation in Early Universe must take into account its interactions with $N_{2,3}$ heavy neutrinos





This talk: restrict mass of N_I by agreement with observed galactic core-halo structure in SIDM versions of the model

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~~$F_{\alpha 1} \approx 10^{10} \rightarrow m_\nu^2 \approx 10^{-3} \text{ eV}^2$~~

Ignore in front of strong self-interactions for our purposes

Right-handed keV Neutrinos with vector self-interactions & galactic structure

Arguelles, NEM, Rueda, Ruffini, JCAP 1604, 038 (2016)

Place the vMSM in **curved space time** $g_{\mu\nu} = \text{diag}(e^\nu, -e^\lambda, -r^2, -r^2 \sin^2 \varphi)$
 $v=v(r) \quad \lambda = \lambda(r)$

$$\mathcal{L} = \mathcal{L}_{GR} + \mathcal{L}_{N_{R1}} + \mathcal{L}_V + \mathcal{L}_I$$

$$\mathcal{L}_{GR} = -\frac{R}{16\pi G}, \quad \mathcal{L}_{N_{R1}} = i \bar{N}_{R1} \gamma^\mu \nabla_\mu N_{R1} - \frac{1}{2} m \bar{N}_{R1}^c N_{R1},$$

$$\mathcal{L}_V = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \frac{1}{2} m_V^2 V_\mu V^\mu, \quad \mathcal{L}_I = -g_V V_\mu J_V^\mu = -g_V V_\mu \bar{N}_{R1} \gamma^\mu N_{R1}$$

$$\nabla_\mu = \partial_\mu - \frac{i}{8} \omega_\mu^{ab} [\gamma_a, \gamma_b]$$

Classical fields (eqs of motion) satisfy detailed **thermodynamic equilibrium conditions** in a galaxy at a temperature $T < O(\text{keV})$

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Right-handed keV Neutrinos with vector self-interactions & galactic structure

Measure of Strength of self Interactions

$$C_V \equiv g_V^2 / m_V^2$$

$$C_V(r) = \begin{cases} C_0 & \text{at } r < r_m \quad \text{when } \lambda_B / l > 1 \\ 0 & \text{at } r \geq r_m \quad \text{when } \lambda_B / l < 1 \end{cases}$$

effective interactions
in galactic medium

r_m = core-halo matching point = $r_c + \delta r$
core radius

inter-particle mean distance l
at temperature T

$$\text{de-Broglie wavelength } \lambda_B = \frac{\hbar}{\sqrt{2\pi m k_B T}}$$

Right-handed keV Neutrinos with vector self-interactions & galactic structure

**sterile ν
mass**

Milky Way ($M_c = 4.4 \times 10^6 M_\odot$)

m (keV)	\bar{C}_0	θ_0	β_0	r_c (pc)	δr (pc)	$\theta(r_m)$
47	2	3.70×10^3	1.065×10^{-7}	6.2×10^{-4}	2.1×10^{-4}	-29.3
	10^{14}	3.63×10^3	1.065×10^{-7}	6.2×10^{-4}	2.2×10^{-4}	-29.3
	10^{16}	2.8×10^3	1.065×10^{-7}	6.3×10^{-4}	2.4×10^{-4}	-29.3
350	1	2.40×10^6 (†)	1.431×10^{-7}	1.3×10^{-6}	6.7×10^{-7}	-37.3
	10^{14}	1.27×10^5	1.104×10^{-7}	5.9×10^{-6}	9.4×10^{-7}	-37.3
	4.5×10^{18}	1.7×10^1	1.065×10^{-7}	5.9×10^{-4}	2.0×10^{-4}	-37.3

Elliptical ($M_c^{cr} = 2.3 \times 10^8 M_\odot$)

47	2	1.76×10^5 (†)	1.7×10^{-6}	7.9×10^{-5}	3.9×10^{-5}	-31.8
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	10^{16}	1.5×10^4	1.3×10^{-6}	3.0×10^{-4}	7.0×10^{-5}	-31.8

Large Elliptical ($M_c = 1.8 \times 10^9 M_\odot$)

47	10^{16}	1.02×10^4	3.0×10^{-6}	3.8×10^{-4}	1.8×10^{-5}	-32.8
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$$\beta \equiv k_B T/m = \beta_0 e^{(\nu_0 - \nu(r))/2}$$

$$\theta \equiv \mu/(k_B T)$$

at the core (β_0, θ_0)

No solution for

gravitational collapse →

$$m < 47 \text{ keV}/c^2$$

$$m > 350 \text{ keV}/c^2$$

Right-handed keV Neutrinos with vector self-interactions & galactic structure

**sterile ν
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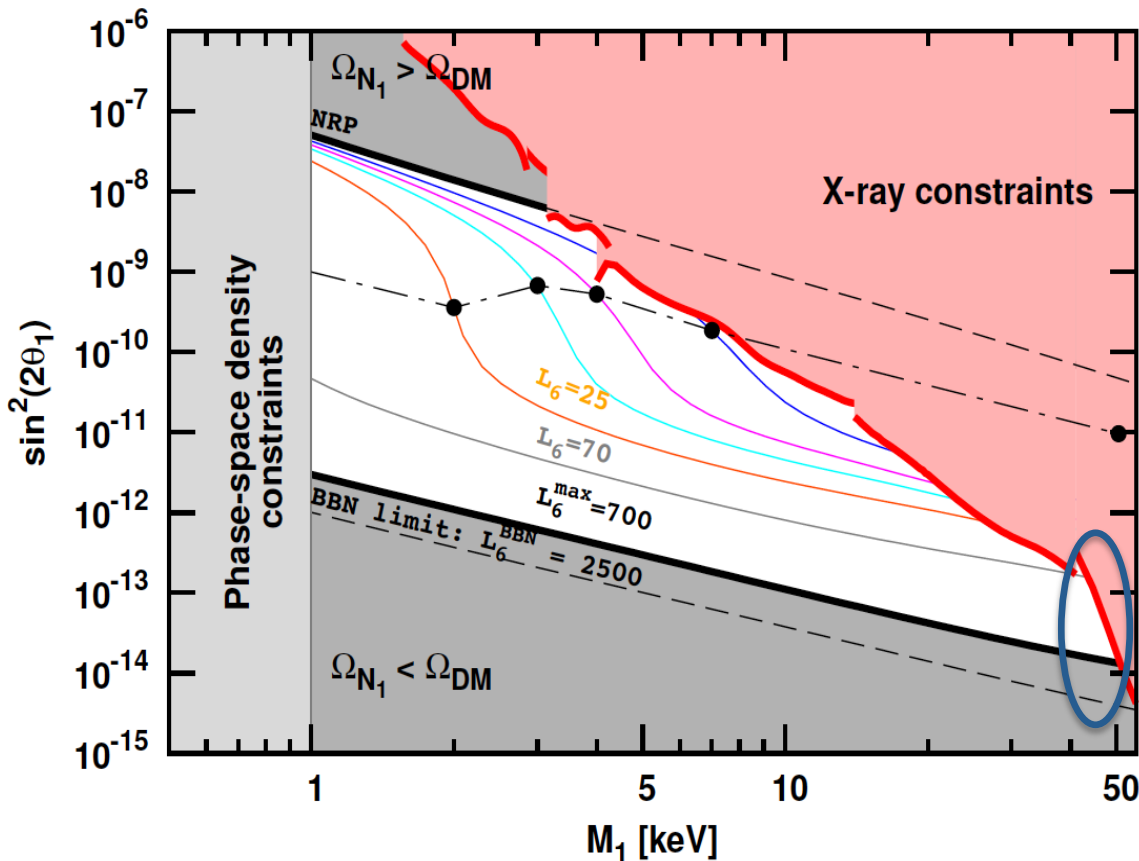
$$\theta \equiv \mu/(k_B T)$$

at the core (β_0, θ_0)

**Allowed WDM mass
range**

47 keV $c^{-2} \leq m \leq 350$ keV c^{-2}

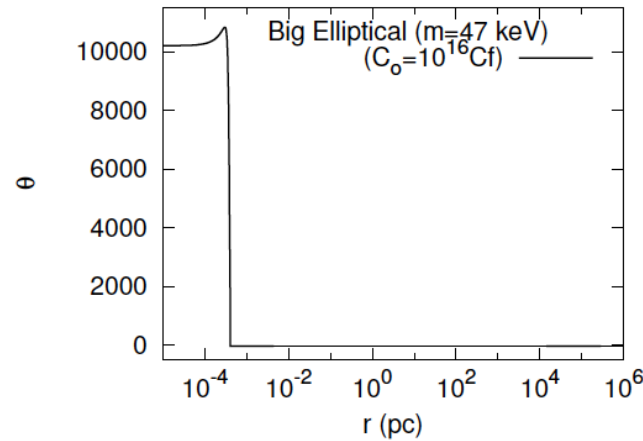
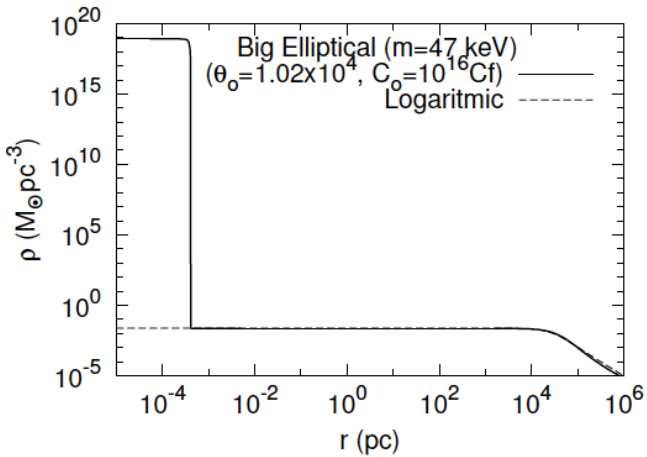
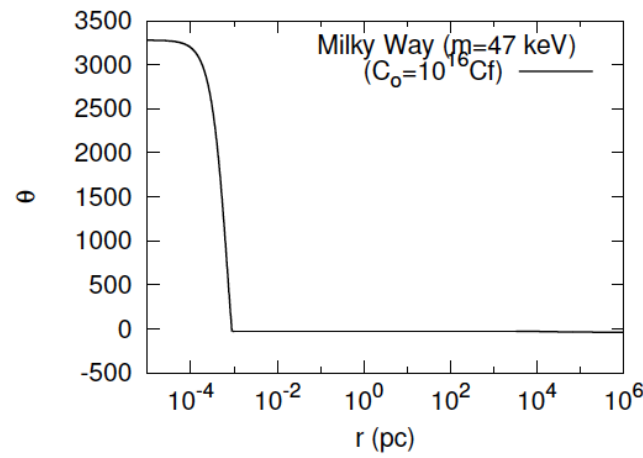
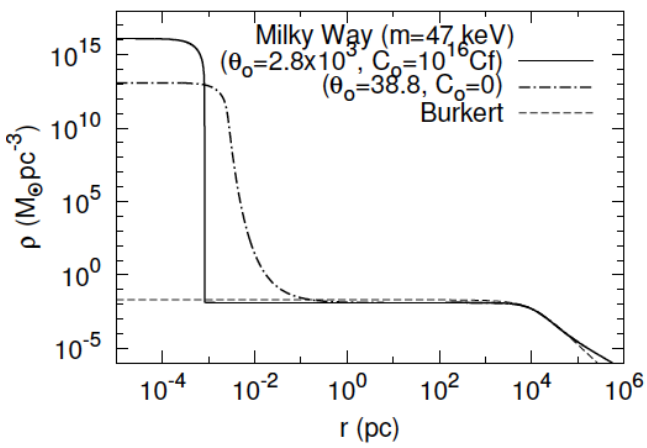
Right-handed keV Neutrinos with vector self-interactions & galactic structure



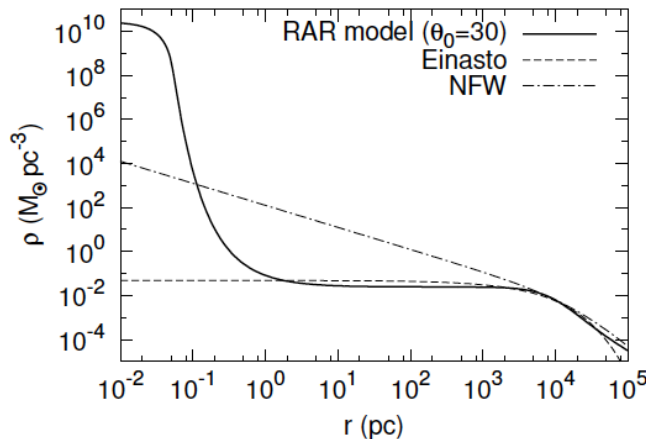
If **mixing** with observable sector is **non zero** (vMSM)
 → **narrow window**
 of allowed WDM mass!

$$47 \text{ keV } c^{-2} \leq m \leq 50 \text{ keV } c^{-2}$$

Arguelles, NEM,
Rueda, Ruffini,
JCAP 1604, 038 (2016)



Interactions
make inner Core
more compact
and increase
central degeneracy
compared to non-
interacting case



Non interacting
right-handed neutrino case
with $m = O(10)$ keV

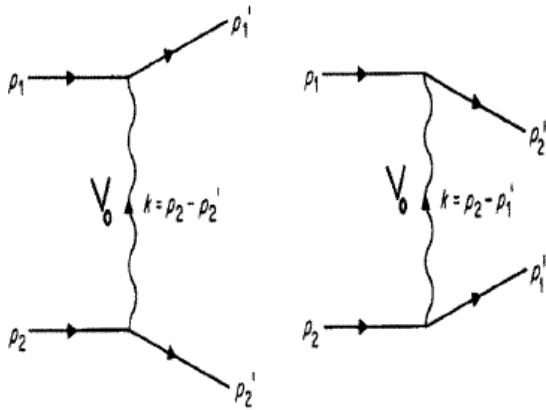
Ruffini, Arguelles, Rueda,
MNRAS (2015)

Provide natural resolution of Core-Cusp Problem because the density profiles based on **fermionic (as RH neutrinos)** **phase-space distributions** develop always an **extended plateau on halo scales**, resembling Burkert or cored Einasto profiles



Moreover, as the right-handed neutrino DM mass is **'colder'** by a few keV ($m \approx 47 \text{ keV } c^{-2}$) compared to most of the WDM models available in the literature, our model does **not suffer from standard WDM problems**, associated with the **'too warm'** nature of the particles involved

N-N Cross sections under massive vector exchange (perturbation theory $g_V < 1$ OK)



$$m \in (47, 350) \text{ keV}$$

$$\sigma_{core}^{tot} \approx \frac{(g_V / m_V)^4}{4^3 \pi} 29 m^2 \quad (p^2 / m^2 \ll 1)$$

Hidden sector vector interactions -> Much stronger than weak interactions in visible sector

$$\bar{C}_V = \left(\frac{g_V}{m_V} \right)^2 G_F^{-1} \longrightarrow \bar{C}_V \in (2.6 \times 10^8, 7 \times 10^8)$$

to resolve issues of small-scale cosmology crisis

Arguelles, NEM,
Rueda, Ruffini,
JCAP 1604, 038 (2016)

$$m_V \lesssim 3 \times 10^4 \text{ keV}$$

Conclusions-Outlook - so far

- At galactic scales **Λ CDM model suffers** from discrepancies with observations regarding the **core-cusp, missing satellite, and too big to fail** problems of ***small-scale Cosmology "crisis"*** ...
- To remediate this, **self interactions among DM** have been introduced with relatively strong cross sections per unit dark matter mass σ/m :

$$0.1 \leq \frac{\sigma_{\text{SIDM}}/m}{\text{cm}^2 \text{g}^{-1}} \leq 0.47$$

- We have considered the role of **the lightest of the right-handed neutrinos in vMSM** extensions of the standard model, and **added appropriately strong vector interactions** in the dark sector among the neutrinos \rightarrow **increase inner degeneracy and inner core** region in dwarf satellites of the Milky Way or Large elliptical galaxies
For interaction strengths **$10^8 G_F$, WDM mass = 47-50 keV, & vector mass < 10^4 keV**, we can **resolve the three small-scale Cosmology problems**.
- **The RH neutrino WDM**, which solves core-halo structure in galaxies, may **co-exist** with other **CDM DM species** \rightarrow **search** for it in **particle physics** and neutrino **oscillation** experiments

Conclusions - Outlook

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Conclusions - Outlook

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- **The RH neutrino WDM**, which solves core-halo structure in galaxies, may **co-exist** with other **CDM DM species** \rightarrow coupling with **axions** may lead to **Mass generation for Right Handed Neutrinos**

THANK YOU !

SPARES

Dark Matter

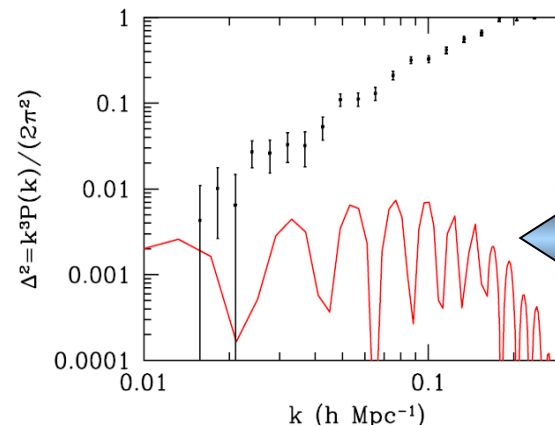
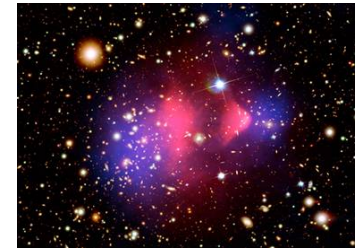
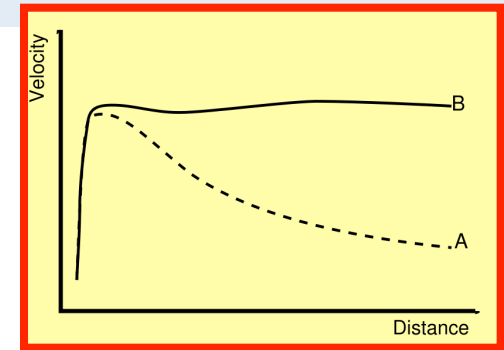
DARK MATTER (DM):
CURRENT EVIDENCE
Arguments in Favour

TYPES OF DM: hot, warm, cold

ASTROPHYSICAL CONSTRAINTS
(MODEL INDEPENDENT)

INDIRECT SEARCHES:
collider (LHC & beyond) searches
photons, neutrinos,
matter-antimatter asymmetries
(electron-positron, proton-antiproton)

Rotational Curves of galaxies,
gravitational lensing
growth of structure

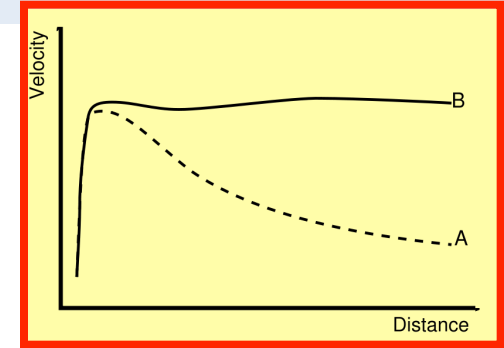


Baryon-only
Models, without
Dark Matter

Dark Matter

DARK MATTER (DM):
CURRENT EVIDENCE
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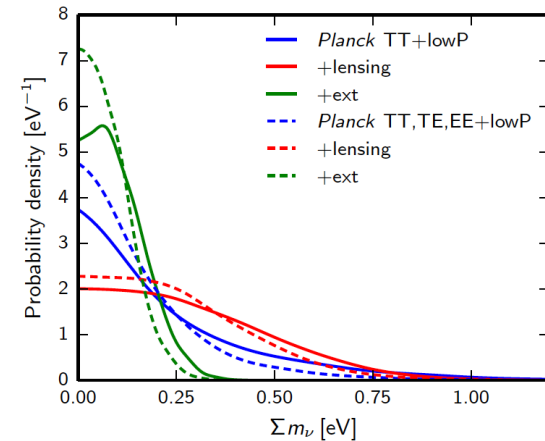
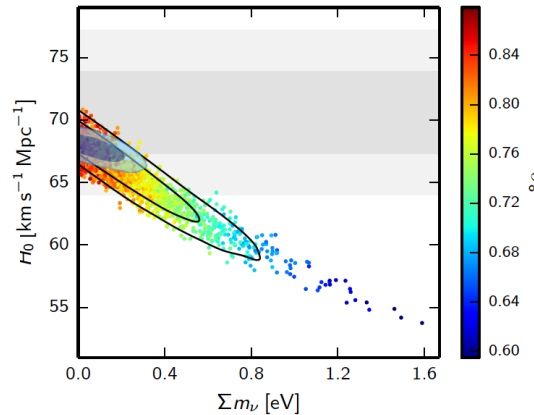
Rotational Curves of galaxies,
gravitational lensing
growth of structure



TYPES OF DM: **hxt**, warm, cold



ASTROPHYSICAL CONSTRAINTS
(MODEL INDEPENDENT)

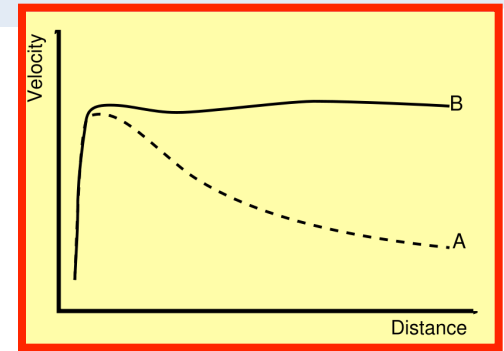


$$\left. \begin{aligned} \Sigma m_\nu &< 0.23 \text{ eV} \\ \Omega_\nu h^2 &< 0.0025 \end{aligned} \right\} 95\%, \text{ Planck TT+lowP+lensing+ext.}$$

Dark Matter

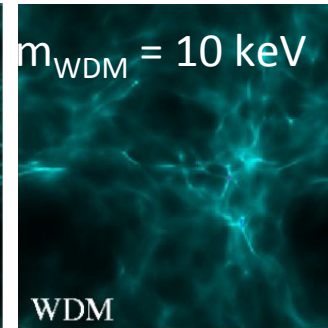
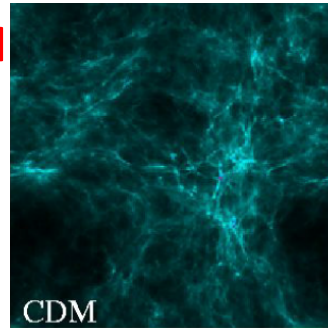
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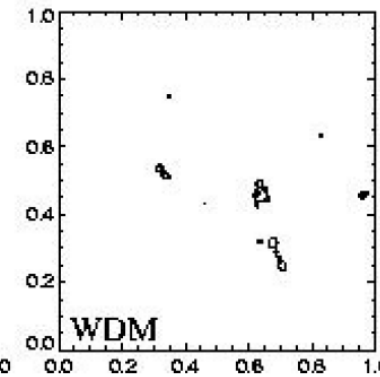
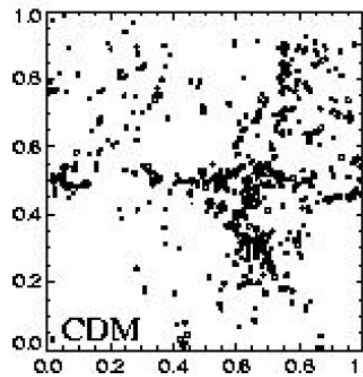
ASTROPHYSICAL CONSTRAINTS
(MODEL INDEPENDENT)



WMAP,
Planck Coll 2015
Yoshida *et al.*
astro-ph/0303622

Distribution of dark haloes with mass $M > 10^5 M_{\odot}$

excludes Warm DM
 $m_{\text{WDM}} \leq 10 \text{ keV} !$

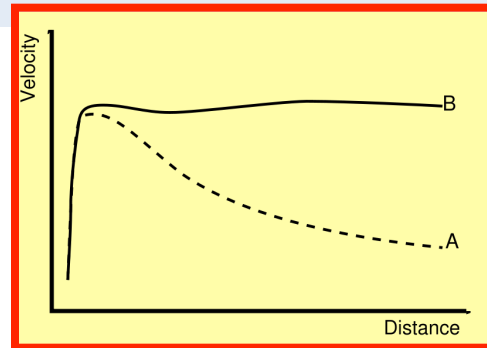


Re-ionization of the Universe @ redshift $z=20$
 numerical N-body simulations based on warm & Λ CDM models

Dark Matter

DARK MATTER (DM):
CURRENT EVIDENCE
Arguments in Favour

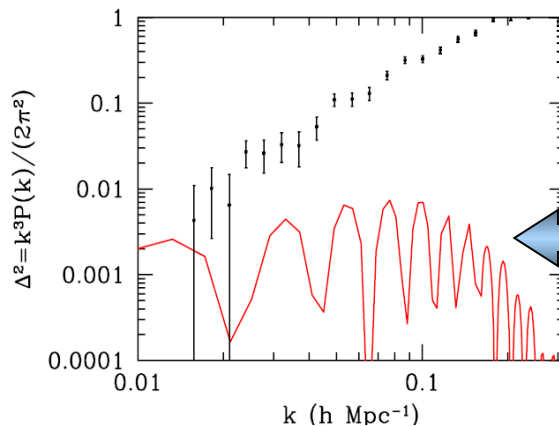
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(MODEL INDEPENDENT)

INDIRECT SEARCHES:
collider (LHC & beyond) searches
photons, neutrinos,
matter-antimatter asymmetries
(electron-positron, proton-antiproton)



Baryon-only Models, without Dark Matter

Compatible with all current data !
 $m \geq 100$ keV
 $100 \text{ keV} \leq m_{\text{WDM}} = m_{\text{CDM}}$



Dark Matter

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CURRENT EVIDENCE

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(MODEL INDEPENDENT)**

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THEORETICAL SCENARIOS

SUPERSYMMETRY *neutralino*

SUPERGRAVITY *gravitino (if sufficiently light)*

AXIONS *(standard QCD or stringy)*

STERILE NEUTRINOS

...

Dark Matter

e.g. typical **thermal WIMPs**
CMB-observations-compatible
DM relic abundance

$$\Omega_\chi \simeq \frac{0.1 \text{ pb} \cdot c}{\langle \sigma(\chi\chi \rightarrow \text{SM } v) \rangle} \simeq 0.22$$

occurs cross sections of
weak-interactions type

$$\sigma(\chi\chi \rightarrow \text{SM } v) \simeq 3 \cdot 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

“WIMP miracle”

$$m_\chi \sim O(100 \text{ GeV} - \text{TeV})$$

THEORETICAL SCENARIOS

SUPERSYMMETRY ***neutralino***

SUPERGRAVITY ***gravitino*** (*if sufficiently light*)

AXIONS (*standard QCD or stringy*)

STERILE NEUTRINOS

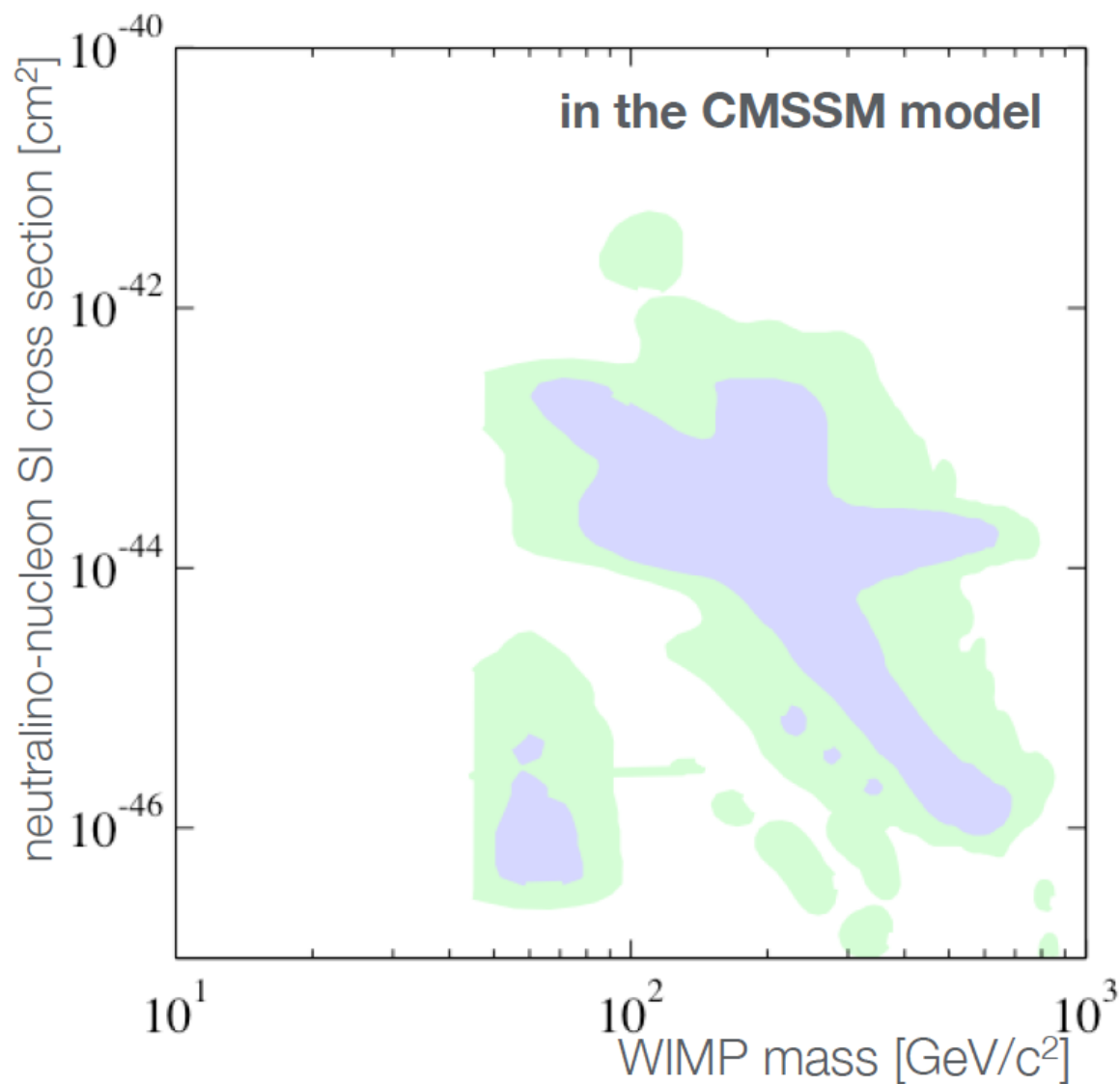
...

Theoretical Model dependence
in deriving bounds in experimental searches



- Predictions from supersymmetry [10^{-8} pb = 10^{-44} cm²]:

$$\sigma/m \approx 10^{-22} \text{ barn/GeV}$$



CMSSM2008
(Roszkowski, Ruiz, Trotta)

Dark Matter

e.g. typical **thermal WIMPs**
CMB-observations-compatible
DM relic abundance

$$\Omega_\chi \simeq \frac{0.1 \text{ pb} \cdot c}{\langle \sigma(\chi\chi \rightarrow \text{SM}v) \rangle} \simeq 0.22$$

occurs cross sections of
weak-interactions

$$\sigma(\chi\chi \rightarrow \text{SM}v)$$

“**WIMP miracle**”

$$m_\chi \sim O(100 \text{ GeV} - \text{TeV})$$

**But...None of these particles
has been observed as yet....**

THEORETICAL SCENARIOS

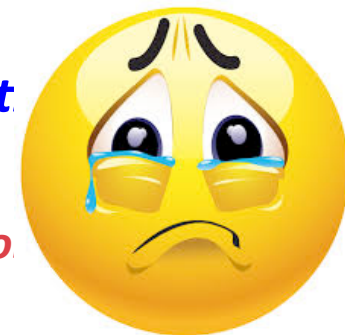
SUPERSYMMETRY *gravitino*

AXIONS *(standard QCD or string theory)*

STERILE NEUTRINOS

...

Theoretical Model dependence
in deriving bounds in experimental searches



Dark Matter

DARK MATTER (DM):

CURRENT EVIDENCE

Arguments in Favour

TYPES OF DM: **hot, warm**

ASTROPHYSICAL

(MODEL INDEPENDENT)

INDIRECT

collider (LHC), searches

photons, neutrinos,

matter-antimatter asymmetries

(electron-positron, proton-antiproton)

THEORETICAL SCENARIOS

neutralino

GRAVITINO (if sufficiently light)

AXIONS (standard QCD or stringy)

STERILE NEUTRINOS

This talk

Theoretical Model dependence

in deriving bounds in experimental searches

Moreover.....
DM may consist of more than one dominant species!

